Enhanced transmission of light through subwavelength nanoapertures by far-field multiple-beam interference

S. V. Kukhlevsky

Department of Physics, University of Pécs, Ifjúság u. 6, H-7624 Pécs, Hungary (Received 19 December 2007; published 15 August 2008)

Subwavelength aperture arrays in thin metal films can enable enhanced transmission of light waves. The phenomenon relies on resonant excitation and interference of the plasmon-polariton waves on the metal surface. We show a mechanism that could provide great resonant and nonresonant transmission enhancements of the light waves passed through the apertures not by the surface waves, but by the constructive interference of diffracted waves (beams generated by the apertures) at the detector placed in the far-field zone. In contrast to other models, the mechanism depends on neither the nature of the beams (continuous waves and pulses) nor material and shape of the multiple-beam source (arrays of one- and two-dimensional subwavelength apertures, fibers, dipoles, and atoms). The Wood anomalies in transmission spectra of gratings, a long standing problem in optics, follow naturally from the interference properties of our model. The point is the prediction of the Wood anomaly in a classical Young-type two-source system. The mechanism could be interpreted as a nonquantum analog of the super-radiance emission of a subwavelength ensemble of atoms the light power and energy scales as the number of light-sources squared, regardless of periodicity) predicted by the well-known Dicke quantum model.

DOI: [10.1103/PhysRevA.78.023826](http://dx.doi.org/10.1103/PhysRevA.78.023826)

PACS number(s): 42.25.Bs, 42.25.Fx, 42.79.Ag, 42.79.Dj

The scattering of waves by apertures is one of the basic phenomena in wave physics. The most remarkable feature of the light scattering by subwavelength apertures in a metal screen is enhancement of the light by excitation of plasmons in the metal. Since the observation of enhanced transmission of light through a two-dimensional (2D) array of subwavelength metal nanoholes $[1]$ $[1]$ $[1]$, the phenomenon attracts increasing interest of researchers because of its potential for applications in nano-optics and nanophotonics $[2-25]$ $[2-25]$ $[2-25]$. The enhancement of light is a process that can include resonant excitation and interference of surface plasmons $[3-5]$ $[3-5]$ $[3-5]$, Fabry-Perot-like intraslit modes $[6-10]$ $[6-10]$ $[6-10]$, and evanescent electromagnetic waves at the metal surface $[11]$ $[11]$ $[11]$. Most of the related published work concerns the transmission though thick (many skin depths) metals. It is clear that there would be almost no transmission through a thick metal in the absence of waveguide and plasmon resonances. In the case of a thin screen whose thickness is too small to support the intraslit resonance, the extraordinary transmission is caused by the excitation and interference of plasmons on the metal surface [[3–](#page-4-3)[5](#page-4-4)]. For some experimental conditions, many studies [[12–](#page-4-8)[23](#page-4-9)] indicated a nonessential role of the surface plasmons in the enhancement of light waves. For an example, the study $\lceil 18 \rceil$ $\lceil 18 \rceil$ $\lceil 18 \rceil$ showed that a perfect conductor whose surface is patterned by an array of holes can support surface polaritons, which just mimic a surface plasmon in channeling of additional energy into the aperture. Nowadays, it is generally accepted $\left[24\right]$ $\left[24\right]$ $\left[24\right]$ that the excitation and interference of surface plasmon-polaritons play a key role in the process of enhancement of light waves in most of the experiments (also, see the recent comprehensive reviews $[25,26]$ $[25,26]$ $[25,26]$ $[25,26]$). In the present study [[27](#page-5-0)], we show a mechanism that could provide great resonant and nonresonant transmission enhancements of the light waves passed through the apertures not by the surface waves, but by the constructive interference of diffracted waves (beams generated by the apertures) at the detector placed in the far-field zone.

