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## Long-range interactions and entanglement of slow single-photon pulses

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We show that very large nonlocal nonlinear interactions between pairs of colliding slow-light pulses can be realized in atomic vapors in the regime of electromagnetically induced transparency. These nonlinearities are mediated by strong, long-range dipole-dipole interactions between Rydberg states of the multilevel atoms in a ladder configuration. In contrast to previously studied schemes, this mechanism can yield a homogeneous conditional phase shift of  $\pi$  even for weakly focused single-photon pulses, thereby allowing a deterministic realization of the photonic phase gate.

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Whether or not quantum-information processing and quantum computing [1] become practical technologies crucially depends on the ability to implement high-fidelity quantum logic gates in a scalable way [2]. Among alternative routes to this challenging goal, the schemes operating with photons as qubits [3,4] are of particular interest, since photons are ideal carriers of quantum information in terms of transfer rates, distances, and scalability. A current trend makes use of linear optical elements and photodetectors for the implementation of key components of quantum communications and information processing in a probabilistic way [4]. The desirable objective though is a *deterministic* realization of entangling operations between individual photons, which require sufficiently strong nonlinearities or long interaction times. These are achievable, at the single-photon level, by tight spatial confinement of the photons, in the very demanding regime of strong atom-field coupling in high-Q cavities [5].

A promising alternative is to enhance both the nonlinear susceptibility and interaction time by employing the ultraslow light propagation in resonant media subject to electromagnetically induced transparency (EIT) [6–8]. In a pioneering work, Schmidt and Imamoğlu have suggested the possibility of enhanced, nonabsorptive, cross-phase modulation of two weak fields in the EIT regime [9], provided their interaction time is long enough. However, upon entering the EIT medium light pulses become spatially compressed by the ratio of group velocity v to the vacuum speed of light c [10], so that the interaction time of two colliding pulses is a constant independent of v. In order to maximize this time, copropagating pulses with nearly matched group velocities have been proposed [11,12]. The essential drawback of such an approach is the spatial inhomogeneity of the conditional phase shift, causing spectral broadening of the interacting pulses, thereby preventing the realization of a high-fidelity quantum phase gate. Alternative approaches free of spectral broadening have been suggested [13–15]. In all of them, however, a rather tight transverse confinement through waveguiding or focusing of the pulses, close to the diffraction limit of  $\lambda^2$ , is needed in order to attain a phase shift of  $\pi$ , which is technically challenging.

When the light pulses enter EIT media, photonic excitations are temporarily transferred to atomic excitations through the formation of quasiparticles, the so-called darkstate (or slow-light) polaritons, which are superpositions of light and matter degrees of freedom [16]. The spatial compression of the pulses leads to an *amplification* of the matter components of polaritons. In this paper we propose a hitherto unexplored mechanism for the collisional entanglement of two single-quantum polaritons mediated by the long-range interaction of their matter (atomic) components and demonstrate its effectiveness. In contrast to the previous schemes which employ *local* interactions, namely either two photons interact with the same atom [11–14] or two atoms after absorbing the photons undergo s-wave scattering [15], here the two polaritons interact via the long-range dipole-dipole interactions between their atomic components in the highly excited Rydberg states. In a static electric field, these internal Rydberg states, populated only in the presence of polaritons, possess large permanent dipole moments [17]. We will show that under experimentally realizable conditions, the conditional phase shift accumulated during a collision of two single-quantum polaritons is spatially homogeneous and can be sufficiently large for the implementation of the quantum phase gate, even for moderate focusing or transverse confinement of interacting pulses. We note that quantum gates for individual Rydberg atoms, coupled by dipole-dipole interaction, have been proposed in [18], while the manipulation of quantum information with mesoscopic atomic ensembles using the dipole blockade technique, based on longrange interactions of atomic Rydberg states, was discussed in [19].

