Enhanced polarization and mechanisms in optically pumped hyperpolarized ³He in the presence of ⁴He

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This work reports an enhanced polarization and mechanisms in optically pumped (OP) hyperpolarized ³He in the presence of ⁴He. The cells contain Rb metal, 60-torr N₂, and different pressures of ³He and ⁴He. In the absence of ⁴He, the polarization of ³He increases monotonically from 4.5% to 8% when the pressure of ³He is increased from 300 to 1500 torr. In the presence of 1850-torr ⁴He gas, the polarization of ³He is enhanced from 7% to 30% for a cell containing 600-torr ³He and 60-torr N₂. The wall relaxation factors *X* for OP cells with and without buffering ⁴He gas were derived. It was found that the ⁴He gas confines the ³He atoms to a diffusion-limited region which effectively reduces the wall relaxation factor *X*. Mechanisms contributed to relaxation are addressed and discussed.

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I. INTRODUCTION

Spin-exchange optical pumping (SEOP) [1–5] is widely used to produce hyperpolarized ³He for a wide variety of scientific and medical applications. The applications include neutron spin filters [6], quantum computation [7], surface nuclear magnetic resonance (NMR) [8], and magnetic resonance imaging (MRI) [9–11]. In all these experiments, to obtain a high polarization and maintain a long relaxation time for hyperpolarized noble gas are both essential issues. Fabrication of different kinds of cells [12,13] or cells with surface coatings [14] has been attempted to achieve these goals. High polarization of $P_{\rm Rb}$ can be reached if the cells are constructed from GE 180 glass (GE Lighting Component Sales, Cleveland, OH 44117) [14]. However, these cells are difficult to fabricate. Coatings can effectively reduce the wall relaxation and increase the longitudinal relaxation time T_1 [15]. However, the coating procedures can be tedious or time consuming. This study reports an alternative method for enhancing polarization by buffering refillable cells with ⁴He gas. The cells originally filled with Rb, \sim 60-torr N₂ and ³He, are then buffered with different pressures of ⁴He. Enhancement of polarization in optically pumped (OP) hyperpolarized ³He were observed in the presence of ⁴He. In the absence of ⁴He, the polarization of ³He is enhanced from 4.5% to 8% when the pressure of 3 He is increased from 300 to 1500 torr at 200°C. In the presence of 1850-torr ⁴He, the polarization of ³He is enhanced from 7% to 30% for a cell filled with 600-torr ³He. Hyperpolarized ³He with longitudinal relaxation time T_1 is longer than 6 h and can be routinely produced after 4 h of optical pumping. The polarization as a function of time at various temperatures during optical pumping and relaxation, respectively, was used to derive the wall relaxation factors X for OP cells with buffering 4 He gas. The results were compared with that of an OP cell without buffering ⁴He. It was found that the ⁴He gas confines the ³He

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atoms to a diffusion-limited region which effectively reduces the value of X. We demonstrate that the gradient field causes a diffusive motion of ³He and enhances the relaxation. It is highly recommended to produce hyperpolarized noble ³He in high homogenous magnetic fields. Hyperpolarized ³He with 30% polarization can be routinely produced and a longitudinal relaxation time T_1 of 6 h after 4 h of optical pumping can be obtained. Mechanisms of relaxation in OP ³He will be addressed and the results will be discussed.

II. EXPERIMENT

Figure 1 shows a schematic of a system with optical pumping and NMR detection used for characterizing hyperpolarized ³He with and without the presence of ⁴He gas. A Helmholtz coil generated a magnetic field of 1.5 mT in optical pumping with field homogeneity of ~ 1 part per 1×10^3 . A refillable Pyrex glass cell containing ⁴He, N₂, ³He, and a few mg of Rb was heated up with hot air. The cell was situated in a magnetic field B_0 which dictates the orientation for polarizing the spins of atoms. A right-hand circularly polarized (σ^+) laser light at 794.7 nm was used to pump the cells. The ³He NMR signals were measured with a pulse NMR spectrometer. A radio-frequency (rf) coil placed around the cell inside the oven was used to tilt the magnetization. The sequences used to investigate the free induction decay NMR signal are shown in Fig. 1(c). In order to remove impurities and moisture absorbed in the inner-wall surface of the glass, the cells were baked at 200°C and pumped with a high-vacuum pumping station for 2–3 days. A high-vacuum pumping system evacuated the cell to a base pressure of 10^{-6} torr. After the cell had been evacuated, the cell was filled with Rb metal. The cell was then connected to the gas filling system to fill or refill cells with³He (99.5% pure), ⁴He (99.9995% pure), and N₂ (99.9995% pure) gases. The surplus oxygen and moisture were collected via a moisture and oxygen trap (OT3 trap, Agilent Technologies, Santa Clara, CA). Homemade refillable cells with glass valves allowed one to repeatedly refill gases. The cell body was in a