The transmission enhancement by the constructive interference of diffracted waves at the detector can be explained in terms of the following theoretical formulation. We first consider the transmission of light through a structure that is similar, but simpler than an array of holes, namely an array of parallel subwavelength-width slits in the metal screen. In some respects, the resonant excitation and interference of surface plasmon-polaritons in these two systems are different from each other $[28]$ $[28]$ $[28]$. The difference, however, is irrelevant from the point of view of our model. Indeed, the excitation of plasmon-polaritons and coupling between the apertures do not affect the principle of the enhancement based on the constructive interference of diffracted waves (beams generated by the independent apertures) at the detector placed in the far-field zone. The resonant excitation of the plasmons or trapped electromagnetic modes, as well as the coupling between apertures could provide just additional, in comparison to our model, enhancement by increasing the power (energy) of each beam. Therefore our model considers an array of slits, which are completely independent from each other. We also assume, for the sake of simplicity, that the metal is a perfect conductor. Such a metal is described by the classic Drude model for which the plasmon frequency tends towards infinity. The beam produced by each independent slit is found by using the Neerhoff and Mur model, which uses a Green's function formalism for a rigorous numerical solution of Maxwell's equations for a single, isolated slit $\left[29-34\right]$ $\left[29-34\right]$ $\left[29-34\right]$. In the model, the screen placed in vacuum is illuminated by a normally incident TM-polarized wave with the wavelength $\lambda = 2\pi c/\omega = 2\pi/k$. The magnetic field of the incident wave $H(x, y, z, t) = U(x) \exp[-i(kz + \omega t)]\vec{e}_y$ is supposed to be time harmonic and constant in the *y* direction. The transmission of the slit array is determined by calculating all the light power of the ensemble of beams in the observation plane. To clarify the numerical results, we then present an analytical model, which quantitatively explains the resonant and nonresonant

FIG. 1. The per-slit transmission $T_M(\lambda)$ of an array of independent slits of period Λ in a thin $(b \ll \lambda)$ screen vs the wavelength for the different number *M* of slits. There are three Fabry-Perot-like resonances at the wavelengths $\lambda_n \approx \Lambda/n$, where *n*=1, 2, and 3.

enhancement in the intuitively transparent terms of the constructive interference of diffracted waves (beams generated by the apertures) at the detector placed in the far-field zone. Finally, we show that the mechanism depends on neither nature of the beams (continuous waves and pulses) nor material and shape of the multiple-beam source (arrays of 1D) and 2D subwavelength apertures, fibers, dipoles, and atoms).

Let us first investigate the light transmission versus the wavelength by using the rigorous numerical model. The model considers an ensemble of *M* waves (beams) produced by *M* independent slits of width $2a$ and period Λ in a screen of thickness *b*. The transmission of the slit array is determined by calculating all the light power $P(\lambda)$ radiated by the slits into the far-field diffraction zone, $x \in [-\infty, \infty]$ at the distance $z \gg \lambda$ from the screen. The total per-slit transmission coefficient, which represents the per-slit enhancement in transmission achieved by taking a single, isolated slit (beam) and placing it in an M -slit (M -beam) array, is then found by using an equation $T_M(\lambda) = P(\lambda) / MP_1$, where P_1 is the power radiated by a single slit. Figure [1](#page-1-0) shows the transmission coefficient $T_M(\lambda)$, in the spectral region 500–2000 nm, calculated for the array parameters: $a = 100$ nm, $\Lambda = 1800$ nm, and $b=5\times10^{-3}\lambda_{max}$. The transmitted power was computed by integrating the total energy flux at the distance $z=1$ mm over the detector region of width $\Delta x=20$ mm. The transmission spectra $T_M(\lambda)$ is shown for different values of *M*. We notice that the spectra $T_M(\lambda)$ is periodically modulated, as a function of wavelength, below and above a level defined by the transmission $T_1(\lambda) = 1$ of one isolated slit. As *M* is increased from 2 to 10, the visibility of the modulation fringes increases approximately from 0.2 to 0.7. The transmission T_M exhibits the Fabry-Perot-like maxima around wavelengths $\lambda_n = \Lambda/n$. The spectral peaks increase with increasing the number of slits and reach a saturation $(T_M^{max} \approx 5)$ in amplitude by $M = 300$, at $\lambda \approx 1800$ nm. The peak widths and the spectral shifts of the resonances from the Fabry-Perot wavelengths decrease with increasing the number *M* of beams (slits). An analysis of Fig. [1](#page-1-0) indicates that the power (energy) enhancement and dispersion are the general interference properties of the ensemble of beams. Therefore the enhancement and suppression in the transmission spectra could be considered as the natural properties also of the periodic array of independent subwavelength slits. The spectral peaks are characterized by asymmetric Fano-like profiles. Such modulations in the transmission spectra are known as Wood's anomalies. The minima and maxima correspond to Rayleigh anomalies and Fano resonances, respectively $\lceil 35 \rceil$ $\lceil 35 \rceil$ $\lceil 35 \rceil$. The Wood anomalies in transmission spectra of gratings, a long standing problem in optics, follow naturally from the interference properties of our model. The point, in comparison to other models $[36,37]$ $[36,37]$ $[36,37]$ $[36,37]$), is the prediction of a weak Wood anomaly in a classical Young-type two-source system (see, Fig. [1](#page-1-0)).

