

Isotope shifts of natural Sr^+ measured by laser fluorescence in a sympathetically cooled Coulomb crystal

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We measured by laser spectroscopy the isotope shifts between naturally occurring even isotopes of strontium ions for both the $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ (violet) and the $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ (infrared) dipole-allowed optical transitions. Fluorescence spectra were taken by simultaneous measurements on a two-component Coulomb crystal in a linear Paul trap containing 10^3 – 10^4 laser-cooled Sr^+ ions. The isotope shifts are extracted from the experimental spectra by fitting the data with the analytical solution of the optical Bloch equations describing a three-level atom interacting with two laser beams. This technique allowed us to increase the precision with respect to previously reported data obtained by optogalvanic spectroscopy or fast atomic-beam techniques. The results for the $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ transition are $\nu_{88} - \nu_{84} = +378(4)$ MHz and $\nu_{88} - \nu_{86} = +170(3)$ MHz, in agreement with previously reported measurements. In the case of the previously unexplored $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ transition we find $\nu_{88} - \nu_{84} = -828(4)$ MHz and $\nu_{88} - \nu_{86} = -402(2)$ MHz. These results provide more data for stringent tests of theoretical calculations of the isotope shifts of alkali-metal-like atoms. Moreover, they simplify the identification and the addressing of Sr^+ isotopes for ion frequency standards or quantum-information-processing applications in the case of multi-isotope ion strings.

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I. INTRODUCTION

Isotope shift measurements by optical spectroscopy provide information about nuclear structure and constitute an important complement to nuclear-physics experiments that investigate nuclear-charge distribution (e.g., muonic x-ray isotope shifts or electron scattering) [1]. The case of strontium ($Z = 38$) is particularly studied because it belongs to the elements close to the $Z = 40$ subshell closure that causes rapid variation of the nuclear properties as a function of the neutron number [2]. In order to extract information about the nucleus, spectroscopic data (i.e., isotope shifts and hyperfine splitting) have to be compared to some theoretical model that is able to evaluate the “electronic factors” that take into account the effect of nuclear-charge distributions on the electronic wave functions. For the alkaline-earth elements, these factors are calculated in an easier way for the singly ionized state, with a single electron in the outer shell. Recently, impressive progress has been made in performing these calculations that estimate hyperfine structures and the sequences of energy levels, especially in the case of strontium [3]. Typical precisions for these calculations can reach terahertz for the energy levels and some tens of megahertz for the isotope shifts [4]; therefore experimental data are important to put constraint on calculated shifts.

From an experimental point of view, the first quantitative data about isotope shifts of dipole-allowed transitions in Sr^+ were obtained by hollow-cathode spectroscopy [5] that reached a precision of 8 MHz using a Doppler-free technique [6]. The development of the method of fast-beam

laser spectroscopy in a particle accelerator [7] opened the possibility to study a larger number of isotopes (including the unstable ones) and increased the precision to better than 5 MHz in the most favorable cases. In the particular case of Sr^+ , the data made available by this technique concern the $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{3/2}$ transition ($\nu = 735$ THz, $\lambda = 408$ nm) for all the isotopes between ^{78}Sr and ^{100}Sr [2], as well as some preliminary data for the $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ transition ($\nu = 711$ THz, $\lambda = 422$ nm) for $^{84}\text{Sr}^+$, $^{86}\text{Sr}^+$, and $^{87}\text{Sr}^+$ [8] (all the shifts are measured with respect to the most abundant isotope $^{88}\text{Sr}^+$). This technique also gives reliable information about hyperfine splitting of the odd isotopes with a precision still of the order of 5 MHz. Fast-beam laser spectroscopy is based on the excitation of a strong dipole-allowed transition from the fundamental state. This circumstance allows for direct detection of the fluorescence or for accumulation in a metastable state that can be state-selectively neutralized or ionized [7]. While very important for nuclear physics, the technique is not well adapted to the study of dipole-forbidden transitions or transitions from an excited state. Another possibility to obtain such spectroscopic information is offered by laser-cooled trapped-ion experiments, which can provide data with a precision limited by only signal-to-noise issues, with the Doppler broadening being negligible. Some alkaline-earth ions [9] and other species [10] have been studied by this technique, providing also useful data for quantum information experiments based on trapped ions. The use of trapped ions as frequency standards in the optical domain (in particular the $^{88}\text{Sr}^+$ ion [11]) triggered several measurements of the absolute frequency of the dipole-forbidden “clock” $5s\ ^2S_{1/2} \rightarrow 4d\ ^2D_{5/2}$ Sr^+ transition ($\nu = 446$ THz, $\lambda = 674$ nm) together with its isotope shifts $\nu_{88} - \nu_{87}$ down to 40-kHz precision [12]. A recent paper reports on the $\nu_{88} - \nu_{86}$ isotope shift in this same clock transition with 4-kHz precision [13].

