Versatile electrostatic trap

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A four electrode electrostatic trap geometry is demonstrated that can be used to combine a dipole, quadrupole, and hexapole field. A cold packet of $^{15}ND_3$ molecules is confined in both a purely quadrupolar and hexapolar trapping field and additionally, a dipole field is added to a hexapole field to create either a double-well or a donut-shaped trapping field. The profile of the $^{15}ND_3$ packet in each of these four trapping potentials is measured, and the dependence of the well-separation and barrier height of the double-well and donut potential on the hexapole and dipole term are discussed.

I. INTRODUCTION

The creation of cold molecules offers unique possibilities for studying cold collisions [1–4], dipole-dipole interaction [5–7], or for doing high-resolution spectroscopy [8,9]. In each of these fields, traps are either necessary, or they enhance the potential of the method considerably. Electrostatic traps in particular are highly versatile. They are rather deep (on the order of 1 K) and by changing electrode geometries, many different trapping potentials can be formed [10–15]. Here we demonstrate an electrode geometry that is used to form different trapping fields by changing the voltage applied to the electrodes. In the trap a predominantly dipolar, quadrupolar, or hexapolar field can be created. When implementing the latter two, a pure quadrupole or a pure hexapole trapping potential is generated. Combining a dipole field with a hexapole field gives rise to two additional trapping potentials, a double-well or a ring-shaped potential, depending on the sign of the dipole term. As voltages can be switched on relatively short time scales, rapid changing between these trapping fields is feasible as well.

A double-well trap in particular has proven to be fruitful in atomic physics experiments. For instance, double-well potentials have been used in interference experiments to study coherence properties of BECs [16] and to visualize phase singularities associated with vortices in a Na BEC [17]. Furthermore, two weakly coupled BECs in a double-well potential have been shown to form a Josephson junction [18], and collision studies have been performed in a double-well interferometer, enabling the determination of the *s*- and *d*-wave scattering amplitudes of ^{87}Rb [19].

In electrostatic traps the formation of a double-well potential with variable barrier height and well separation is relatively straightforward. Along with the possibility of rapid switching to other types of trapping fields, this creates favorable conditions for the study of cold collisions. Molecules trapped in either of the two wells of a double-well trap will gain potential energy when switching to a single-well trap, resulting in two packets of molecules that are accelerated toward each other. As they reach the center of the trap, they will collide with a velocity that is dependent on the shape of both the single- and double-well potential. As these shapes

can be readily varied, the velocity of the molecules is tunable. Combining this feature with an inherently low velocity spread of the trapped molecules makes rapid single- to double-well conversion an excellent starting point for studying collisions at low temperatures.

II. THE VARIOUS TRAPPING CONFIGURATIONS

In a cylindrically symmetric geometry, the electric potential $\Phi(\rho, z)$ can be expressed as [14,15,20]:

$$\Phi(\rho, z) = \Phi_0 + \Phi_1 \frac{z}{z_0} + \Phi_2 \frac{(z^2 - \rho^2/2)}{z_0^2} + \Phi_3 \frac{(z^3 - 3\rho^2 z/2)}{z_0^3} + \cdots, \qquad (1)$$

with z_0 a characteristic length scale. Here, the first term is a constant voltage, the second term a constant electric field, the third a quadrupolar electric field, and the fourth a hexapolar electric field. A molecule with a quadratic Stark shift will experience a harmonic force in a quadrupolar electric field, whereas a hexapolar field is needed to form a harmonic trap for a molecule with a linear Stark shift. In our experiments we use $^{15}ND_3$ molecules in the low-field seeking hyperfine levels of the $|J, K\rangle = |1, 1\rangle$ inversion doublet of the vibrational and electronic ground state. These molecules experience a quadratic Stark shift for small electric field strengths and a linear Stark shift for larger electric field strengths. The dependence of the Stark shift on the electric field strength E for $^{15}ND_3$ in these levels is given by [21]

$$W_{\text{Stark}}(E) = \sqrt{\left(\frac{W_{\text{inv}}}{2}\right)^2 + \left(\frac{1}{2}\mu E\right)^2} - \left(\frac{W_{\text{inv}}}{2}\right), \qquad (2)$$

with W_{inv} the inversion splitting and μ the dipole moment. For $^{15}ND_3$ the inversion splitting is 1430.3 MHz [8] and the dipole moment is taken to be the same as for $^{14}ND_3$, i.e., 1.48 D [22]. At even larger field strengths, the effect of mixing with higher rotational levels becomes more important and higher order terms have to be taken into account.

