## <span id="page-0-0"></span>**Stark shift and parity nonconservation for near-degenerate states of xenon**

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We identify a pair of near-degenerate states of opposite parity in atomic Xe, the  $5p^510s^2[3/2]_2^o$  at  $E =$ 94 759*.*927 cm<sup>−</sup><sup>1</sup> and 5*p*56*f* 2[5*/*2]2 at *E* = 94 759*.*935 cm<sup>−</sup>1, for which parity- and time-odd effects are expected to be enhanced by the small energy separation. We present theoretical calculations which indicate narrow widths for both states and we report a calculated value for the weak matrix element, arising from configuration mixing, of  $|W| = 2.1$  Hz for <sup>132</sup>Xe. In addition, we measured the Stark effect of the  $5p^56f^2[5/2]_2$  and  $5p^56f^2[3/2]_2$ (*E* = 94 737*.*121 cm<sup>−</sup>1) states. The Stark shift of the 6*f* states is observed to be negative, revealing the presence of nearby 6*g* states at higher energies, which have not been observed before. The Stark-shift measurements imply an upper limit on the weak matrix element of  $|W|$  < 5 Hz for the near-degenerate states  $(10s<sup>2</sup>[3/2]<sub>2</sub><sup>o</sup>$  and  $6f^{2}[5/2]_{2}$ , which is in agreement with the presented calculations.

DOI: [10.1103/PhysRevA.89.042513](http://dx.doi.org/10.1103/PhysRevA.89.042513) PACS number(s): 32*.*10*.*Dk*,* 32*.*60*.*+i*,* 31*.*15*.*A−

# **I. INTRODUCTION**

High-*Z* atoms with near-degenerate opposite-parity states are promising spectroscopic systems for experiments studying parity  $(P)$  and time-reversal invariance  $(T)$  violating phenomena, due to the enhancement of the *P*- and *P,T* -odd effects by the small energy intervals between the atomic levels [\[1\]](#page-9-0). In 1986, Dzuba, Flambaum, and Khriplovich [\[2\]](#page-9-0) identified the importance of various pairs of near-degenerate states of opposite parity in rare earth atoms, such as samarium (Sm), erbium (Er), and dysprosium (Dy), for possible enhancement of such effects. In particular, atomic Dy has been used in measurements of parity nonconservation (PNC) [\[3\]](#page-9-0) and also in search for the time variation of the finestructure constant [\[4\]](#page-9-0), and to investigate the gravitationalpotential dependence on the fine-structure constant [\[5\]](#page-9-0), with more recent results additionally setting limits on violations of Lorentz symmetry and the Einstein equivalence principle [\[6\]](#page-9-0).

Here we identify a pair of near-degenerate opposite-parity states, both with total angular momentum  $J = 2$ , in atomic

xenon (Xe) as a candidate system for *P*- and *T* -violation experiments, Fig.  $1(a)$ ; see Ref. [\[7\]](#page-9-0):

$$
5p510s2[3/2]_2^o \t E = 94759.927 \text{ cm}-1,
$$
 (1)

$$
5p56f2[5/2]_2 \tE = 94759.935 \text{ cm}^{-1}. \t(2)
$$

Xe is a noble gas with nuclear charge  $Z = 54$  and therefore the  $Z^3$  enhancement of  $P$ - and  $T$ -odd effects is significant for the chosen states [\[8\]](#page-9-0). The wide range of stable Xe isotopes (eight, ranging from  $^{129}\text{Xe}$  to  $^{136}\text{Xe}$ ) gives the possibility to perform PNC measurements in different isotopes, in which the large error associated with atomic theory calculations can be largely eliminated by taking ratios of measurements in different isotopes [\[1,2\]](#page-9-0). Additionally, two of the stable Xe isotopes have nonzero nuclear spin  $(129)$ Xe with  $I = 1/2$  and <sup>131</sup>Xe with  $I = 3/2$ , and therefore PNC measurements in different hyperfine components give access to the nuclear anapole moment [\[9\]](#page-9-0). In close analogy to experiments in Dy, possible searches for variations of the fine-structure constant using this pair of near-degenerate states may become feasible due to the wide choice of rf transitions, arising from the availability of many isotopes.

The principal motivation for this work is the prospect of measuring parity violating phenomena using the

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<span id="page-1-0"></span>

FIG. 1. (Color online) (a) Partial energy-level diagram of Xe (not to scale) showing the pair of near-degenerate states [\(1\)](#page-0-0) and [\(2\)](#page-0-0). The solid lines represent the∼211 nm radiation used for the measurements of the Stark effect of the  $6f$  states using a  $(2+1)$  REMPI scheme, see Sec. [IV.](#page-6-0) The analysis of the measurements of the Stark effect of the two 6*f* states reveals the presence of the 6*g* and 6*h* states, which have not been observed before. (b) Schematic drawing of the experimental setup used for the Stark-shift measurements. (i) A collimated Xe beam is intersected at right angles by a linearly polarized light beam from a ∼211 nm pulsed laser. The laser pulse excites the atoms from the ground state to the excited state of interest, and subsequently ionizes the atoms. The electric field along the *z* axis is used to accelerate the ions down the time-of-flight (TOF) tube towards a microchannel-plate (MCP) detector; this is also the electric field in the Stark effect measurements. The polarization of the laser beam is controlled with a  $\lambda/2$  plate. For excitation to the  $|M| = 2$ sublevels (with quantization axis along  $\hat{z}$ ) of the 6*f* excited states, the polarization of the laser beam is set perpendicular to the *z* axis. (ii) Additional optics used only for the calibration of the electric field, which is realized through the Stark-shift measurements of the  $n = 2$ states in H using a Doppler-free REMPI scheme (see discussion in Sec. [III B\)](#page-5-0).

near-degenerate opposite-parity states [\(1\)](#page-0-0) and [\(2\)](#page-0-0). Parity violation in atomic systems arises primarily due to the weak interaction between the electron and the nucleus, which results in mixing of the parity eigenstates of the system. In particular, the weak interaction mixes predominantly *s* and *p* states [\[8,9\]](#page-9-0). Therefore, mixing arising from PNC between the dominant configurations  $(6f-10s)$  of the levels  $(1)$  and  $(2)$  is negligible. However, if the 6*f* state has significant *p* character from configuration mixing with nearby *np* states (dominated by the nearest  $10p$ ), then the weak interaction will mix the oppositeparity states  $(1)$  and  $(2)$ . In this article we present theoretical calculations of the composition of the states  $(1)$  and  $(2)$ , from which we can estimate the electric-dipole matrix element between these states, as well as the matrix element arising from the weak interaction, both required to assess the possibility of performing PNC experiments using the Stark-interference technique [\[3\]](#page-9-0). In addition, experimental measurements of the Stark shift of the 6*f* state [\(2\)](#page-0-0) are presented, which support the accuracy of the presented theoretical calculations.