We consider an ensemble of cold alkali atoms with level configuration as in Fig. 1. All the atoms are initially prepared in the ground state  $|g\rangle$ . Two weak (quantum) fields  $E_{1,2}$  having orthogonal polarizations and propagating in the opposite directions along the z axis resonantly interact with the atoms on the transitions  $|g\rangle \rightarrow |e_{1,2}\rangle$ , respectively. The intermediate states  $|e_{1,2}\rangle$  are resonantly coupled by two strong (classical) driving fields with Rabi frequencies  $\Omega_{1,2}$  to the highly excited Rydberg states  $|d\rangle$  possess large permanent dipole moments  $\mathbf{p} = \frac{3}{2}nqea_0\mathbf{e}_z$ , where n and  $q \equiv n_1 - n_2$  are, respectively, the (effective) principal and parabolic quantum numbers, e is the electron charge, and  $a_0$  is the Bohr radius [17]. A pair of atoms i and j at positions  $\mathbf{r}_i$  and  $\mathbf{r}_j$  excited to states  $|d\rangle$ 

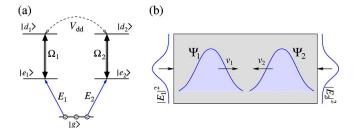


FIG. 1. (Color online) (a) Level scheme of atoms interacting with weak (quantum) fields  $E_{1,2}$  on the transitions  $|g\rangle \rightarrow |e_{1,2}\rangle$  and strong driving fields of Rabi frequencies  $\Omega_{1,2}$  on the transitions  $|e_{1,2}\rangle \rightarrow |d_{1,2}\rangle$ , respectively.  $V_{\rm dd}$  denotes the dipole–dipole interaction between pairs of atoms in Rydberg states  $|d\rangle$ . (b) Upon entering the medium, each field having Gaussian transverse intensity profile is converted into the corresponding polariton  $\Psi_{1,2}$  representing a coupled excitation of the field and atomic coherence. These polaritons propagate in the opposite directions with slow group velocities  $v_{1,2}$  and interact via the dipole–dipole interaction.

interact with each other via the dipole-dipole potential

$$V_{\rm dd} = \frac{\mathbf{p}_i \cdot \mathbf{p}_j - 3(\mathbf{p}_i \cdot \mathbf{e}_{ij})(\mathbf{p}_j \cdot \mathbf{e}_{ij})}{4\pi\epsilon_0 |\mathbf{r}_i - \mathbf{r}_j|^3},$$

where  $\mathbf{e}_{ij}$  is a unit vector along the interatomic direction. This dipole–dipole interaction results in an energy shift of the pair of Rydberg atoms, while we assume that the state mixing within the same n manifold is suppressed by the proper choice of parabolic q and magnetic m quantum numbers [17,18]. In the frame rotating with the frequencies of the optical fields, the interaction Hamiltonian has the following form:

$$H = V_{\rm af} + V_{\rm dd},\tag{1}$$

where the atom-field and dipole-dipole interaction terms are given, respectively, by

$$V_{\rm af} = - \hbar \sum_{j}^{N} \left[ g_{1}^{j} \hat{\mathcal{E}}_{1} \hat{\sigma}_{e_{1}g}^{j} + \Omega_{1} \hat{\sigma}_{d_{1}e_{1}}^{j} + g_{2}^{j} \hat{\mathcal{E}}_{2} \hat{\sigma}_{e_{2}g}^{j} + \Omega_{2} \hat{\sigma}_{d_{2}e_{2}}^{j} + \text{H.c.} \right], \tag{2a}$$

$$V_{\rm dd} = \hbar \sum_{i>j}^{N} \hat{\sigma}_{dd}^{i} \Delta(\mathbf{r}_{i} - \mathbf{r}_{j}) \hat{\sigma}_{dd}^{j}. \tag{2b}$$

Here  $N = \rho V$  is the total number of atoms,  $\rho$  being the (uniform) atomic density and V the volume;  $\hat{\sigma}^{j}_{\mu\nu} \equiv |\mu\rangle_{jj}\langle\nu|$  is the transition operator of the jth atom;  $\hat{\mathcal{E}}_{l}$  is the slowly varying operator, corresponding to the electric field  $E_{l}$  (l = 1, 2), which obeys the commutation relations  $[\hat{\mathcal{E}}_{l}(\mathbf{r}), \hat{\mathcal{E}}^{\dagger}_{l'}(\mathbf{r}')] = V \delta_{ll'} \delta(\mathbf{r} - \mathbf{r}')$ ;  $g_{l}^{j}$  is the corresponding atom-field coupling constant on the transition  $|g\rangle_{j} \rightarrow |e_{l}\rangle_{j}$ ; and  $\hbar\Delta(\mathbf{r}_{i} - \mathbf{r}_{j}) \equiv_{i}\langle d|_{j}\langle d|V_{\rm dd}|d\rangle_{i}|d\rangle_{j}$  is the dipole–dipole energy shift for a pair of atoms i and j, given by

