# **Generation of polarization entanglement from spatially correlated photons in spontaneous parametric down-conversion**

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(Received 28 November 2007; published 24 March 2008)

We propose a scheme to generate polarization entanglement from spatially correlated photon pairs. We experimentally realized a scheme by means of a spatial correlation effect in a spontaneous parametric downconversion and a modified Michelson interferometer. The scheme we propose in this paper can be interpreted as a conversion process from spatial correlation to polarization entanglement.

DOI: [10.1103/PhysRevA.77.032338](http://dx.doi.org/10.1103/PhysRevA.77.032338)

PACS number(s): 03.67.Bg, 42.50.Dv, 03.65.Ud, 03.65.Ta

#### **I. INTRODUCTION**

Polarization entanglement of photons provides a superior environment in which to demonstrate quantum information and communication protocols in quantum mechanical two-level states (qubits), e.g., quantum teleportation [[1](#page-3-0)] and quantum cryptography  $\lceil 2 \rceil$  $\lceil 2 \rceil$  $\lceil 2 \rceil$ . Thus far, several methods using spontaneous parametric down-conversion have been developed to generate a polarization-entangled state: one using a nonlinear crystal with type-II phase matching conditions  $\lceil 3 \rceil$  $\lceil 3 \rceil$  $\lceil 3 \rceil$ , another using two type-I crystals oriented at 90° with respect to each other  $\lceil 4 \rceil$  $\lceil 4 \rceil$  $\lceil 4 \rceil$ , and a third using nonlinear crystals with an interferometer  $\lceil 5-8 \rceil$  $\lceil 5-8 \rceil$  $\lceil 5-8 \rceil$ . The phase-matching condition in a spontaneous parametric down-conversion causes strong correlations between the constituent photons with respect not only to polarization but also to other degrees of freedom, e.g., energy or momentum. Recently, these degrees of freedom of photons have attracted much attention in the performance of quantum information protocols in a larger dimensional Hilbert space. For instance, such multidimensional quantum states (qudits) are expected to improve security for quantum key distribution  $[9]$  $[9]$  $[9]$  and robustness against noise [ $10$ ]. Although there are some experimental demonstrations for creating entangled qudits using angular momentum  $\lceil 11 \rceil$  $\lceil 11 \rceil$  $\lceil 11 \rceil$ and time binning  $[12]$  $[12]$  $[12]$ , the use of a transverse spatial degree of freedom provides a simple method for investigating entangled qudit states  $\lceil 13,14 \rceil$  $\lceil 13,14 \rceil$  $\lceil 13,14 \rceil$  $\lceil 13,14 \rceil$ . In addition, entanglement in two or more degrees of freedom of photons has also been reported. In particular, the state of being simultaneously entangled in multiple degrees of freedom, a so-called hyperentangled state, has been realized and characterized  $[15,16]$  $[15,16]$  $[15,16]$  $[15,16]$ . Actually, the polarization-spatial, hyperentangled state has been used to demonstrate a direct entanglement measure  $|17|$  $|17|$  $|17|$ .

In this paper, we propose an approach to generating polarization-entangled photon pairs and demonstrate its experimental verification. As described below, our scheme is interpreted as converting entanglement from spatial degrees of freedom to polarization ones.

#### **II. PRINCIPLE OF ENTANGLEMENT GENERATION**

To see the essence of our proposal, let us consider the situation in which two coherent, orthogonally polarized pho-

tons pass through an object having two slits [see Fig.  $1(a)$  $1(a)$ ]. Together with the polarization and spatial degrees of freedom, we can consider the following symmetrical two-photon state:

$$
|\psi\rangle = \frac{1}{2\sqrt{2}} (|H,A\rangle |V,A\rangle + |H,B\rangle |V,B\rangle
$$
  
+  $|H,A\rangle |V,B\rangle + |H,B\rangle |V,A\rangle) + \text{t.t.}$  (1)

Here  $H$  (V) represents the horizontal (vertical) polarization state of a photon,  $A(B)$  the spatial mode as determined by the slit  $A$   $(B)$ , and t.t. means the transposed terms in which the first and second photons are transposed. In this situation, we assume that the first and second photons are indistinguishable from one another except for the polarization or spatial degrees of freedom. Thus the transpose operation is identical for both photons in the two-photon state. Hereafter, we omit the transposed terms for simplicity.