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FIG. 1. (Color online) (a) Schematic of a system with optical pumping and NMR detection used for characterizing hyperpolarized ³He with and without the presence of ⁴He gas. (b) Refillable cell. (c) Sequences used to detect NMR signals.

cylindrical shape (3 cm inner diameter and 6 cm long), rounded at both ends, with a volume of 42 cm³. The valve was right angle, all glass [16], and connected to the cell via a glass tube which was 11 cm in length and 5 mm in inner diameter. The cells were heated from 150°C to 200°C while a constant field of 1.5 mT was applied during the NMR experiments. An appropriate B_1 pulse level and time duration generated a 15° low flip angle of polarization and the free induction decay NMR signals were measured.

To characterize the ³He polarization $P_{^{3}\text{He}}$, the measured NMR signal $S_{^{3}\text{He}}$ was compared with that of tap water $S_{^{1}\text{H}}$. The geometry of tap water was the same as that of the ³He cell. Measurements of polarization were done at the same

NMR frequency and rf pulse amplitude. The polarization ratio $P_{^{3}\text{He}}/P_{^{1}\text{H}}$ is obtained from the relation [17]

$$\frac{P_{^{3}\text{He}}}{P_{^{1}\text{H}}} = \frac{S_{^{3}\text{He}}}{S_{^{1}\text{H}}} \frac{\gamma_{^{1}\text{H}}^{2}}{\gamma_{^{3}\text{He}}^{2}} \frac{n_{^{1}\text{H}}}{n_{^{3}\text{He}}},$$
(1)

where *P* is the polarization, *S* is the signal amplitude, γ is the gyromagnetic ratio, and *n* is the spin density. The spin density for the ³He cell was calculated from the measured pressure.

III. RESULTS AND DISCUSSION

Figure 2 shows the polarization as a function of time during optical pumping and relaxation without buffering ⁴He at different temperatures in magnetic field of 1.5 mT. The pressure of ³He is 500 torr while that of N₂ is 70 torr. The polarization increases as the temperature of the OP cell is increased. To avoid damaging the insulation of the receiving coils, the experiments were performed only up to 200°C.

Figure 3 shows the polarization of ³He as a function of time for a cell buffered with different pressures of ⁴He at 200°C during optical pumping and relaxation. The cell was filled with 600-torr ³He and 60-torr N₂, whereas the pressure of buffered ⁴He varied from zero to 1850 torr. The maximum polarization of ³He at 4 h of optical pumping increases linearly from 7% to 30% when the pressure of ⁴He is increased from 0 to 1850 torr. The polarization during optical pumping can be described by the following equation [18]:

$$P_{^{3}\mathrm{He}} = P_{\mathrm{Rb}} \frac{\gamma_{\mathrm{se}}}{\gamma_{\mathrm{se}} + \Gamma_{1}} [1 - e^{-(\gamma_{\mathrm{se}} + \Gamma_{1})t}], \qquad (2)$$

where $P_{^{3}\text{He}}$ is the polarization of ³He, P_{Rb} is the polarization of Rb, γ_{se} is the spin-exchange rate, and Γ_{1} is the longitudinal relaxation rate of ³He that relates to T_{1} by the equation $T_{1} = 1/\Gamma_{1}$. During the relaxation period, polarization P_{off} can be described by the formula

$$P_{\rm off} = P_0 e^{-\Gamma_1 t},\tag{3}$$

in which P_0 is the polarization at the instant that the optical pump was turned off. γ_{se} and the longitudinal relaxation time T_1 were derived by fitting the experimental data into Eqs. (2) and (3). In the fitting, the ideal gas law $n_{Rb} = RT/p$ was used to calculate the rubidium density n_{Rb} , where R is Avogadro's constant, T is the temperature, and p is the pressure. The



FIG. 2. (Color online) Polarization of ³He as a function of time during optical pumping and relaxation at different temperatures.



FIG. 3. (Color online) Polarization of ³He as a function of time during optical pumping and relaxation for cells filled with different pressures of ⁴He at 200°C.



