Quantum-noise randomized data encryption for wavelength-division-multiplexed fiber-optic networks

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We demonstrate high-rate randomized data-encryption through optical fibers using the inherent quantummeasurement noise of coherent states of light. Specifically, we demonstrate 650 Mbit/s data encryption through a 10 Gbit/s data-bearing, in-line amplified 200-km-long line. In our protocol, legitimate users (who share a short secret key) communicate using an *M*-ry signal set while an attacker (who does not share the secret key) is forced to contend with the fundamental and irreducible quantum-measurement noise of coherent states. Implementations of our protocol using both polarization-encoded signal sets as well as polarization-insensitive phase-keyed signal sets are experimentally and theoretically evaluated. Different from the performance criteria for the cryptographic objective of key generation (quantum key-generation), one possible set of performance criteria for the cryptographic objective of data encryption is established and carefully considered.

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I. INTRODUCTION

For more than 20 years, physicists and engineers have investigated quantum-mechanical phenomena as mechanisms to satisfy certain cryptographic objectives. Such objectives include user authentication, bit commitment, key generation, and, recently, data encryption. To date, the cryptographic objective most considered in the literature has been key generation. In key generation, two users, who initially share a small amount of secret information, remotely agree on a sequence of bits that is both larger than their original shared information and is known only to them. The newly generated bits (keys) are then used to publicly communicate secret messages over classical channels by driving data encrypters like the information theoretically perfect onetime pad [1] or more efficient (but less secure) encrypters, such as the Advanced Encryption Standard, where security is described in terms of complexity assumptions [2,3].

Several approaches to key generation using quantum effects have been proposed and demonstrated. The most famous of these protocols, the BB84 protocol [4] and the Ekert protocol [5], have enjoyed considerable theoretical consideration as well as experimental implementation [6-8]. A major technical limitation of the BB84 (Ekert) protocol is that the achievable key-generation rate (more importantly, the ratedistance product) is relatively low due to the protocol's requirement for single-photon (entangled-photon) quantum states. This requirement is a burden not only in the generation of such states, but also in that such states are acutely susceptible to loss, are not optically amplifiable (in general), and are difficult to detect at high rates. Furthermore, because the received light must be detected at the single-photon level, integration of the protocol implementations into today's wavelength-division-multiplexed (WDM) fiber-optic infrastructure is problematic because cross-channel isolation is typically no better than 30 dB.

Recently, we have demonstrated a new quantum cryptographic scheme, based on Yuen's KCQ approach [9], in which the inherent quantum noise of coherent states of light is used to perform the cryptographic service of data encryption [10,11]. Unlike single-photon states, coherent states (of moderate energy level) are easily generated, easily detected, and are optically amplifiable, networkable, and loss-tolerant. Note that key generation and data encryption are two *different* cryptographic objectives with *different* sets of criteria by which to judge performance—a direct comparison between the two is not appropriate.

In our scheme, legitimate users extend a short, shared secret key by using a publicly known deterministic function. The transmitter uses the extended key to select a signal set for each transmitted bit such that the legitimate receiver, using the same extended key, is able to execute a simple binary-decision measurement on each bit. An eavesdropper, on the other hand, who does not possess the secret key, is subject to an irreducible quantum uncertainty in each measurement, even with the use of ideal detectors. This uncertainty results in randomization of the eavesdropper's observations, thereby realizing a true randomized cipher [12] which effectively limits the eavesdropper's ability to decipher the transmitted message. This randomization is "free" in that it does not require any additional action on the part of the transmitter, in contrast to other randomized ciphers [13,14] where active randomization of the signal set is required by the transmitter. Our scheme, running at dataencryption rates up to 650 Mbit/s, uses off-the-shelf compoand is compatible with today's optical nents telecommunications infrastructure. This paper is organized as follows: in Sec. II we outline our quantum-noise protected data-encryption protocol (call the $\alpha \eta$ protocol), in Sec. III we address issues of security and performance, and in Sec. IV we summarize our experimental results.

II. DATA-ENCRYPTION PROTOCOL

We have implemented two versions of our quantum-noise protected data-encryption protocol using different signal

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FIG. 1. Top: M pairs of orthogonal polarization states uniformly span a great circle of the Poincaré sphere; bottom: M pairs of antipodal phase states uniformly span a phase circle.

sets—one using polarization states [11] (polarization-mode scheme) and the other using phase states [15,16] (time-mode scheme). In both implementations, the fundamental and irreducible measurement uncertainty of coherent states is the key element giving security. In the polarization-mode scheme, the two-mode coherent states employed are

$$|\Psi_m^{(a)}\rangle = |\alpha\rangle_x \otimes |\alpha \, e^{i\theta_m}\rangle_y,\tag{1}$$

$$|\Psi_m^{(b)}\rangle = |\alpha\rangle_x \otimes |\alpha \ e^{i(\theta_m + \pi)}\rangle_y, \tag{2}$$

where $|\alpha\rangle$ is a coherent state, $\theta_m = \pi m/M, m \in \{0, 1, 2, ..., (M-1)\}, M$ is odd, and the subscripts *x* and *y* indicate the two orthogonal polarization-mode-functions. Viewed on the Poincaré sphere, these 2*M* polarization states form *M* bases that uniformly span a great circle, as shown in Fig. 1 (top). In the time-mode scheme, the single-mode coherent states employed are

$$|\Psi_m^{(a)}\rangle = |\alpha e^{i\theta_m}\rangle,\tag{3}$$

$$|\Psi_m^{(b)}\rangle = |\alpha e^{i(\theta_m + \pi)}\rangle,\tag{4}$$

where again $\theta_m = \pi m/M, m \in \{0, 1, 2, ..., (M-1)\}$, and *M* is odd. These 2*M* states form *M* antipodal-phase pairs (bases) that uniformly span the phase circle, as shown in Fig. 1 (bottom).

