# Structure and thermochemistry of $\mathbf{K}_{\mathbf{2}} \mathbf{R b}, \mathrm{KRb}_{\mathbf{2}}$, and $\mathbf{K}_{\mathbf{2}} \mathbf{R} \mathbf{b}_{\mathbf{2}}$ 

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#### Abstract

The formation and interaction of ultracold polar molecules is a topic of active research. Understanding possible reaction paths and molecular combinations requires accurate studies of the fragment and product energetics. We have calculated accurate gradient optimized ground-state structures and zero-point corrected atomization energies for the trimers and tetramers formed by the reaction of KRb with KRb and corresponding isolated atoms. The $\mathrm{K}_{2} \mathrm{Rb}$ and $\mathrm{KRb}_{2}$ trimers are found to have global minima at the $C_{2 v}$ configuration with atomization energies of 6065 and $5931 \mathrm{~cm}^{-1}$ while the tetramer is found to have two stable planar structures, of $D_{2 h}$ and $C_{s}$ symmetry, which have atomization energies of $11131 \mathrm{~cm}^{-1}$ and $11133 \mathrm{~cm}^{-1}$, respectively. We have calculated the minimum energy reaction path for the reaction $K R b+K R b$ to $K_{2}+R b_{2}$ and found it to be barrierless.


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The formation and interaction of ultracold polar molecules is a topic of great current interest in physics. New techniques for the formation of rovibrational ground-state polar molecules via stimulated rapid adiabatic passage (STIRAP) [1] or Feshbach-optimized photoassociation (FOPA) [2] allow experiments to be performed with $v=0$ heteronuclear diatomic molecules, including KRb [3-6] and LiCs [7]. Proposals for quantum computation with polar molecules [8,9] have generated a growing need for understanding of the dynamics of diatom-diatom collisions. Such studies of diatomic dynamics require knowledge of the open and closed channels relevant in those reactions. The purpose of the present paper is to present accurate $a b$ initio calculations of the structure and thermochemistry of several chemical species relevant to the study of $\mathrm{KRb}-\mathrm{KRb}$ dimer interactions.

Theoretical work on electronic structure of few-body alkali systems has been limited to lighter homonuclear trimers, in particular, doublet [10] and quartet [11] $\mathrm{Li}_{3}$, doublet $\mathrm{K}_{3}$ [12], and quartet $\mathrm{Na}_{3}$ [13]. The recent work of Żuchowski and Hutson [14] has characterized the atomization energy of the alkali-metal homo- and heteronuclear triatomic species formed from $\mathrm{Li}, \mathrm{Na}, \mathrm{K}, \mathrm{Rb}$, and Cs. These homonuclear trimers have $A^{\prime}$ ground electronic states in $C_{s}$ symmetry that correlate to $B_{2}$ symmetry in $C_{2 v}$. Previous mixed alkali tetramer studies have been limited to structure studies of $\operatorname{Li}_{n} X_{m}(X=\mathrm{Na}$ and K) $[15,16]$ and that of $\mathrm{RbCs}+\mathrm{RbCs}$ [17]. To date no such calculations have been reported for the heteronuclear $\mathrm{K}_{n} \mathrm{Rb}_{m}$ tetramer molecules.

Electronic structure calculations were performed on $\mathrm{K}_{2}$, $\mathrm{Rb}_{2}, \mathrm{KRb}, \mathrm{K}_{2} \mathrm{Rb}, \mathrm{KRb}_{2}$, and $\mathrm{K}_{2} \mathrm{Rb}_{2}$ at the $\operatorname{CCSD}(\mathrm{T})$ [18] level of theory. As core-valence effects can be important in alkali metals, we correlate the inner valence electrons in potassium, keeping only $1 s^{2} 2 s^{2} 2 p^{2}$ in the core. Rubidium is heavy enough that relativistic effects are significant, so we replace its inner shell electrons by the Stuttgart small-core relativistic (ECP28MDF) effective core potential (ECP) [19]. Basis sets are taken from the Karlsruhe def2-TZVPP [20] and def2-QZVPP [21] orbital and fitting sets.