FIG. 4. (a) Spin-exchange rate γ_{se} and (b) P_{Rb} as a function of the pressure of ⁴He at 200°C.

pressure p(T) of Rb vapor was estimated from the relation [19,20] Log₁₀ p(T) = 9.318-4040/T, where *p* is in Newtons/m² and *T* is in Kelvin.

Figure 4 shows γ_{se} and P_{Rb} as functions of the pressure of ⁴He at 200. During optical pumping γ_{se} is found to be ~ 0.005 l/min and is independent of the pressure of ⁴He. The $P_{\rm Rb}$ is 20% when ⁴He is absent. The $P_{\rm Rb}$ is enhanced linearly from 20% to 80% when the pressure of ⁴He is increased from zero to 1850 torr. The ⁴He gas broadens the absorption linewidth of Rb atoms [21,22], which enhances the absorption of laser light. Therefore, there is an enhancement of ³He polarization when the pressure of ⁴He is increased. During the relaxation, the polarization $P_{\rm off}$ can be described by the relation: $P_{\text{off}} = P_0 e^{-\Gamma_1 t}$. The relaxation time $T_1 = 1/\Gamma_1$ of ³He, measured in a field homogeneity of 1 part per 10^3 , is improved from 2.05 to 2.46 h when the pressure of ⁴He is increased from zero to 1850 torr. In addition to enhancing the polarization of ³He and the buffering, ⁴He can reduce the wall relaxation rate.

Figure 5 shows the polarization of 3 He as a function of time at 200°C in different field homogeneities. The cell used for pumping contains 70-torr N₂, 1200-torr ³He, and 600-torr ⁴He and Rb metal. The $\Delta f/f = 0.00102$ corresponds to a field homogeneity of 1.02 parts in 10^3 in the sample region while the $\Delta f/f = 0.000933$ corresponds to a field homogeneity 0.933 parts in 10³, where Δf is the spectral linewidth and f is the resonance frequency. When the field homogeneity in the sample space is improved from 1.02 parts per 10^3 to 0.933 per 10^3 (8.529% improvement), the polarization of ³He is increased from 10.06% to 19.3% (82.1% improvement) and the relaxation time T_1 from 1.82 to 5.75 h (216% improvement). However, the change in the γ_{se} is not changed much. The results suggest that the field gradient affects the polarization of both Rb and ³He significantly, but not γ_{se} . The effective relaxation rate T_1^{-1} is affected by the ³He interacted with the wall [23],



FIG. 5. (Color online) Polarization of ³He as a function of time when $\Delta f/f = 0.00102$ and $\Delta f/f = 0.000933$ at 200°C.

gradient field, dipole-dipole interaction [24], etc. The T_1^{-1} can be decomposed mainly into following components:

$$1/T_{1} = 1/T_{1,\text{wall}} + 1/T_{1,\text{field gradient}} + 1/T_{1,\text{dipole-dipole}} + 1/T_{1,\text{others}}, \qquad (4)$$

where $1/T_1 = 1/T_{1,\text{wall}} + 1/T_{1,\text{field gradient}} + 1/T_{1,\text{dipole-dipole}}$, and $1/T_{1,others}$ are the relaxation rate due to the wall, field gradient, dipole-dipole interaction, and other interactions, respectively. "Other interactions" refers to factors not considered, for instance, the interaction of atoms in the dark region, etc. The basic mechanism of wall relaxation is the result of the interaction between ³He and paramagnetic electrons in the wall. If the magnetic impurities present in the wall can be removed, then the relaxation time can be improved significantly. The gradient field causes a diffusive motion of atoms that deteriorates the polarization. The field gradient plays an essential role in enhancing the polarization of ³He. The polarization is significantly enhanced by reducing the field gradient and its improvement is demonstrated in this work. The intrinsic dipole-dipole interaction is important at high pressures of several atmospheres and negligible at low pressures of several torr in the cells. In the present study, the dipole-dipole interaction is not significant. In addition to wall relaxation, dipole-dipole, and field gradient interactions, other interactions, such as anisotropic dipole interaction, can become significant at a high pressure of 3 He.