The above-presented analysis is based on calculation of the energy flux of a beam array, in which the electromagnetic field of a single beam is evaluated numerically. The transmission enhancement and dispersion were achieved by taking a single, isolated slit (beam) and placing it in a slit (beam) array. The interference of diffracted waves (beams generated by the slits) at the detector placed in the far-field zone could be considered as a physical mechanism responsible for the enhancement and dispersion. To clarify the results of the computer code and gain physical insight into the enhancement mechanism, we have developed an analytical model, which yields simple formulas for the electromagnetic field of the beam produced by a single slit. For the field diffracted by a narrow $(2a \le \lambda, b \ge 0)$ slit into the region $|z|$ $>$ 2*a*, the Neerhoff and Mur model simplifies to an analytical one [[38](#page-5-7)]. For the magnetic $\vec{H} = (0, H_y, 0)$ and electric \vec{E} $=(E_x, 0, E_z)$ components of the single beam we found the following analytical expressions:

$$
H_y(x,z) = iaDF_0^1(k[x^2 + z^2]^{1/2}),
$$
\n(1)

$$
E_x(x,z) = - az[x^2 + z^2]^{-1/2} DF_1^1(k[x^2 + z^2]^{1/2}),
$$
 (2)

and

$$
E_z(x,z) = ax[x^2 + z^2]^{-1/2}DF_1^1(k[x^2 + z^2]^{1/2}),
$$
 (3)

$$
D = 4k^{-1}\{[\exp(ikb)(aA - k)]^{2} - (aA + k)^{2}\}^{-1}
$$
 (4)

and

where

$$
A = F_0^1(ka) + \frac{\pi}{2} [\bar{F}_0(ka) F_1^1(ka) + \bar{F}_1(ka) F_0^1(ka)].
$$
 (5)

Here, F_1^1 , F_0^1 , \bar{F}_0 , and \bar{F}_1 are the Hankel and Struve functions, respectively. The beam is spatially inhomogeneous, in contrast to a common opinion that a subwavelength aperture diffracts light in all directions uniformly $\lceil 39 \rceil$ $\lceil 39 \rceil$ $\lceil 39 \rceil$. The electrical and magnetic components of the field produced by a periodic array of *M* independent slits (beams) is given by $E(x, z)$ → $=\sum_{m=1}^{M} \vec{E}_m(x+m\Lambda, z)$ and $\vec{H}(x, z) = \sum_{m=1}^{M} \vec{H}_m(x+m\Lambda, z)$, where \vec{E}_m and \vec{H}_m are the electrical and magnetic components of the → *m*th beam generated by the respective slit. As an example,

FIG. 2. The electrical and magnetic components of the field produced by an array of M independent slits (beams). (a) The distributions $\text{Re}[E_x(x)]$ (*A* and *D*), $\text{Re}[H_y(x)]$ (*B* and *E*), and $\text{Re}[10E_z(x)]$ (*C* and *F*) calculated for $M=10$ and $\lambda=1600$ nm. The curves *A*, *B*, and *C*: rigorous computer code; curves *D*, *E*, and *F*: analytical model. (b) $Re[E_x(x)]$ for $M=1$: analytical model. (c) $\text{Re}[E_x(x)]$ for $M=5$: analytical model.

→

Fig. [2](#page-2-0)(a) compares the far-field distributions \vec{E} and \vec{H} calculated by using the analytical formulas (1) (1) (1) – (5) (5) (5) to that obtained by the rigorous computer model. We notice that the distributions are undistinguishable. The field power $P(\vec{E}, \vec{H})$ is found by integrating the energy flux $\vec{S} = \vec{E} \times \vec{H}^* + \vec{E}^* \times \vec{H}$. Therefore the analytical model accurately describes also the coefficient T_M of the system of *M* independent subwavelength slits (beams). The analytical model not only supports results of our rigorous computer code (Fig. [1](#page-1-0)), but presents an intuitively transparent explanation (physical mechanism) of the enhancement and suppression in transmission spectra in terms of the constructive or destructive interference of the waves (beams produced by the subwavelength-width sources) at the detector placed in the far-field zone. The array-induced decrease of the central beam divergence by the far-field multiple beam interference [Figs. $2(b)$ $2(b)$ and $2(c)$] is relevant to the beaming light $[40]$ $[40]$ $[40]$, as well as the "diffractionfree" light and matter beams $[41, 42]$ $[41, 42]$ $[41, 42]$. The amplitude of a beam (evanescent spherical-like wave) produced by a single slit rapidly decreases with increasing the distance from the slit [Eqs. (1) (1) (1) – (3) (3) (3)]. However, due to the multiple beam interference mechanism of the enhancement and beaming, the array produces in the far-field zone a propagating wave with low divergence. Such a behavior is in agreement with the Huygens-Fresnel principle, which considers a propagating wave as a superposition of secondary spherical waves.

