

Tailoring the correlation and anticorrelation behavior of path-entangled photons in Glauber-Fock oscillator lattices

Armando Perez-Leija,^{1,*} Robert Keil,² Alexander Szameit,² Ayman F. Abouraddy,¹
Hector Moya-Cessa,³ and Demetrios N. Christodoulides¹

¹CREOL/College of Optics, University of Central Florida, Orlando, Florida, USA

²Institute of Applied Physics, Friedrich-Schiller Universität Jena, Max-Wien-Platz 1, D-07743 Jena, Germany

³INAOE, Coordinación de Óptica, A.P. 51 y 216, 72000 Puebla, Puebla, Mexico

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We demonstrate that single-photon as well as biphoton revivals are possible in a new class of dynamic optical systems—the so-called Glauber-Fock oscillator lattices. In these arrays, both Bloch-like oscillations and dynamic delocalization can occur which can be described in closed form. The bunching and antibunching response of path-entangled photons can be pre-engineered in such coupled optical arrangements, and the emulation of fermionic behavior in this family of lattices is also considered. We elucidate these effects via pertinent examples.

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I. INTRODUCTION

The prospect of manipulating and engineering quantum states has become an issue of great importance within the framework of quantum information and computation [1,2]. Along these lines, several physical settings have been envisioned as viable avenues to achieve this goal. Among them, one may mention trapped-ion arrangements and optical lattices as well as spin systems and quantum dots [3,4]. While the list of such possibilities keeps increasing with time, quantum optics has so far provided a versatile platform where such ideas can be experimentally realized and tested. As previously indicated, in optics, quantum information processing can be achieved entirely linearly, using simple passive components like beam splitters and phase shifters along with standard photodetectors and single-photon sources [5]. In this same optical realm, quantum entanglement can arise as a natural byproduct of photon interactions—a clear manifestation of their particle-wave duality. Perhaps, nowhere is this process more apparent than in the so-called Hong-Ou-Mandel two-photon interference effect [6]. In this latter configuration, photon entanglement is made possible via quantum interference—afforded after scattering from a beam splitter. Lately, optical arrays of evanescently coupled waveguides have been suggested as a possible route toward the implementation of multiport systems with moldable quantum dynamics [7]. The flexibility offered by such compact and often miniaturized optical $N \times N$ configurations is made possible by the exceptional control achievable these days in microfabrication techniques [8,9]. In this regard, Bloch oscillations of NOON and W entangled states as well as quantum random walks have been theoretically considered and observed in such arrays [10–12]. In addition, the evolution of quantum correlations in both periodic and random (Anderson) lattices has also been investigated [13–15]. The possibility of classically emulating Jaynes-Cummings systems on such lattices has also recently been proposed [16]. The question naturally arises as to whether such multiport array systems can be utilized as a means to manipulate quantum states of light.

In this paper we investigate the propagation dynamics of nonclassical light in a new class of dynamic photonic systems—the so-called Glauber-Fock oscillator lattices. We demonstrate that Bloch-like revivals and dynamic delocalization effects can naturally occur in spite of the fact that the structure itself is semi-infinite and not periodic. Interestingly, these interactions can be described in closed form, from where one can analytically deduce the turning points of these quantum oscillations. More importantly, the bunching and antibunching response of path-entangled biphotons can be pre-engineered in such coupled optical arrangements. Emulating fermionic dynamics in such arrangements are also considered and compared to those expected from bosonic systems in these same arrays. Finally, the possibility of experimentally realizing such Glauber-Fock oscillator lattices is discussed.