In particular, in Sec.  $\Pi$  we present calculations of the width of the states  $(1)$  and  $(2)$ , which are important for assessing the experimental sensitivity for future *P*- and *T* -odd experiments, and of the matrix elements of the electric-dipole interaction and of the weak interaction between these states. In addition, we study the magnetic dipole transitions involving our states of interest, as these are sensitive to the composition of states [\(1\)](#page-0-0) and [\(2\)](#page-0-0). In Sec. [III](#page-4-0) we present measurements of the Stark effect of two 6*f* states (at 94 737*.*121 and at 94 759*.*935 cm<sup>−</sup>1) with the aim to determine the admixture of the  $5p<sup>5</sup>np$  configurations to the  $5p<sup>5</sup>6f$  configuration. Finally, the analysis of the Stark measurements, performed in Sec. [IV,](#page-6-0) determines an upper limit on the weak mixing between states [\(1\)](#page-0-0) and [\(2\)](#page-0-0), in agreement with the presented theoretical calculations.

#### **II. THEORY**

### **A. Width of the states**

The energy difference between the states  $(1)$  and  $(2)$  is only 0.008 cm<sup>−</sup>1. Such a small value might be comparable to the linewidth. The requirement that the widths of the states involved are small is of importance for PNC measurements. Therefore, we estimate the widths of both states. The natural width is determined by the electric dipole transitions from the states [\(1\)](#page-0-0) or [\(2\)](#page-0-0) into appropriate lower states (we use atomic units  $|e| = \hbar = m = 1$ :

$$
\Gamma_a = \sum_b \frac{4}{3} \alpha^3 \omega_{ab}^3 \frac{A_{ba}^2}{2J_a + 1},
$$
\n(3)

where  $a$  stands for  $(1)$  or  $(2)$ , while  $b$  represents all possible lower states connected to [\(1\)](#page-0-0) or [\(2\)](#page-0-0) via the electric dipole operator,  $\omega_{ab}$  is the transition frequency,  $J_a$  is the total angular momentum quantum number of state  $a$ , and  $A_{ba}$  is the transition amplitude from state *a* to *b*.

For estimations we consider the 10*s*-6*p* and 6*f* -5*d* transitions in the single-electron approximation. Transitions to higher states (7*p,*8*p,*6*d*, etc.) can be neglected because of the smaller frequencies of the transitions. For example, the suppression of the 10*s*-7*p* transition probability compared to the 10*s*-6*p* transition probability is approximately a factor of ∼20, i.e.,  $\{[E(10s) - E(6p)]/[E(10s) - E(7p)]\}^3$  ∼ 20. This cannot be compensated by the larger transition amplitude since the corresponding ratio, as calculations show, is much smaller,  $[A(10s-7p)/A(10s-6p)]^2 \sim 3$ .

Taking the electric dipole amplitudes from the randomphase approximation (RPA) calculations (see, for example, Ref. [\[10\]](#page-9-0)):  $A_{10s,6p} = 0.5$  *ea*<sub>0</sub>,  $A_{6f,5d} = 3$  *ea*<sub>0</sub>, and assuming  $\omega_{10s,6p} \approx 17\,000 \text{ cm}^{-1} = 0.08 \text{ a.u., } \omega_{6f,5d} \approx 15\,000 \text{ cm}^{-1} =$ 0.07 a.u leads to  $\Gamma_{10s} = 1.3 \times 10^{-11}$  a.u. =  $3 \times 10^{-6}$  cm<sup>-1</sup>, and  $\Gamma_{6f} = 3 \times 10^{-10}$  a.u. = 6 × 10<sup>-5</sup> cm<sup>-1</sup>.

<span id="page-2-0"></span>TABLE I. Electric dipole transition amplitudes (reduced matrix elements,  $A_{ab}$  in atomic units) from the degenerate states [\(1\)](#page-0-0) and [\(2\)](#page-0-0) to lower states and the corresponding linewidths  $\Gamma_a$ .

From $(a)$	$5p^5 10s, J = 2$ 5p <sup>5</sup> 6p			$5p^56f, J = 2$ $5p^55d$		
to $(b)$	$J_h$	$E_h$ (cm <sup>-1</sup> )	$A_{ab}$	$J_h$	$E_h$ (cm <sup>-1</sup> )	$A_{ab}$
	1	77 269	0.44(9)	1	79 987	1.1(2)
	2	78 119	0.32(6)	3	80 970	0.35(7)
	3	78 403	0.72(14)	2	80 323	0.65(13)
	1	78 956	0.14(3)	1	83 890	2.0(4)
	2	79 212	0.519(10)	2	81 925	1.3(3)
				3	82 430	0.24(5)
$\Gamma_a$		$\sim$ 1 $\times$ 10 <sup>-5</sup>			$\sim$ 3 × 10 <sup>-5</sup>	

To get a more precise estimate, we turn to the configuration interaction (CI) method. We calculate the transition amplitudes from the  $5p^510s$  <sup>2</sup>[3/2]<sup>o</sup><sub> $J=2$ </sub> state to five lower states of the  $5p^56p$  configuration and from the  $5p^56f^2[5/2]_{J=2}$  state to six states of the  $5p^55d$  configuration. The calculated *E*1 transition amplitudes are presented in Table I. The main source of uncertainties is the incompleteness of the basis. Given that the main contributions are included and that the results are stable against variation of the basis, we estimate that the uncertainty for the *E*1 transition amplitudes should not exceed 20%. The uncertainties for the linewidths are larger because the amplitudes are squared in the transition probabilities and because higher lying states, to which decay can occur, are neglected in the calculations. We estimate the uncertainties for the linewidth calculations to be ∼50%.

The results for the linewidths of states  $(1)$  and  $(2)$  are listed in Table I. The corresponding lifetimes are  $\tau_{10s} = 500(250)$ ns,  $\tau_{6f} = 170(85)$  ns. The theoretical result for the lifetime of the 6*f* state is consistent with the experimental value of 153(12) nsec presented in Ref. [\[11\]](#page-9-0).

### **B. PNC and Stark mixing**

One possibility in using states [\(1\)](#page-0-0) and [\(2\)](#page-0-0) for PNC studies in xenon is to perform an experiment similar to that in dysprosium [\[3\]](#page-9-0), in which the interference between Stark mixing and PNC mixing of the two degenerate states of opposite parity was studied. The mixing is determined by the matrix elements of the weak interaction and the electric-dipole interaction between states  $(1)$  and  $(2)$ ,

$$
W = \langle 1 | H_W | 2 \rangle \quad \text{and} \quad D = -\langle 1 | e \mathbf{r} | 2 \rangle. \tag{4}
$$

The Hamiltonian  $H_W$  of the weak interaction is given by

$$
H_W = -\frac{G_F}{2\sqrt{2}} Q_W \gamma_5 \rho(r). \tag{5}
$$

The  $G_F$  in (5) is the Fermi constant of the weak interaction  $(G_F \approx 2.2225 \times 10^{-14} \text{ a.u.}), Q_W$  is the nuclear weak charge,  $\gamma$ <sub>5</sub> is a Dirac matrix, and  $\rho$ (**r**) is the nuclear density normalized to 1 ( $\int \rho dV = 1$ ).