In both schemes, the transmitter (Alice) extends an *s*-bit secret key, **K**, to a (2^s-1) -bit pseudorandom extended key, **K**', using a publicly known *s*-bit linear feedback shift register [2] (LFSR) of maximal length. The extended key is grouped into continuous disjointed *r*-bit blocks and then passed through an invertible *r*-bit-to-*r*-bit deterministic mapping function, referred to as a "mapper," resulting in running keys, **R**, where $r=int[log_2M]$ and $s \ge r$. The mapper, which is publicly known, helps to distribute an attacker's measurement uncertainty throughout each running key. Without the

use of a mapper, an attacker's measurement uncertainty would, the majority of the time, obscure just the least significant bits of each *r*-bit running key, thereby leaving most of the *r* bits clearly identifiable. Also, note that an LFSR is just one of many functions that the users can use to extend **K** into **K**'. The reason LFSRs are used in these experiments is because they are mathematically simple to describe, which could be useful when quantifying the precise level of security provided by $\alpha \eta$.

Depending on the data bit and an instantiation of the running key R, one of the states in Eq. (1) and (3) or Eq. (2) and (4) is transmitted where *m* is the decimal representation of *R*. Specifically, for the polarization-mode scheme, if *m* is even, then $(0,1) \rightarrow (|\Psi_m^{(a)}\rangle, |\Psi_m^{(b)}\rangle)$ and if *m* is odd, then $(0,1) \rightarrow (|\Psi_m^{(b)}\rangle, |\Psi_m^{(a)}\rangle)$. This results in the logical bit mapping of the polarization states on the Poincaré sphere to be interleaved 0, 1, 0, 1,..., as shown in Fig. 1 (top). The time-mode scheme is similarly organized but slightly more complicated in that the data bits are defined differentially [differentialphase-shift keying (DPSK)]. Specifically, if m is even, then the DPSK mapping is $(0, \pi) \rightarrow (|\Psi_m^{(a)}\rangle, |\Psi_m^{(b)}\rangle)$, and $(0, \pi) \rightarrow (|\Psi_m^{(b)}\rangle, |\Psi_m^{(a)}\rangle)$ for *m* odd. If we relabel the states corresponding to DPSK phases of "0" and " π " as μ and ν , respectively, then logical zero is mapped to $|\Psi_m^{(\mu)}\rangle(|\Psi_m^{(\nu)}\rangle)$ if the previously transmitted state was from the set $\{|\Psi_m^{(\mu)}\rangle\}(\{|\Psi_m^{(\nu)}\rangle\})$ and the logical one is mapped to $|\Psi_m^{(\mu)}\rangle(|\Psi_m^{(\nu)}\rangle)$ if the previously transmitted state was from the set $\{|\Psi_m^{(\nu)}\rangle\}$ ($\{|\Psi_m^{(\mu)}\rangle\}$). This results in the mapping of the symbols on the phase circle to be interleaved $\mu, \nu, \mu, \nu, ...$, as shown in Fig. 1 (bottom).

At the receiving end, the intended receiver (Bob) uses the same *s*-bit secret key and LFSR/mapper to apply unitary transformations to his received quantum states according to the running keys. These transformations correspond to polarization-state rotations for the polarization-mode scheme and phase shifts for the time-mode scheme—in either case the transmitted M-ry signal set is reduced to a binary signal set. The resulting states under measurement, depending on the logical bit, are

$$|\Psi^{(a)}\rangle' = |\eta\alpha\rangle_x \otimes |\eta\alpha\rangle_y, \tag{5}$$

$$|\Psi^{(b)}\rangle' = |\eta\alpha\rangle_x \otimes |-\eta\alpha\rangle_y \tag{6}$$

for the polarization-mode scheme and

$$|\Psi^{(a)}\rangle' = |\eta\alpha\rangle,\tag{7}$$

$$|\Psi^{(b)}\rangle' = |-\eta\alpha\rangle \tag{8}$$

for the time-mode scheme, where η is the channel transmissivity. For both schemes, the states are then demodulated and differentially detected. Specifically, a fixed $\pi/4$ polarization rotation on the states in the polarization-mode scheme results in the detected states



$$|\tilde{\Psi}^{(a)}\rangle = |\sqrt{2}\,\eta\alpha\rangle_x \otimes |0\rangle_y,\tag{9}$$

$$|\tilde{\Psi}^{(b)}\rangle = |0\rangle_x \otimes |\sqrt{2}\,\eta\alpha\rangle_y,\tag{10}$$

whereas temporally asymmetric interferometry in the timemode implementation results in the detected states

$$|\tilde{\Psi}^{(a)}\rangle = |\eta\alpha\rangle_1 \otimes |0\rangle_2, \tag{11}$$

$$|\tilde{\Psi}^{(b)}\rangle = |0\rangle_1 \otimes |\eta\alpha\rangle_2. \tag{12}$$

An important feature to note is that Bob does not require high precision in applying decryption transformations to a transmitted bit. While the application of a slightly incorrect polarization/phase transformation results in a larger probability of error for the bit, it does not categorically render a bit to be in error. For small perturbations to the polarization/phase rotation, the majority of the signal energy stays in one of the two detection modes. The same applies to Bob's detector noise; while an ideal detector allows for optimized performance, a noisy detector does not limit Bob's decryption ability beyond an increased probability of bit error.

A high-level block diagram of the $\alpha \eta$ protocol is provided in Fig. 2. Note that some elements of our protocol that help to protect the secret key against attack have been intentionally omitted from this description for the purpose of clarity. These omitted elements are mentioned in the following section and are further described in Ref. [9].

