## Nonsequential double ionization of  $D_2$  molecules with intense 20-fs pulses

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The kinetic-energy distribution of  $D^+$  fragments obtained from the ionization of  $D_2$  molecules with intense 20-fs pulses includes a high-energy component extending up to  $\sim$  10 eV. These fragments are only present for linearly, or slightly elliptically, polarized light. Both the maximum kinetic-energy and the ellipticity dependence are consistent with nonsequential double ionization caused by recollision.

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Many new strong laser field phenomena, such as bond softening  $[1]$  and zero photon dissociation  $[2]$ , were first identified in  $H_2$  ionization experiments. Two recent papers have measured high-kinetic-energy distribution of the fragment ions produced when  $H_2$  is ionized with a short intense laser pulse  $[3,4]$ . The high energy cutoff of the fragment kinetic-energy approaches (but is a bit less than) the energy expected, if the  $H_2$  ground state wave function were transferred instantly to the double ion. At least some of the fragments come in correlated pairs  $[4]$ .

These new observations are compatible with a number of possible mechanisms.

 $(1)$  The molecule might double ionize instantaneously [5] and Coulomb explode. If so, the kinetic-energy distribution provides information about the correlated electron dynamics in H<sub>2</sub>. It might also be used to measure  $[6,7]$  the vibrational wave function of excited  $H_2$ .

(2) The molecule might ionize sequentially. First  $H_2^+$  is formed. Then those  $H_2^+$  molecules that do not decay by other means (bond softening [1] or enhanced ionization  $[8-10]$ ) ionize again in the remaining part of the pulse  $[3,4]$ .

~3! The high-kinetic-energy fragments might be produced by recollision. If so, the recollision electrons can serve as probes in pump-probe experiments  $[11]$ . We show that the high-kinetic-energy fragments originate from nonsequential double ionization caused by recollision.

Our paper is related to a recent work  $[12]$  in which lower intensity laser pulses were used. In that paper, recollision electrons are identified as the source of the high-energy component in the fragment distribution when  $H_2$  is ionized. However, in that experiment the laser intensity was kept very low to discourage sequential processes. Our intensity is about ten times that in Ref.  $[12]$ , but similar to that used in Ref.  $\lceil 3 \rceil$  and to one of the intensities used in Ref.  $\lceil 4 \rceil$ . Our results show that recollision also remains the dominant mechanism at high intensities in the order of  $10^{15}$  W/cm<sup>2</sup>, which is misinterpreted in Ref.  $\lceil 3 \rceil$  and not mentioned in Ref.  $[4]$ .

Our paper is also related to recent works that identify recollision excitation and double ionization in more complex

We identify recollision by studying the number of energetic fragments as a function of laser ellipticity. Sensitivity to ellipticity of the ionizing laser light is fundamental to all recollision processes [15,16]. First an electron tunnels through the potential modified by the strong linearly polarized laser field, then the electron is driven away from the ion by the field, only to be forced with  $\sim$  50% probability to return after the field reverses its direction. In the electron-ion recollision that might follow, the remaining electrons are collisionally excited or ionized  $[17,18]$ . If the light deviates very much from linear when the electron returns to the ion, it is offset in the lateral direction and it can miss.

Our results only include data for  $D_2$  molecules. That is because, for  $H_2$ , we must subtract background signals originating from  $H<sup>+</sup>$  produced by dissociative ionization of contaminants in the vacuum chamber. However, the observed features were the same for both  $D_2$  and  $H_2$  molecules. In agreement with previous measurements  $[3,4]$ , we observe that the kinetic-energy distribution of  $D^+$  fragments extends continuously up to  $\sim$  10 eV.

We now briefly describe the experimental setup. A fuller description is given elsewhere  $[19,20]$ . A pulsed supersonic beam, formed by expanding  $\sim$  600 Torr of D<sub>2</sub> gas through a 0.5-mm-diameter nozzle, is crossed at 90° by the focused laser beams. The 800-nm 20-fs pulses were generated using a hollow wave guide for spectral broadening and two prisms for chirp compensation  $[21]$ . A 10-cm-focal-length parabolic mirror, placed in the vacuum chamber, focused the laser beam to an intensity  $\sim$  2  $\times$  10<sup>15</sup> W/cm<sup>2</sup>. Since the saturation intensity is  $\sim 10^{15}$  W/cm<sup>2</sup> [22], we can assume that most molecules ionize near that intensity. A zero-order quarterwave plate adjusted the ellipticity.