Using the four electrode geometry shown in Fig. 1 it is possible to create a field with dominant dipolar, quadrupolar, or hexapolar contributions, by applying the appropriate volt-
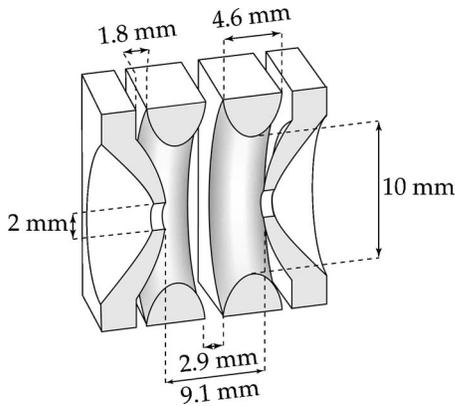
FIG. 1. Scheme of the trap. The trap is cylindrically symmetric and consists of two parallel rings in the middle and two endcaps at the sides.

ages. The geometry of the trap is the same as was used previously to create an ac electric trap [23]. It consists of two rings with an inner diameter of 10 mm and two endcaps. The two rings have a width of 4.6 mm and are separated by 2.9 mm, whereas the two endcaps are separated by $2z_0 = 9.1$ mm. They each have a hole with a diameter of 2.0 mm, the first to allow molecules to enter and the second to extract the ions that are produced in the detection scheme.

In Fig. 2 the voltages needed for two different trapping fields are shown. When a voltage $-U_2$ is applied to the two ring electrodes and a voltage U_2 is applied to both endcaps, such as shown on the left-hand side of the figure, a field is formed with a dominant quadrupole term. Using a commercially available finite difference program [24] the potential of this configuration is simulated. Below the trap cross section the electric field strength as a function of position is shown for both the ρ direction (solid line) and the z direction (dotted line). Fitting the corresponding potential to Eq. (1), we find that $\Phi_0 \approx -0.43 \, U_2$, $\Phi_2 \approx 1.05 \, U_2$, $\Phi_4 \approx 0.35 \, U_2$, and $\Phi_6 \approx -0.04 \, U_2$ and that the uneven terms are zero due to symmetry. Beneath the electric field strength in Fig. 2 the Stark energy in mK ($T = W_{\mathrm{Stark}}/k$, with k the Boltzmann constant) of a $^{15}\mathrm{ND}_3$ molecule in this field is shown. The electric field in the quadrupole trap increases linearly with distance, but, because of the nonlinear dependence of the Stark energy on the electric field, the potential is harmonic near the center of the trap. Further away from the center the potential is linear. The resulting trap is tight (the trapping frequency is $\omega_z/2\pi = 1.7$ kHz at the center of the trap) and has a depth of 0.09 K for $^{15}\mathrm{ND}_3$.