II. SINGLE-PHOTON DYNAMICS IN GLAUBER-FOCK OSCILLATOR LATTICES

We begin our analysis by considering a semi-infinite Glauber-Fock oscillator array consisting of evanescently coupled waveguides. In this arrangement the coupling coefficients among neighboring channels vary with the square root of the site index (i.e., $C_{k,k+1} \propto \sqrt{k+1}$) [9]. For generality, we also allow this coupling to depend on the propagation distance in this lattice, in which case $C_{k,k+1} \propto f(Z)\sqrt{k+1}$ where $f(Z)$ is an arbitrary real function. In addition, we also assume that the propagation constant (local eigenvalue) of each waveguide element varies linearly with the site position. In essence, in this arrangement the refractive index is linearly increasing—in a way analogous to that of an externally biased crystal in solid state physics. Starting from these premises, one can show that, in this class of arrays, the Heisenberg equation of motion for the creation operator of a single photon in waveguide mode k is given by

$$i \frac{da_k^\dagger}{dZ} - f(Z)(\sqrt{k+1}a_{k+1}^\dagger + \sqrt{k}a_{k-1}^\dagger) - \lambda ka_k^\dagger = 0. \quad (1)$$

In the above equation, Z represents the normalized propagation distance given by $Z = \kappa_1 z$, where κ_1 stands for the coupling coefficient between sites 0 and 1, and λ is a real constant associated with the strength of the aforementioned linear

*Corresponding author: aleija@creol.ucf.edu

index change among adjacent sites. We emphasize that, unlike standard infinite Bloch oscillator arrays [17–19], the proposed structure is semi-infinite and asymmetric (e.g., the waveguides are no longer equidistant). As we will see later, these additional degrees of freedom may enable one to observe Bloch-like oscillations even in the neighborhood of the array boundary ($k = 0$). This is in contra-distinction to the well-known Dunlap-Kenkre system, the only other integrable oscillator lattice [17].

In general, the quantum dynamics in this Glauber-Fock oscillator array can be described through the evolution matrix \bar{T} relating the input-output states; that is,

$$a_k^\dagger(0) = \sum_{n=0}^{\infty} T_{k,n}^*(Z) a_n^\dagger(Z). \quad (2)$$

In Eq. (2), $T_{k,n}^*(Z)$ represents the Hermitian conjugate of the (k,n) element of the \bar{T} matrix or unitary transformation. We would like to emphasize that, in the present case, the evolution matrix cannot be simply obtained from $\exp(-iZH)$ since the Hamiltonian of the problem is Z (or time) dependent [20]. Yet, in spite of this complexity, one can show that the evolution elements $T_{k,n}^*$ of the system can be obtained in closed form (see appendix for details). Starting from Eq. (1), one can show that these elements are given by

$$T_{k,n} = \begin{cases} \sqrt{\frac{n!}{k!}} e^A B^{k-n} e^{Dn} L_n^{k-n}(\Phi), & n \leq k \\ \sqrt{\frac{k!}{n!}} e^A C^{n-k} e^{Dk} L_k^{n-k}(\Phi), & n \geq k, \end{cases} \quad (3)$$

where $\Phi = \exp(-i\lambda Z) \exp(-D)|B|^2$, and

$$\begin{aligned} D(Z) &= e^{-i\lambda Z} - 1, \\ B(Z) &= -i \int_0^Z e^{-i\lambda Z'} f(Z') dZ', \\ C(Z) &= -i e^{-i\lambda Z} \int_0^Z e^{i\lambda Z'} f(Z') dZ', \\ A(Z) &= - \int_0^Z \left[\int_0^{Z''} e^{i\lambda Z'} f(Z') dZ' \right] f(Z'') e^{-i\lambda Z''} dZ''. \end{aligned}$$

In Eqs. (3) $L_n^m(x)$ represents the associated Laguerre polynomials. In addition, Eqs. (3) imply that $\sum_{n=0}^{\infty} |T_{k,n}|^2 = 1$, in agreement with the fact that \bar{T} is itself a unitary transformation. In order to gain insight into the quantum dynamics in this class of arrays, let us first consider the case where only a single photon is launched into the k th waveguide element. We begin by analyzing here the simplest possible scenario where the Hamiltonian of the system is Z independent, thus $f(Z) = \kappa_0$, where κ_0 is a real constant. Thus, the evolution matrix elements are given by