$$\Delta(\mathbf{r}_i - \mathbf{r}_j) = C \frac{1 - 3\cos^2\vartheta}{\left|\mathbf{r}_i - \mathbf{r}_i\right|^3},$$

where  $\vartheta$  is the angle between vectors  $\mathbf{e}_z$  and  $\mathbf{e}_{ij}$ , and  $C = \wp_{d_l}\wp_{d_{l'}}/(4\pi\epsilon_0\hbar)$  is a constant proportional to the product of atomic dipole moments  $\wp_{d_l} = \langle d_l | \mathbf{p} | d_l \rangle$  assumed the same for both states  $|d_{1,2}\rangle$ ,  $\wp_{d_{1,2}} = \wp_{d}$ .

Let us introduce collective atomic operators  $\hat{\sigma}_{\mu\nu}(\mathbf{r}) = 1/N_r \sum_{j=1}^{N_r} \hat{\sigma}_{\mu\nu}^j$  averaged over the volume element  $d^3r$  containing  $N_r = \rho d^3r \gg 1$  atoms around position  $\mathbf{r}$ . Then Eqs. (2a) and (2b) can be cast in the continuous form

$$V_{\rm af} = -\hbar\rho \int d^3r \sum_{l=1,2} \left[ g_l \hat{\mathcal{E}}_l \hat{\sigma}_{e_l g}(\mathbf{r}) + \Omega_l \hat{\sigma}_{e_l d_l}(\mathbf{r}) \right] + \text{H.c.},$$
(3a)

$$V_{\rm dd} = \hbar \rho^2 \int \int d^3r \, d^3r' \, \hat{\sigma}_{dd}(\mathbf{r}) \Delta(\mathbf{r} - \mathbf{r}') \hat{\sigma}_{dd}(\mathbf{r}'). \tag{3b}$$

Using Eqs. (3a) and (3b), one can derive a set of Heisenberg-Langevin equations for the atomic operators  $\hat{\sigma}_{\mu\nu}$  [7]. When the number of photons in the quantum fields  $\hat{\mathcal{E}}_l$  is much smaller than the number of atoms, these equations can be solved perturbatively in the small parameters  $g_l\hat{\mathcal{E}}_l/\Omega_l$  and in the adiabatic approximation for all the fields [16], with the result

$$\hat{\sigma}_{ge_l}(\mathbf{r}) = -\frac{i}{\Omega_l} \left[ \frac{\partial}{\partial t} + i\hat{\alpha}(\mathbf{r}) \right] \hat{\sigma}_{gd_l}(\mathbf{r}), \tag{4a}$$

$$\hat{\alpha}(\mathbf{r}) = \rho \int d^3 r' \Delta(\mathbf{r} - \mathbf{r}') [\hat{\sigma}_{d_1 d_1}(\mathbf{r}') + \hat{\sigma}_{d_2 d_2}(\mathbf{r}')], \quad (4b)$$

$$\hat{\sigma}_{gd_l}(\mathbf{r}) = -\frac{g_l \hat{\mathcal{E}}_l}{\Omega_l^*}, \quad \hat{\sigma}_{d_l d_l}(\mathbf{r}) = \hat{\sigma}_{d_l g}(\mathbf{r}) \hat{\sigma}_{gd_l}(\mathbf{r}). \tag{4c}$$

Let us assume that the transverse profile of both quantum fields is described by a Gaussian  $e^{-r_\perp^2/w^2}$  of width w, where  $r_\perp = |\mathbf{r}_\perp|$  is the distance from the field propagation axis, while the Rabi frequencies of classical driving fields  $\Omega_l$  are uniform over the entire volume V. We may then write  $g_l\hat{\mathcal{E}}_l = g_l(\mathbf{r}_\perp)\hat{\mathcal{E}}_l(z)$ , where the traveling-wave electric field operators  $\hat{\mathcal{E}}_l(z) = \sum_k a_l^k e^{ikz}$  are expressed through the superposition of bosonic operators  $a_l^k$  for the longitudinal field modes k, while the (transverse-position-dependent) coupling constants are given by  $g_l(\mathbf{r}_\perp) = \widetilde{g}_l e^{-r_\perp^2/2w^2}$ , with  $\widetilde{g}_l = (\wp_{ge_l}/\hbar)\sqrt{\hbar\omega/2\epsilon_0V}$ ,  $\wp_{ge_l}$  being the dipole matrix element on the transition  $|g\rangle \rightarrow |e_l\rangle$ ,  $V = \pi w^2 L$ , and L the medium length. Under this approximation, the propagation equations for the slowly varying quantum fields have the form