Within the standard model the weak nuclear charge  $Q_W$  is given by [\[12\]](#page-9-0)

Here *N* is the number of neutrons and *Z* is the number of protons. For example, for <sup>132</sup>Xe,  $Q_W = -73.17$ .

The matrix elements  $W$  and  $D$  in Eq. (4) have nonzero values due to configuration mixing in either odd- and evenparity states. Indeed, the parity violating matrix elements of the weak interaction are nonzero only for states of the same total angular momentum *J*, opposite parity, and whose configurations are different only by one electron. For the electric dipole operator the selection rule for the total angular momentum is  $|\Delta J| \leq 1$ . For such configurations, the matrix element between many-electron states is reduced to the singleelectron matrix element between two different single-electron states.

The nominal configurations of states  $(1)$  and  $(2)$  differ by the 10*s* and 6*f* orbitals. The matrix elements of the weak (*W*) and the electric dipole (*D*) interactions between these states are zero. One has to include mixing of appropriate configurations to either of the states  $(1)$  or  $(2)$  to obtain nonzero matrix elements. The dominant contribution arises when mixing with the  $5p^5np_{1/2}$  configurations is included in the wave function of the  $5p^56f$  state [\(2\)](#page-0-0). The corresponding diagram is shown in Fig. 2. There are seven similar diagrams that can be obtained from Fig. 2 by moving the operator of the weak or the electric dipole interaction in turn to every electron line and by swapping the 6*f* and 5*p* orbitals on the right.

To calculate the matrix element corresponding to the diagram, we need to know the many-electron wave function of each of the initial and final states  $(1)$  and  $(2)$ . It is convenient to use the hole-particle representation for the wave functions. In this representation, the wave function of the odd-parity state [\(1\)](#page-0-0) is simple. It contains one 10s electron and one  $5p_{3/2}$  hole. Since the total angular momentum is two, there is only one way to obtain  $J = 2$  and  $J_z = 2$ —by combining the  $10s_{1/2,1/2}$ electron state with the  $5p_{3/2,3/2}$  hole state. The corresponding wave function is just the product of two single-particle wave functions.

The  $5p6f$ ,  $J = 2$  state is more complicated and standard configuration interaction (CI) techniques and angular momentum algebra are used to construct it. The expansion of this state over states composed of the single-electron state 6*f* and the single-hole state 5*p* is presented in Table [II.](#page-3-0)



FIG. 2. The dominant diagram for the weak matrix element between the near-degenerate states [\(1\)](#page-0-0) and [\(2\)](#page-0-0). Dashed line is the Coulomb interaction, and the cross stands for the weak interaction. Other diagrams can be obtained by adding an exchange diagram (swapping states 6*f* and 5*p*) and by moving the operator of the weak interaction in turn to every other electron line. Similar diagrams describe the electric dipole transition amplitude. In the latter case, the cross would stand for the electric dipole operator.

<span id="page-3-0"></span>TABLE II. Expansion of the state  $5p6f$   $J = 2, J_z = 2$  over states with different total angular momentum *j* and its projection  $j_z$  (|5*p*6*f* <sup>2</sup>[5/2]<sub>22</sub> $\rangle = \sum_i c_i |6f_{j_im_i}5p_{j'_im'_i}$  $\rangle$ ).

		6 f		5 <i>p</i>	
i	$c_i$	$J_i$	$m_i$	j¦	$m_i'$
1	0.046866	7/2	1/2	3/2	3/2
2	$-0.104795$	7/2	3/2	3/2	1/2
3	0.181510	7/2	5/2	3/2	$-1/2$
$\overline{4}$	$-0.277262$	7/2	7/2	3/2	$-3/2$
5	0.000855	5/2	3/2	1/2	1/2
6	$-0.001912$	5/2	5/2	1/2	$-1/2$
7	0.353957	5/2	1/2	3/2	3/2
8	$-0.578009$	5/2	3/2	3/2	1/2
9	0.646233	5/2	5/2	3/2	$-1/2$

The mathematical expression for the diagram presented in Fig. [2](#page-2-0) is the following:

$$
W_1 = \sum_{i,n} c_i \frac{\langle 10s | \tilde{H}_W | np \rangle \langle np, 5p | \frac{e^2}{r_{12}} | 6f_{j_i, m_i} 5p_{j'_i, m'_i} \rangle}{\epsilon_{10s} - \epsilon_{np}}.
$$
 (7)

Here  $c_i$  are the expansion coefficients from Table II,  $\hat{H}_W =$  $H_W + \delta V_W$ ,  $H_W$  is the Hamiltonian of the weak interaction [\(5\)](#page-2-0), and  $\delta V_W$  is the correction to the self-consistent Hartree-Fock potential due to the weak interaction (RPA-type correction [\[10\]](#page-9-0)). The expressions for the other seven diagrams are similar to  $(7)$ .

To calculate the weak matrix element *W* ( $W = \sum_{i=1}^{8} W_i$ ) we use the relativistic Hartree-Fock (RHF) method and the B-spline technique [\[13\]](#page-9-0). The calculations are performed in the  $V^{N-1}$  approximation with one electron removed from the uppermost  $5p$  core shell. The states of the external electron are calculated in the frozen  $V^{N-1}$  potential using the B-spline technique. Summation over *np* in (7) goes over the complete set of single-electron states constructed with the use of B-splines.

The result for <sup>132</sup>Xe is

$$
|W| = 0.34 \times 10^{-15} (-Q_W/N) \text{ a.u.} = 2.1 \text{ Hz.}
$$
 (8)

Note that the dominating term  $W_1$  (7) gives 105% of the matrix element while other seven diagrams give only −5%.

Similar calculations for the reduced electric-dipole matrix element *D* lead to

$$
A(E1) = \langle 10s5pJ = 2||E1||6f5pJ = 2 \rangle = 1.55 \text{ }ea_0 \quad (9)
$$

or

$$
A(E1)_z = 0.57 \text{ }ea_0 \to 0.024 \text{ cm}^{-1}/(\text{kV/cm}) \tag{10}
$$

for the electric dipole transition amplitude between states [\(1\)](#page-0-0) and [\(2\)](#page-0-0).

### **C. Magnetic-dipole transition amplitudes**

It is instructive to study the magnetic dipole transitions (*M*1) involving our states of interest, [\(1\)](#page-0-0) and [\(2\)](#page-0-0). The *M*1 amplitudes are sensitive to the composition of the states of interest, similar to the *E*1 transition amplitudes and the weak

matrix element *W*, and therefore provide valuable information about the composition of the states. Knowledge of these matrix elements is also needed to assess the systematic effects in PNC experiments (see, for example, Ref. [\[14\]](#page-9-0)). Moreover, here we have better control over the accuracy of the calculations, since the calculation of the *M*1 amplitudes is similar to the calculation of the *g* factors, and *g* factors of many states of xenon are known from experiment.