Efforts were put into improving the polarization of hyperpolarized ³He. Coatings can effectively reduce the wall relaxation [15]. Jacob *et al.* [25] developed a protocol for the consistent fabrication of glass cells. In general, a typical pumping time ranging from 12 to 20 h is required to reach a polarization of 40%, and 20% polarization of ³He is reached in 3-5 h. Instead, the OP ³He in the presence of ⁴He demonstrated in this study shows a significant enhancement in polarization. The polarization of ³He is enhanced to 30% by buffering ⁴He to a pressure of 1850 torr. The polarization of Rb is enhanced by a factor of 4 after 4 hours of optical pumping. The present method of enhancing polarization of ³He by buffering ⁴He is simple, easy to handle, and can be of great interest for lung imaging in small animals.

In a study of the limits of polarization for SEOP of ³He, Babcock *et al.* [26,27] measured the temperature dependence of ³He relaxation in a wide temperature range. An excess



FIG. 6. (Color online) (a) Polarization of 3 He as a function of the pressure of 3 He. (b) Polarization of 3 He as a function of pumping time.

relaxation that scales with the alkaline metal density was discovered. Also, the surface relaxation and anisotropic spinexchange contributions to the relaxation were reported. In the present study of polarization of Rb and ³He gas in the presence of ⁴He, it was found that P_{Rb} and $P_{^3He}$ are enhanced significantly. The enhancement of $P_{^3He}$ is dominated by exchanging P_{Rb} to $P_{^3He}$ via collision. Furthermore, the field gradient affects the polarization of Rb and hence relaxation time of ³He, but the changes to γ_{se} are minimal. The present observed unchanged γ_{se} is consistent with the reported data [28], which shows that the γ_{se} is expected to be constant for OP cells pumped at fixed temperatures.

Figure 6(a) shows the polarization of ³He as a function of pressure in the absence of ⁴He. The polarization of ³He increases from 4.5% to ~8% when the pressure is increased from 300 to 1500 torr. Figure 6(b) shows the polarization of ³He as a function of time for OP cells filled with 300- and 1500-torr ³He, respectively, with the pressure of N₂ at 60 torr. Each cell was pumped at 200 °C. After optical pumping of 6 h, the polarization of ³He was 4.5% for the cell containing 300 torr of ³He and the polarization enhanced to 8% when the pressure of ³He increased to 1500 torr. There is an enhanced polarization due to the increased γ_{se} when the pressure of ³He is increased. The relaxation rate Γ_1 is estimated to be 5×10^{-5} 1/s ($T_1 = 1/\Gamma_1 = 5.55$ h) when the pressure of ³He is 300 torr and reduces to 3.75×10^{-5} 1/s ($T_1 = 7.4$ h) when the pressure of ³He increases to 1500 torr.

Figures 7(a) and 7(b) show the polarization as a function of time for an OP cell filled with 1200-torr ³He, 1200-torr ⁴He, and 60-torr N_2 at various temperatures during optical pumping



FIG. 7. (Color online) Polarization of 3 He as a function of time for an OP cell at various temperatures during (a) optical pumping and (b) relaxation.

and relaxation, respectively. The polarization of ³He increases as the temperature of the OP cell increases. The increased polarization is attributed to the increased concentration of Rb. Therefore, more Rb atoms are contributed to the enhanced polarization during the optical pumping.

The relaxation rate, Γ_1 , at the higher temperature can be written as $\Gamma_1 = \Gamma_r + k_{se}$ [Rb] = $\Gamma_r + \gamma_{se}$, where Γ_r is the relaxation rate at 300 K and $\gamma_{se} = k_{se}$ [Rb]. Therefore, the polarization $P_{^3\text{He}}(T)$ of ³He at a fixed temperature *T* can be expressed as [28]

$$P_{^{3}\text{He}}(T) = \{P_{\text{Rb}}\gamma_{\text{se}}/[\gamma_{\text{se}}(1+X) + \Gamma_{\text{r}}]\}\{1 - e^{-[\gamma_{\text{se}}(1+X) + \Gamma_{\text{r}}]t}\},$$
(5)

where X is the wall relaxation factor. The temperaturedependent parameters T_1 and Γ_{He} were obtained by fitting the data acquired during relaxation into Eq. (5) at various temperatures. The results are shown in Table I, where

TABLE I. The longitudinal relaxation time $T_1 = 1/\Gamma_1$ and the relaxation rate Γ_{He} of hyperpolarized ³He at various temperatures. Also shown is the concentration of Rb given by [29]: [Rb] = $10^{(9.55-4132/T)}/(1.38 \times 10^{-17})T$ in units of cm⁻³, in which T is the temperature and is in units of Kelvin.