A hexapole trap results when the voltages U_3 and $-U_3$ are applied alternately to the four electrodes of the trap as shown on the right-hand side of Fig. 2. A fit of the potential of this field to Eq. (1) yields $\Phi_1 = 0$, $\Phi_3 \approx U_3$ and $\Phi_5 \approx -0.04 \, U_3$, with the even terms being zero due to symmetry. Again, both the electric field strength along the ρ and z directions (solid and dotted line, respectively) and the Stark energy of a $^{15}\mathrm{ND}_3$ molecule in this field are shown below the cross sections of the trap. The electric field strength in this trap is quadratically dependent on the distance from the center. However, due to the nonlinear Stark effect the potential is essentially flat near the center of the trap. Away from the
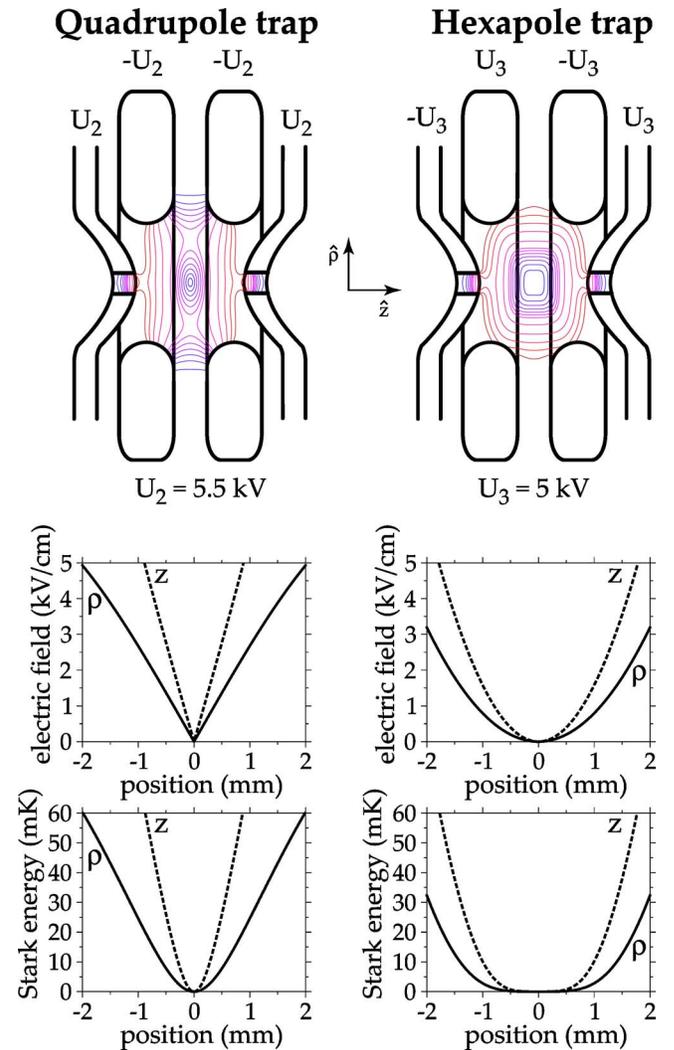

FIG. 2. (Color online) Two cross sections of the trap. On the left-hand side, the voltages that result in a quadrupole trap are shown, along with lines of constant electric field for electric field strengths of every kV/cm from 1 to 7 kV/cm and every 5 kV/cm from 10 to 25 kV/cm (shown in color online, with increasing field strength going from blue to red). On the right-hand side, the same is shown for a hexapole trap. Below the two cross sections, the electric field is shown along with the Stark energy of a $^{15}\mathrm{ND}_3$ molecule as a function of position in the ρ and z directions (solid line and dotted line, respectively).

center the potential becomes harmonic. This trap is less tight (the trapping frequency is $\omega_z/2\pi = 0$ at the center of the trap and goes to $\omega_z/2\pi = 750$ Hz further away from the center) and has a depth of 0.35 K for $^{15}\mathrm{ND}_3$.

When applying voltages of $-U_1$, $-0.6 \, U_1$, $0.6 \, U_1$, and U_1 consecutively to the four electrodes of the trap, a dipolar field is formed. Fitting the potential of this field to Eq. (1) results in $\Phi_1 \approx 0.88 \, U_1$, $\Phi_3 = 0$, and $\Phi_5 \approx 0.09 \, U_1$, with the even terms being zero due to symmetry. Adding a dipole field to a hexapole field results in either a double-well potential or a donut potential, depending on the relative sign of the dipole and hexapole term. In Fig. 3 both configurations are shown, along with the electric field strength and the Stark energy of a $^{15}\mathrm{ND}_3$ molecule in this field along the ρ and z