$$T_{k,n} = \begin{cases} \sqrt{\frac{n!}{k!}} e^{(\delta+Dn)} [\Theta]^{k-n} L_n^{k-n}(\Phi), & n \leq k \\ \sqrt{\frac{k!}{n!}} e^{(\delta+Dk)} [\Theta]^{n-k} L_k^{n-k}(\Phi), & n \geq k, \end{cases} \quad (4)$$

where

$$\begin{aligned} \delta &= (\kappa_0^2/\lambda^2)[i\lambda Z + \exp(-i\lambda Z) - 1], \\ \Theta &= [\kappa_0 D(Z)/\lambda], \\ D(Z) &= [\exp(-i\lambda Z) - 1], \\ \Phi &= \{2\kappa_0[1 - \cos(\lambda Z)]/\lambda^2\} \exp(i\lambda Z) \exp(D). \end{aligned}$$

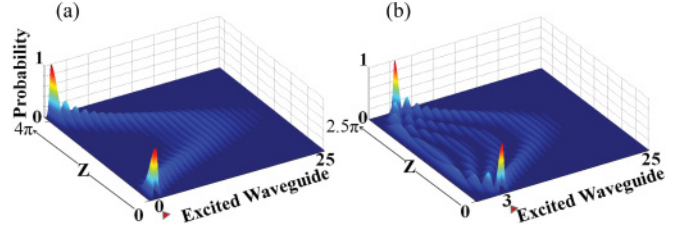


FIG. 1. (Color online) Bloch-like oscillation for a single photon propagating through Glauber-Fock oscillator lattices. The red arrow indicates the site where the photon is being launched. The lattice parameters used are $\kappa_0 = 1$, and $\lambda = 1/2$, $\lambda = 4/5$ for (a) and (b), respectively.

In this case the probability of finding this single photon at waveguide site n when launched at k , can be obtained from $P_{n,k}(Z) = \langle a_n^\dagger a_n \rangle = |T_{k,n}|^2$. Equations (4) clearly indicate that the associated probability distribution exhibits revivals at regular intervals, for example, at $Z = 2\pi s/\lambda$ (with s being an integer). At these revival points, for single-photon excitation, all the $T_{k,n}$ coefficients of Eq. (4) vanish except for $n = k$; that is, the probability collapses into the initial waveguide site k . Figure 1 depicts this process for such a Glauber-Fock oscillator array for two different values of λ . These side views clearly show the previously mentioned *collapse* and revivals of the probability at $Z = 2\pi s/\lambda$ irrespective of the site where the photon was initially coupled. In all cases, these Bloch-like oscillations occur and the photon does not escape into the bulk region—toward the right. This in spite of the fact that the optical potential linearly increases and the waveguide elements get physically closer toward higher values of n . We note that, unlike standard Bloch oscillations occurring in periodic lattices [17–19], in this system the dynamics are asymmetric. This broken symmetry is a result of the semi-infinite nature of this particular array.

We now focus our attention on the case where the coupling coefficients are Z dependent; that is, when the Glauber-Fock oscillator is dynamic. For illustration purposes we consider the periodic variation: $f(Z) = \kappa_0 + \epsilon \cos(\varpi Z)$, where κ_0 is a constant, ϵ is a coupling modulation amplitude, and ϖ stands for the modulation frequency along the propagation direction. In this dynamic environment, when a single photon is launched into the k site, the probability will periodically “collapse” into the initial waveguide at exactly the first zero

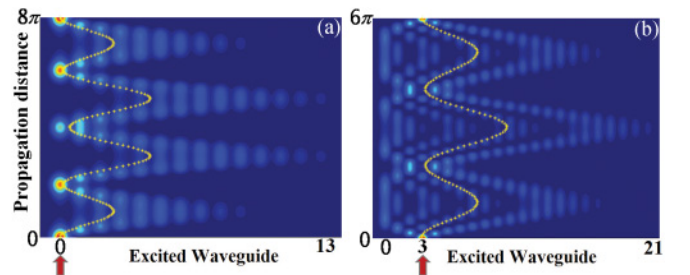


FIG. 2. (Color online) Evolution of the probability distributions for single photons propagating through this Glauber-Fock oscillator lattices with $\lambda = 1$ and $\varpi = 3/4$ for (a), and $\varpi = 2/3$ for (b). Dashed lines show the evolution of $|B(Z)|^2$ along Z , predicting the corresponding revival distance at 8π and 6π , respectively.