A signal and its conjugate idler photons are generated in almost the same position in a nonlinear crystal as explained by Fourier-optical analysis for the two-photon state generated by spontaneous parametric down-conversion  $[18–20]$  $[18–20]$  $[18–20]$  $[18–20]$ . Thus if frequency-degenerate photon pairs are collinearly generated by a type-II phase matching condition and two slits are placed just after the crystal [see Fig.  $1(b)$  $1(b)$ ], we can prepare the following two-photon state as a result of a spatial correlation effect:

$$
|\phi\rangle = \frac{1}{\sqrt{2}} (|H, A\rangle |V, A\rangle + |H, B\rangle |V, B\rangle). \tag{2}
$$

<span id="page-0-1"></span>Such an effect has attracted great interest because of its possible application to a novel imaging technology that is called

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FIG. 1. (Color online) Situations proposed in our scheme.

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FIG. 2. (Color online) Schematic drawing of our experimental setup. LBO, lithium triborate crystal for frequency doubling; TS, two slits; L, collimating lens; PBS, polarizing beam splitter; QWP, quarter-wave plate; P, polarization analyzer; BPF, 3-nm bandpass filter centered at 800 nm; and APD, avalanche photodiode. QWPs are used to change polarization from  $H(V)$  to  $V(H)$ .

"quantum imaging"  $[21,22]$  $[21,22]$  $[21,22]$  $[21,22]$ . The two-photon state in Eq.  $(2)$  $(2)$  $(2)$ is a spatially entangled state in which both photons pass together through either of the slits; the photons are at this time not entangled in polarization degrees of freedom. If we exchange the spatial mode for one of the polarization modes, an action which corresponds to a controlled-NOT (CNOT) operation on the spatial part depending on the polarization part  $[23]$  $[23]$  $[23]$ , the two-photon state in Eq.  $(2)$  $(2)$  $(2)$  is converted to the following state:

$$
|\phi'\rangle = \frac{1}{\sqrt{2}}(|H,A\rangle|V,B\rangle + |H,B\rangle|V,A\rangle). \tag{3}
$$

<span id="page-1-0"></span>Since these two-photon states have identical forms in the transpose operation, the polarization state of Eq.  $(3)$  $(3)$  $(3)$  is rewritten with respect to the spatial mode as follows:

$$
|\phi'\rangle = \frac{1}{\sqrt{2}} (|H\rangle_A |V\rangle_B + |V\rangle_A |H\rangle_B).
$$
 (4)

This is the standard notation of a polarization-entangled state. The scheme we proposed here can be understood as an entanglement conversion process from spatial degrees of freedom to polarization ones.

## **III. EXPERIMENT**

A schematic diagram of the setup used to realize our proposal described above is depicted in Fig. [2.](#page-1-1) A wellcollimated, frequency-doubled, mode-locked Ti:sapphire laser operating at 400 nm, whose average power is 110 mW and repetition rate is 80 MHz, pumps a  $\beta$ -barium borate (BBO) crystal with the thickness of 1.5 mm. Frequencydegenerate photon pairs are collinearly generated according to type-II phase matching conditions. Putting two slits (each slit width: 150  $\mu$ m; interval: 450  $\mu$ m) just after the nonlinear crystal, we can produce the two-photon state described in