Double well

$U_3-0.6\,U_1$ $-U_3+0.6\,U_1$

$-U_3-U_1$ U_3+U_1

$U_3 = 5$ kV
$U_1 = -0.55$ kV

Donut

$U_3-0.6\,U_1$ $-U_3+0.6\,U_1$
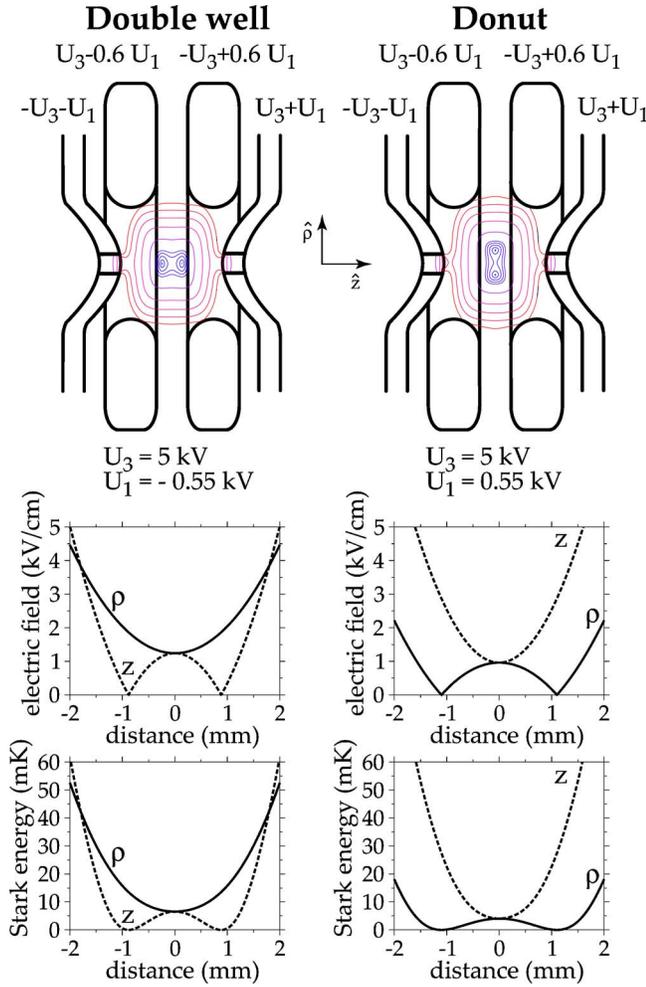
$-U_3-U_1$ U_3+U_1

$U_3 = 5$ kV
$U_1 = 0.55$ kV

FIG. 3. (Color online) Two cross sections of the trap. On either side the voltages that are applied when a dipole field is added to a hexapole field are shown. Lines of constant electric field are shown for electric field strengths of 0.1 kV/cm, every 0.5 kV/cm from 0.5 to 2 kV/cm, and every 5 kV/cm from 5 to 25 kV/cm (shown in color online, with increasing field strength going from blue to red). On the left-hand side (right-hand side) U_1 and U_3 have the same (opposite) sign. In each case both the electric field and the Stark energy of a $^{15}ND_3$ molecule as a function of position are shown in both the ρ and z directions (solid line and dotted line, respectively).

directions (solid and dotted line, respectively). Both the distance between the two minima in the double-well trap and the diameter of the ring-shaped minimum in the donut trap are dependent on the ratio between the dipole and hexapole term. In the upper graph of Fig. 4 the distance between the two wells is shown as a function of the ratio $|U_1/U_3|$ in the case of an ideal hexapole and dipole field (solid line). The dotted line shows the same for the diameter of the donut-shaped minimum. The crosses and triangles (double-well trap and donut trap, respectively) indicate the simulated value of this well separation, using the finite difference program with $U_3=5$ kV and different values of U_1.

The height of the barrier between the two wells is shown in the lower graph of Fig. 4, given in mK for $^{15}ND_3$. In the case of an ideal hexapole and dipole field (solid line), this height is the same for the double-well and donut trap and is
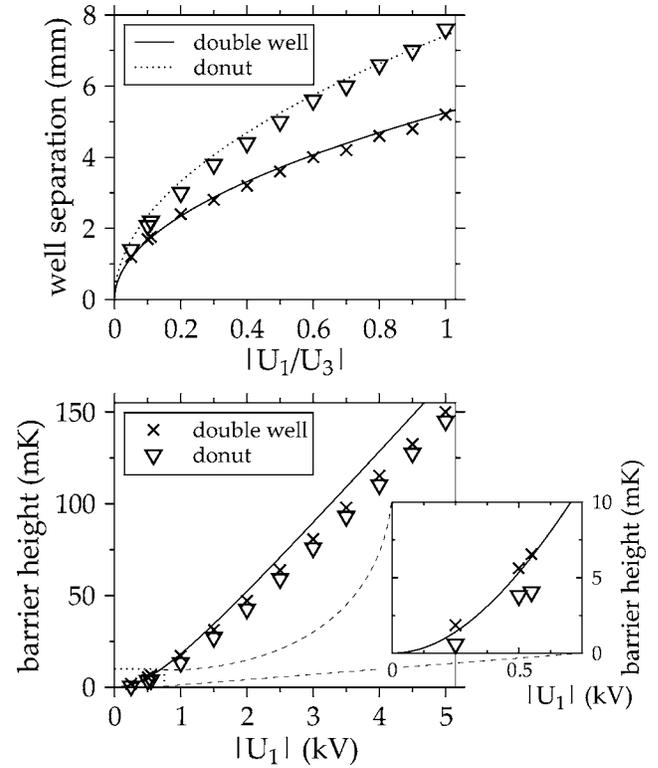
FIG. 4. Well separation as a function of $|U_1/U_3|$ and barrier height (for $^{15}ND_3$) as a function of $|U_1|$ in the ideal double-well (solid line) and donut trap (dotted line). In both graphs the crosses (double-well trap) and triangles (donut trap) show the same quantities obtained from electric field simulations of the actual trap geometry.