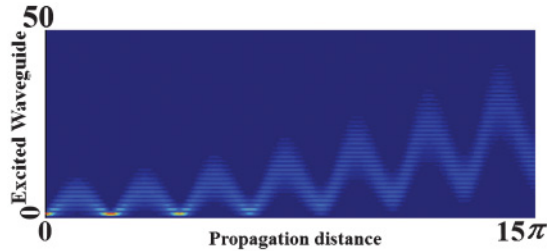


FIG. 3. (Color online) Theoretical evolution of the probability of having one photon at waveguide n when launched at channel 0, $P_{n,0}(Z) = \langle a_n^\dagger a_n \rangle$, under the resonance condition.

\widehat{Z} of the function $|B(Z)|^2$. For the particular example examined here these revivals occur when the ratio $\varpi/\lambda = P/Q$ is a rational number, and P and Q are relatively prime integers. This condition is necessary for the two oscillatory processes independently occurring in this array to lock together synchronously. From here one can deduce that $\widehat{Z} = 2P\pi/\varpi$. This behavior is explicitly illustrated in Fig. 2 for $\kappa_0 = 1$, $\lambda = 1$, and $\epsilon = 0.2$ for the cases $\varpi = 3/4, 2/3$, in (a) and (b), respectively. The dashed lines, on the other hand, represent the evolution of the $|B(Z)|^2$ function which dictates the period of oscillations. Note that exact revivals do not occur if the ratio ϖ/λ is irrational. On the other hand, at the resonance $\varpi = \lambda$, *dynamic delocalization* occurs. In this regime $|B(Z)|^2 \propto Z$, and hence a drift motion is induced toward higher site indices [21]. Therefore, no pure oscillatory behavior is possible at resonance. This delocalization process at resonance is depicted in Fig. 3, where it is shown that the probability of finding the photon among the waveguides gradually shifts toward the upper side of the array oscillator.

III. QUANTUM OSCILLATIONS OF CORRELATED AND ANTICORRELATED PHOTON PAIRS

We next consider the quantum dynamics of an entangled pair of photons, launched either spatially correlated or anticorrelated into this class of Glauber-Fock oscillator arrays. As we will see, this new class of photonic lattices can tailor the bunching and antibunching behavior of path-entangled biphotons (spatially extended state). Conceptually, photon pairs (biphotons) with correlated positions will couple into the same waveguide (within a certain excitation window W ; i.e., a set of waveguides where the photons can be launched) with an equal probability. In this regime, the corresponding input state is written as $|\psi_C\rangle = \sqrt{1/2W}[(a_f^\dagger)^2 + (a_{f+1}^\dagger)^2 + \dots + (a_l^\dagger)^2]|0\rangle$. Throughout our paper, f and l will represent the first and last waveguide site, respectively, within the excitation window. This input state can be generated by placing the waveguide array immediately after a type-I collinear degenerate narrow-band spontaneous parametric down conversion (SPDC) thin-crystal source [22]. On the other hand, an entangled pair of photons with anticorrelated positions corresponds to the physical situation where the photon pair is always coupled to waveguides on opposite sides of the excitation window W —again with equal probability. Thus, the input state is written as $|\psi_A\rangle = \sqrt{2/W}[a_f^\dagger a_l^\dagger + a_{f+1}^\dagger a_{l-1}^\dagger + \dots + a_R^\dagger a_{R'}^\dagger]|0\rangle$, where W is even and (R, R') represent the floor and ceiling integers,

respectively, of the quantity $(l+f)/2$. In order to obtain the correlation between the array modes, we analyze at the output the coincidence rate at waveguides p and q , which is given by $\Gamma_{p,q} \equiv \langle a_p^\dagger a_q^\dagger a_q a_p \rangle$. In this case one can show that, for correlated inputs $|\psi_C\rangle$, the correlation map is described by $\Gamma_{p,q} = (1/W) |\sum_{k=f}^l T_{p,k} T_{q,k}|^2$, whereas for anticorrelated $|\psi_A\rangle$ it becomes $\Gamma_{p,q} = (1/W) |\sum_{k=0}^{W-1} T_{p,f+k} T_{q,l-k}|^2$. In order to demonstrate these effects and for comparison purposes, we will always assume here that $W = 10$ with the excitation contained between $(f,l) = (0,9)$.