III. SECURITY

As stated in the Introduction, key generation and data encryption are different cryptographic objectives and, therefore, have different sets of criteria by which to evaluate performance. The delineation between key generation and data encryption is somewhat confused by terminology. Because keys procured by a key-generation protocol are usually assumed to drive deterministic encrypters, the terms "quantum key-generation" and "quantum data-encryption" are sometimes used interchangeably. This easily leads to confusion in that (a) there are potential uses for generated keys beyond data encryption, and (b) there are methods of realizing quantum-based data encryption without key generation.

In quantum key-generation, a necessary (but not sufficient) condition that must be satisfied is FIG. 2. Summary of the quantum-noise protected dataencryption protocol. In our experiments, the "pseudorandom key extender" is implemented by a maximal-length LFSR and an " *r*-bit-to-*r*-bit mapping function."

$$H(\mathbf{X}|\mathbf{Y}^{\mathbf{E}},\mathbf{K}) - H(\mathbf{X}|\mathbf{Y}^{\mathbf{B}},\mathbf{K}) - H(\mathbf{K}) > 0, \qquad (13)$$

where **X** is a classical *n*-bit random vector describing the transmitted bits, $\mathbf{Y}^{\mathbf{E}}$ and $\mathbf{Y}^{\mathbf{B}}$ are *n*-bit vectors describing the observations of an attacker (Eve) and Bob, respectively, **K** is an *s*-bit, previously shared secret between Alice and Bob that might become public on completion of the protocol, and $H(\cdot)$ is the Shannon entropy function. Note that while often omitted in descriptions of the BB84 and Ekert protocols, both schemes require a secret key **K** for the purpose of message authentication. Also note that the $H(\mathbf{K})$ term in Eq. (13) may be omitted if both (a) information about **K** is never publicly announced and (b) **K** remains secret even when under a general attack (as in some of Yuen's KCQ key-generation protocols).

The mathematical definition of $H(\mathbf{X} | \mathbf{Y})$, to be read as "the uncertainty of **X** given **Y**," is given by

$$H(\mathbf{X}|\mathbf{Y}) \equiv -\sum_{\mathbf{x},\mathbf{y}} p(\mathbf{X} = \mathbf{x}, \mathbf{Y} = \mathbf{y}) \log p(\mathbf{X} = \mathbf{x}|\mathbf{Y} = \mathbf{y}),$$
(14)

which, with application of Bayes' theorem and the law of total probability, becomes

$$H(\mathbf{X}|\mathbf{Y}) = -\sum_{\mathbf{x},\mathbf{y}} p(\mathbf{X} = \mathbf{x}) p(\mathbf{Y} = \mathbf{y}|\mathbf{X} = \mathbf{x})$$
$$\times \log \left[\frac{p(\mathbf{X} = \mathbf{x}) p(\mathbf{Y} = \mathbf{y}|\mathbf{X} = \mathbf{x})}{\sum_{\mathbf{x}'} p(\mathbf{X} = \mathbf{x}') p(\mathbf{Y} = \mathbf{y}|\mathbf{X} = \mathbf{x}')} \right]. \quad (15)$$

The conditional probability distribution $p(\mathbf{Y}|\mathbf{X})$ is completely and uniquely specified by the probability distribution of the secret key $p(\mathbf{K})$, the probability distribution of the plaintext message $p(\mathbf{X})$, and the encryption function that takes \mathbf{X} to $\mathbf{Y}=E_{\mathbf{K}}(\mathbf{X})$. While $E_{\mathbf{K}}(\mathbf{X})$ is usually assumed known to the attacker via the *Kerckhoff assumption*, it is important to emphasize that the calculation of $H(\mathbf{X}|\mathbf{Y})$ also depends on the probability distributions $p(\mathbf{K})$ and $p(\mathbf{X})$ according to Eve. This means that Eve's conditional entropy $H(\mathbf{X}|\mathbf{Y})$ may change if Eve's probability distribution $p(\mathbf{X})$ changes due to the acquisition of some side information (such as the language of the plaintext message).

For the cryptographic objective of data encryption, be it classical or quantum-noise-protected, some relevant information-theoretic quantities are (ii) $H(\mathbf{X}|\mathbf{Y}^{\mathbf{E}}),$ (17)

(iii)
$$H(\mathbf{K}|\mathbf{Y}^{\mathbf{E}}),$$
 (18)

where **X** is the *n*-bit transmitted message (plaintext), $\mathbf{Y}^{\mathbf{B}}$ and $\mathbf{Y}^{\mathbf{E}}$ are Bob's and Eve's *n*-bit observations of the encrypted plaintext (ciphertext), and **K** is the *s*-bit secret key shared by the legitimate users. In words, these quantities describe (i) the error rate for the legitimate users, (ii) the secrecy of the data bits when under attack, and (iii) the secrecy of the secret key when under attack. When launched on either the data bits or the secret key, cryptographic attacks are usually divided into two categories, known-plaintext (KPT) attacks and ciphertext-only (CTO) attackes. CTO attacks correspond to situations where $p(\mathbf{X})$ is uniform, according to an attacker. In other words, all 2^n possible messages are transmitted with equal probability. A KPT attacks corresponds to all situations where $p(\mathbf{X})$ is non uniform including the totally degenerate case of chosen plaintext. Some examples of KPT attacks include knowledge of the native language of the message or perhaps some statistical knowledge of the message content. While there are clearly varying degrees of KPT attacks, a CTO attack refers to the specific case of uniform $p(\mathbf{X})$.