solely dependent on the value of $|U_1|$. Note that the barrier height is identical to the amount of potential energy gained by a $^{15}ND_3$ molecule in the center of one of the wells when switching to the single-well configuration. This can be seen by realizing that in the center of the double-well trap, i.e., at the top of the barrier, the electric field strength is determined by the dipole term only, as the hexapole field is zero there. In the center of one of the wells the hexapole field is equal to the dipole field, although opposite in direction. Therefore, when switching the dipole field off to produce a single-well trap, molecules originally at the center of one of the two wells will now have a potential energy equal to the barrier height. Values for the barrier height were obtained using the finite difference program as well and are shown as crosses (double-well trap) and triangles (donut trap) in the lower graph of Fig. 4. From these two graphs it is clear that both the well separation and the barrier height, and therefore also the collision energy of the molecules upon double- to single-well conversion, can easily be changed by varying the voltages on the four electrodes. At the maximum value of $|U_1|$ used in the experiment, $|U_1|=0.55$ kV, the barrier height is on the order of 5 mK. The separation between the wells is 1.8 mm in this case ($U_3=5$ kV),whereas the diameter of the donut-shaped minimum is 2.2 mm.
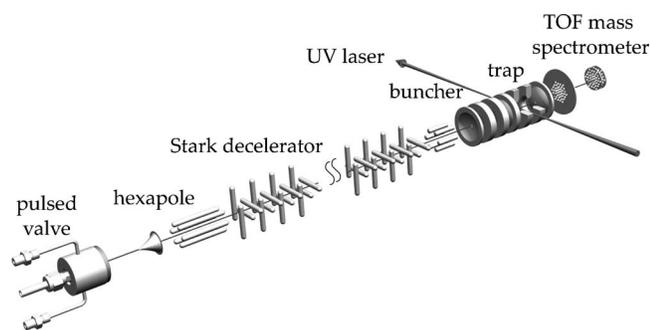
FIG. 5. (Color online) Experimental setup. A pulsed supersonic beam of $^{15}ND_3$ molecules seeded in xenon exits a cooled valve with a velocity of 280 m/s. Ammonia molecules in the low-field seeking hyperfine levels of the $|J,K\rangle=|1,1\rangle$ state are focused into the decelerator by a hexapole, decelerated, and then transversally and longitudinally focused into the trap by a hexapole and buncher, respectively. The molecules are detected in a TOF-mass spectrometer.