The evolution of the correlation map $\Gamma_{p,q}$ as a function of distance when $f(Z) = 1$ and $\lambda = 0.5$ is then examined. In this case, revivals are expected at multiples of $Z = 4\pi$. When the input state is initially correlated, the map flips and antibunching occurs at $Z = \pi$ and $Z = 3\pi$, while it returns to a broadened bunched state in the middle of a cycle. This situation is altered when an anticorrelated biphoton input is used. In this case the map tends to flip over to that of a bunched state at $Z = \pi$ and $Z = 3\pi$, while in the middle of this oscillation it attains a correlation mixture—with bunching being predominant. This evolution is altogether different from that occurring in uniform lattices [13]. The present dynamics is a direct outcome of the revivals and of the phase acquired upon reflection from the boundary of this semi-infinite Glauber-Fock oscillator array—which is absent in periodic arrays. We next consider the evolution of correlations when two periods are simultaneously involved in the lattice [e.g., when the function $f(Z)$ is periodic]. For this example we again take $f(Z) = \kappa_0 + \epsilon \cos(\varpi Z)$, with $\kappa_0 = 1$, $\lambda = 0.5$, $\epsilon = 0.2$, and $\varpi = 3/4$, in which case the revival period is 8π . For a correlated input $|\psi_C\rangle$ the correlation map exhibits periodic transitions from bunching to antibunching [Figs. 4(a)–4(e)]. However, at the half-cycle point the bunching is now not entirely complete [Fig. 4(e)], due to the incomplete revival of the single-photon trajectories. This scenario becomes very different when the initial biphoton state $|\psi_A\rangle$ is anticorrelated [Figs. 4(f)–4(j)]. The correlation dynamics corresponding to both cases are shown up to half a cycle (4π). Evidently, right after the origin, bunching is seen to occur [Fig. 4(g)] while midway in the cycle signatures of antibunching behavior appear. This latter pattern is different from that obtained before [$f(Z) = 1$] when only one oscillation frequency was involved in the Glauber-Fock oscillator.

We have also explored the response of this system under dynamic delocalization conditions. Figure 5 depicts again the correlations for the same parameters used in the previous case, except that here $\lambda = \varpi = 1$. In this delocalization regime, a correlated input $|\psi_C\rangle$ tends to initially oscillate between bunching and antibunching, as was shown in Figs. 4(a)–4(c), and eventually settles into an antibunched state [Fig. 5(a)]. On the other hand, for an anticorrelated biphoton input $|\psi_A\rangle$ the entangled photons very quickly and irreversibly become bunched and they remain in this state [Fig. 5(b)]. The reason why delocalization itself affects the correlation evolution has to do with the fact that, in this case, the photons tend to eventually escape into the bulk of the lattice—away from the boundary. Simulations indicate that, by adjusting the two oscillation frequencies, one can at will lock the output into a particular bunching or antibunching state. In essence the presence of revivals of quantum states (or absence of revivals)