$$\left(\frac{\partial}{\partial t} \pm c \frac{\partial}{\partial z}\right) \hat{\mathcal{E}}_l(z,t) = i\tilde{g}_l N \hat{\sigma}_{ge_l}(z), \tag{5}$$

the sign "+" or "-" corresponding to l=1 or 2, respectively.

Following [16], we introduce new quantum fields  $\hat{\Psi}_{\Gamma}$ —dark state polaritons—via the canonical transformations

$$\hat{\Psi}_l = \cos \theta_l \hat{\mathcal{E}}_l - \sin \theta_l \sqrt{N} \hat{\sigma}_{gd,}, \tag{6}$$

where the mixing angles  $\theta_l$  are defined through  $\tan^2\theta_l = \tilde{g}_l^2 N/|\Omega_l|^2$ . These polaritons correspond to coherent superpositions of electric field  $\hat{\mathcal{E}}_l$  and atomic coherence  $\hat{\sigma}_{gd_l}$  operators. Employing the plane-wave decomposition of the polariton operators, one can show that in the weak-field limit, they obey the bosonic commutation relations  $[\hat{\Psi}_l(z), \hat{\Psi}_{l'}^{\dagger}(z')] \simeq L \delta_{ll'} \delta(z-z')$ . Using Eqs. (4a)–(4c) and (5), we obtain the following propagation equations for the polariton operators,

$$\left(\frac{\partial}{\partial t} \pm v_l \frac{\partial}{\partial z}\right) \hat{\Psi}_l(z,t) = -i \sin^2 \theta_l \hat{\alpha}(z,t) \hat{\Psi}_l(z,t). \tag{7}$$

Here  $v_l = c \cos^2 \theta_l$  is the group velocity, while operator  $\hat{\alpha}(z,t)$  is responsible for the self- and cross-phase modulation between the polaritons. It is related to the polariton intensity (excitation number) operators  $\hat{\mathcal{I}}_l = \hat{\Psi}_l^{\dagger} \hat{\Psi}_l$  via

$$\hat{\alpha}(z,t) = \frac{1}{L} \int_0^L dz' \Delta(z-z') \left[ \sin^2 \theta_1 \hat{\mathcal{I}}_1(z',t) + \sin^2 \theta_2 \hat{\mathcal{I}}_2(z',t) \right], \tag{8}$$

where the one-dimensional (1D) dipole-dipole interaction potential  $\Delta(z-z')$  is obtained after the integration over the transverse profile of the quantum fields,

$$\Delta(z-z') = \frac{1}{\pi w^2} \int_0^{2\pi} d\varphi' \int_0^{\infty} dr'_{\perp} r'_{\perp} e^{-r'_{\perp}^2/w^2} \Delta(z\mathbf{e}_z - \mathbf{r}')$$

$$= \frac{2C}{w^3} \left[ \frac{2|z-z'|}{w} - \sqrt{\pi} \left( 1 + 2\frac{|z-z'|^2}{w^2} \right) \right]$$

$$\times \exp\left( \frac{|z-z'|^2}{w^2} \right) \operatorname{erfc}\left( \frac{|z-z'|}{w} \right), \tag{9}$$

and is shown in Fig. 2(a).