III. EXPERIMENT

In Fig. 5 the experimental setup is shown. In the experiments, the trap is loaded from a Stark-decelerated molecular beam. A mixture of 5% $^{15}ND_3$ seeded in xenon is supersonically expanded from a pulsed valve at a 10 Hz rate. Due to cooling of the valve to -70 °C, the gas pulse has a velocity of 280 m/s. In the expansion, about 60% of the ammonia molecules are internally cooled to the ground state of para-ammonia, the $|J,K\rangle=|1,1\rangle$ inversion doublet in the electronic and vibrational ground state. After passing through a skimmer, those molecules that reside in the low-field seeking hyperfine levels of the upper component of the inversion doublet are focused into the Stark decelerator by a 6-cm-long hexapole. Molecules in high-field seeking levels are attracted by the high electric fields of both the hexapoles and the decelerator and will be lost from the beam. Molecules that reside in the remainder of the hyperfine levels of the inversion doublet, that only have a higher order Stark effect, will hardly be affected by the electric fields. The decelerator consists of 95 pairs of parallel 3 mm-diam rods, with a closest distance of 2 mm between two rods and a closest distance of 2.5 mm between pairs of rods. Each consecutive pair of rods is rotated over 90° and within each pair, a positive voltage of 10 kV is applied to one electrode, whereas the same negative voltage is applied to the other. A more extensive description of this part of the setup, along with the operation principle of the decelerator, can be found elsewhere [8,25]. Using a phase angle of 57.5°a subset of low-field seeking molecules with an initial velocity of around 280 m/s is decelerated to about 15 m/s at the exit of the decelerator. After 5 mm the molecules are transversally focused into the trap by a second (12.5 mm long) hexapole. Subsequently, they are longitudinally focused into the trap using a buncher that is placed another 5 mm downstream of the hexapole. The buncher has a similar geometry as the trap. Before the ammonia molecules enter the trap, voltages are applied to the trap such that a last electric field slope is formed. In gaining Stark energy when entering the trap, the low-field seeking molecules lose their last kinetic energy and reach a stand-still in
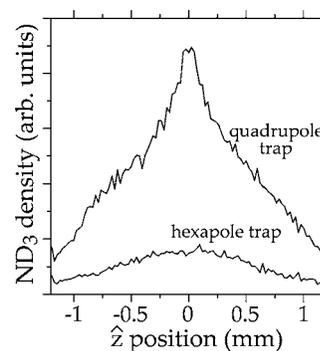

FIG. 6. Density of trapped $^{15}ND_3$ molecules as a function of position in the z direction for both the quadrupole trap (upper trace) and the hexapole trap (lower trace), after trapping for about 72 ms.

the middle of the trap. At this moment the voltages on the four electrodes are switched to generate a particular trapping potential, thereby confining the molecules in either a quadrupole, hexapole, double-well or donut potential. After a certain trapping time, the trap is turned off and molecules in the upper component of the inversion doublet are ionized in a state-selective $(2+1)$-resonance enhanced multiphoton ionization scheme, using a pulsed UV laser around 317 nm [26]. The resulting ions are subsequently detected in a time-of-flight mass-spectrometer. Using a 75 cm lens the ionization laser is focused into the trap passing through the 2.9 mm gap between the two ring electrodes. The laser focus is estimated to be about 200 μm in diameter. Applying small bias voltages of 200, 150, -150, and -200 V to the four electrodes of the trap results in an electric field that accelerates the ions toward the detector. The ions are detected over a length of 2 mm along the laser beam, limited by the size of the hole in the endcap. Using a computer controlled translation stage, the focus of the laser beam can be moved along the beam axis, i.e., along the z direction, over about 2.5 mm. In this way, the spatial distribution of the trapped molecules can be measured.

IV. RESULTS AND DISCUSSION

In Fig. 6, the density of trapped $^{15}ND_3$ molecules is shown as a function of position in the z direction, both for hexapole and for quadrupole trapping voltages. The measurements are taken after the molecules have been trapped for about 72 ms. We found that in order to obtain a single-well profile for the molecules confined in the hexapole trap a small dipole term had to be added. We attribute this to deviations of the distances between the electrodes from the ideal geometry. This compensating dipole term is added in all subsequent measurements. As the quadrupole trap is much tighter than the hexapole trap (see Fig. 2), a signal difference arises between the two traces. The peak density of molecules in the hexapole trap is about 10^7 cm^{-3}, whereas it is about ten times higher in the quadrupole trap. The loading process is identical for both traps and is matched to the hexapole trap, resulting in a less than perfect match of the decelerated packet to the quadrupole trap. This gives rise to the peculiar shape of the measured distribution in the quadrupole
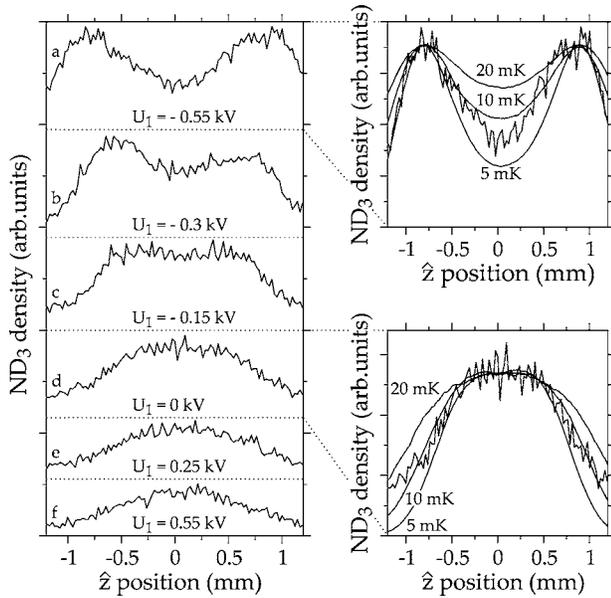
FIG. 7. Density of $^{15}ND_3$ molecules confined in a hexapole trap as a function of position in the z-direction. A negative dipole term of -0.55, -0.3, and -0.15 kV is added to the hexapole term (U_3=5 kV) in the upper three traces (a)–(c), resulting in a double-well potential. Trace (d) shows a packet in a purely single well. A positive dipole term of 0.25 and 0.55 kV is added for the lower two traces (e),(f), thereby creating a donut potential. On the right-hand side, traces (a) and (d) are shown once more, along with simulations of the density distribution of the packet of molecules for temperatures of 5, 10, and 20 mK.