Optimized geometries for $\mathrm{K}_{2}, \mathrm{Rb}_{2}, \mathrm{KRb}, \mathrm{K}_{2} \mathrm{Rb}, \mathrm{KRb}_{2}$, and $\mathrm{K}_{2} \mathrm{Rb}_{2}$ were found at the $\operatorname{CCSD}(\mathrm{T}) /$ def2-TZVPP level of theory. Calculation of the harmonic vibrational frequencies was done to verify that the calculated structures were minima
on the potential energy surface, and the calculated frequencies were used to obtain vibrational zero-point energy (ZPE) corrections. These structures were further optimized at the $\operatorname{CCSD}(\mathrm{T}) /$ def2-QZVPP level of theory, leading to a $0.07-\AA$ correction in the bond lengths and $60 \mathrm{~cm}^{-1}$ in final atomization energies. The CCSD(T)/def2-QZVPP geometries are tabulated in Table I.

Evaluation of the contribution of scalar relativistic corrections to $\mathrm{K}_{2}$ indicate a small $0.005-\AA$ and $<8-\mathrm{cm}^{-1}$ contribution in all electron correlation calculations [24], while for $\mathrm{Rb}_{2}$ it has been shown [25] that the small core Stuttgart pseudopotential gives an accurate representation of relativistic effects on the bond length and dissociation energy.

Single-point energy calculations were then done using the $\operatorname{CCSD}(\mathrm{T})-\mathrm{F} 12 \mathrm{~b}$ [26,27] [explicitly correlated $\operatorname{CCSD}(\mathrm{T})$ ] level of theory. The use of explicitly correlated methods accelerate the slow convergence of the one-particle basis set by including terms containing the interelectron coordinates into the wave function [28], thus yielding very accurate results using triple and quadruple zeta basis sets. In addition, we estimate the complete basis set (CBS) limit using the two-point extrapolation formula of Helgaker et al. [29],

$$
\begin{equation*}
E_{\mathrm{CBS}}=\frac{n^{3} E_{n}-(n-1)^{3} E_{n-1}}{n^{3}-(n-1)^{3}} \tag{1}
\end{equation*}
$$

In Table II the $\operatorname{CCSD}(\mathrm{T})$ and $\operatorname{CCSD}(\mathrm{T})-\mathrm{F} 12 \mathrm{~b}$ dissociation energies for the def2-TZVPP and def2-QZVPP basis sets are tabulated as well as the zero-point energy corrected atomization energies. After extrapolation, the diatomic $\operatorname{CCSD}(\mathrm{T})-$ F12b ZPE corrected dissociation energies agree very well with the experimental diatomic dissociation energies, as shown in Table II. The $a b$ initio calculations were done using the GAUSSIAN 09 [30] and MOLPRO [31-33] packages.

We have found that both $\mathrm{K}_{2} \mathrm{Rb}$ and $\mathrm{KRb}_{2}$ have two energetically close local minima on the ground-state surface, one of $C_{2 v}$ symmetry and another less symmetric $C_{s}$ structure (geometries given in Table I). While dependent on the level of theory used to evaluate the atomization energy, we conclude that the symmetric $C_{2 v}$ geometry is the global minima for each trimer. The atomization energies calculated are found to be in good agreement with those recently published by Żuchowski and Hutson [14].