In this section we study the *M*1 transitions between the odd-parity state [\(1\)](#page-0-0) and states of the  $5p^5 5d$  configurations, and the even-parity state [\(2\)](#page-0-0) and states of the  $5p<sup>5</sup>6p$  configuration. We limit ourselves to states of total angular momentum  $J = 2$ . The former transitions can be described as the 10*s*-5*d* singleelectron transitions while the later as the 6*f* -6*p* single-electron transitions. The corresponding single-electron matrix elements are relatively small,

$$
\langle 10s_{1/2}||M1||5d_{3/2}\rangle = 0.0107 \,\mu_0,\tag{11}
$$

$$
\langle 6f_{5/2}||M1||6p_{3/2}\rangle = 0.0067 \,\mu_0,\tag{12}
$$

where  $\mu_0$  is the Bohr magneton. These values were obtained in the RPA calculations. They are dominated by the corepolarization effect (also known as the RPA correction).

At first glance, the transitions between many-electron states should be reduced to the matrix elements  $(11)$  and  $(12)$  with some modification due to configuration mixing. In fact, the nature of the many-electron transitions is completely different and the matrix elements  $(11)$  and  $(12)$  play little role in it. For example, in the case of the 10*s*-5*d*, the single-electron transition amplitudes when configuration mixing is included can be reduced to

$$
\langle 1\tilde{0}s||M1||\tilde{5d}\rangle = \alpha \langle 10s||M1||5d\rangle + \beta \langle 10s||M1||10s\rangle + \gamma \langle 5d||M1||5d\rangle.
$$
 (13)

For pure configurations  $\alpha = 1$  and  $\beta = \gamma = 0$ . When configuration mixing is included *α* ∼ 1; *β*, *γ*  $\ll$  1. However, the second and third terms in Eq.  $(13)$  dominate over the first one in spite of the small values of  $\beta$  and  $\gamma$ , because these *M*1 matrix elements have values of  $~\sim \mu_0$ , as these belong to transitions between states with the same principal and angular quantum numbers *n,l* (i.e., diagonal in *n,l*) while also satisfying  $\Delta j = 0, \pm 1$ . This leads us to the contributions which have diagonal *M*1 single-electron matrix elements or matrix elements between the fine-structure partners. Therefore, an estimate for the  $5p^510s-5p^55d$  transitions can be written as

$$
M1 \approx \frac{\tilde{g}(10s, 5p, 5d, 5p)}{\epsilon_{10s} - \epsilon_{5d}} \mu_0,\tag{14}
$$

where  $\tilde{g}(a,b,c,d) = g(a,b,c,d) - g(a,b,d,c)$  is the sum of the direct and the exchange Coulomb integrals. Substituting these numbers leads to  $M1 \sim \mu_0$ .

For a more accurate estimate we turn to the CI calculations and we start from the *g* factors to get some idea about the accuracy of the calculations. The values of the *g* factors can be expressed via diagonal *M*1 matrix elements as

$$
g_a = \frac{1}{J_a} \begin{pmatrix} J_a & 1 & J_a \\ -J_a & 0 & J_a \end{pmatrix} \langle a||M1||a\rangle, \tag{15}
$$

where  $J_a$  is the total angular momentum of the state  $a$ .

<span id="page-4-0"></span>TABLE III. Experimental and calculated *g* factors of the states of the  $5p^55d$ ,  $5p^510s$ ,  $5p^56p$ , and  $5p^56f$  configurations with total angular momentum  $J = 2$ .

		Energy $(cm^{-1})$	g factors		
N	Configuration		Experiment	Calculations	
1	$5p^55d$	80 323	1.3750	1.35	
2	$5p^55d$	81925		0.95	
3	$5p^55d$	91 153		0.79	
4	$5p^55d$	91 447	1.274	1.25	
5	$5p^510s$	94 760	1.512	1.50	
6	5p <sup>5</sup> 6p	78 120	1.11103	1.10	
7	5p <sup>5</sup> 6p	79 212	1.3836	1.39	
8	5p <sup>5</sup> 6p	89 162	1.190	1.17	
9	$5p^56f$	94 737	1.09	1.11	
10	$5p^56f$	94 760	0.87	0.84	

The results for the *g* factors are presented in Table III together with available experimental data. The deviation of the theory from the experiment does not exceed 4%. Given that the accuracy for the diagonal matrix elements is often higher than that for the off-diagonal ones, we can say that this finding is consistent with our earlier estimate of the 20% uncertainty for the electric dipole matrix elements. To be on the safe side we adopt the same 20% uncertainty for the *M*1 transition amplitudes. The results are presented in Table IV. Note that some amplitudes for the transitions between states of the  $5p<sup>5</sup>10s$  and  $5p<sup>5</sup>5d$  configurations are larger than the single-electron matrix element [\(11\)](#page-3-0). One can say that configuration mixing can lead to enhancement of the *M*1 transition amplitudes.

# **D. Comparison with dysprosium**

It is interesting to compare the weak matrix element between the degenerate states of Xe  $[(1)$  $[(1)$  and  $(2)]$  $(2)]$ , with the weak matrix elements of the degenerate states A and B for Dy [\[3,15\]](#page-9-0). The experimental value for Dy is  $|W_{AB}|=|2.3 \pm 2.9 \pm 0.7|$ Hz [\[3\]](#page-9-0), while the theoretical value is  $W_{AB} = 4(4)$  Hz [\[15\]](#page-9-0). Note that highly excited  $np_{1/2}$  states give significant contribution to the value [\(8\)](#page-3-0) for the weak matrix element for Xe, making it smaller. Such states were not included into calculation of the weak matrix element for Dy. At the present level of accuracy

TABLE IV. Calculated magnetic-dipole transition amplitudes (reduced matrix elements given in units of Bohr magneton  $\mu_0$ ) between the states numerated in Table III (labeled here as *N* and *N* ).

$N-N'$	M1	$N-N'$	M1
	$10s-5d$ transitions		$6f$ - $6p$ transitions
$5-1$	0.20(4)	$9-6$	0.0064(13)
$5-2$	0.052(10)	$9 - 7$	0.023(5)
$5-3$	0.023(5)	$9-8$	0.0093(19)
$5 - 4$	0.26(5)	$10-6$	0.0030(6)
	$6f-6f$ transition	$10-7$	0.0011(2)
$9-10$	0.19(4)	$10-8$	0.0089(18)

the predicted values of the PNC matrix elements for these two systems are similar.

### **III. STARK EFFECT OF THE 6** *f* **STATES**

To study the states of prospective PNC measurements, the Stark shift of the energies of two 6*f* states with total angular momentum  $J = 2$  in a uniform dc electric field were measured. One state is the  $5p^56f^2[5/2]_2$  with energy  $E = 94759.935$ cm<sup>-1</sup> [\(2\)](#page-0-0) and the other state is the  $5p^56f^2[3/2]_2$  state with energy  $E = 94737.121$  cm<sup>-1</sup> [Fig. [1\(a\)\]](#page-1-0).

From the energy shifts and splittings of the lines, one can deduce the scalar and tensor polarizabilities, and therefore identify respective contributions from nearby opposite-parity states [\[16–18\]](#page-9-0).

### **A. Experimental apparatus and methods**

For the measurement of the Stark shift of the 6*f* states a 2+1 resonance-enhanced multiphoton ionization (REMPI) scheme using light at about 211 nm was implemented [\[19\]](#page-9-0). A schematic diagram of the experimental setup is presented in Fig. [1,](#page-1-0) and the details of the apparatus can be found in Refs. [\[20–22\]](#page-9-0).