In the present paper we report the measurements of the isotope shifts for both natural even isotopes $^{84}\text{Sr}^+$ and $^{86}\text{Sr}^+$

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with respect to $^{88}\text{Sr}^+$. We address the case of the dipole-allowed transitions $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ ($\nu = 711\ \text{THz}$) and $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ ($\nu = 275\ \text{THz}$, $\lambda = 1092\ \text{nm}$), which we study in laser-cooled trapped-ion samples consisting of two-component Coulomb crystals [14]. This technique allows us to probe the two isotopes in the same sample during the same frequency scan, reducing the requirements for long-term laser stabilization needed in the case of sequential experiments [13]. The isotope shifts are extracted from the spectra by fitting the experimental data with the solution of the optical Bloch equations (OBE) describing a Λ three-level atom interacting with two laser beams [15]. The final precision, estimated by the dispersion of the data, is between 2 and 4 MHz, depending on the isotope and on the transition (in the case of $^{84}\text{Sr}^+$ two distinct measurement are necessary). This precision is mainly limited by the laser stabilization technique. As mentioned above, such information can inform theoretical models of isotope shifts that are, at the moment, available with larger uncertainties [4,13]. This mapping of isotope shifts in the case of Sr^+ is useful for quantum information experiments based on this species [16], especially in the case of multi-isotope sympathetically cooled ion strings [17].

This paper is organized as follows. In Sec. II we present the experimental setup, and we give some details concerning the ion trapping, the frequency stabilization of the lasers, and the isotope-enrichment procedure. Then in Sec. III we briefly present the theoretical model used to fit the experimental data. We present the results in Sec. IV, and we compare them to the literature. Finally, in Sec. V we discuss the limitations of the present measurements and some possible improvements.

II. EXPERIMENTAL METHODS

A. Trapping, cooling, and laser locking

Sr^+ ions are loaded in a linear Paul trap from an oven containing a strontium dendrite (Aldrich, 99.9% pure). Neutral atoms are ionized by driving a two-photon transition towards a self-ionizing level [18]. The photoionizing laser pulses are issued from a frequency-doubled Ti:sapphire oscillator (Tsunami, Spectra-Physics) with a central frequency of 695 THz ($\lambda = 431\ \text{nm}$) and a pulse duration of $\simeq 100\ \text{fs}$. The spectral width associated with these ultrafast pulses ($\simeq 10\ \text{THz}$) makes this loading process insensitive to both Doppler effect and isotope shift, providing samples with a composition that respects the natural abundances. The abundances of the four natural isotopes of strontium (^{84}Sr , ^{86}Sr , ^{87}Sr , ^{88}Sr) are 0.56%, 9.86%, 7%, and 82.58%, respectively. The ion-trap geometry has been described previously [19]. The trap is driven with a rf voltage amplitude $V_{rf} \sim 750\ \text{V}$ at a frequency of 7.6 MHz and typically displays a radial frequency of 200 kHz for Sr^+ . The “end cap” electrodes (arranged between the rods and separated by 26 mm) are independently brought to static voltages V_{ec} of the order of 100 V. The stray electric fields can be compensated by adding a different dc voltage on each trap rod, following a technique similar to that of Ref. [20].

Trapped Sr^+ ions (even isotopes) are Doppler cooled using the 711-THz $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ optical transition (natural linewidth $\Gamma_b/2\pi = 21.5\ \text{MHz}$; see Fig. 1). This transition is driven using laser light generated by a commercial single-mode Ti:sapphire cw laser (Coherent MBR 110) frequency