According to information theory [17,18], quantities (ii) and (iii) satisfy the following inequalities:

$$H(\mathbf{X}|\mathbf{Y}^{\mathbf{E}}) \leq H(\mathbf{K}), \tag{19}$$

$$H(\mathbf{K}|\mathbf{Y}^{\mathbf{E}}) \leq H(\mathbf{K}), \tag{20}$$

where Eq. (19) is known as the Shannon limit [19], which is valid when $H(\mathbf{X}|\mathbf{Y}^{\mathbf{E}}, \mathbf{K}) = 0$ [our data-encryption protocol operates in a regime where $H(\mathbf{X}|\mathbf{Y}^{\mathbf{E}}, \mathbf{K}) \cong 0$ [23]]. Note that in $\alpha \eta$, contrary to the case for key generation [cf. Eq. (13)], the condition $H(\mathbf{X}|\mathbf{Y}^{\mathbf{E}}, \mathbf{K}) > H(\mathbf{X}|\mathbf{Y}^{\mathbf{B}}, \mathbf{K})$ need *not* be satisfied. In fact, the opposite is normally true where an attacker (given the secret key after measurement) has a lower biterror rate than the legitimate receiver. This is the case when a significant amount of loss and/or additive noise exists between the two users where it is assumed that the attacker, performing an adequate quantum measurement, is located near the transmitter.

The one-time pad encrypter achieves what Shannon called "perfect security," which corresponds to $=H(\mathbf{X})$ in the inequality of Eq. (19) when s=n. The practical problem with the one-time pad is that every data bit to be encrypted requires one bit of key. More "efficient," albeit less secure, encrypters operate in the regime where $s \ll n < \infty$, thereby allowing short secret keys to encrypt long messages. A reasonable information-theoretic goal of such "imperfect but efficient" encrypters (practical encrypters) could be to show

$$H(\mathbf{X}|\mathbf{Y}^{\mathbf{B}},\mathbf{K}) \to 0, \tag{21}$$

$$H(\mathbf{X}|\mathbf{Y}^{\mathbf{E}}) = \lambda_1 H(\mathbf{K}), \qquad (22)$$

$$H(\mathbf{K}|\mathbf{Y}^{\mathbf{E}}) = \lambda_2 H(\mathbf{K}), \qquad (23)$$

where $s \le n < \infty$ and $\lambda_{1,2} \to 1$. It is extremely important to emphasize that even if $\lambda_1, \lambda_2 \to 0$, there still may exist a large complexity-based problem of finding the correct **x** even when given $\mathbf{y}^{\mathbf{E}}, p(\mathbf{X}), p(\mathbf{K})$, and $E_{\mathbf{K}}(\mathbf{X})$ —it is in this complexity-based limit in which all of today's commercial deterministic encrypters are considered.

According to the given information-theoretic criteria, a goal of practical data encrypters could be to (a) drive $\lambda_{1,2}$ as close to 1 as possible for a reasonably large *s* while still keeping $s \le n < \infty$; (b) attempt to mathematically prove Eqs. (22) and (23); and (c) if conditions (a) and (b) cannot be met, insure that the computational (search) complexity is high even when $\lambda_{1,2}H(\mathbf{K})=0$. To date, no practical data encrypter exists for which Eqs. (22) and (23) can be rigorously proven, for nontrivial λ , when under a KPT attack; no significant complexity-based security have been proven either.

Note that the appropriate information-theoretic criteria by which to quantify the security of a data encrypter may be different for different sociological situations. For example, satisfying the criteria given in Eqs. (22) and (23) ($\lambda_{1,2}=1$) may yield security in some situations, but not in others. A different set of operationally meaningful criteria for the cryptographic objective of data encryption, which does not rely on Shannon entropy, has been described in Ref. [9].

Towards the goal of satisfying the cryptographic objective of data encryption, according to any reasonable informationtheory-based criteria, we offer a new approach to data encryption wherein the irreducible uncertainty inherent in the quantum measurement of coherent states of light is used to perform high-speed randomized encryption that does not sacrifice the data rate. In our protocol (Sec. II), the logical mappings of the symbols are interleaved (Fig. 1). While the users (who share a short secret key) are able to make simple binary decisions on the *M*-ry signal set, an attacker (who does not share the secret key) is left with an irreducible uncertainty in her measurements due to the quantum fluctuations inherent to coherent states of light. Specifically, with M and $|\alpha|^2$ in a particular regime, measurements of neighboring states, on either the Poincaré sphere or the phase circle, overlap and obscure one another. To an attacker, this overlap is equivalent to Alice broadcasting digital representations of the M-ry signal that are then actively randomized over the signal's closest neighbors in the signal constellation. By using coherent states with a relatively weak amplitude, a similar randomization is achieved through quantum-measurement noise which requires no active effort on the part of the transmitter, but still obscures the true identity of the state called for by the protocol. Such randomization is realized through any quantum measurement including direct detection, balanced homodyne/heterodyne detection, and optimal quantum-phase detection.

Given some restrictive assumptions, one can even describe the performance of a quantum-mechanically optimal attack—the best attack allowed by quantum mechanics. While the physical structure of such an optimal attack may be unknown, quantum mechanics can establish bounds on the maximum information rate of an attacker. For individual



FIG. 3. Shannon information recovered through individual attacks on the message when launching either the optimal positive operatorvalued measure or an ideal heterodyne measurement on the time-mode (left) and polarization-mode (right) implementations. Plotted as a function of $|\alpha|^2$, for several values of *M*.

attacks on the message where classical correlations are ignored, the quantum-mechanically optimal attack—known as the optimal positive operator-valued measure—corresponds to optimally distinguishing all of the states mapped to logical one from those mapped to logical zero. Figure 3 plots the information rate of the optimal positive operator-valued measure as a function of $|\alpha|^2$ and M for the time- and polarization-mode implementations where information [17] is defined as $1 + \bar{P}_e \log_2(\bar{P}_e) + (1 - \bar{P}_e) \log_2(1 - \bar{P}_e)$ for a biterror rate \bar{P}_e .