We now consider the predictions of our analytical model in light of the key observations published in the literature for the two fundamental systems of wave optics, the one-slit and two-slit systems. The major features of the transmission through a single subwavelength slit are the intraslit resonances and the spectral shifts of the resonances from the Fabry-Perot wavelengths $[7]$ $[7]$ $[7]$. In agreement with the predic-

FIG. 3. The per-slit transmission coefficient $T_2(\lambda)$ vs wavelength for the Young type two-slit experiment $\lceil 36 \rceil$ $\lceil 36 \rceil$ $\lceil 36 \rceil$. Solid curve: experiment; dashed curve: analytical model. Parameters: *a* $= 100$ nm, $\Lambda = 4900$ nm, and $b = 210$ nm.

tions $\begin{bmatrix} 7 \end{bmatrix}$ $\begin{bmatrix} 7 \end{bmatrix}$ $\begin{bmatrix} 7 \end{bmatrix}$, the formula ([4](#page-1-4)) shows that the transmission *T* $= P/P_0 = (a/k)[\text{Re}(D)]^2 + [\text{Im}(D)]^2$ exhibits Fabry-Perot-like maxima around wavelengths $\lambda_n = 2b/n$, where P_0 is the power impinging on the slit opening. The enhancement and spectral shifts are explained by the wavelength dependent terms in the denominator of Eq. (4) (4) (4) . The enhancement $[T(\lambda_1) \approx b / \pi a$ [[38](#page-5-7)]] is in contrast to the attenuation predicted by the model $\lceil 7 \rceil$ $\lceil 7 \rceil$ $\lceil 7 \rceil$. Although our model considers a screen of perfect conductivity, polarization charges develop on the metal surface. The surface polaritons do not adhere strictly to traditional surface plasmons. Nevertheless, at the resonant conditions, the system redistributes the electromagnetic energy by the surface polaritons in the intraslit region and around the screen. Thus additional energy could be channeled thought the slit in comparison to the energy impinging on the slit opening. The mechanism is somewhat similar to that described in the study $[18]$ $[18]$ $[18]$. This study showed that a perfect conductor whose surface is patterned by an array of holes can support surface polaritons that mimic a surface plasmon in the process of channeling additional energy into the slit. We considered TM-polarized modes because TE modes are cut off by a thick slit. In the case of a thin screen, TE modes propagate into the slit so that magnetopolaritons develop. Because of the symmetry of Maxwell's equations the scattering intensity is formally identical with \vec{E} and \vec{H} swapping roles. Again, the magnetopolaritons could provide channeling of additional energy into the slit. This enhancement mechanism is different from those based on the constructive interference of the waves (beams produced by the subwavelength-width sources) at the detector placed in the far-field zone. The Young type two-slit (two-beam) configuration is characterized by a sinusoidal modulation of the transmission spectra [for an example, see $T_2(\lambda)$ in Refs. [[36,](#page-5-5)[37](#page-5-6)]]. The modulation period is inversely proportional to the slit separation Λ . The visibility *V* of the fringes is of order 0.2, independently of the slit separation. In our model, the transmission T_2 depends on the interferencelike cross term \int { $F_1^1(x_1)[iF_0^1(x_2)]^* + F_1^1(x_1)^*iF_0^1(x_2)$ }*dx*, where $x_1 = x$ and $x_2 = x + \Lambda$. The high-frequency interferencelike modulations with the sideband-frequency $f_s(\Lambda) \approx f_1(\lambda) + f_2(\Lambda, \lambda) \sim 1/\Lambda$ (Figs. [1](#page-1-0) and [3](#page-2-1)) are produced like that in a classic heterodyne system by mixing two waves having different spatial frequencies, f_1 and f_2 . Although our model ignores the enhancement by the plasmon-polaritons, its prediction for the transmission $(T_2^{max} \approx 1.1)$, the visibility $(V \approx 0.1)$ of the fringes, and the resonant wavelengths $\lambda_n \approx \Lambda/n$ compare well with the plasmon-assisted Young's type experiment $[36]$ $[36]$ $[36]$ (Fig. [3](#page-2-1)).