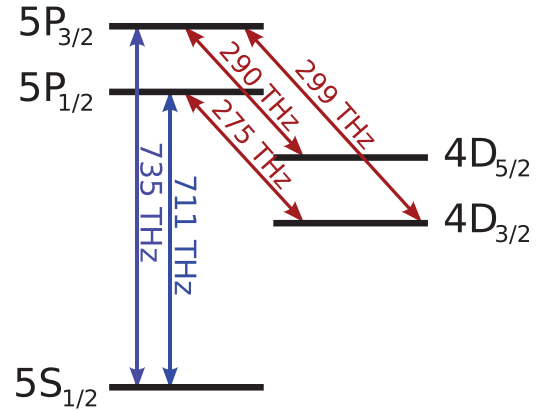


FIG. 1. (Color online) Low-energy-level scheme for Sr^+ . In the present work we address the 711-THz violet transition (cooling) and the 275-THz infrared transition (“repumping”).

doubled in a single-pass geometry using a periodically poled Potassium Titanyl Phosphate crystal (PPKTP, Raicol Crystals). Up to 20 mW are available after the doubling process and coupling into a single-mode polarization-maintaining optical fiber. The laser frequency is locked to an atomic reference, taking advantage of the near coincidence ($\nu_{\text{Sr}^+} - \nu_{\text{Rb}} = 440\ \text{MHz}$) between the $^{88}\text{Sr}^+ 5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ and the $^{85}\text{Rb} 5s\ ^2S_{1/2}(F=2) \rightarrow 6p\ ^2P_{1/2}(F'=3)$ transitions [21]. The 710 962 401 328(40) kHz absolute frequency of this ^{85}Rb transition has recently been measured by the frequency-comb technique [22].

The electronic signal for laser locking is obtained by a saturated-absorption setup based on a natural rubidium cell heated to 120 °C. The probe-beam signal is demodulated at the first harmonic of the $\sim 90\text{-kHz}$ frequency-modulation produced by the laser-driver electronics to lock the laser to the intracavity thin etalon. The residual FWHM of the saturated-absorption lines is on the order of 16 MHz, dominated by the residual (unlocked) laser linewidth and modulation (the natural linewidth being $\sim 1.3\ \text{MHz}$ [23]). The overall stability of the lock has been evaluated by monitoring the beat note between the Ti:sapphire laser and an extended-cavity GaN diode laser (TOPTICA DL100) stabilized with the same technique on the same atomic transition in a different Rb cell and then shifted by an acousto-optic modulator. The long-term (10 min) full width of the beat note acquired on a spectrum analyzer (2.5 MHz at $-3\ \text{dB}$) gives us an upper limit to the performance of the locking method. Note that all the systematic error contributions evaluated in a similar setup [22] are largely smaller than these fluctuations.

A commercial fiber laser (Koheras Adjustik Y10) drives the $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ 275-THz “repumping” transition (see Fig. 1) to avoid accumulation of the ions in the metastable $4d\ ^2D_{3/2}$ state during the cooling process. This laser has a nominal linewidth of 70 kHz, and it is stabilized against long-term drifts by a transfer-lock technique using a scanning ring cavity referenced to a stabilized 711-THz laser diode [24,25]. This feedback loop is, in our case, relatively slow (bandwidth $\simeq 3\ \text{Hz}$). Nevertheless, the computer-controlled lock allows us to scan the 275-THz fiber laser over many free spectral ranges of the ring cavity [229.2(4) MHz]. We estimated

the statistical uncertainty on the frequency of this laser by acquiring the error signal over several tens of hours. The histograms show a Gaussian behavior with a FWHM of 1.2 MHz; this quantity gives us an upper limit to the slow drift error on the “two-photon detuning” $\delta_b - \delta_r$ (see Fig. 3 below). Ring-cavity piezoactuator nonlinearities are corrected for dynamically (i.e., for each acquisition of a ring-cavity scan) in order to obtain a linear and calibrated frequency scan. After correction we estimate at 500 kHz the upper limit of the residual systematic shift affecting two frequencies separated by a free spectral range of the cavity.

A magnetic field of the order of 0.3×10^{-4} T defines a quantization axis along the trap axis, orthogonal with respect to the linear polarization of the repumping and cooling laser beams. This configuration prevents the ions from being optically pumped into a metastable dark state by the repumping laser alone [26]. However, it does not prevent the existence of “two-color” dark states that cause a dip in the infrared spectra for $\delta_r = \delta_b$ [27] (see Fig. 3 below). As explained in the following, we take advantage of this circumstance to measure violet and infrared isotope shifts in a single-frequency scan. The presence of a longitudinal magnetic field induces a Zeeman splitting of the $5s\ ^2S_{1/2}$, $4d\ ^2D_{3/2}$, and $5p\ ^2P_{1/2}$ levels. As explained below, these splittings induce a broadening of the (unresolved) dark resonance of the order of 2 MHz.