Figure 3 also plots the information rate of the described attack when performing an ideal heterodyne measurement. The performance of this measurement is included because it represents the "highest performing" receiver structure that an attacker could practically implement using today's technology. The difference between the information rates of the time- and polarization-mode implementations, for both the optimal positive operator-valued measure and ideal heterodyne attacks, is due to the fact that logical bits are defined differentially across two modes in the time-mode scheme-a bit is correctly determined if and only if two consecutive state measurements are both correct or both incorrect. It is important to remember that both the optimal positive operator-valued measure and ideal heterodyne analyses are for a very limited attack where Eve does not use her information on the correlations between the running keys to determine the plaintext or secret key-a real attacker would presumably use all information at her disposal.

While the inability to distinguish neighboring states plays a role in protecting the secret key against attacks, additional mechanisms are required to improve the secrecy of the secret key. By introducing deliberate state randomization at the transmitter, perfect security against CTO attacks on the secret key $[H(\mathbf{K} | \mathbf{Y}^{\mathbf{E}}) = H(\mathbf{K})$, uniform $p(\mathbf{X})]$ can be assured as well as strongly ideal security against CTO attacks on the message $[H(\mathbf{X} | \mathbf{Y}^{\mathbf{E}}) = H(\mathbf{K})$, uniform $p(\mathbf{X})]$. More information on deliberate state randomization is available in Ref. [9]. Note that the mapper and deliberate state randomization have not yet been implemented in our published experimental realizations.

Physical "Trojan horse" attacks can also be launched on the message and the secret key by attempting to *probe* Alice's transmitter settings. In such an attack, an eavesdropper would send strong light into Alice's transmitter and measure the state of her reflected light. Attacks of this type can be passively thwarted by using an optical isolator at the output of Alice's transmitter.

Confusion over the cryptographic service that our protocol ($\alpha \eta$) offers as well as how quantum noise is exploited in our scheme prompted a criticism [20] to Ref. [10] and some of the authors of Ref. [10] have replied [21]. In Ref. [22], it is claimed that the $\alpha \eta$ data-encryption protocol, operating in a regime where $H(\mathbf{X} | \mathbf{Y}^{\mathbf{E}}, \mathbf{K}) < H(\mathbf{X} | \mathbf{Y}^{\mathbf{B}}, \mathbf{K})$, already permits key generation. We disagree with that conclusion.

IV. EXPERIMENTS

Using both the polarization- and time-mode implementations, we demonstrate high-speed quantum-noise-protected data encryption. The primary objective of these experiments is to successfully demonstrate quantum data-encryption through a realistic classical-data bearing WDM fiber line. A secondary objective is to show that the quantum-noise encrypted signal does not negatively impact the performance of the classical data-bearing channels. The following two subsections summarize the physical setups as well as the experimental results for both implementations.

A. Polarization-mode implementation

A description of the polarization-mode experimental setup naturally breaks into two parts: the quantum-noise-protected data-encryption transmitter-receiver pair and the WDM fiber line (which also carries classical data traffic) over which the encrypted data travel. We first describe the transmitterreceiver pair. As illustrated in Fig. 4 (left), a polarizationcontrol paddle (PCP) is adjusted to project the light from a 1550.1-nm-wavelength distributed-feedback (DFB) laser equally into the two polarization modes of Alice's 10-GHzbandwidth fiber-coupled LiNbO₃ phase modulator (PM). Driven by the amplified output of a 12-bit digital-to-analog (D-A) board, the modulator introduces a relative phase

 $(0-2\pi$ radians) between the two polarization modes. A 32-bit software LFSR, which is implemented on a personal computer (PC), yields a running key that, when combined with



FIG. 4. Left, transmitter/receiver setup: G1, RF power amplifier; OA1, low-noise EDFA followed by a Bragg-grating filter; G2, RF signal amplifier. Right, WDM network setup: OA1, low-noise EDFA; G3, IM driver; OA2, in-line EDFA followed by an optical isolator; OA3, EDFA.

the data bit, instructs the generation of one of the two states described in Eqs. (1) and (2). Due to electronic bandwidth limitations of some amplifiers, Manchester coding is applied on top of the signal set that results in a factor of 2 reduction of the data rate (250 Mbit/s) relative to the line rate (500 Mbit/s). Note that in the time-mode implementation, described in Sec. IV B, such Manchester coding is not required due to the use of wider bandwidth amplifiers. With the use of an optical attenuator (not shown), an optical power of 25 dBm across the two polarization modes of the $\alpha\eta$ signal is fixed. At —25 dBm, the mean photon number per bit is approximately 40,000 at a line rate of 500 Mbps ($\alpha^2 = 20\ 000$),

On passing through the 100-km-long WDM fiber line [shown in Fig. 4 (right), *Crypto. in* and *Crypto. out*], the received light is amplified by a home-built erbium-doped-fiber amplifier (EDFA) with \approx 30 dB of small-signal gain and a noise figure very close to the quantum limit (NF \approx 3 dB). Before passing through Bob's PM, the received light is sent through a second PCP to cancel out the unwanted polarization rotations that occurs in the 100-km-long fiber line. While these rotations fluctuate with a bandwidth on the order of kilohertz, the magnitude of the fluctuations drops quickly with frequency, allowing the use of a manual PCP to track out such unwanted polarization rotations. In future implementations, Bob's measurements could be used

to drive an automated feedback control on the PCP.