It should be noted that in the case of $b \ge \lambda/2$, the far-field interference resonances at $\lambda_n \approx \Lambda/n$ could be accompanied by the intraslit polariton resonances at $\lambda_n \approx 2b/n$. One can easily demonstrate such behavior by using the analytical formulas (1) (1) (1) – (5) (5) (5) . The interference of two beams at the detector is not the only contribution to enhanced transmission. There could be enhancement also due to the energy redistribution by the resonant intraslit plasmon-polaritons and/or by the surface waves with resonant coupling through the slits. We stress, however, that the plasmons or trapped electromagnetic modes do not affect the principle of the enhancement based on the constructive interference of diffracted waves (beams generated by the independent subwavelength-width apertures) at the detector placed in the far-field zone. The plasmon-polaritons could provide just additional enhancement by increasing the power and energy of each beam. This kind of enhancement is of different nature compared to our model because the model requires neither resonant excitation of the intraslit plasmon-polaritons nor coupling between the slits (see, also Refs. $[22, 43, 44]$ $[22, 43, 44]$ $[22, 43, 44]$ $[22, 43, 44]$ $[22, 43, 44]$ $[22, 43, 44]$ $[22, 43, 44]$).

In order to gain physical insight into the mechanism of plasmonless and polaritonless enhancement in a multiple-slit or multiple-beam $(M \ge 2)$ system, we now consider the dependence of the transmission $T_M(\lambda)$ on the slit (beam) separation Λ . According to the Van Citter-Zernike coherence theorem, a light source (even incoherent) of radius $r = M(a)$ $+\Lambda$) produces a transversely coherent wave at the distance $z \leq \pi R r / \lambda$ in the region of radius *R*. In the case of $\Lambda \ll \lambda$, the collective coherent emission of an ensemble of slits (beams) generates the coherent electromagnetic field $\vec{E} = \sum_{m=1}^{M} \vec{E}_m \exp(i\varphi_m) \approx M \vec{E}_1 \exp(i\varphi)$ and $\vec{H} \approx M \vec{H}_1 \exp(i\varphi)$ in the far-field zone of the region of radius $R = \infty$. This means that the beams arrive at the detector with nearly the same phases $\varphi_m(x) \approx \varphi(x)$ (see also Ref. [[45](#page-5-14)]). Consequently, the beams add coherently and the power (energy) of the emitted light scales as the number of beams squared, regardless of periodicity, $P \approx M^2 P_1$. Thus the transmission enhancement $(T_M = P/MP_1)$ grows linearly with the number of slits, T_M \sim *M*. For a given value of *M*, in the case of $\Lambda \ll \lambda$, the transmission $T_M(\lambda)$ monotonically (nonresonantly) varies with λ (see Fig. [4](#page-3-0)). At the appropriate conditions, the transmission can reach the 1000-times nonresonant enhancement $[M = \lambda z / \pi R(a + \Lambda)]$. In the case of $R > \lambda z / \pi r$ or $\Lambda > \lambda$, the beams arrive at the detector with different phases $\varphi_m(x)$. Consequently, the power and transmission enhancement grow slowly with the number of beams (Figs. $1-4$ $1-4$). The constructive or destructive interference of the beams leads, respectively, to the enhancement or suppression of the transmission amplitudes. Although the addition of beams is not so efficient, the multiple beam interference leads to enhancements and resonances (versus wavelength) in the total power transmitted. In such a case, the transmission coefficient T_M exhibits the Fabry-Perot-like maxima around the wavelengths $\lambda_n = \Lambda/n$. We stress again that the constructive or destructive interference of beams at the detector requires neither the resonant excitation of plasmon-polaritons nor the coupling between radiation phases of the slits. The plasmonpolariton effects could provide just additional enhancement by increasing the power and energy of each beam. Our con-