It follows from Eq. (7) that the intensity operators  $\hat{\mathcal{I}}_l$  are constants of motion:  $\hat{\mathcal{I}}_l(z,t) = \hat{\mathcal{I}}_l(z \mp v_l t,0)$ , the upper (lower) sign corresponding to l=1 (l=2). Then the formal solution for the polariton operators can be written as

$$\hat{\Psi}_{l}(z,t) = \exp[-i\sin^{2}\theta_{l}\int_{0}^{t}dt'\,\hat{\alpha}(z \mp v_{l}(t-t'),t')]$$

$$\times \hat{\Psi}_{l}(z \mp v_{l}t,0). \tag{10}$$

Equation (10) is our central result. Let us outline the approximations involved in the derivation of this solution. In order to accommodate the pulses in the medium with negligible losses, their duration T should exceed the inverse of the EIT bandwidth  $\delta\omega = |\Omega_l|^2 (\gamma_{ge_l} \sqrt{\kappa_0 L})^{-1}$ , where  $\gamma_{ge_l}$  is the transversal relaxation rate and  $\kappa_0 \approx 3\lambda^2/(2\pi)\rho$  is the resonant absorption coefficient on the transition  $|g\rangle \rightarrow |e_l\rangle$ . This yields the condition  $(\kappa_0 L)^{-1/2} \ll T v_l/L < 1$  which requires a medium with large optical depth  $\kappa_0 L \gg 1$  [16]. In addition,

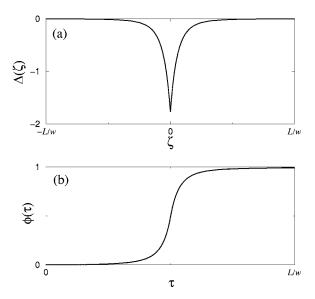


FIG. 2. (a) The 1D dipole–dipole potential  $\Delta(\zeta)$  of Eq. (9) as a function of dimensionless distance  $\zeta = (z-z')/w$ , in units of  $2C/w^3$  Hz. (b) The resulting phase shift  $\phi(\tau) \equiv \phi(vt, L-vt, t)$  of Eq. (14) as a function of dimensionless time  $\tau = vt/w$ , in units of  $2C/(vw^2)$  rad.

the dipole–dipole energy shift should lie within the EIT bandwidth  $\delta \omega$  for all  $|z-z'| \leq L$ , which implies that  $|\Delta(0)| = 2\sqrt{\pi}C/w^3 < \delta \omega$ . Finally, the propagation/interaction time of the two pulses  $t_{\text{out}} = L/v_l$  is limited by the relaxation rate  $\gamma_{gd_l}$  of the  $\hat{\sigma}_{gd_l}$  coherence via  $t_{\text{out}}\gamma_{gd_l} \leq 1$ .

From now on, we assume that  $\theta_{1,2} = \theta$ , i.e.,  $\tilde{g}_1^2 N / |\Omega_1|^2 = \tilde{g}_2^2 N / |\Omega_2|^2$ , which yields  $v_{1,2} = v = c \cos^2 \theta$ . We are interested in the evolution of input state

$$|\Phi_{\rm in}\rangle = |1_1\rangle \otimes |1_2\rangle,$$
 (11)

composed of two single-excitation polariton wave packets

$$|1_l\rangle = \frac{1}{L} \int dz f_l(z) \hat{\Psi}_l(z)^{\dagger} |0\rangle,$$

where  $f_l(z)$  define the spatial envelopes of the corresponding wave packets l=1, 2 which initially (at t=0) are localized around z=0, L, respectively. For such an initial state, all the relevant information is contained in the expectation values of the polariton intensities  $\langle \hat{\mathcal{I}}_l(z,t) \rangle = \langle \Phi_{\rm in} | \hat{\mathcal{I}}_l(z,t) | \Phi_{\rm in} \rangle$  and the two-particle wave function [7,11,12]

$$F_{12}(z_1, z_2, t) = \langle 0|\hat{\Psi}_1(z_1, t)\hat{\Psi}_2(z_2, t)|\Phi_{\rm in}\rangle.$$
 (12)

With the above solution, for the polariton intensities we have  $\langle \hat{\mathcal{I}}_{1,2}(z,t) \rangle = \langle \hat{\mathcal{I}}_{1,2}(z \mp vt,0) \rangle = |f_{1,2}(z \mp vt)|^2$ , which describes the shape-preserving counterpropagation of the two polaritons with group velocity v. Substituting the operator solution (10) into Eq. (12), after some algebra, we obtain the following expression for the two-particle wave function:

$$F_{12}(z_1, z_2, t) = f_1(z_1 - vt)f_2(z_2 + vt)\exp[i\phi(z_1, z_2, t)], \tag{13}$$