B. Isotope enrichment and addressing

After loading the trap, the composition of the Doppler-cooled Coulomb crystal can be modified by taking advantage of both the radial segregation induced by the mass differences and the axial segregation induced by the radiation pressure of the axial cooling beams. For example, as described in detail elsewhere [28], by lowering the potential of the end cap corresponding to the input side of the cooling beams, it is possible to selectively remove the uncooled species (dark ions) that are not pushed towards the other side of the trap. Such a strategy requires laser addressing at least two different isotopes [for both cooling (711 THz) and repumping (275 THz) transitions]. By this technique we routinely obtain almost-pure two-isotope Coulomb crystals consisting of up to 10^4 $^{88}\text{Sr}^+$ + 10^4 $^{86}\text{Sr}^+$ ions or 10^3 $^{86}\text{Sr}^+$ + 10^3 $^{84}\text{Sr}^+$ ions.

The 711-THz beam (frequency locked to the ^{85}Rb transition) is split into two separate beams in order to address simultaneously two isotopes (either $^{88}\text{Sr}^+$ + $^{86}\text{Sr}^+$ or $^{86}\text{Sr}^+$ + $^{84}\text{Sr}^+$). Each of these beams is then frequency upshifted by a double-pass acousto-optical modulator (AOM). When addressing a $^{88}\text{Sr}^+$ + $^{86}\text{Sr}^+$ Coulomb crystal, the first AOM is driven by a rf source with a frequency of 220 MHz, and the second one is driven by a rf source with a frequency of 135 MHz. The 275-THz laser is also split into two beams that are frequency up- and downshifted by $\simeq 200$ MHz, respectively. As shown in Fig. 2, these frequency shifts allow us to address transitions of both $^{88}\text{Sr}^+$ and $^{86}\text{Sr}^+$ and to set detunings δ_b and δ_r (Fig. 3) within a band of ± 50 and ± 60 MHz, respectively.

While addressing the pair $^{86}\text{Sr}^+$ + $^{84}\text{Sr}^+$, the 711-THz laser is locked instead to the $^{85}\text{Rb}\ 5s\ ^2S_{1/2}(F=2) \rightarrow 6p\ ^2P_{1/2}(F'=2)$ transition, red detuned by 117 366(72) kHz with respect to the $F=2 \rightarrow F'=3$ transition [22]. In this way, driving the first violet AOM with $\simeq 180$ MHz and the

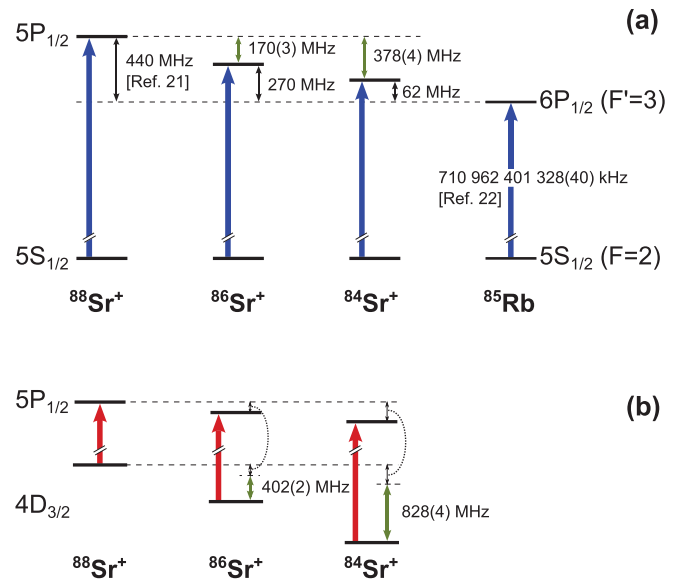


FIG. 2. (Color online) Schematic drawing of the isotope shifts of the even Sr⁺ isotopes studied in this paper. (a) $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ violet transition [711 THz, blue (dark gray) arrows]; green (light gray) arrows represent the measured isotope shifts, while black arrows indicate the frequency shift with respect to the $^{85}\text{Rb}\ 5s\ ^2S_{1/2}(F=2) \rightarrow 6p\ ^2P_{1/2}(F'=3)$ reference transition. Note that we referenced the energies to the ground states. (b) $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ infrared transition [275 THz, red (medium gray) arrows]; thick green (light gray) arrows represent the measured isotope shifts with respect to the $^{88}\text{Sr}^+$ repumping transition. As both levels are isotope shifted in this diagram, we also show the isotope shift that affects the 711-THz transition with thin black arrows. The errors given are an estimate of the statistical variance in our measurements.