Eq. ([2](#page-0-1)). In this condition, the pump beam diameter on the two slits is approximately 1.7 mm. After passing through a cylindrical lens (focal length: 50 mm), the photon pairs are fed into a modified polarization Michelson interferometer that consists of a polarization beam splitter (PBS), a roof mirror (RM), and a plane mirror (M). In the PBS, the photon pairs are divided into two arms of the interferometer, depending on their polarization. In arm 1, where the roof mirror is placed, the path mode *A* (*B*) of a *V*-polarized photon changes into  $B'$   $(A')$ , while the path mode of a *H*-polarized photon in arm 2 does not change. Thus after the recombination in the PBS, the output state from through the interferometer produces the polarization-entangled state described in Eq. ([3](#page-1-0)). In addition, this interferometer has the ability to compensate both transverse and longitudinal walk-off effects coming from birefringence of the BBO crystal because *H*and *V*-polarized photons are divided by the PBS and can be independently controlled in each arm. The output photons from the interferometer were detected with avalanche photodiodes (EG&G SPCM AQ161) through a pair of polarization analyzers consisting of a half-wave plate (HWP) and a polarizing beam splitter, and through 3-nm interference filters centered at 800 nm. We recorded the number of coincident events with a time-interval analyzer (EG&G 9308).

### **IV. RESULTS AND DISCUSSION**

Figure  $3(a)$  $3(a)$  shows the coincidence counts as a function of the path-length difference  $(\Delta L)$  of the interferometer. In this measurement, we set the polarization analyzer angle in the path *A'*  $(\theta_{A'})$  to +45° (open squares) or −45° (open circles), while that in the path  $B'$  ( $\theta_{B'}$ ) was fixed at +45°. We observed a constructive quantum interference fringe with a visibility of 89% when  $\theta_{A}$  was set to +45° and a destructive interference fringe when  $θ_{A'}$  was set to  $-45^\circ$ . In addition, we performed polarization correlation measurements at  $\Delta L = 0$   $\mu$ m. In these measurements, as shown in Fig. [3](#page-2-0)(b),  $\theta_{B'}$  was set to +45° (open squares) or −45° (open circles), and  $\theta_{A}$  was varied by rotating the HWP. These resultant quantum interference fringes indicate that the output state forms a triplet state in polarization degrees of freedom:  $\frac{d}{dx}$   $\frac{d}{dx}$   $\frac{d}{dx}$   $\frac{d}{dx}$   $\frac{d}{dx}$   $\frac{d}{dx}$   $\frac{d}{dx}$   $\frac{d}{dx}$   $\frac{d}{dx}$  successfully demonstrated our proposal utilizing spatial correlation in a spontaneous parametric down-conversion. As discussed in Refs.  $[14,24]$  $[14,24]$  $[14,24]$  $[14,24]$ , we can decompose the spatial modes of signal and idler photons to a complete and orthonormal set of eigenvectors known as Schmidt modes. In our experiment, there would be several Schmidt modes in each slit due to the large slit size, while we explain our proposal assuming a single spatial mode treatment. Furthermore the contribution from each mode should result in the observed interference fringes. Therefore the slight degradation of the quantum interference visibility observed in Fig. [3](#page-2-0) was likely caused by intensity mismatch and phase disorder between a Schmidt mode in the slit *A* and its conjugate mode in the slit *B*. In addition, while the interference fringes in Fig.  $3(b)$  $3(b)$  should be out of phase by 180° with each other, they show in practice the slightly asymmetric patterns. This discrepancy may originate from the imbalance of the total pump beam intensity between the slits *A* and *B*.

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FIG. 3. (Color online) Experimental results (open circles and squares) and fitted curves of coincidence counts as a function of (a) the path-length difference  $(\Delta L)$  of the modified polarization Michelson interferometer and (b) the polarization analyzer angle  $(\theta_{A})$  in the path *A'*.