The relative phase shift (polarization rotation) introduced by Bob's modulator is determined by the running-key R generated through a software LFSR in Bob's PC and applied via the amplified output of a second D-A board. After this phase shift has been applied, the relative phase between the two polarization modes is 0 or π , corresponding to a 0 or 1 according to the running key: if R is even, then $(0,\pi)$ $\rightarrow (0,1)$ and if R is odd, then $(0,\pi) \rightarrow (1,0)$. With use of a fiber-coupled polarization beam splitter (FPBS) oriented at $\pi/4$ radians with respect to the modulator's principal axes, the state under measurement [Eq. (9) or Eq. (10)] is directdetected by using two 1-GHz-bandwidth In-Ga-As p-i-n photodiodes operating at room temperature, one for each of the two polarization modes. The resulting photocurrents are amplified by a 40-dB-gain amplifier, sampled by an analogto-digital (A-D) board, and stored for analysis. The overall sensitivity of Bob's preamplified receiver is measured to be 660 photons/bit for 10^{-9} error probability.

As shown in Fig. 4 (right), the 100-km-long WDM line consists of two 40-channel 100-GHz-spacing arrayedwaveguide gratings (AWGs), two 50 km spools of singlemode fiber (Corning, SMF-28), and an in-line EDFA with an output isolator. Along with the quantum-noise protected 0.25 Gbit/s encrypted-data channel, two 10 Gbit/s channels of classical data traffic also propagate through the described WDM line. Light from two DFB lasers on the 100 GHz ITU grid (1546.9 nm and 1553.3 nm) is mixed on a 3 dB coupler, where one output is terminated and the other enters a 10 GHz-bandwidth fiber-coupled Mach-Zender-type LiNbO₃ intensity modulator (IM). The IM is driven by an amplified 10 Gbit/s pseudorandom bit sequence (PRBS) generated by a pattern generator of $(2^{31}-1)$ period. The PRBS modulated channels (hereafter referred to as PRBS channels) then pass through an EDFA to compensate for losses before entering, and being spectrally separated by AWG1. By introducing approximately one meter fiber length difference between the separated PRBS channels before combining them into the 100-km-long WDM line with AWG2, the bit sequences of the two channels are shifted by 50 bits. This shift reduces temporal correlations between the two PRBS channels, thereby more effectively simulating random, real-world data traffic. The 100-km-long WDM line is loss compensated by an in-line EDFA. The 10 dB power loss in the first 50 km spool of fiber (0.2 dB/km loss) is compensated by 10 dB of saturated gain from the in-line EDFA. The overall loss of the line is therefore 15 dB, where 10 dB come from the second 50 km spool of fiber and the remaining 5 dB from the two AWGs (2.5 dB each).

After propagating through the WDM line, the channels are separated by AWG3. Either of the two PRBS channels is amplified with a 20 dB gain EDFA (OA3) and the group-velocity dispersion (GVD) is compensated by a -1530 ps/nm dispersion-compensation module (DCM). While the GVD introduced in the WDM line is approximately 1700 ps/nm, the DCM used is sufficient for our demonstration. The amplified, GVD-compensated PRBS channel is detected using an In-Ga-As *p-i-n* TIA receiver (RCVR) and analyzed for errors by a 10 Gbit/sbit-error-rate tester (BERT). Bit-error rates for each PRBS channel are measured separately using the BERT.



FIG. 5. (a) Optical spectrum (left) and eye pattern (right) of a PRBS channel at launch [after AWG2 in Fig. 4 (right)]. (b) Optical spectrum (left) and eye pattern (right) of a PRBS channel at the end of the line [before AWG3 in Fig. 4 (right)].

Figure 5(a) (left) shows the optical spectrum of the light after AWG2 measured with 0.01 nm resolution bandwidth. The launch powers in the quantum channel and in each of the PRBS channels are -25 dBm and 2 dBm, respectively. An eye pattern of the 1546.9 nm PRBS channel at launch is shown in Fig. 5(a) (right). Measuring after AWG2 (i.e., at launch), neither PRBS channel showed any error in 10 terabits of pseudorandom data communicated. Figure 5(b) (left) shows the optical spectrum (0.01 nm resolution bandwidth) of the light received after the second 50 km spool of fiber. While this figure accurately shows the 10 dB loss in signal



FIG. 6. Five-kbit segments of 9.1-Mbit transmissions through the WDM link. Insets, the received bitmap images. Top, Bob's detection; bottom, Eve's detection.



FIG. 7. Left: Transmitter-receiver setup. G1, RF power amplifier; OA2, low-noise EDFA followed by a 25-GHz-passband Bragggrating filter; PMF, polarization-maintaining fiber; Circ., optical circulator. Right: 200-km in-line amplified line. IM, 10 Gbit/s intensity modulator; DCM, dispersion-compensation module; RCVR, 10 Gbit/s In-Ga-As *p-i-n* TIA optical receiver; G2, 10 Gbit/s modulator driver.

power for all three channels, it erroneously implies that the amplified spontaneous-emission (ASE) noise floor increased by 13 dB rather than decrease by 7 dB as expected. The reason why the noise floor looks artificially low in Fig. 5(a)(left) is because AWG1 and AWG2 filter the majority of the out-of-band ASE (sim \sim 25 dB of isolation from each AWG). The actual noise floor is $\sin \sim 7$ dB higher than the noise floor in Fig. 5(b) (minus 10 dB from the 50 km fiber spool plus sim \sim 3 dB from the in-line EDFA). An eye pattern of the 1546.9 nm PRBS channel, post dispersion compensation, is shown in Fig. 5(b) (left). While the effect of the residual GVD is clearly visible in the eye pattern, the bit-error rate for each of the PRBS channels remains nearly "error-free" at 5 $\times 10^{-11}$. Neither the bit-error rates nor the eye patterns of the PRBS channels change when the quantum channel is turned off.