An atomic beam of Xe atoms was supersonically expanded through a homemade piezoelectrically actuated nozzle valve (∼1 mm orifice diameter, backing pressure 1 atm) [\[22\]](#page-9-0). The atomic beam was skimmed and collimated, and ∼10 cm from the nozzle was intersected at right angles by a linearly polarized pulsed-laser beam. In the interaction region, the atomic beam density was estimated to be 10<sup>14</sup> atoms*/*cm3, and the residual gas pressure in the vacuum chamber was  $\sim 10^{-6}$  mbar.

The 211 nm light was generated with a tunable dye laser (Lambda Physik LPD300) that was pumped with a XeCl excimer laser LPX. The laser operated at a repetition rate of 10 Hz and had a pulsewidth of ∼30 ns, while the laser linewidth was approximately 0.2 cm<sup>−</sup>1. To produce the desired fundamental wavelength ( $\lambda \sim 422$  nm), stilbene 3 dye was used. The typical output pulse energy was ∼7 mJ. A BBO-II crystal was used to frequency double the output of the dye laser, producing the desired 211 nm radiation. Typical pulse energies of the light at 211 nm were ∼0.5 mJ.

The particular states of interest were populated via twophoton absorption ( $\lambda \sim 211$  nm) starting from the ground state  $5p^6$  ( $^1S_0$ ). The laser and atomic beam interaction region lies in the focus of the ion-imaging system consisting of a single-electrode repeller grid (60 mm outer diameter and 2 mm aperture) and grounded extractor with a 20 mm aperture [see Fig. [1\(b\)\]](#page-1-0) [\[21\]](#page-9-0). The 2 mm hole on the repeller was also covered with a flat grid (1000 lines/in.) to ensure homogeneity of the electric field. The distance between the repeller and the extractor was set at 2.5 mm. High voltage, up to 9 kV, is applied to the repeller grid using a high-voltage feedthrough. Calibration of the supplied voltage was performed using a high-voltage probe (Tektronix P6015A).

Following the two-photon excitation to a resonant state, the absorption of an additional 211 nm photon ionizes the excited atom. The produced ions, located in the center of the repeller-extractor arrangement, are accelerated in a time-of-flight (TOF) apparatus toward a microchannel-plate

<span id="page-5-0"></span>TABLE V. Selection rules for the  $J = 0 \rightarrow J = 2$  two-photon monochromatic excitation for the geometry shown in Fig. [1](#page-1-0) (electric field along  $\hat{z}$  axis, and laser beam propagating along  $\hat{y}$  axis). The quantization axis is chosen parallel to the electric-field axis (*z* axis). Controlling the polarization of the laser beam, different Zeeman sublevels of the excited state with angular momentum  $J = 2$  can be identified.

Polarization of laser beam		Zeeman sublevels	
$\hat{x}$	$\Delta M = 0$		$\Delta M = \pm 2$
$\hat{z}$	$\Delta M = 0$		
$\frac{1}{\sqrt{2}}(\hat{x} + \hat{z})$	$\Delta M = 0$	$\Delta M = \pm 1$	$\Delta M = \pm 2$

(MCP) detector. In the presence of a dc static electric field (the one used for the acceleration in the TOF apparatus), the atomic levels are shifted due to the Stark effect, and therefore the frequency for the two-photon absorption changes. Maximizing the signal on the MCP detector by adjusting the wavelength of the laser, allows one to directly measure the resonant transition wavelength for a specific value of the electric field, and consequently measure the Stark effect of the state of interest. The MCP signal was displayed on a digitizing oscilloscope (LeCroy WaveRunner 104MXi-A) which permitted signal averaging. Approximately 40 pulses were averaged per each data point. For each relevant transition, we performed three wavelength scans as a function of the electric field. At the end of each scan, the grating position of the dye laser for zero electric field was recorded. Determination of the wavelength of the transition in the absence of electric field was possible by adjusting the delay between the laser pulse and the rapid switching-on of the electric field after the excitation or ionization has taken place. The resolution on the position of the grating was 0.001 nm.

Finally, the orientation of the polarization of the laser beam with respect to the electric field was controlled with a *λ/*2 waveplate (Fig. [1\)](#page-1-0), allowing us to identify the observed shifted lines with particular Zeeman sublevels of the state under investigation, by exploiting the selection rules for transitions driven by two photons of the same color  $[23]$  for the specific geometry of our experiment (Table V).

### **B.** Electric-field calibration: Stark effect of the  $n = 2$ **states in hydrogen**

To verify the performance of the apparatus for the investigation of the Stark effect in the excited states of Xe we measured the Stark effect on the two-photon 1*s*-2*s* transition of the hydrogen atom (at 243 nm). The Stark splitting and mixing of the  $2s_{1/2}$  and  $2p_{\{1/2,3/2\}}$  states of atomic H can be calculated exactly and therefore provide an accurate determination of the electric field strength in the interaction region [\[24–26\]](#page-9-0).

*Method.* The presence of diffusion-pump oil in the chamber is the main source of H atoms in our experiment. A  $(2+1)$ REMPI scheme at 243 nm was used to excite and ionize H atoms produced by the photodissociation of pump-oil hydrocarbons. The photodissociation produces a top-hat Doppler frequency profile approximately  $4 \text{ cm}^{-1}$  wide. For low electric fields, the large Doppler widths on the observed line mask the expected Stark shifts of the  $n = 2$  states (of the order of a few wave numbers). For that reason, a Doppler-free  $(2+1)$ REMPI scheme was adopted to produce and ionize H atoms at a single laser wavelength regardless of the atoms' laboratoryframe velocity (Doppler shift) using circularly polarized light [\[27,28\]](#page-9-0). Doppler-free excitation produces narrow absorption features, increasing the electric-field detection sensitivity through the Stark effect  $[26]$ . By varying the intensity of the laser we have verified that light-induced (ac) Stark shifts are negligible.

For the production of 243 nm radiation, Coumarin 120 dye was used, yielding energies of ∼1 mJ per pulse at 243 nm (after the frequency-doubling stage). For the realization of a Doppler-free REMPI scheme, additional optics were used [see Fig.  $1(b)$ ]. The linear polarized beam was converted to a circularly polarized beam using a *λ/*4 waveplate, and focused in the center of the repeller and extractor geometry using a  $f = 15$  cm lens. Upon exiting the chamber, the beam passed through another lens ( $f = 20$  cm), creating a collimated beam, which was then reflected back to the chamber with the use of a plane mirror [dashed box in Fig.  $1(b)$ ]. Between the lens and the retroreflecting mirror, an additional  $\lambda/4$  waveplate was used to control the polarization of the reflected light. Spatial overlap in the focus was ensured by directing the reflected beam back through the initial beam path, and by adjusting the position of the retroreflecting mirror to produce a beam matched with the input one. Creating counterpropagating beams by using a mirror reflection, introduces a delay between the two beams (in our case ∼2 ns) but temporal overlap was ensured by the fact that the laser pulse width is ∼30 ns, maintaining, thus, a high ionization efficiency [\[28\]](#page-9-0). Calibration of the polarization of the counterpropagating beams was performed by exploiting the selection rules for two-photon transitions. The 243 nm resonant signal disappears when the counterpropagating beams have opposite helicities.