TABLE I. Calculated CCSD(T)/QZVPP molecular geometries (in Ångströms and degrees).

|  | $r_{e}$ |  |  |  |  |
| :--- | :---: | :--- | :--- | :--- | :--- |
| $\mathrm{~K}_{2}$ | 3.956 |  |  |  |  |
| $\mathrm{Rb}_{2}$ | 4.233 |  |  |  |  |
| KRb | 4.160 |  |  |  |  |
|  | $r_{\mathrm{K}-\mathrm{Rb}}$ | $r_{\mathrm{K}-\mathrm{Rb}}^{\prime}$ | $\theta$ |  |  |
| $\mathrm{K}_{2} \mathrm{Rb}_{2 v}$ | 4.279 | 4.279 | 70.68 |  |  |
| $\mathrm{~K}_{2} \mathrm{Rb} \mathrm{C}_{s}$ | 4.361 | 5.234 | 48.81 |  |  |
| $\mathrm{KRb}_{2} C_{2 v}$ | 4.271 | 4.271 | 82.13 |  |  |
| $\mathrm{KRb}_{2} C_{s}$ | 4.193 | 5.179 | 57.07 |  |  |
|  | $r_{\mathrm{Rb}-\mathrm{Rb}}$ | $r_{\mathrm{K}-\mathrm{K}}$ | $r_{\mathrm{K}-\mathrm{Rb}}$ | $\theta_{\mathrm{K}-\mathrm{Rb}-\mathrm{Rb}}$ | $\theta_{\mathrm{K}-\mathrm{K}-\mathrm{Rb}}$ |
| $\mathrm{K}_{2} \mathrm{Rb}_{2} D_{2 h}$ | 8.224 | 4.0307 | 4.579 |  | 55.48 |
| $\mathrm{~K}_{2} \mathrm{Rb}_{2} C_{s}$ | 4.761 | 4.408 | 4.189 | 53.34 | 5.48 |

The $\mathrm{K}_{2} \mathrm{Rb}_{2}$ tetramer is found to have two nearly degenerate minima on the potential energy surface. One is a rhombic structure of $D_{2 h}$ symmetry, and another planar $\left(C_{s}\right)$ structure that corresponds to an interchange of K and Rb atoms. These structures are bound by $\sim 3000 \mathrm{~cm}^{-1}$ with respect to $K_{2}+\mathrm{Rb}_{2}$ or $\mathrm{KRb}+\mathrm{KRb}$. The electronic structure of these two isomers is very similar, and their stability is likely due to three-center bonds of the sort proposed for $\mathrm{Li}_{n} \mathrm{Na}_{4-n}$ clusters [15,16]. The rhombic $\mathrm{K}_{2} \mathrm{Rb}_{2}$ structure has a short ( $\sim 4 \AA$ ) distance and a long ( $\sim 8 \AA$ ) Rb-Rb distance. The equivalent structure where the $\mathrm{K}-\mathrm{K}$ distance is short and the $\mathrm{Rb}-\mathrm{Rb}$ distance is long is found to be a transition state, not a stable minimum.

To determine if there is any barrier to the $\mathrm{KRb}+\mathrm{KRb} \rightarrow$ $\mathrm{K}_{2} \mathrm{Rb}_{2} \rightarrow \mathrm{Rb}_{2}+\mathrm{K}_{2}$ reaction, we calculate a minimum energy path for the $\mathrm{KRb}+\mathrm{KRb} \rightarrow \mathrm{K}_{2} \mathrm{Rb}_{2}$ and $\mathrm{Rb}_{2}+\mathrm{K}_{2} \rightarrow \mathrm{~K}_{2} \mathrm{Rb}_{2}$ reactions. We start by locating the minimum energy geometric configuration at long range. This is done by calculating $a b$ initio the dipole and quadrupole electrostatic moments of $\mathrm{K}_{2}, \mathrm{Rb}_{2}$, and KRb and then minimizing the long-range electrostatic interaction energy [34] with respect to the angular configuration of the molecules. This minimization resulted in a T-type geometry for both $\mathrm{K}_{2}+\mathrm{Rb}_{2}$ and $\mathrm{KRb}+\mathrm{KRb}$. We have recently shown that long-range expansions of this type accurately reproduce diatom-diatom interaction energies [35].