Figure 6 shows results of 5000 A-D measurements (one of the two detector outputs) of a 9.1 Mb bitmap file transmitted on the encrypted channel from Alice to Bob (top) and to Eve (bottom) through the 100-km-long WDM line at 250 Mbit/s data rate. The insets show the respective decoded images. In this experiment, the actions of Eve are physically simulated by Bob starting with an incorrect secret key. Clearly, a real eavesdropper would aim to make better measurements by

placing herself close to Alice and implementing a more optimized quantum measurement. While Fig. 6 does not explicitly demonstrate Eve's inability to distinguish logical ones from zeros, it does show that a simple bit decision is impossible. In the current setup, the 12-bit D-A conversion allows Alice to generate and transmit 4094 distinct polarization states (M=2047 bases). The numerical calculation used to plot Fig. 3 (right) then shows that for -25 dBm launch power at 250 Mbit/s (500 Mbit/s line rate, $|\alpha|^2 \approx 20000$) and M=2047, Eve's maximum obtainable information in an individual attack on the message is less than 10^{-14} bits/bit. Under an attack implementing an ideal heterodyne measurement (performed at the output of Alice's transmitter), these values of α^2 and M result in approximately seven neighboring states falling within one standard deviation of the Gaussian-distributed measurement noise.

B. Time-mode implementation

While technically possible, as demonstrated above, the polarization-state alignment required at the receiver by the polarization-mode scheme makes it much less attractive than a polarization-insensitive version with equivalent performance. The time-mode implementation of $\alpha \eta$ is *totally* polarization-state-insensitive and is therefore much more desirable for performing quantum-noise-protected data encryption over real-world WDM networks.

As with the polarization-mode implementation, a description of the time-mode experimental setup naturally breaks into two parts: the transmitter-receiver pair and the WDM fiber line. We first describe the transmitter-receiver pair. As illustrated in Fig. 7 (left), -25 dBm of power from a 1550.9nm-wavelength DFB laser is projected into Alice's 10-GHzbandwidth fiber-coupled PM. Driven by the amplified output of a 12-bit D-A board, the modulator introduces a relative phase (0 to $0-2\pi$ radians) between temporally neighboring symbols. A 4.4-kb software LFSR, which is implemented on a PC, yields a running key that, when combined with the data bit, instructs the generation of one of the two states described in Eqs. (3) and (4) at a 650 Mbit/s data rate. At this data rate, the mean photon number per bit, α^2 , is approximately 40 000. Before leaving the transmitter, the encrypted signal is amplified with an EDFA (OA1) to a saturated output power of 2 dBm.

On passing through the 200-km-long WDM line [shown in Fig. 7 (right), Crypto. in and Crypto. out], the received light is amplified by another EDFA (OA2) with $\simeq 30 \text{ dB}$ of small-signal gain and a noise figure very close to the quantum limit (NF \approx 3 dB). The light then passes through a pair 10-GHz-bandwidth polarization-maintaining-fiberof coupled PMs oriented orthogonally with respect to each other so that the $\hat{x}(\hat{y})$ polarization mode of the first modulator projects onto the $\hat{y}(\hat{x})$ mode of the second modulator. The effect of such concatenation is to apply an optical phase modulation that is independent of the polarization state of the incoming light. The relative phase shift introduced by Bob's modulator pair is determined by the running key R generated through a software LFSR in Bob's PC and applied via the amplified output of a second D-A board. After this phase



FIG. 8. (a) Optical spectrum (left) and eye pattern of a PRBS channel (right) at launch [after AWG2 in Fig. 7 (right)]. (b) Optical spectrum (left) and eye pattern of a PRBS channel (right) after in-line amplification [before AWG3 in Fig. 7 (right)].

shift has been applied, the relative phase between temporally neighboring states is 0 or π (differential phase-shift keying), differentially corresponding to a 0 or 1. Note that the phase modulators and the D-A boards used in the time-mode experiments are the same as those used in the polarization-mode experiments.

The decrypted signal then passes through a fiber-coupled optical circulator and into a temporally asymmetric Michelson interferometer with one bit-period round-trip path-length delay between the two arms. Use of Faraday mirrors (FM) in the Michelson interferometer ensures good polarization-state overlap at the output, yielding high visibility interference. The interferometer is path-length-stabilized with a piezoelectric transducer (PZT) and dither-lock circuit.

Light from the two outputs of the interferometer is directdetected by using two room-temperature 1-GHz-bandwidth In-Ga-As *p-i-n* photodiodes set up in a difference photocurrent configuration. The resulting photocurrent is either sampled by an A-D board and stored for analysis, or put onto a communications signal analyzer (CSA) to observe eye patterns.