second with $\simeq 85$ MHz allows us to address the cooling transitions (see Fig. 2); however, a shorter detuning range is available. The repumping beams can be simply tuned to the new isotope pair by redshifting the master 275-THz laser by ~ 400 MHz and slightly adjusting the AOM frequencies. The final precision of the isotope shift measurements relies

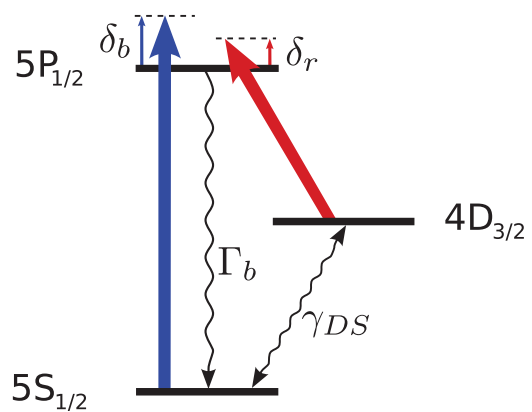


FIG. 3. (Color online) Schematic drawing of the atomic levels of Sr⁺ (Λ configuration). One laser (cooling) addresses the $S \rightarrow P$ transition with a detuning δ_b and a Rabi frequency Ω_b , while another laser (repumping) drives the $D \rightarrow P$ transition (detuning δ_r and Rabi frequency Ω_r). The decoherence rate between the D and S levels is given by γ_{DS} .

on the precision of the AOM driving frequency based on voltage-controlled oscillators (VCO). In order to take into account the possible drifts of the rf drivers, we recorded the frequencies of all the AOM drivers (measured with a spectrum analyzer) during each acquisition of a spectrum. The precision of these frequency shifts is then limited by the bandwidth of the measurement on the spectrum analyzer (~ 50 kHz), the absolute calibration error of the instrument being negligible at that level.

C. Fluorescence spectra

After loading the trap and applying the isotope-selection procedure, we acquire fluorescence spectra. The fluorescence signal is obtained by imaging the whole ion crystal on a CCD camera (Prosilica GC1600) with an $f = 58$ mm standard camera lens. Typical integration times are of the order of 1 s; the images are corrected for background that is acquired in the absence of ions at the beginning and at the end of a spectrum. Spectra are acquired in an interlaced way following this sequence: (i) The detuning of the master 275-THz laser is changed. (ii) Both isotopes are cooled for 500 ms. (iii) The lasers addressing the first isotope are switched off while the second isotope cycles in the cooling transition; one fluorescence image is taken. (iv) The lasers addressing the second isotope are switched off while the first isotope cycles in the cooling transition; one fluorescence image is taken. This procedure reduces the susceptibility of the isotope shift measurement to possible long-term drifts of the locked lasers. Moreover, sympathetic cooling makes the ion loss rate indistinguishable from that measured in a continuous cooling regime (lifetime $\simeq 3$ h for the whole crystal).

In the experiments we obtained in a single spectral determination both the isotope shifts of the $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ Sr⁺ and $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ Sr⁺ transitions. Fluorescence spectra were recorded by setting the cooling laser frequency at a moderate red detuning $\delta_b \simeq -30$ MHz and by frequency scanning the 275-THz laser beam moving the locking point of the transfer lock. In this way the repumpers of both isotopes are scanned simultaneously with a mutual detuning determined by the frequencies of the two AOM drivers, which are kept fixed during the experiment. Experiments were repeated several times for different repumper intensities and δ_b in order to verify the reproducibility and to obtain an estimate of statistical errors. Moreover, we also fixed a detuning on AOMs far from the isotope-shift matching condition: in this way the spectra of the two isotopes appear shifted by a non-negligible amount that should allow for the detection of crosstalk in the fluorescence recordings, which, however, has not been observed. As mentioned before, the spectra obtained in this way display a dip for $\delta_r = \delta_b$ [27]. This spectral feature gives us the opportunity to measure in a single spectrum the position of both transitions. This information is extracted from the experimental spectra by fitting the data with a theoretical model, as described in the next section.