*Results and analysis.* In Fig. [3](#page-6-0) we present the results of the calibration experiment. The solid lines (Fig. [3\)](#page-6-0) represent the theoretical calculations for the Stark shift of the  $n = 2$  states in H as a function of the electric field.

In the absence of electric field, only the two-photon transition to the  $2s_{1/2}$  state is allowed. With increasing electric field, the  $2p_{1/2}$  component of the mixed state appears and is red-shifted, while the  $2p_{3/2}$  component of the mixed state is blue-shifted. For sufficiently high electric fields ( $\geq 4$  kV/cm) the fine structure is negligible and  $j$  is not a good quantum number. In two-photon processes, for collinear and of equalfrequency photons, the selection rules state that the photons cannot participate in any process that would require them to be in a state of total angular momentum one [\[23\]](#page-9-0). Therefore as a function of the electric field, the probability of exciting into states characterized by angular momentum of one should tend to zero. That is apparent in Fig.  $1(b)$  of Ref. [\[26\]](#page-9-0), where the normalized two-photon absorption line intensities are presented. Note that for fields higher than 5 kV*/*cm the 2*s*1*/*<sup>2</sup> intensity drops to less than ∼5% of its initial value. This fact explains the inability to observe transitions to the  $2s_{1/2}$  in our experiment, where for low electric fields the signal-to-noise ratio was approximately SNR ∼ 5. For this work we chose to take data at electric fields higher than 4 kV*/*cm for better resolution. Moreover, the interaction of

<span id="page-6-0"></span>

FIG. 3. (Color online) Theory and experimental data for the Stark effect of the two-photon 1*s*-2*s* transition of hydrogen. The calculated shifts for the mixed  $2s_{1/2}$  (orange, dashed),  $2p_{1/2}$  (gray, solid), and  $2p_{3/2}$  (blue, solid) states are presented as a function of the electric field strength. The zero value in the energy axis which corresponds to the unperturbed energy of the  $2p_{1/2}$  state, and consequently the energy splittings between the  $2p_{1/2}$  state and the  $2s_{1/2}$  and  $2p_{3/2}$  states, represent the Lamb shift and the fine-structure splitting, respectively [\[7\]](#page-9-0) (see inset). The unperturbed  $2p_{3/2}, m_j = \pm 3/2$  (blue, dashed) state is also presented. The hyperfine structure is neglected under our experimental conditions; see text for discussion.

the atom with the electric field does not mix states of different  $m_j$  when the quantization axis is chosen parallel to the electric field [\[29\]](#page-9-0), and therefore the  $2p_{3/2}$ , $m_{j=\pm 3/2}$  sublevels remain unperturbed by the presence of the electric field (as seen in Fig. 3). In addition, note that for the polarizations chosen in our experiment, the transition to the  $2p_{3/2}$ , $m_{j=\pm 3/2}$  could not be observed. Furthermore, the hyperfine structure of hydrogen is neglected, as the hyperfine splittings of the  $n = 2$  levels of hydrogen are much smaller than our experimental energy resolution [\[30\]](#page-9-0), while Stark shifts of the hyperfine structure for the electric-field strengths used, are negligible [\[31\]](#page-9-0).

The dye laser's grating positions corresponding to signal peaks were recorded for each value of the electric field. Each data point shown in Fig. 3 represents the average from three consecutive scans. The error bar for each point shown in Fig. 3 includes the correlated systematics which correspond to the uncertainty in the reading of the grating position.

The experimental data are in good agreement with the theoretical predictions, as seen in Fig. 3, verifying the performance of the apparatus for the Stark-shift measurements of the 6*f* states of Xe presented in the next section.

### **IV. RESULTS AND DISCUSSION**

### **A. Stark effect of 6** *f* **states**

In Fig. 4 we present the Stark-shift measurements of the 6*f* states. There are two important features of these shifts which should be noted. First, in the case of the  $6f^2[5/2]_2$  state [\(2\)](#page-0-0), the magnitude of the shift  $(15–20 \text{ cm}^{-1})$  is much larger than the energy interval between states [\(1\)](#page-0-0) and [\(2\)](#page-0-0). Therefore, the Stark shift should be generally treated nonperturbatively via



FIG. 4. (Color online) Experimental data of the Stark shift of states (a)  $6f^{2}[3/2]$  *J* = 2 (94 737.121 cm<sup>-1</sup>); *M* = 0 (solid line),  $|M| = 1$  (dotted line),  $|M| = 2$  (dashed line) Zeeman sublevels and (b)  $6f^{2}[5/2]$  *J* = 2 (94 759.935 cm<sup>-1</sup>), *M* = 0 (solid line),  $|M| = 2$ (dashed line) Zeeman sublevels, along with the theoretical prediction for the Stark shift of the  $|M| = 1$  Zeeman sublevels (dotted line) using the polarizability and hyperpolarizability obtained from fitting Eq. [\(17\)](#page-8-0) to the observed energy shifts of the  $M = 0$  and  $|M| = 2$ Zeeman sublevels. In both cases, the different Zeeman sublevels were identified by exploiting the degenerate two-photon selection rules (Table [V\)](#page-5-0), made possible via the control of the polarization state of the laser beam.

matrix diagonalization. Second, the shifts for both states are negative, i.e., the energy intervals between the ground state and the excited 6*f* states decrease with increasing electric field. This means that the shifts are dominated by mixing with odd-parity states above the 6*f* states. The largest contribution should come from the 6*g* states. Their position is not known experimentally but it is natural to expect that the energies of the 6*g* states are close to the energies of the 6*f* states. Indeed, both configurations correspond to almost pure Coulomb states screened from the atomic core by a centrifugal barrier. Their energies ( $E \approx -Ry/n^2$ , where *Ry* is the Rydberg constant and *n* is the principal quantum number) in the Coulomb limit do not depend on angular momentum, as confirmed by Hartree-Fock calculations.

The energy interval between the 6*f* and 6*g* states is not known, and for that reason it is treated as a fitting parameter in our analysis of the experimental data. Using the Stark-shift

TABLE VI. Stark shift matrix for the  $6f^{2}[5/2]_{J=2}$  state with  $E = 94759.935$  cm<sup>-1</sup>.  $d_1$  and  $d_2$  are the electric dipole transition amplitudes to the 10s and 6g states (see text);  $k_f$  and  $k_g$  are the second-order energy corrections due to transitions to the states not included in the matrix;  $\delta$  is the 6*f*-6*g* energy interval; and  $\mathcal{E}$  is the static electric field strength. Transition amplitudes  $d_1$  and  $d_2$  are taken from calculations; and  $k_f$ ,  $k_g$ , and  $\delta$  are treated as fitting parameters.