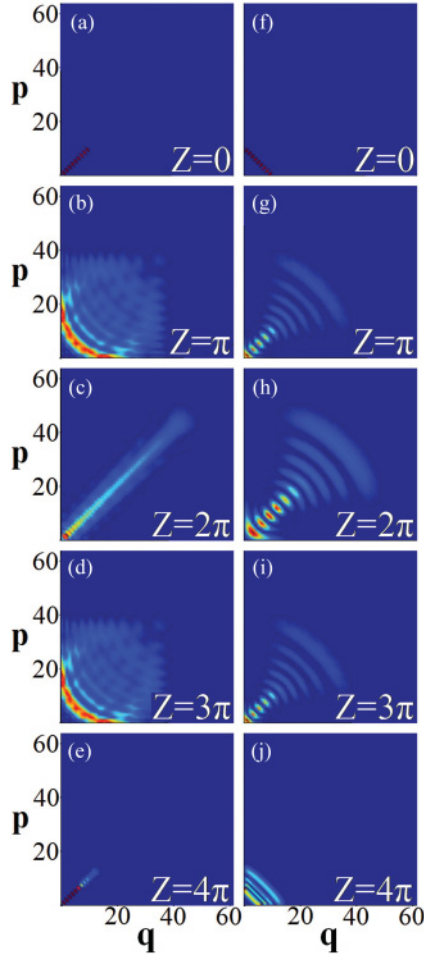


FIG. 4. (Color online) Left column shows the quantum correlation maps when the input state $|\psi_C\rangle$ is coupled into a modulated-tilted Glauber-Fock oscillator array ($\lambda = 1/2$, $\varpi = 3/4$). Similarly, the right column depicts the correlation evolution for the input state $|\psi_A\rangle$.

allows one to engineer the quantum dynamics in this class of dynamic Glauber-Fock oscillator lattices.

Finally, we also consider this same arrangement when fermionic-like input states are used [23]. Figure 5(c) shows how the correlation evolves in this case under delocalization conditions for parameters identical to those used in Fig. 3. The input in this case is assumed to be of the type $|\psi_F\rangle = b_f^\dagger b_l^\dagger |0\rangle$, where b_n (b_n^\dagger) represents the annihilation (creation) operator for fermions in a lattice [20]. For this input, the antibunching behavior in the correlation matrix is evident. See [24] for a movie visualizing the propagation of Figs. 5(a)–5(c).

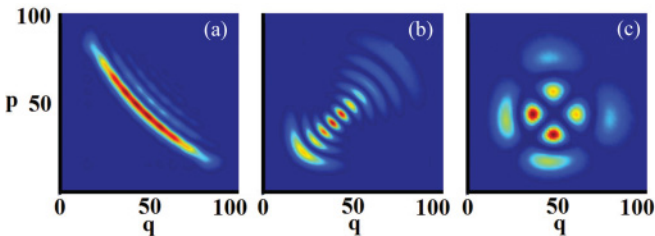


FIG. 5. (Color online) Correlation matrices at $Z = 15\pi$ for the initial states (a) $|\psi_C\rangle$, (b) $|\psi_A\rangle$ and (c) $|\psi_F\rangle$.

IV. CONCLUSION

In conclusion, we have shown that a new family of dynamic arrays—the so-called Glauber-Fock oscillator lattices—can be used as a way to mold the quantum evolution of path-entangled photons. In these systems, revivals and dynamic delocalization are possible—each leaving a specific mark on the correlation map. If the two oscillation periods associated with these Bloch-like oscillators are irrational with respect to each other, the dynamics become aperiodic. At this point several intriguing questions remain. For example, of interest will be to examine how such structures respond to other maximally entangled states (like NOON states) or whether they can be used to synthesize other quantum states of interest. The response of these lattices may be also useful in considering other classes of problems in other physical configurations having similar quantum analogs like those of the Bose-Hubbard or Jaynes-Cummings type with time-varying couplings [16,25].

APPENDIX

In order to obtain the solution to Eq. (1), we use operator techniques. We start by introducing the *Schrödinger equation* associated with Eq. (1) [26]

$$i \frac{dT(a^\dagger, a, Z)}{dZ} = [f(Z)(a^\dagger + a) + \lambda a^\dagger a] T(a^\dagger, a, Z), \quad (\text{A1})$$

where $a = \frac{1}{2}(x + \frac{d}{dx})$ and $a^\dagger = \frac{1}{2}(x - \frac{d}{dx})$ are the annihilation and creation operators, respectively, that satisfy the relations [27]

$$a|n\rangle = \sqrt{n}|n-1\rangle, \quad a^\dagger|n\rangle = \sqrt{n+1}|n+1\rangle. \quad (\text{A2})$$