From these initial geometries, the reaction path was followed by freezing the diatom-diatom distance and optimizing the diatomic bond lengths and angular orientations at the frozen core CCSD(T)/def2-TZVPP level of theory. Single-point energies were evaluated along this path using the CCSD(T)-F12b level of theory including the core-valence correlation energy and extrapolated to the CBS limit as discussed above. This procedure, in which a high-level energy profile is evaluated along a reaction path calculated at a lower level of theory, is known to be a good approximation to the energy profile along the reaction path calculated at the high level of theory [36].

We find that the $\mathrm{KRb}+\mathrm{KRb}$ dissociation limit connects to the $D_{2 h}$ minima while the $\mathrm{K}_{2}+\mathrm{Rb}_{2}$ dissociation limit connects to the $C_{s}$ minima, with no barrier found to either reaction. A similar conclusion was obtained for the $\mathrm{RbCs}+$ $\mathrm{RbCs} \rightarrow \mathrm{Rb}_{2}+\mathrm{Cs}_{2}$ reaction by Tscherbul et al. [17]. To finish characterizing the reaction path going from one dissociation limit to the other, we locate the transition state and calculate the intrinsic reaction coordinate (IRC) [37] reaction path connecting the $C_{s}$ and $D_{2 h}$ minima structures at the same level of theory as described previously. Optimizing the transitionstate geometry at the inner valence $\operatorname{CCSD}(\mathrm{T}) /$ def2-TZVPP discussed previously and evaluating an accurate atomization energy using our $\operatorname{CCSD}(\mathrm{T})$-f12b prescription we find that the transition state is $1167.3 \mathrm{~cm}^{-1}$ above the $D_{2 h}$ dissociation energy. The calculated reaction path is plotted in Fig. 1 using the approximate reaction coordinate,

$$
\begin{equation*}
\Delta R=\frac{1}{2}\left(R_{\mathrm{K}-\mathrm{K}}+R_{\mathrm{Rb}-\mathrm{Rb}}\right)-\frac{1}{2}\left(R_{\mathrm{K}-\mathrm{Rb}}+R_{\mathrm{K}-\mathrm{Rb}}^{\prime}\right) \tag{2}
\end{equation*}
$$

where $R_{\mathrm{A}-\mathrm{B}}$ is the distance between atoms A and B .
The formation and trapping of rovibrational ground-state KRb diatoms with a high phase-space density [5] offers the opportunity to study chemical reactions in the ultracold regime [6]. As seen in Fig. 2, the three-body reaction $\mathrm{KRb}+$ $\mathrm{Rb} \rightarrow \mathrm{Rb}_{2}+\mathrm{K}$ is energetically forbidden at ultracold temperatures, leaving the endothermic four-body reaction $\mathrm{KRb}+$ $\mathrm{KRb} \rightarrow \mathrm{Rb}_{2}+\mathrm{K}_{2}$ as the only pathway to forming $\mathrm{Rb}_{2}$ within the trap. Measurements of the population of $\mathrm{Rb}_{2}$ within the trap will then allow direct probing of the exchange reaction

TABLE II. Dissociation and zero-point energies calculated using $\operatorname{CCSD}(\mathrm{T})$ and $\operatorname{CCSD}(\mathrm{T})$-F12b correlation methods with successive basis sets and CBS extrapolated values (in $\mathrm{cm}^{-1}$ ).