FIG. 4. The per-slit transmission $T_M(\lambda)$ vs wavelength for the different values of Λ and *M*: (A) Λ =100 nm, *M*=2; (B) Λ $= 500$ nm, $M=2$; (C) $\Lambda = 3000$ nm, $M=2$; (D) $\Lambda = 100$ nm, $M=5$; (E) Λ =500 nm, M =5; and (F) Λ =3000 nm, M =5. Parameters: *a* $= 100$ nm and $b = 10$ nm. There are two enhancement regimes at $\Lambda \ll \lambda$ and $\Lambda > \lambda$.

sideration of the subwavelength gratings is similar in spirit to the dynamical diffraction models $[12]$ $[12]$ $[12]$, Airy-like model $[13]$ $[13]$ $[13]$, and especially to a surface evanescent wave model $[11]$ $[11]$ $[11]$. In the case of $\Lambda \gg \lambda$, our model is in agreement with the theo-ries of conventional (non-subwavelength) gratings [[46](#page-5-15)].

In the above-presented multiple-beam interference model, we have considered a particular light source, namely an array of subwavelength metal slits. One can easily demonstrate the interference mediated enhancement and suppression in the transmission and reflection spectra of an arbitrary array of subwavelength-dimension sources of light by taking into account the interference properties of Young's double-source system. At the risk of belaboring the obvious, we now describe the phenomenon. In the far-field diffraction zone, the radiation from two pinholes of Young's setup is described by two spherical waves. The light intensity at the detector is given by $I(\vec{r}) = |(E/r_1) \exp(ikr_1 + \varphi_1) + (E/r_2) \exp(ikr_2 + \varphi_2)|^2$ $=I_1+I_2+2(I_1I_2)^{1/2}\cos([kr_1+\varphi_1]-[kr_2+\varphi_2]).$ The corresponding energy is $W = \int \int \{I_1 + I_2 + 2(I_1 I_2)^{1/2} \cos([kr_1 + \varphi_1]$ $-\left[kr_2 + \varphi_2\right]$ }*dxdy*. Here, we use the units *c*∆*t*=1. In a conventional Young's setup, which contains the pinholes separated by the distance $\Lambda \gg \lambda$, the interference cross term (energy) vanishes. Therefore the energy is given by $W = \int \int (I_1)$ $+I_2$) $dxdy = W_1 + W_2 = 2W_0$, where $W_1 = W_2 = W_0$. In the case of Young's subwavelength system ($\Lambda \ll \lambda$, correspondingly r_1) $=r_2$ for any coordinate *x* or *y*), the energy $W = W_1 + W_2$ +2 $\int \int (I_1 I_2)^{1/2} \cos(\varphi_1 - \varphi_2) dx dy$. The first-order correlation term could provide the enhancement or suppression of both the intensity and energy of the light field at the detector (see also Refs. [[44,](#page-5-13)[47](#page-5-16)]). Indeed, at the phase condition $\varphi_1 - \varphi_2$ $= 0$, the energy enhancement is given by $W = 4W_0$. In the case of $\varphi_1 - \varphi_2 = \pi$, the destructive interference of the two waves leads to the zero transmission, *W*= 0. The same phase conditions could provide the enhancement or suppression of transmitted energy by quantum two-source interference (for example, see formulas $4.A.1-4.A.9$ $[48]$ $[48]$ $[48]$). The enhancement or

suppression by the classic or quantum interference at the detector depends on neither nature of the beams (continuous waves and pulses) nor material and shape of the multiplebeam source (arrays of 1D and 2D subwavelength apertures, fibers, dipoles, and atoms). Due to Babinet's principle, the model predicts the enhancement and suppression also in the reflection spectra. According to our model, the power and energy of the light emitted by the subwavelength-dimension ensemble of light sources scales as the number of lightsources squared, regardless of periodicity of the array of sources. Such an effect is not unknown in the physics. The famous Dicke quantum model of the super-radiance emission of a subwavelength ensemble of atoms predicts the same scaling behavior $[49]$ $[49]$ $[49]$. Therefore the mechanism described in the present paper could be interpreted as a nonquantum analog of the super-radiance emission of a subwavelength ensemble of coherent light-sources. The evident resemblance between our model and the Dicke model also indicates that the interference of waves at the detector could lead to the enhancements and resonances (versus period of the array) in the total power emitted by the periodic array of quantum oscillators (atoms). A quantum reformulation of our model, which will be presented in the next paper, could also help us to understand better why a quantum entangled state is preserved on passage through a hole array $\lceil 50 \rceil$ $\lceil 50 \rceil$ $\lceil 50 \rceil$.