Temperature (K)	<i>T</i> ₁ (h)	$\Gamma_{\rm He} (1/s)$	[Rb](cm ⁻³)
190	5.37	5.68×10^{-5}	6.65×10^{14}
180	5.39	4.20×10^{-5}	4.32×10^{14}
170	5.95	2.83×10^{-5}	2.75×10^{14}
160	6.07	1.99×10^{-5}	1.71×10^{14}
150	6.50	1.26×10^{-5}	1.04×10^{14}
140	7.09	6.39×10^{-6}	6.20×10^{13}
130	7.28	3.76×10^{-6}	3.59×10^{13}



FIG. 8. (Color online) (a) $(\Gamma_{\text{He}} - \Gamma_{\text{r}})$ as a function of the concentration of rubidium [Rb], where $\Gamma_{\text{He}} = k_{\text{se}}[\text{Rb}](1 + X) + \Gamma_{\text{r}}$ is the total relaxation rate. (b) The X for a cell buffering with 1200-torr ⁴He is marked with red squares, while the X for cells without buffering ⁴He is marked with blue diamonds. Also shown are the parameters (+'s) from Ref. [28].

 $\Gamma_{\text{He}} = k_{\text{se}} [\text{Rb}] (1 + X) + \Gamma_{\text{r}}$. It was found that T_1 is 7.28 h when $T = 130 \,^{\circ}\text{C}$ and T_1 reduces to 5.37 h when the temperature is increased to $T = 200 \,^{\circ}\text{C}$. The value of Γ_{He} is $3.76 \times 10^{-6} (1/\text{s})$ at $T = 130 \,^{\circ}\text{C}$ and it increases linearly to $5.68 \times 10^{-5} (1/\text{s})$ when $T = 200 \,^{\circ}\text{C}$. Both $1/T_1$ and Γ_{He} increase linearly as the temperature increases. This fact is attributed to the increasing wall relaxation.

Figure 8(a) shows $(\Gamma_{\text{He}} - \Gamma_{\text{r}})$ as a function of the concentration of rubidium [Rb], where $\Gamma_{\text{He}} = k_{\text{se}}$ [Rb] $(1 + X) + \Gamma_{\text{r}}$ is the total relaxation rate for cells A and B. Cell A was filled with 1200-torr ³He, 1200-torr ⁴He, and 60-torr N₂. Cell B was filled with 1200 torr of 3 He and 60 torr of N₂. It is found that $(\Gamma_{\text{He}} - \Gamma_{\text{r}})$ increases linearly when the concentration [Rb] of Rb is increased for both cells. From the curve of (Γ_{He} – Γ_r) vs [Rb], the wall relaxation factor can be derived and is X = 0.37 for cell A, shown as red squares in Fig. 8(a). The wall relaxation factor is X = 0.56 for cell B, shown in Fig. 8(a) as blue diamonds. The wall relaxation factor for cell A is smaller compared with that of cell B. Figure 8(b) shows the wall relaxation factor X's reported by Babcock et al. [28] as +'s, showing the X's as a function of S/V for cells without buffering ⁴He, where S is the surface area and V is the volume. In this figure, the results from our study are also included for the comparison purpose. In addition, to enhance the polarization of $P_{\rm Rb}$ and $\gamma_{\rm se}$ of ³He effectively, the buffering ⁴He can reduce the wall relaxation factor of OP cells. The present results suggest that the ⁴He gas confines the ³He atoms to a diffusion-limited region which effectively reduces the wall relaxation factor X.

IV. CONCLUSION

In summary, an enhancement of polarization in OP ³He in the presence of ⁴He is demonstrated. In the absence of ⁴He, the polarization of ³He is 4.5% for a cell containing 300-torr ³He and enhanced to 8% when the pressure is increased to 1500 torr. In the presence of 1850-torr ⁴He gas, the polarization of ³He is enhanced from 7% to 30% for a cell containing 600-torr ³He and 60-torr N₂. ³He with 30% polarization and T_1 longer than 6 h can be routinely produced after 4 h of optical pumping. The buffering ⁴He gas can significantly enhance the polarization of ³He and reduce the wall relaxation factor X. Enhancing the polarization of hyperpolarized ³He in the presence of ⁴He can be promising in lung imaging [30].