$$\phi(z_1, z_2, t) = -\sin^4\theta \int_0^t dt' \Delta[z_1 - z_2 - 2v(t - t')], \quad (14)$$

which indicates that the dipole–dipole interaction between the two single-excitation polaritons results in the conditional phase-shift  $\phi(z_1, z_2, t)$ . We consider a situation in which at time t=0, the first pulse is localized at  $z_1=0$  and the second pulse is at  $z_2=L$ , while after the interaction, at time  $t_{\text{out}}=L/v$ , the coordinates of the two pulses are  $z_1=L$  and  $z_2=0$ , respectively [Fig. 2(b)]. Then the phase shift accumulated during the interaction is spatially uniform, and is given by

$$\phi(L, 0, L/v) = -\frac{\sin^4 \theta}{v} \int_0^L dz' \Delta (2z' - L) = \frac{2C \sin^4 \theta}{vw^2}.$$
 (15)

This remarkably simple result is obtained upon replacing the variable  $(2z'-L)/w \to \zeta'$  and extending the integration limits to  $L/w \to \infty$ . The main limitation on the phase shift is imposed by the condition  $|\Delta(0)| < \delta \omega$ . In terms of experimentally relevant parameters, the group velocity is  $v \approx 2|\Omega|^2/(\kappa_0 \gamma_{pe}) \ll c(\sin^2\theta \approx 1)$ , and we have

$$\phi < \frac{w}{2} \sqrt{\frac{\kappa_0}{\pi L}}.\tag{16}$$

To relate the foregoing discussion to a realistic experiment, let us assume an ensemble of cold alkali atoms in the ground state  $|g\rangle$  with density  $\rho \sim 10^{14}$  cm<sup>-3</sup> confined in a trap of length  $L \sim 100~\mu m$ . The resonant quantum fields with  $\lambda \sim 0.6~\mu m$  have the transverse width  $w \sim 30~\mu m$ . In the presence of driving fields with appropriate frequencies, the single-photon pulses lead to the (two-photon) excitation of single atoms to the Rydberg states  $|d\rangle$  with quantum numbers  $n \approx 25~$  and q = n - 1. The corresponding dipole moment is  $\wp_d \approx 900ea_0$ , while the decay rate of  $|d\rangle$  is  $2\gamma_d \sim 3 \times 10^3~\text{s}^{-1}$ 

[17]. With  $\gamma_{ge} \sim 10^7 \, \mathrm{s}^{-1}$  and  $\Omega \sim 1.8 \times 10^7 \, \mathrm{rad/s}$ , the group velocity is  $v \simeq 4 \, \mathrm{m/s}$ , and the accumulated phase shift is  $\phi \simeq \pi$ . The corresponding fidelity F of the phase gate is determined by the bandwidth of the transparency window  $\delta \omega$  and the two-photon coherence relaxation rate  $\gamma_{gd}$ , as discussed above. For the present parameters, condition (16) is satisfied, the optical depth is large  $\kappa_0 L \sim 1.7 \times 10^3$ , while for a cold atomic gas we have  $\gamma_{gd} \simeq \gamma_d$ . Therefore the fidelity is mainly limited by the relaxation rate  $\gamma_d$  of Rydberg states and is given by  $F = \exp(-\gamma_d L/v) \gtrsim 0.96$ .

To summarize, we have studied a highly efficient scheme for cross-phase modulation and entanglement of two counterpropagating single-photon wave packets, employing their ultrasmall group velocities in atomic vapors, under the conditions of electromagnetically induced transparency, and the strong long-range dipole-dipole interactions of the accompanying Rydberg-state excitations in a ladder-type field-atom coupling setup. We have solved, in the weak-field and adiabatic approximations, the effective one-dimensional propagation equations for the polariton operators and have shown that the dipole-dipole interaction leads to a homogeneous conditional phase shift that can reach the value of  $\pi$  even if the transverse cross section of the pulses  $w^2$  is much (three orders of magnitude) larger than the diffraction limit  $\lambda^2$ . This is the obvious merit of the present proposal, as compared to previous schemes based on local interactions of photons or slow-light polaritons [9–15], which require the photonic beam cross section to be comparable to the cross section for atomic resonant absorption. Hence our proposal paves the way to the coveted deterministic entanglement of two singlephoton pulses and the realization of the universal photonic phase gate [12].

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