In conclusion, we have demonstrated a mechanism that could provide great resonant and nonresonant transmission enhancements of the light waves passed through the apertures not by the surface waves, but by the constructive interference of diffracted waves (beams generated by the apertures) at the detector placed in the far-field zone. The model shows that the beams generated by multiple, subwavelengthwide slits can have similar phases and can add coherently. If the spacing of the slits is smaller than the optical wavelength, then the phases of the multiple beams at the detector are nearly the same and beams add coherently (the light power and energy scales as the number of light-sources squared, regardless of periodicity). If the spacing is larger, then the addition is not so efficient, but still leads to enhancements and resonances (versus wavelength) in the total power transmitted. In contrast to other models, the mechanism depends on neither nature of the beams (continuous waves and pulses) nor material and shape of the multiple-beam source arrays of 1D and 2D subwavelength apertures, fibers, dipoles, and atoms). The verification of the results by comparison with data published in the literature supports the model predictions. The Wood anomalies in transmission spectra of gratings, a long standing problem in optics, follow naturally from the interference properties of our model. The point is the prediction of the Wood anomaly in a classical Youngtype two-source system. The mechanism could be interpreted as a nonquantum analog of the super-radiance emission of a subwavelength ensemble of atoms (the light power and energy scales as the number of light-sources squared, regardless of periodicity) predicted by the well-known Dicke quantum model. We stress again that the plasmons or trapped electromagnetic modes do not affect the principle of the enhancement based on the classic or quantum interference of diffracted waves (beams generated by the independent subwavelength sources) at the detector placed in the far-field zone. The plasmon-polaritons could provide just additional enhancement by increasing the power and energy of each beam. The analytical formulas derived in the present study could be useful for experimentalists who develop nanodevices based on transmission and beaming of the light waves by subwavelengths apertures.

This study was supported in part by the Framework for European Cooperation in the field of Scientific and Technical Research (COST, Contract No. MP0601) and the Hungarian Research and Development Program (KPI, Contract No. GVOP 0066-3.2.1.-2004-04-0166/3.0).

- [1] T. W. Ebbesen et al., Nature (London) 391, 667 (1998).
- [2] W. L. Barnes *et al.*, Nature (London) **424**, 824 (2003).
- [3] U. Schröter and D. Heitmann, Phys. Rev. B 58, 15419 (1998).
- [4] M. B. Sobnack, W. C. Tan, N. P. Wanstall, T. W. Preist, and J. R. Sambles, Phys. Rev. Lett. **80**, 5667 (1998).
- [5] J. A. Porto, F. J. Garcia-Vidal, and J. B. Pendry, Phys. Rev. Lett. **83**, 2845 (1999).
- [6] S. Astilean, P. Lalanne, and M. Palamaru, Opt. Commun. 175, 265 (2000).
- [7] Y. Takakura, Phys. Rev. Lett. **86**, 5601 (2001).
- [8] P. Lalanne C. Sauvan, J. P. Hugonin, J. C. Rodier, and P. Chavel, Phys. Rev. B 68, 125404 (2003).
- [9] A. Barbara et al., Eur. Phys. J. D 23, 143 (2003).
- [10] S. V. Kukhlevsky, M. Mechler, L. Csapo, K. Janssens, and O. Samek, Phys. Rev. B 70, 195428 (2004).
- [11] H. J. Lezec and T. Thio, Opt. Express 12, 3629 (2004).
- [12] M. M. J. Treacy, Phys. Rev. B 66, 195105 (2002).
- [13] Q. Cao and P. Lalanne, Phys. Rev. Lett. 88, 057403 (2002).
- [14] M. Sarrazin, J. P. Vigneron, and J. M. Vigoureux, Phys. Rev. B

67, 085415 (2003).