An electrostatic field accelerated the  $D^+$  ions toward an ion detector positioned on-axis with the molecular beam. The \*Electronic address: hsakai@phys.s.u-tokyo.ac.jp ion detector consists of a microsphere plate backed by a

molecules  $[13,14]$ . By clearly demonstrating double ionization in  $D_2$ , we have identified a simple molecule in which to explore the similarities and differences between double ionization in atoms and in molecules. In addition, working at an intensity of  $10^{15}$  W/cm<sup>2</sup> adds an extra degree of simplification, since any excited state of  $D_2^+$  produced by inelastic scattering will almost immediately ionize.



FIG. 1. A typical image of  $D_2^+$  and  $D^+$  ions. Three different components of fragment ions are observed: (1)  $D_2$ <sup>+</sup> ions appear at the center of the image;  $(2)$  the inner pairs  $(0.3-$  and 1-eV peaks) of ions originate from bond softening, producing  $D^+$ +D; and (3) the outer pair originates from enhanced ionization, producing  $D^+$  $+D^+$ . The image is not Abel inverted.

phosphor screen. A charge-coupled device (CCD) camera recorded the ion image on the phosphor screen. Fast electronic gating of the CCD camera allows us to record mass and charge selected ion images. We used velocity map imaging [23] to achieve good energy resolution.

Figure 1 shows a typical image of  $D_2^+$  and  $D^+$  ions (the image is not Abel inverted  $[23,24]$ . The direction of the laser polarization is shown in the figure. Three distinct components of ion image are observed.

(1)  $D_2$ <sup>+</sup> ions appear at the center of the image. These are the molecules that only ionized once, and did not fragment.

 $(2)$  A pair of D<sup>+</sup> peaks (kinetic-energy 0.3 and 1 eV per fragment) on each side of the  $D_2$ <sup>+</sup> feature forms the next prominent feature. They originate from the dissociation of  $D_2^+$ . These are the well-known bond softening peaks [1].

~3! The broad set of peaks that are the outermost feature in the figure are due to enhanced ionization  $[8-10]$ .

As the  $D_2^+$  begins to dissociate, it enters a region where the ionization rate is greatly enhanced. After ionization,  $D_2^2$ <sup>+</sup> Coulomb explodes, yielding pairs of D<sup>+</sup> ions with kinetic-energy  $\sim$  3 eV/fragment. The ion image shows a strong spatial anisotropy along the polarization direction. Coupling between  $\Sigma_g$  and  $\Sigma_u$  is essential for both bond softening and enhanced ionization.

Not seen in the figure is a diffuse cloud of very high kinetic-energy fragments. Their angular distribution is about twice as broad as the fragments due to enhanced ionization, but integrated over all angles, they make up a significant fraction of the signal.

Figure 2 shows kinetic-energy distributions of  $D^+$  ions obtained by angularly integrating the signals from images such as that in Fig. 1, where the peak intensity was kept constant and the ellipticity  $\varepsilon$  was varied from  $\varepsilon = 0$  (linear polarization) to  $\varepsilon = 1$  (circular polarization). Data for six different ellipticities are included. Concentrating on the linearly



FIG. 2. The relative number of ions plotted as a function of the radial kinetic-energy of  $D^+$  ions. The peak intensity of 2  $\times$ 10<sup>15</sup> W/cm<sup>2</sup> was kept constant and the ellipticity  $\varepsilon$  was varied from  $\varepsilon = 0$  (linear polarization) to  $\varepsilon = 1$  (circular polarization).

polarized results (solid curve), the three peaks that were clearly seen as pairs of peaks (equal energy but oppositely directed) in Fig. 1 are now single peaks in Fig. 2, since each member of the pair had the same energy.

The kinetic-energy calibration of the fragment ions was performed by simulation software. For the horizontal axis of Fig. 2 (and Fig. 4 shown below), we use "radial kineticenergy,'' which corresponds to the projection of the velocity vector onto our two-dimensional ion detector. The real kinetic-energy distribution can only be obtained when the laser polarization is linear, through Abel inversion. For the data recorded with elliptical polarization the lack of cylindrical symmetry prevents Abel inversion. Clearly visible in the figure is a high-energy component extending up to  $\sim$  10 eV. Although our data are uninverted, they agree well with previous observations  $[3,4]$ .