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- M. A. Bouchiat, T. R. Carver, and C. M. Varnum, Phys. Rev. Lett. 5, 373 (1960).
- [2] T. G. Walker and W. Happer, Rev. Mod. Phys. 69, 629 (1997).
- [3] W. Happer, Rev. Mod. Phys. 44, 169 (1972).
- [4] R. L. Gamblin and T. R. Carver, Phys. Rev. 138, A946 (1965).
- [5] X. Zeng, E. Miron, W. A. van Wijngaarden, D. Schreiber, and W. Happer, Phys. Lett. A 96, 191 (1983).
- [6] D. R. Rich, T. R. Gentile, T. B. Smith, and A. K. Thomson, and G. L. Jones, Appl. Phys. Lett. 80, 2210 (2002).
- [7] T. Rõõm, S. Appelt, R. Seydoux, E. L. Hahn, and A. Pines, Phys. Rev. B 55, 11604 (1997).
- [8] M. S. Albert, D. G. Cates, B. Driebuys, W. Happer, B. Saam, C. S. Springer, and A. Wishnia, Nature (London) 370, 199 (1994).

- [9] C. H. Tseng, G. P. Wong, V. R. Pomeroy, R. W. Mair, D. P. Hinton, D. Hoffmann, R. E. Stoner, F. W. Hersman, D. G. Cory, and R. L. Walsworth, Phys. Rev. Lett. 81, 3785 (1998).
- [10] S.-H. Liao, H.-C. Yang, H.-E. Horng, S. Y. Yang, M. J. Chen, and C.-H. Yang, J. Appl. Phys. **104**, 063918 (2008).
- [11] B. Chann, E. Babcock, L. W. Anderson, T. G. Walker, W. C. Chen, T. B. Smith, A. K. Thomson, and T. B. Gentile, J. Appl. Phys. 94, 6908 (2003).
- [12] R. E. Jacob, J. Teter, and B. Saam, W. C. Chen, and T. R. Gentile, Phys. Rev. A 69, 021401(R) (2004).
- [13] W. Heil, H. Humblot, E. Otten, M. Schafer, R. Sarkau, and M. Leduc, Phys. Lett. A 201, 337 (1995).
- [14] G. L. Jones, T. R. Gentile, A. K. Thompson, Z. Chowdhuri, M. S. Dewey, W. M. Snow, and F. E. Wietfeldt, Nucl. Instrum. Methods Phys. Res. A 440, 772 (2000).

- [15] S. R. Breeze, S. Lang, I. M. Moudrakoviki, C. I. Rotchiffe, J. A. Ripmeester, and B. Simard, J. Appl. Phys. 86, 4040 (1999).
- [16] Part No. 826460-004, Kimble/Kontes, Vineland, NJ.
- [17] B. Saam and M. S. Conradi, J. Magn. Reson. 134, 67 (1998).
- [18] R. E. Jacob, S. W. Morgan, B. Saam, and J. C. Leawoods, Phys. Rev. Lett. 87, 143004 (2001).
- [19] C. B. Alcock, V. P. Itkin, and M. K. Horrigan, Can. Metall. Q. 23, 309 (1984).
- [20] in CRC Handbook of Chemistry and Physics, edited by David R. Lide (CRC Press, Boca Raton, FL, 1994), 75th ed.
- [21] D. Aumiler, T. Ban, and G. Pichler, Phys. Rev. A 70, 032723 (2004)
- [22] A. Andalkar and R. B. Warrington, Phys. Rev. A 65, 032708 (2002)

- [23] F. D. Colegrove, L. D. Schearer, and G. K. Waltes, Phys. Rev. 132, 2561 (1963).
- [24] R. Barbé, M. Leduc, and F. Laloë, J. Phys. 35, 699 (1974).
- [25] R. E. Jacob, S. W. Morgan, and B. Saam, J. Appl. Phys. 92, 1588 (2002).
- [26] B. Chann, E. Babcock, L. W. Anderson, and T. G. Walker, Phys. Rev. A 66, 032703 (2002).
- [27] E. Babcock, B. Chann, T. G. Walker, W. C. Chen, and T. R. Gentile, Phys. Rev. Lett. 96, 083003 (2006).
- [28] E. Babcock, B. Chann, T. G. Walker, W. C. Chen, and T. R. Gentile, Phys. Rev. Lett. 96, 083003 (2006).
- [29] T. J. Killian, Phys. Rev. 27, 578 (1926).
- [30] H. E. Möller, X. J. Chen, B. Saam, K. D. Hagspiel, G. A. Johnson, T. A. Altes, E. E. de Lange, and H.-U. Kauczor, Magn. Reson. Med. 47, 1029 (2002).