|  | ZPE TZVPP CCSD(T) | $D_{e}$ TZVPP |  | $D_{e} \mathrm{QZVPP}$ |  | $D_{0} \mathrm{CBS}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\operatorname{CCSD}(\mathrm{T})$ | $\operatorname{CCSD}(\mathrm{T})-\mathrm{F} 12 \mathrm{~b}$ | $\operatorname{CCSD}(\mathrm{T})$ | CCSD(T)-F12b | $\operatorname{CCSD}(\mathrm{T})$ | CCSD (T)-F12b |
| $\mathrm{K}_{2}{ }^{\text {a }}$ | 46.0 | 4098.8 | 4276.9 | 4460.0 | 4369.7 | 4677.6 | 4391.5 |
| $\mathrm{Rb}_{2}{ }^{\text {b }}$ | 26.8 | 3494.3 | 3723.3 | 3842.7 | 3885.4 | 4070.2 | 3976.8 |
| $\mathrm{KRb}^{\text {c }}$ | 35.4 | 3829.4 | 4015.6 | 4135.6 | 4128.7 | 4323.6 | 4175.7 |
| $\mathrm{K}_{2} \mathrm{Rb} C_{2 v}$ | 69.8 | 5588.2 | 5805.5 | 6067.7 | 5995.7 | 6574.2 | 6009.4 |
| $\mathrm{K}_{2} \mathrm{Rb} C_{s}$ | 72.4 | 5606.3 | 5843.7 | 6179.1 | 6015.9 | 6524.7 | 6069.1 |
| $\mathrm{KRb}_{2} C_{2 v}$ | 62.8 | 5394.5 | 5635.1 | 5911.0 | 5842.2 | 6043.5 | 5788.3 |
| $\mathrm{KRb}_{2} C_{s}$ | 59.0 | 5215.9 | 5475.4 | 5728.5 | 5690.4 | 6225.1 | 5930.5 |
| $\mathrm{K}_{2} \mathrm{Rb}_{2} D_{2 h}$ | 129.5 | 10210.8 | 10669.4 | 11275.3 | 11011.1 | 11922.7 | 11131.0 |
| $\mathrm{K}_{2} \mathrm{Rb}_{2} C_{s}$ | 126.2 | 10198.3 | 10629.9 | 11211.4 | 10993.7 | 11824.6 | 11133.0 |

[^0]

FIG. 1. Minimum energy path connecting the $\mathrm{KRb}+\mathrm{KRb}$ and $\mathrm{K}_{2}$ $+\mathrm{Rb}_{2}$ dissociation limits. Included are schematic geometric points of interest, where open and solid circles represent rubidium and potassium atoms, respectively.
rate of $K R b+K R b$. Inherent in this exchange reaction is the possibility of studying the role of fermionic or bosonic spin statistics in ultracold chemical reactions [38-44]. In this temperature regime, $s$-wave scattering of fermionic ${ }^{40} \mathrm{KRb}$ is suppressed which should greatly diminish the reaction rate of ${ }^{40} \mathrm{KRb}+{ }^{40} \mathrm{KRb}$, thus leaving the trap stable to four-body losses. If instead the trap was formed with bosonic ${ }^{39} \mathrm{KRb}$ or ${ }^{41} \mathrm{KRb}$ molecules, no such collisional suppression is expected, where we then expect comparably large reaction rates to occur. It is also possible to explore recent theoretical predictions [44] which show that if a bosonic dimer is composed of two


FIG. 2. Schematic energy-level diagram for fragment and structure energies involving $K R b$ with $K R b$ and separated atoms. Inset shows the small difference between the $\mathrm{KRb}+\mathrm{KRb}$ and $\mathrm{K}_{2}+\mathrm{Rb}_{2}$ asymptotes.
fermions of very different masses the resulting exchange reaction should still be suppressed despite the overall bosonic nature. This could be accomplished by using fermionic ${ }^{40} \mathrm{~K}$ and a long-lived ${ }^{84} \mathrm{Rb}$ or ${ }^{86} \mathrm{Rb}$. The comparison between reaction rates in the previously described interactions can then be used to directly study the effects of fermion or boson spin statistics to that of chemical reactions.

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[^0]:    ${ }^{a}$ Experimental value $4405.389 \mathrm{~cm}^{-1}$ [22].
    ${ }^{\mathrm{b}}$ Experimental value $3965.8 \mathrm{~cm}^{-1}$ [23].
    ${ }^{\text {c }}$ Experimental value $4180.417 \mathrm{~cm}^{-1}$ [5].