FIG. 8. Determination of the temperature of a packet of $^{15}ND_3$ molecules trapped in the hexapole trap. On the left, the profile of a packet is shown 20 and 420 μs after the trap is turned off (upper and lower trace, respectively). From a fit to a Gaussian line shape the FWHM of the distribution is obtained, as shown as a function of free-flight time (solid line with crosses) on the right-hand side.

$$n(\rho,z) = n_0 e^{-W_{\text{Stark}}(\rho,z)/kT}, \qquad (3)$$

trap, which seems to consist of two packets with different temperatures.

In Fig. 7 the density of $^{15}ND_3$ molecules in the hexapole trap is shown as a function of position in the z direction. By adding a dipole term to the hexapole term, the shape of the trap and thereby the profile of the trapped molecules can be changed significantly. Each trace in Fig. 7 corresponds to a different value of the added dipole term. When no dipole is added, the trap consists of only a single well. A single peak results, as trace (d) shows. Adding a negative dipole term transforms the single well to a double well, with a distance and barrier between the two wells that depend on the value of the dipole term. The upper three traces of Fig. 7 show two peaks that move closer together as the dipole term is increased from -0.55 kV [trace (a)] to -0.3 kV [trace (b)] to -0.15 kV [trace (c)]. When a positive dipole term is added, the shape of the trap becomes that of a donut. As only molecules in the relatively small laser focus near the center of the trap are ionized in the detection scheme, this transformation to a donut-shaped trap leads to a reduction in signal only, as is shown by traces (e) and (f) (U_1=0.25 kV and U_1=0.55 kV, respectively).

At the densities that we have in the trap, no thermalizing collisions occur, and formally no temperature can be assigned. The distribution of the trapped sample is determined by the details of the loading process. To characterize this distribution in terms of a temperature, we fitted the density profile to the thermal density distribution [27]:
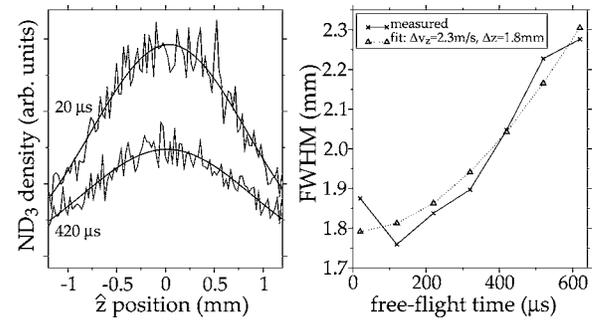
with n_0 the density at the trap minimum and $W_{\text{Stark}}(\rho,z)$ the potential energy as a function of position. On the right-hand side of Fig. 7 the measurements with a dipole term of U_1= -0.55 kV and U_1=0 kV are shown once more, along with the thermal density distribution as obtained from Eq. (3) for temperatures of 5, 10, and 20 mK. It can be seen that in either case the simulated distribution with a temperature of 10 mK matches the measurement best. This temperature is slightly higher than the barrier height at U_1=-0.55 kV ($\sim$5 mK). The same simulation has been performed for the spatial distribution of molecules confined in a quadrupole trap. Due to the seemingly double profile, it is more difficult to describe this distribution with a single temperature. A temperature of 75 mK seems to best describe the broad base, whereas the sharp center peak agrees best with a temperature of 5 mK. An alternative method to deduce a temperature is to measure the width of the packet of trapped molecules as a function of time after the trap has been turned off. Measurements of this type are shown in Fig. 8. On the left-hand side two profiles of $^{15}ND_3$ molecules are seen, one after 20 μs and one after 420 μs after switching off the hexapole trap (upper and lower curve, respectively). In either case the molecules have been confined for about 72 ms. Due to the velocity spread of the molecules the packet spreads out after the trap has been turned off, resulting in less signal and an increased width. To obtain this width a Gaussian line shape is fitted to each profile. The acquired full-width-half-maximum (FWHM) is shown as a function of free-flight time on the right-hand side of the figure (solid line with crosses). To deduce a temperature, this curve is fitted to $\sqrt{(\Delta z)^2 + (\Delta v_z \cdot t)^2}$ (dotted line with triangles), resulting in a velocity spread of 2.3 m/s and a position spread of 1.8 mm (both FWHM). Using $\Delta v_z = \sqrt{8 \ln 2} \cdot \sqrt{kT/m}$ [28], this gives a temperature of about 2.5 mK.