- [15] W. L. Barnes, W. A. Murray, J. Dintinger, E. Devaux, and T. W. Ebbesen, Phys. Rev. Lett. 92, 107401 (2004).
- [16] K. J. Klein Koerkamp, S. Enoch, F. B. Segerink, N. F. van Hulst, and L. Kuipers, Phys. Rev. Lett. 92, 183901 (2004).
- 17 A. E. Miroshnichenko and Y. S. Kivshar, Phys. Rev. E **72**, 056611 (2005).
- [18] J. B. Pendry, Science 305, 847 (2004).
- [19] R. Gomez-Medina, M. Laroche, and J. J. Saenz, Opt. Express 14, 3730 (2006).
- [20] E. Moreno, L. Martin-Moreno, and F. G. Garcia-Vidal, J. Opt. A, Pure Appl. Opt. 8, S94 (2006).
- [21] B. Ung and Y. Sheng, Opt. Express 15, 1182 (2006).
- [22] X. R. Huang, R. W. Peng, Z. Wang, F. Gao, and S. S. Jiang, Phys. Rev. A **76**, 035802 (2007).
- [23] Y. Ben-Aryeh, Appl. Phys. B: Lasers Opt. 91, 157 (2008).
- [24] H. Liu and P. Lalanne, Nature (London) **452**, 728 (2008).
- [25] F. J. Garcia de Abajo, Rev. Mod. Phys. **79**, 1267 (2007).
- 26 A. K. Sarychev and V. M. Shalaev, *Electrodynamics of*

Metamaterials (World Scientific, Singapore, 2007), p. 185.

- [27] The study was presented at the Nanoelectronic Devices for Defense and Security (NANO-DDS) Conference, 2007, Washington, DC (unpublished).
- [28] E. Popov, M. Neviere, S. Enoch, and R. Reinisch, Phys. Rev. B **62**, 16100 (2000).
- [29] F. L. Neerhoff and G. Mur, Appl. Sci. Res. **28**, 73 (1973).
- [30] R. F. Harrington and D. T. Auckland, IEEE Trans. Antennas Propag. **AP28**, 616 (1980).
- 31 E. Betzig, A. Harootunian, A. Lewis, and M. Isaacson, Appl. Opt. 25, 1890 (1986).
- [32] S. V. Kukhlevsky, M. Mechler, L. Csapo, K. Janssens, and O. Samek, Phys. Rev. B **72**, 165421 (2005).
- [33] M. Mechler, O. Samek, and S. V. Kukhlevsky, Phys. Rev. Lett. **98**, 163901 (2007).
- 34 S. V. Kukhlevsky, in *Lasers and Electro-optics Research at the* Cutting Edge, edited by Steven B. Larkin (Nova Science Publishers, New York, 2007), Chap. 1, pp. 1–42.
- [35] A. Hessel and A. A. Oliner, Appl. Opt. 4, 1275 (1965).
- 36 H. F. Schouten, N. Kuzmin, G. Dubois, T. D. Visser, G. Gbur, P. F. Alkemade, H. Blok, G. W. t'Hooft, D. Lenstra, and E. R. Eliel, Phys. Rev. Lett. **94**, 053901 (2005).
- [37] P. Lalanne, J. P. Hugonin, and J. C. Rodier, Phys. Rev. Lett.

95, 263902 (2005).

- [38] S. V. Kukhlevsky, M. Mechler, O. Samek, and K. Janssens, Appl. Phys. B: Lasers Opt. **84**, 19 (2006).
- [39] H. J. Lezec *et al.*, Science **297**, 820 (2002).
- [40] L. Martin-Moreno, F. J. Garcia-Vidal, H. J. Lezec, A. Degiron, and T. W. Ebbesen, Phys. Rev. Lett. **90**, 167401 (2003).
- 41 S. V. Kukhlevsky, in *Localized Waves*, edited by H. E. Hernandez-Figueroa, M. Zamboni-Rached, and E. Recami (Wiley, Hoboken, N.J., 2008), Chap. 10, pp. 273-297.
- [42] S. V. Kukhlevsky, G. Nyitray, and V. L. Kantsyrev, Phys. Rev. E **64**, 026603 (2001).
- [43] R. Gordon, J. Opt. A, Pure Appl. Opt. 8, L1 (2006).
- [44] S. V. Kukhlevsky, e-print arXiv:physics/0602190.
- [45] C. Genet *et al.*, J. Opt. Soc. Am. A 22, 998 (2005).
- [46] R. Petit, *Electromagnetic Theory of Gratings* (Springer-Verlag, London, 1980).
- 47 R. W. Schoonover and T. D. Visser, Opt. Commun. **271**, 323 $(2007).$
- [48] M. O. Scully and M. S. Zubairy, *Quantum Optics* (Cambridge University Press, New York, 1997).
- [49] R. H. Dicke, Phys. Rev. **93**, 439 (1954).
- [50] E. Altewischer *et al.*, Nature (London) 418, 304 (2002).