<b>States</b>	6 f	10s	6g
6f	$k_f \mathcal{E}^2$	$d_1 \mathcal{E}$	$d_2 \mathcal{E}$
10s	$d_1 \mathcal{E}$		0
6 <sub>g</sub>	$d_2 \mathcal{E}$		$\delta + k_g \mathcal{E}^2$

measurements for the 6*f* states, a range of values for the energy interval between the 6*f* and 6*g* states can be obtained. In particular we use the Stark-shift matrices presented in Tables VI and VII, and, for example, focus our analysis on the Stark-shift data for the  $|M| = 2$  Zeeman sublevels for both 6*f* states (Fig. [4\)](#page-6-0).

The electric-dipole matrix element  $d_1$  appearing in Table VI is given by Eq.  $(10)$ . The electric-dipole matrix elements  $d_2$ and *d*, appearing in Tables VI and VII, include all possible transitions from the  $6f^2[5/2]_2$  and the  $6f^2[3/2]_2$  states to the 6*g* states, respectively [\[32\]](#page-9-0). Theoretical estimates for these electric-dipole transition amplitudes  $d_2$  and  $d$  suggest that  $d_2 \approx d \approx 20(5) \text{ } e_{0} \rightarrow 0.86(22) \text{ cm}^{-1}/(\text{kV/cm})$ . Therefore, the small value of the electric-dipole transition amplitude between the  $6f$  and  $10s$  states,  $d_1$  [Eq. [\(10\)](#page-3-0)], should have little effect on the analysis of the measurements. This is verified by setting  $d_1 = 0$ , where we see that the Stark-shift analysis of the measurements on the  $6f^2[5/2]_2$  [Fig. [4\(a\)\]](#page-6-0) is not significantly affected. Moreover, we neglect the contribution of the 10*s* state in the Stark shift of the  $6f$  <sup>2</sup>[3/2]<sub>2</sub> state (see Table VII). This state is not so close to the 10*s* state, and thus, the corresponding mixing is further suppressed by orders of magnitude.

We proceed with the analysis of the Stark-shift measurements for the  $|M| = 2$  Zeeman subleveles of both 6*f* states by imposing two extra conditions. The parameters  $k_f$  and *kg*, appearing in the Stark-shift analysis for both 6*f* states (Tables VI and VII) are second-order energy corrections, due to transitions to states not included in the matrices. In particular, the  $k<sub>g</sub>$  parameter appearing in both matrices, is the same as it corresponds to the same set of the 6*g* states. The  $k_f$  and  $k_g$  parameters model the quadratic behavior of the Stark-shift measurements, while the other terms describe

TABLE VII. Stark-shift matrix for the  $6f^{2}[3/2]_{J=2}$  state with  $E = 94737.121$  cm<sup>-1</sup>. *d* is the electric dipole transition amplitude to the 6*g* states (see text);  $k_f$  and  $k_g$  are second-order energy corrections due to transitions to the states not included in the matrix; *δ* is the 6*f* -6*g* energy interval; and  $\mathcal E$  is the static electric field strength. Transition amplitude *d* is taken from calculations; and  $k_f$ ,  $k_g$ , and  $\delta$  are treated as fitting parameters.

<b>States</b>	6 f	6g
6f	$k_f \mathcal{E}^2$	$d\mathcal{E}$
6 <sub>g</sub>	$d\mathcal{E}$	$\delta + k_g \mathcal{E}^2$

the deviation from the quadratic behavior. The parameter *δ*, which corresponds to the energy interval between the 6*g* state and the  $6f^2[5/2]_2$  state ( $\Delta\delta = 23$  cm<sup>-1</sup> is the experimental value for the energy interval between the two 6*f* states), is included in both Stark-shift-matrix diagonalizations. For Stark shifts smaller than  $\delta$ , one expects a quadratic Stark effect, while for larger values, a linear behavior. Therefore, the parameter *δ* is constrained by the deviation from the quadratic behavior, and thus, its value is directly linked to the value of  $k_f$ . Furthermore, one sees from the analysis that for large values of  $d_2$  and *d*, one gets  $k_f > 0$  as expected, while for small values, one gets  $k_f < 0$ . Imposing these constraints on the analysis of the Stark-shift data for both 6*f* states, along with the theoretical estimations for the  $d_2 \approx d \approx 20(5)$  *ea*<sub>0</sub>, for which  $k_f > 0$ , we find an energy interval  $\delta = 30(10)$  cm<sup>-1</sup>.

For the physically expected range of values for  $k_f$  and  $\delta$ , we see from the theoretical analysis that  $k<sub>g</sub>$  is negative. This is probably due to a contribution from the 6*h* states, similar to the negative Stark shift for the 6*f* states arising due to the contributions of the 6*g* states. Therefore, the measured Stark shift of the two 6*f* states reveals the presence of the 6*g* and 6*h* states.

Finally, the data on the Stark shift for state [\(2\)](#page-0-0) can be used to put a limit on the weak mixing of the degenerate states [\(1\)](#page-0-0) and [\(2\)](#page-0-0). This is because the weak matrix element between these states and the amplitude of the electric dipole transition between them are affected by configuration mixing in a similar way. Indeed, if both matrix elements are dominated by the 10*s*-*np* transitions, then the value of both matrix elements is determined by the admixture of the  $5p<sup>5</sup>np$  configurations to the  $5p^56f$  configuration. This is estimated by the value of the  $d_1$  parameter in the Stark shift matrix (Table VI). If the calculated value of  $d_1$  ( $\approx 0.5$  *ea*<sub>0</sub>) is used, very good fitting of the experimental Stark-shift data can be achieved. However, since this matrix element is not zero due to configuration mixing only, the uncertainty in its value is large. The same is true for the weak matrix element *W* [Eq. [\(8\)](#page-3-0)]. As a way to estimate this uncertainty we check how much one can change the value of  $d_1$  without affecting the fitting of the Stark-shift data. It turns out that the analysis becomes unstable for  $d_1 > 1$  *ea*<sub>0</sub>. The instability manifests itself in the need to use large unrealistic values for the fitting parameters, and deteriorating of the quality of fitting. Taking the value  $d_1 = 1$  *ea*<sub>0</sub> as the upper limit for the electric dipole transition amplitude, we note that it is about 14 times smaller than the 10*s*-10*p*1*/*<sup>2</sup> electric dipole amplitude. Assuming the same ratio for the weak matrix elements and using

$$
\langle 10s|H_W|10p_{1/2}\rangle = 0.12 \times 10^{-13} (-Q_W/N)i\frac{e^2}{a_0},\qquad(16)
$$

obtained in the RPA calculations, we get for the weak matrix element between the degenerate states [\(1\)](#page-0-0) and [\(2\)](#page-0-0): |*W*| *<*  $0.8 \times 10^{-15} (-Q_W/N)$  *ie*<sup>2</sup>/a<sub>0</sub> = 5 Hz in agreement with the calculated value [Eq. [\(8\)](#page-3-0)].