As shown in Fig. 7 (right), the 200-km-long WDM line consists of two 100-GHz-spacing AWGs, two 100 km spools of single-mode fiber (Corning, SMF-28), and an in-line EDFA with an input isolator. Along with the quantum-noise protected 650 Mbit/s encrypted-data channel, two 10 Gbit/s channels of classical data traffic also propagate through the first 100 km of the described WDM line. Light from two DFB lasers with wavelengths on the 100 GHz ITU grid (1550.1 nm and 1551.7 nm) is mixed on a 3 dB coupler, where one output is terminated and the other enters a 10-GHz-bandwidth fiber-coupled Mach-Zender type LiNbO3 intensity modulator (IM). The IM is driven by an amplified 10 Gbit/s PRBS generated by a BERT with a pattern period of $(2^{15}-1)$ bits. The PRBS-modulated channels (hereafter referred to as PRBS channels) then pass through an EDFA to compensate for losses before entering and being spectrally separated by AWG1. Partial decorrelation of the PRBS channels is achieved by introducing approximately one meter fi-



FIG. 9. Top: Eye pattern and histogram of Bob's decrypted signal after 200 km propagation in the WDM line. Bottom: Eye pattern and histogram of Eve's measurements at the transmitter. Insets, received 1 Mb bitmap file transmissions.

ber length difference (\approx 50 bits) between the channels before combining them into the WDM line with AWG2. On launch (i.e., after AWG2), the optical power is -2 dBm/channel for all three channels.

After propagating through the first 100 km of fiber (20 dB of loss) and the in-line EDFA (23 dB of gain), the channels are separated by AWG3 (3 dB of loss). Either of the two PRBS channels is amplified with a 10 dB gain EDFA and the GVD is partially compensated by a -1530 ps/nm DCM. The amplified, GVD-compensated PRBS channel is detected using an In-Ga-As *p-i-n* TIA receiver (RCVR) and analyzed for errors by the BERT. Note that the reason that the PRBS channels do not propagate through the entire 200 km line is because our DCM only provides enough compensation for 100 km of fiber. Figure 8(a) (left) shows the optical spectrum of the light measured after AWG2 with 0.01-nm resolution bandwidth. The launch power in the quantum channel and in each of the PRBS channels is -1.5 dBm. An eye pattern of the 1550.1 nm PRBS channel at launch is shown in Fig. 8(a) (right). Measuring after AWG2 (i.e., at launch), neither PRBS channel showed any errors in 10 terabits of pseudorandom data communicated. Figure 8(b) (left) shows the optical spectrum (0.01 nm resolution bandwidth) of the light received after the in-line amplifier (100 km of fiber). An eye pattern of the 1550.1 nm PRBS channel, post dispersion compensation, is shown in Fig. 8(b) (right). As in the polarization-mode implementation, the bit-error rate for each of the PRBS channels remained nearly "error-free" at 5 $\times 10^{-11}$ despite the incomplete GVD compensation. Neither the bit-error rates nor the eye patterns of the PRBS channels changed when the quantum channel was turned off.

Figure 9 shows the eye patterns for an encrypted 650 Mbit/s $(2^{15}-1)$ -bit-PRBS and for an encrypted 1-Mbbitmap-file transmission (insets) as measured by Bob (top) and Eve (bottom). In these experiments, Bob is located at the end of the 200-km-long line and Eve is located at the transmitter (Alice). Eve's actions are physically simulated by using Bob's hardware, but starting with an incorrect secret key. While Fig. 9 (bottom) does not explicitly demonstrate Eve's inability to distinguish neighboring coherent states on the phase circle, it does, however, show that a simple bit decision is impossible. The Q factor for Bob's eye pattern of the $(2^{15}-1)$ -bit PRBS, as measured on the CSA, was 12.3.

In all of the time-mode implementation experiments, the coherent states are transmitted using a non-return-to-zero (NRZ) format. The return-to-zero-like appearance of Bob's eye pattern is due to the nonzero rise time of the optical phase modulation. This phenomenon is also observed in traditional NRZ-DPSK systems. The apparent banding of Eve's measurements at the top and bottom of the eye pattern is due to the sinusoidal transfer function of the temporally asymmetric interferometer used for demodulation. Despite this apparent banding, the eavesdropper's probability of error is equal for every transmitted bit. If an eavesdropper were to, say, perform optical heterodyne detection, a uniform distribution of phases would be observed.

In the current setup, the 12-bit D-A conversion allows Alice to generate and transmit 4094 distinct phase states (M=2047 bases). Although we simulate an eavesdropper by placing Bob's equipment at the transmitter, a real eavesdropper would aim to make the best measurements allowed by quantum mechanics (just as in the polarization-mode implementation). The numerical calculation used to plot Fig. 3 (left) shows that for -25 dBm signal power at 650 Mbit/s(\approx 40 000 photons/bit) with M=2047, Eve's maximum obtainable information in an individual attack on the message would be less than 10⁻¹⁵ bits/bit. Under an attack implementing an ideal heterodyne measurement (performed at the output of Alice's transmitter), these values of α^2 and M result in approximately five neighboring states falling within one standard deviation of the Gaussian-distributed measurements noise.

V. DISCUSSION AND SUMMARY

In summary, we have developed schemes towards the cryptographic objective of practical data-encryption by using the fundamental and irreducible quantum-measurement uncertainty of coherent states. Unlike currently deployed deterministic encrypters whose security relies solely on unproven computational complexity, we offer a new quantummechanical vehicle to quantifiable information-theoretic security through high-speed randomized encryption. Furthermore, we have clearly a set of specified security criteria for the cryptographic service of data encryption (which are different from those for key generation) and considered some optimal quantum attacks on our scheme. While we have yet to explicitly determine the level of information-theoretic security provided by our scheme under a general attack (which may correspond to finding λ_1, λ_2 , our scheme does provide a physical layer of quantum-noise randomization that can only enhance the security of a message already encrypted with a traditional deterministic cipher.

Experimentally, we have implemented and demonstrated two high-speed versions of the $\alpha \eta$ data-encryption protocol using both polarization and time modes, and evaluated the schemes' performances through active WDM lines. Whereas the polarization-mode experiments have demonstrated the efficacy of the data-encryption protocol, the polarizationindependent time-mode experiments have demonstrated a technology that is "drop-in" compatible with the existing optical telecommunications infrastructure.

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