III. THEORETICAL MODEL FOR THE FLUORESCENCE SPECTRA

Optical Bloch equations within a three-level model describe the behavior of a Λ atomic system driven by two lasers oc-

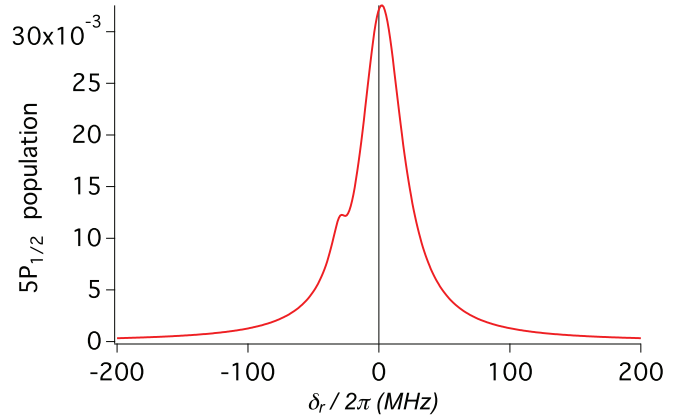


FIG. 4. (Color online) Theoretical fluorescence spectrum as a function of δ_r (optical Bloch equations). The parameters of the plot are $\Gamma_b/2\pi = 21.5$ MHz, branching ratio of 13.4 [29], $\delta_b/2\pi = -28$ MHz, $\Omega_b/2\pi = 12.9$ MHz, $\Omega_r/2\pi = 2$ MHz, and $\gamma_{DS}/2\pi = 5.7$ MHz. These parameters correspond to the fit of the rightmost spectrum in Fig. 5.

curing, for example, in laser-cooled alkaline-earth ions [15]. In brief, after applying the rotating-wave approximation and taking into account the branching ratios and decay rates from the literature ($\Gamma_b/2\pi = 21.5$ MHz, branching ratio of 13.4 [29]), the steady-state solution of the resulting equation can be analytically obtained by matrix inversion. As the transients are short compared to the averaging time, this procedure allows us to fit the experimental data (fluorescence vs δ_r) with the steady-state solution of the OBE, with the following free parameters: Ω_b (Ω_r), the Rabi frequency at the resonance of the cooling (repumping) laser; δ_b , the detuning of the cooling laser; γ_{DS} , the decoherence rate between the D and S levels; and ω_{0r} , the central angular frequency of the repumping transition. The decoherence rate γ_{PS} (γ_{PD}) between the P and S (P and D) levels is fixed to $\Gamma_b/2$.

The three-level approximation neglects multiple Zeeman sublevels but allows us to take into account the light shifts and to reproduce the shape of the experimental spectra. The output from the OBE (Fig. 4) has also been exploited in order to optimize the experimental parameters: when decreasing Ω , the spectra become narrower and should allow for a more precise determination of the $\delta_r = 0$ and $\delta_r = \delta_b$ conditions, but in the experiment, the signal-to-noise ratio decreases down to very poor levels.

Let us now discuss the role of the parameter γ_{DS} , which affects both the width and the contrast of the dip in the spectra. Taking into account the lifetime of the metastable $4^2D_{3/2}$ state [30], we expect $\gamma_{DS}/2\pi = 0.18$ Hz. The fit procedure adjusts γ_{DS} in order to take into account the experimental shape of the dip, which is, however, affected by several additional factors: the relative phase noise of the lasers, the presence of a magnetic field that mixes coupled and uncoupled states [26], and the nonzero temperature of the sample. We also note that the axial magnetic field should split the dip, with the system no longer being correctly described by a three-level model [27]. In our case, however, this splitting is negligible with respect to the observed linewidth, in the 5-MHz range.