The different temperatures of 10 and 2.5 mK, obtained by the two different methods, are indicative of the limitations of either method. The first method relies on an accurate knowledge of the potential energy that the molecules have in the trap. Possible misalignments of the electrodes of the trap
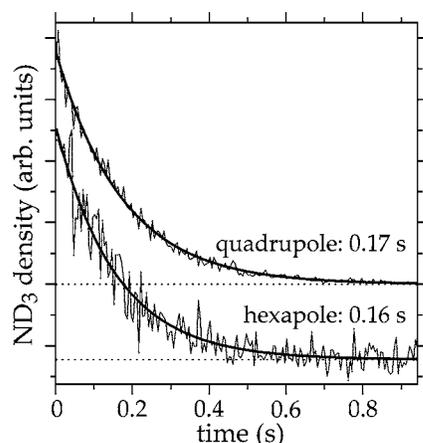
FIG. 9. Density of $^{15}ND_3$ molecules in the quadrupole (upper trace) and the hexapole (lower trace) trap as a function of time that the trap is on.

cause uncertainties in the actual electric field, and therefore in $W_{\text{Stark}}(\rho, z)$. These misalignments are most likely to result in a confining field that is less tight, leading to an overestimation of the temperature. In addition, both methods depend on the determination of the width of the spatial distribution of the packet. In our analysis, we assume the detection volume to be much smaller than the spatial spread of the trapped molecules. For a diffraction-limited laser focus this is certainly the case (in our experiment the waist of the laser beam would be less than 100 μm). However, the laser focus of our multimode laser is most certainly larger. Furthermore, due to a less than ideal pointing stability of the laser beam and a nonplanar entrance window of the vacuum system our effective detection volume is increased. In the first method, this leads to an overestimation of the temperature and in the second to an underestimation. We therefore believe that the actual temperature lies in between the temperatures found using the two methods.

In Fig. 9 the density of ammonia molecules is shown in both the quadrupole and the hexapole trap as a function of time that the trap is on. The molecules are seen to leave the trap with a $1/e$ time of 0.16 s for the hexapole trap and

0.17 s for the quadrupole trap, the same within error bars. The trapping lifetime is mainly limited by background collisions (background pressure 4×10^{-8} mbar) [29].

V. CONCLUSIONS

We have presented a new electrostatic trapping geometry that illustrates the versatility of electric fields in forming tailored trapping potentials. By applying different voltages to a set of four electrodes, different trapping fields are created, between which rapid switching on a time scale of 100 ns is possible. Spatial distributions and lifetimes of a cold packet of $^{15}ND_3$ molecules loaded into both a hexapole and a quadrupole trap are shown. Additionally, we studied a hexapole trap that transforms into a double-well or donut trap when different dipole terms are added. The barrier height and well separation of either one of these two traps depend on the strength of the dipolar and hexapolar electric field and are easily changed.

Rapid switching between, for instance, the double-well trap and a pure hexapole trap offers good prospects for measuring collision cross sections as a function of collision energy at low temperatures. The amount of energy gained by molecules trapped in one of the wells after switching to the single well depends solely on the strength of the electric dipole field, which can be easily varied. Currently, experimental effort is put into increasing the density of trapped molecules, which would bring collisional studies within reach.

ACKNOWLEDGMENTS

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