#### **B. Polarizabilities and hyperpolarizabilities of the 6** *f* **states**

In the case of barium  $(Ba)$  [\[16\]](#page-9-0) and samarium  $(Sm)$ [\[17\]](#page-9-0), Stark-shift measurements of various states were used to estimate the value of the reduced matrix elements of the dipole operator to near opposite-parity "partner" states. This proved to

<span id="page-8-0"></span>TABLE VIII. Observed polarizabilities for each Zeeman sublevel of the  $6f[5/2]$ <sub>2</sub> states, in units of MHz/(kV/cm)<sup>2</sup>.

<b>State</b>	$\alpha(M=0)$	$\alpha( M =1)$	$\alpha( M =2)$	
$6f[3/2]_2$	728(9)	671(8)	762(11)	
$6f[5/2]_2$	1370(11)		1344(12)	

be possible, in most cases, because the observed shifts and sublevel splittings for each state under investigation were the result of contribution by one or a few dominating near opposite-parity partner states in each case (which dominate due to the smallness of the energy-difference denominator). In the case of Xe it appears that this is not possible, and a more refined level of theoretical calculations is required to determine all the reduced matrix elements between the 6*f* states and the 6*g* states.

In this section we present an analysis of the Stark shifts for all the observed Zeeman sublevels of the 6*f* states,

presented in Fig. [4,](#page-6-0) in terms of the polarizabilities and hyperpolarizabilities, following closely the work described in Ref. [\[16\]](#page-9-0) (and references therein).

The polarizability *αηJM* and hyperpolarizability *γηJM* of the state  $|\eta J M\rangle$  is determined from the dependence of the observed energy shifts on the electric field by fitting the data with the following equation:

$$
\Delta E_{\eta JM} = -\frac{1}{2} \alpha_{\eta JM} E^2 - \frac{1}{4!} \gamma_{\eta JM} E^4. \tag{17}
$$

The polarizability  $\alpha_{nJM}$  can be expressed in terms of its scalar and tensor parts as

$$
\alpha_{\eta JM} = \alpha_{0,\eta JM} + \alpha_{2,\eta JM} \frac{3M^2 - J(J+1)}{J(2J-1)},
$$
 (18)

and the hyperpolarizability  $\gamma_{\eta JM}$  can be expressed in terms of its scalar and tensor parts as

$$
\gamma_{\eta JM} = \gamma_{0,\eta JM} + \gamma_{2,\eta JM} \frac{3M^2 - J(J+1)}{J(2J-1)} + \gamma_{4,\eta JM} \frac{35M^4 + [25 - 30J(J+1)]M^2 + J(J-1)(J+1)(J+2)}{J(2J-1)(2J-3)(2J-2)}.
$$
\n(19)

In Tables VIII and IX we present the polarizabilities and hyperpolarizabilities of the 6*f* states obtained in this work. Note that the polarizability of the ground state of Xe is neglected, as the energy shifts of the  $5p<sup>6</sup>$  ground state for the maximum electric fields used in our studies are of the order of a few ∼MHz [\[34\]](#page-9-0) and therefore are negligible compared to the observed shifts.

Using the values for the  $\alpha_0$  and  $\alpha_2$  of the 6*f* <sup>2</sup>[5/2]  $J = 2$  state (Table VIII), we predict the energy shift for the  $|M| = 1$  Zeeman sublevels that we were not able to identify by exploiting the selection rules of the two-photon transition (see Table [V\)](#page-5-0). In addition, because a large deviation from quadratic behavior is observed in the energy shift of the  $6f^{2}[5/2]_{2}$ , we use the hyperpolarizabilities  $\gamma$  obtained from the energy shifts of the  $|M| = 0.2$  sublevels (Table IX) to estimate  $\gamma(|M| = 1)$ . In Fig.  $4(b)$  the prediction for the energy shift of the  $|M| = 1$ sublevel is presented. The predicted overlap between the  $|M| = 1$  and the  $|M| = 2$  Zeeman sublevels explains the inability to identify the Stark shift of the  $|M| = 1$  sublevels considering the experimental resolution of our apparatus (note that the uncertainty in the reading of the dye laser's grating position was  $\sim$ 0.22 cm<sup>-1</sup>).

The Stark shifts of the observed Zeeman sublevels of the  $6f[3/2]_2$  state cannot be explained using a similar procedure as the one followed for analyzing the Stark-shift data of the

TABLE IX. Observed hyperpolarizabilities for each Zeeman sublevel of the  $6f$  states, in units of kHz/(kV/cm)<sup>4</sup>.

State	$\gamma(M=0)$	$\gamma( M =1)$	$\gamma( M =2)$
$6f[3/2]_2$	$-787(107)$	$-689(95)$	125(131)
$6f[5/2]_2$	$-3776(140)$	$\overline{\phantom{0}}$	$-3095(163)$

 $6f[3/2]$ <sub>2</sub> state. The tensor energy shifts are expected to be linear in  $M^2$ , where the observed data show a different behavior. Therefore, different coupled partner states for each |*M*| sublevels are required to explain the observed spectrum. We analyze separately each observed sublevel of the state  $6f[3/2]_2$ using Eq. (17) to obtain their polarizabilities and hyperpolarizabilities. The results are presented in Tables VIII and IX.

Finally, note that the polarizabilities presented in Tables VIII and IX are among the largest measured for atomic systems in states with principal quantum number  $n < 10$  [\[16\]](#page-9-0).

### **V. CONCLUSIONS**

We have studied the properties of a pair of nearly degenerate opposite-parity states in atomic Xe, namely the  $5p^510s^2[3/2]_2^0$ [\(1\)](#page-0-0) and  $5p^56f^2[5/2]_2$  [\(2\)](#page-0-0) states, which are of interest for *P*- and *P,T* -odd experiments. Theoretical calculations of the width of the states, and the value for the weak matrix element between these states are presented. Furthermore, we studied the Stark shift of the even-parity 6*f* state and put a limit on the weak mixing of the  $(1)$  and  $(2)$  near-degenerate states, of  $|W|$  < 5 Hz. The analysis of the experimental Stark-shift measurements also revealed the presence of the 6*g* and 6*h* states in atomic Xe, which have been unobserved so far.

### **ACKNOWLEDGMENTS**

The experimental work was conducted at the Ultraviolet Laser Facility at FORTH-IESL, supported in part by the EC FP7 project LASERLAB-EUROPE (Grant Agreement No. 284464). This work is supported by the European Research Council (ERC) Grant TRICEPS (GA No. 207542), by the National Strategic Reference Framework (NSRF)

<span id="page-9-0"></span>Grant Heracleitus II (MIS 349309-PE1.30) co-financed by EU (European Social Fund) and Greek national funds, by the Australian Research Council, by the Marie Curie Initial Training network ICONIC (PITN-GA-2009-238671), and by the Greek Secretariat of Research and Technology (GSRT) under the THALIS program ISEPUMA. P.C.S. gratefully

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acknowledges financial support from a European Union Marie Curie Reintegration Grant ("GPSDI," Grant No. PIRG07- GA-2010-268305). T.N.K. also acknowledges support by the Alexander von Humboldt foundation. J.S. was supported in part by NSF Grant PHY1068065. D.B. was supported by NSF, Grant PHY-1068875.

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