We now introduce a transformation V which converts $T(a^\dagger, a, t)$ into its normal form in which all the creation operators appear to the left of the annihilation operators. V transforms $T(a^\dagger, a, Z) \rightarrow \tilde{T}(\alpha^*, \alpha, Z)$ by substituting $a \rightarrow (\alpha + \frac{\partial}{\partial \alpha^*})$, and $a^\dagger \rightarrow \alpha^*$ [20]. In other words, V transforms the operator differential equation into an equivalent algebraic variable differential equation. By applying V to Eq. (A1) we obtain

$$i \frac{d\tilde{T}}{dZ} = \left[f(Z) \left(\alpha^* + \alpha + \frac{\partial}{\partial \alpha^*} \right) + \lambda \alpha^* \left(\alpha + \frac{\partial}{\partial \alpha^*} \right) \right] \tilde{T}. \quad (\text{A3})$$

This equation is easily solved by assuming a solution of the form

$$\tilde{T}(\alpha^*, \alpha, Z) = e^{S(\alpha^*, \alpha, Z)}. \quad (\text{A4})$$

With this substitution, Eq. (A3) becomes

$$i \frac{dS}{dZ} = f(Z)\alpha^* + f(Z)\alpha + \lambda \alpha^* \left(\alpha + \frac{\partial S}{\partial \alpha^*} \right) + f(Z) \frac{\partial S}{\partial \alpha^*}. \quad (\text{A5})$$

We now determine S by demanding a functional form that gives algebraically equivalent terms on both sides of Eq. (A5). Therefore, in this case, S must be

$$S(\alpha^*, \alpha, Z) = A(Z) + B(Z)\alpha + C(Z)\alpha^* + D(Z)\alpha^*\alpha, \quad (\text{A6})$$

in this case Eq. (A5) becomes

$$i \left(\frac{dA}{dZ} + \frac{dB}{dZ} \alpha + \frac{dC}{dZ} \alpha^* + \frac{dD}{dZ} \alpha^* \alpha \right) = \lambda \alpha^* \alpha + \lambda \alpha^* (C + D\alpha) + f(Z)(\alpha + \alpha^*) + f(Z)(C + D\alpha). \quad (\text{A7})$$

By equating coefficients of similar terms on both sides of Eq. (A7) we readily obtain the solutions for $A(Z)$, $B(Z)$, $C(Z)$, and $D(Z)$; namely,

$$\begin{aligned} D(Z) &= e^{-i\lambda Z} - 1, \\ B(Z) &= -i \int_0^Z e^{-i\lambda Z'} f(Z') dZ', \\ C(Z) &= -e^{-i\lambda Z} B^*(Z), \\ A(Z) &= - \int_0^Z \left[\int_0^{Z'} e^{i\lambda Z'} f(Z') dZ' \right] f(Z'') e^{-i\lambda Z''} dZ'', \end{aligned} \quad (\text{A8})$$

where $B^*(Z)$ represents the complex conjugate of $B(Z)$. Using the normal-ordering symbol N , which converts a function of the commuting variables (α^*, α) into the same function of the operators (a^\dagger, a) (the resulting operator function being in the normal form), we can now introduce the inverse transformation V^{-1} such that [20]

$$T(a^\dagger, a, Z) = V^{-1}[\tilde{T}(\alpha^*, \alpha, Z)] = N(e^{A+B\alpha+C\alpha^*+D\alpha^*\alpha}). \quad (\text{A9})$$

Then, by applying V^{-1} to Eq. (A4), one obtains

$$T(a^\dagger, a, Z) = e^A e^{C(Z)a^\dagger} e^{Da^\dagger a} e^{Ba}. \quad (\text{A10})$$

Finally, after performing the Taylor series expansion of the exponentials and using the relations given in Eq. (A2), we obtain the matrix elements given in Eq. (3):

$$T_{k,n}(Z) = \langle n | e^A e^{C(Z)a^\dagger} e^{Da^\dagger a} e^{Ba} | k \rangle. \quad (\text{A11})$$

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