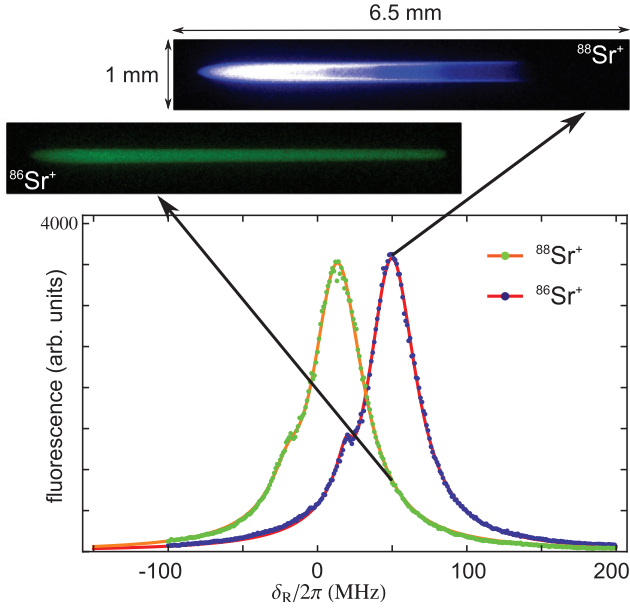


FIG. 5. (Color online) Twin spectra obtained with a Coulomb crystal composed of equivalent proportions of $^{88}\text{Sr}^+$ and $^{86}\text{Sr}^+$ ions. The repumping laser detunings δ_r of the two isotopes are scanned simultaneously, but there is a constant frequency shift between the two beams imposed by fixed-frequency acousto-optic modulators (~ 40 MHz in this example). For each detuning of the master 275-THz laser two images are acquired. As an example we show two such images coded in false colors corresponding to the $^{88}\text{Sr}^+$ [blue (dark gray)] and $^{86}\text{Sr}^+$ [green (light gray)] isotopes. The effect of radial segregation in the trap pushes $^{88}\text{Sr}^+$ in the outer shells, with the core of the crystal being occupied by $^{86}\text{Sr}^+$. The total fluorescence signal plotted in the graph is obtained by integrating these images in the region of interest. The solid lines are the best fit of the spectra by an analytical model based on a three-level atom (optical Bloch equations). The fitting parameters for the $^{88}\text{Sr}^+$ spectrum are listed in the caption of Fig. 4; the fitting parameters of the $^{86}\text{Sr}^+$ spectrum are $\Gamma_b/2\pi = 21.5$ MHz, $\delta_b/2\pi = -25.9$ MHz, $\Omega_b/2\pi = 16.1$ MHz, $\Omega_r/2\pi = 2.7$ MHz, and $\gamma_{DS}/2\pi = 8.6$ MHz.

We emphasize that this width by itself does not put a fundamental limit on the accuracy of the measured isotope shifts, as long as systematic shifts are negligible and the signal-to-noise ratio is high enough. Systematic shifts of

TABLE I. Isotope shifts $\Delta_{88} = \nu_{^{88}\text{Sr}^+} - \nu_{^{86}\text{Sr}^+}$ for the two less abundant even isotopes as obtained by frequency scanning the repumping laser beam. The shifts were retrieved by fitting the experimental data to a three-level-based OBE (δ_b parameters) and by taking into account the fixed AOM shifts imposed on the 711-THz beams. The 88–86 shift comes from a direct measurement, while the 88–84 shift is based on two distinct measurements (the 88–86 shift and the 86–84 shift).

$5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ transition (711 THz)			
Isotope	Δ_{88} (MHz)	Previous result	Ref.
$^{86}\text{Sr}^+$	+170(3)	+168(8)	[6]
$^{84}\text{Sr}^+$	+378(4)	+378(12)	[5]

TABLE II. Isotope shifts $\Delta_{88} = \nu_{^{88}\text{Sr}^+} - \nu_{^{86}\text{Sr}^+}$ for the two even isotopes as obtained by frequency scanning the repumping laser beam. The frequency difference for the $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ Sr⁺ transitions was retrieved by fitting the experimental data to a three-level-based OBE (ω_{0r} parameters) and by taking into account the fixed AOM shifts. The 88–86 shift comes from a direct measurement, while the 88–84 shift is based on two distinct measurements.