Another remarkable feature of our polarization-entangled photon source is that a relative phase between the two terms in Eq. ([3](#page-1-0)) is insensitive to the path-length difference  $\Delta L$  unlike other polarization-entangled photon sources using a Mach-Zehnder interferometer  $\lceil 6 \rceil$  $\lceil 6 \rceil$  $\lceil 6 \rceil$  and a Michelson interferometer  $\lceil 5 \rceil$  $\lceil 5 \rceil$  $\lceil 5 \rceil$ . On the other hand, the relative phase is sensitive to a tilt of the mirror M because it causes a path-length difference between the photon in the path mode  $A'$  and that in  $B'$  for  $H$ -polarization in arm 1. As shown in Fig. [4](#page-2-1) at particular angles of the mirror M, we observed constructive interference with the visibility of 82% when the polarization analyzer was set to  $A' = -45^{\circ}$  and  $B' = +45^{\circ}$  (open circles), and we observed destructive interference with settings of  $A' = +45^{\circ}$  and  $B' = +45^{\circ}$  (open squares). These observations stand in contrast to the two-photon interference fringes discussed in Fig. [3.](#page-2-0) These results indicate that with the same apparatus we can control the relative phase, without sacrificing the system stability, by tuning the angle of the mirror M and consequently produce a singlet state,  $\frac{H}{(H)_A}$ ,  $|V\rangle_{B'} - |V\rangle_{A'}|H\rangle_{B'}$ . Thus our scheme enables us to construct the polarization-entangled photon source having both the system stability and controllability.

Using this polarization-entangled photon source, we have tested the violation of Clauser-Horne-Shimony-Holt (CHSH)

<span id="page-2-1"></span>

FIG. 4. (Color online) Experimental results (open circles and squares) and fitted curves of coincidence counts as a function of the path-length difference  $(\Delta L)$  of the modified polarization Michelson interferometer at particular angles of the mirror M.

Bell inequality  $[25]$  $[25]$  $[25]$ . Following the method described in Ref. [[26](#page-3-23)], we estimated the Bell parameter *S* from coincidence counting measurements for 16 combinations of polar-<br>ization analyzer settings  $(\theta_A = 0^\circ, 45^\circ, 90^\circ, 135^\circ; \theta_B$ ization analyzer settings  $(\theta_{A'}=0^\circ, 45^\circ, 90^\circ, 135^\circ; \theta_{B'}=22.5^\circ, 67.5^\circ, 112.5^\circ, 157.5^\circ)$ . In each measurement, we took coincidence counts for 10 s and obtained the *S* value of  $2.61 \pm 0.04$ , which clearly indicates a violation of the classical limit *S*= 2. This result shows that the output two-photon state in polarization degrees of freedom has a nonlocal correlation.

### **V. CONCLUSION**

We have proposed and demonstrated a scheme for the generation of polarization entanglement utilizing a spatial correlation effect in spontaneous parametric downconversion. We have also shown a violation of Bell's inequality for the entangled photon source described here. Our scheme is similar to the scheme proposed by Kim *et al.* [[8](#page-3-5)] at the fundamental level; the spatial entanglement is created with respect to the path mode of the Sagnac interferometer in Kim's scheme. The brightness of our source is relatively lower than that of Kim's scheme because the use of multiple slits to create the spatial modes results in waste of the pump power. However, our scheme has the advantage that we can easily extend the number of spatial modes. By increasing the number of slits, we can extend the number of spatial modes so as to prepare the entanglement in a Hilbert space with larger dimensions. Especially, increasing the number of slits up to four, we could produce a hyperentangled state in polarization and spatial degrees of freedom: Such states have an advantage that we can easily perform a complete Bell state measurement  $[17,27]$  $[17,27]$  $[17,27]$  $[17,27]$ . In addition, our scheme has the potential to improve the brightness by adopting waveguide structure to create the spatial modes instead of the multiple slits. The use of a quasiphase-matched device with multiple waveguides may allow us to achieve construction of a highflux and high-dimensional entangled photon source.

# **ACKNOWLEDGMENTS**

We are grateful to H. Ishihara for his valuable discussions. This work was supported in part by the Strategic Information and Communications  $R & D$  Promotion Program

(SCOPE) of the Ministry of Internal Affairs and Communications and by a Grant-in-Aid for Creative Scientific Research (17GS1204) of the Japan Society for the Promotion of Science.

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