$4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ transition (275 THz)	
Isotope	Δ_{88} (MHz)
$^{86}\text{Sr}^+$	-402(2)
$^{84}\text{Sr}^+$	-828(4)

the parameters δ_b and ω_{0r} arise through Doppler broadening induced by residual axial ion motion, and we checked this effect by retrieving these parameters from broadened spectra obtained by convolution of the theoretical line shape with a Maxwell-Boltzmann velocity distribution (temperature T). We estimate this systematic shift to be $2\pi \times -4.7$ MHz (ω_{0r}) and $2\pi \times +19$ MHz (δ_b) at $T = 700$ mK, corresponding to the liquid-gas transition of the ion sample [31], which clearly overestimates the actual temperature of the ion ensembles in the experiment. However, the isotope shift is obtained by taking the difference between the parameters δ_b and ω_{0r} of two simultaneously acquired spectra. In such a procedure, the “common mode” shifts induced by a finite temperature cancel out, and the efficient sympathetic coupling is able to hold the differential temperature ΔT between species down to the 10 mK regime [32]. We calculate that differential temperatures should rise to 100 mK in order to induce systematic shifts larger than the statistical errors of the experiment.

IV. RESULTS

As explained above, the isotope shift determination is based on the acquisition of simultaneous infrared spectra on two-isotope crystals, scanning the $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ Sr⁺ transition. A typical example of twin spectra obtained with this technique is shown in Fig. 5 for the pair $^{88}\text{Sr}^+$ and $^{86}\text{Sr}^+$. The solid line is the best fit with the OBE using the six free parameters: Ω_b , Ω_r , γ_{DS} , δ_b , ω_{0r} , and a scale factor that takes into account the photon collection efficiency. The model is able to reproduce all the main features of the experimental spectra. The Ω parameters obtained from the fit agree within a factor of 3 with intensity and beam-size measurements. The δ_b and ω_{0r} parameters can be used (knowing the fixed frequency shift imposed by the AOMs) to retrieve the isotope shifts in both the $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{1/2}$ Sr⁺ and $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ Sr⁺ transitions.

As the points in the two spectra are acquired in an interleaved way, the precision of the isotope shift is not affected by the possible slow drift of the infrared laser and is affected only by the fast fluctuation not corrected by the frequency lock. It was easy to check the validity of this approach by imposing a non-negligible shift between the twin spectra (change in the frequency of one of the 275-THz AOMs; see Fig. 5) or by varying other parameters (mainly laser intensities). We analyze here 12 spectra for the pair $^{88}\text{Sr}^+ + ^{86}\text{Sr}^+$ and 7 spectra for the pair $^{86}\text{Sr}^+ + ^{84}\text{Sr}^+$. The data extracted

from the spectra are summarized in Tables I and II, with the estimated (statistical and systematic) error. Isotope shifts are also compared (whenever possible) to the most precise previously available determinations.

V. DISCUSSION

When compared to existing determinations of isotope shifts, the data that we obtained using cold trapped ions are in excellent agreement with the previous measurements based on very different techniques. The new determinations of the isotope shifts in dipole-allowed transition from the metastable state will allow for more stringent tests of the theory. This technique could easily be used to measure the isotope shift of the two other low-lying transitions in Sr^+ : the $4d\ ^2D_{5/2} \rightarrow 5p\ ^2P_{3/2}$ transition at 290 THz and the $5s\ ^2S_{1/2} \rightarrow 5p\ ^2P_{3/2}$ transition at 735 THz. In order to do this, one needs to address these transitions with stabilized lasers and to add a repumping beam on the $4d\ ^2D_{3/2} \rightarrow 5p\ ^2P_{1/2}$ transition (see Fig. 1).

The observed statistical noise that affects the isotope shift measurements in the present work is dominated by the residual fluctuations of laser frequency due to poor locking techniques. Following Ref. [25], it would be possible to implement a faster (and tighter) transfer lock for the 275-THz laser. Those authors report a stability better than 10 kHz ($t > 1$ s), which would bring the lock stability of the infrared laser down to negligible levels. The locking of the 711-THz laser could

also be improved. The authors of Ref. [22] report a 40-kHz absolute precision when locking the laser to the Rb atomic transition. Improvements in this locking technique should then also allow for an increased precision. In particular, an offset lock of the cooling laser to a Rb-referenced laser could also expand the possible detuning ranges while addressing different isotopes. Finally, reducing the number of ions used in the experiment should drastically reduce the systematic effects of residual magnetic field (easier to compensate in a pointlike geometry) and ion motion (micromotion, residual temperature). Single-ion spectra in an ion chain containing two isotopes should therefore be the optimal geometry for a more precise determination of the isotope shifts. Moreover, in this configuration, the use of sympathetic cooling by another ion [33] could drastically reduce the residual heating effect arising in the positive-slope part of the dip of infrared spectra [34]. This could reduce systematic error (deformation and shift of the spectra) in this kind of experiment.

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