Our concern is less with the kinetic-energy distribution than with the physics that produces it. The high-kineticenergy fragments observed in Fig. 2 and in Refs.  $[3]$  and  $[4]$ can only originate from  $D_2^2$ <sup>+</sup> molecules exploding at small internuclear distances. They extend into the region of direct Coulomb explosion of  $D_2$ , although not up to the maximum kinetic energy expected from Coulomb explosion of  $D_2$ , corresponding to the Coulomb energy at the equilibrium internuclear distance. We first concentrate on the ellipticity dependence seen in Fig. 2, then on the kinetic-energy distribution.

In any recollision event involving such high laser fields, the classical motion of the electron following ionization is important. An electron leaving the molecule with near zero initial energy, moves about a distance  $s \sim 2qE/m\omega^2$  (*E* is the electric field amplitude of the laser pulse at angular frequency  $\omega$ , and  $q$  and  $m$  are the electron's charge and mass, respectively)  $\sim 60$  Å in the direction of the field vector before its motion is reversed. Depending on the phase of birth of the electron, it can recollide with its parent ion with the maximum recollision kinetic-energy of  $3.17m(gE/2m\omega)^2$  $\sim$ 200 eV—enough to knock the remaining electron from  $D_2^+$  (ionization potential is ~30 eV). The electron-impact ionization cross section for  $D_2^+$  ion is more than 1.0



FIG. 3. The relative number of  $D^+$  ions in the 1.6–5 eV range (open circles show enhanced ionization) and  $5-10$  eV range (solid circles show recollision) plotted as a function of the laser ellipticity. All the error bars for enhanced ionization and some for recollision are smaller than the size of their symbols. The peak intensity of 2  $\times$ 10<sup>15</sup> W/cm<sup>2</sup> was kept constant and the signals were normalized to 10 at  $\varepsilon=0$ .

 $\times 10^{-17}$  cm<sup>2</sup> for incident electron energies of 45–345 eV  $\lceil 25 \rceil$ .

A slight ellipticity of the laser light affects the recollision process, offsetting the electron from the ion by  $\sim$  5 $\varepsilon qE/m\omega^2$ , making recollision less probable [16]. Looking closely at Fig. 2, we find that the yield of all channels decreases with ellipticity, but the high-energy component falls rapidly with increasing ellipticity and almost disappears at ellipticity  $\varepsilon = 0.5$ . This is the behavior expected for recollision phenomena. To make the ellipticity dependence clearer, we integrated the  $D^+$  ion signals from 1.6 eV to 5.0 eV and from 5.0 eV to 10 eV and plotted them as a function of ellipticity. The 5-eV limit was determined by referring to the kinetic-energy distributions for linear and circular polarizations with the  $E$ -field magnitude kept constant (see Fig. 4). The result is shown in Fig. 3. The yield in each energy region is normalized to ten at  $\varepsilon = 0$ .

In addition to the sensitivity of recollision to ellipticity, there are three processes that influence the ion yield as a function of ellipticity.

 $(1)$  The maximum electric field falls as the ellipticity increases. In the tunneling regime, the ion yield follows the maximum electric field. Therefore, the yield should decrease as well. In Fig. 2, the yield of all components decreases with increasing ellipticity. However, the high-energy peak decreases more quickly, as shown in Fig. 3.

 $(2)$  We change the ellipticity by rotating a quarter-wave plate. This rotates the major axis of the ellipse by the same angle that the wave plate rotates. The projection of the kinetic-energy distribution of all fragments is affected. Based on the shifts of the peaks due to enhanced ionization, we can estimate the effect of the rotation of major axis to be  $\sim$ 0.3 eV. Since the high-kinetic-energy component ranges from  $\sim$  5 eV to  $\sim$  10 eV and is broader than other components, it is reasonable to think that it is less affected by the small shift of  $\sim$  0.3 eV.

(3) It is possible that  $D_2$ , or more likely  $D_2^+$ , aligns to



FIG. 4. The relative number of ions plotted as a function of the radial kinetic-energy of  $D^+$  ions for linear polarization (solid curve) and circular polarization (dotted curve). The same laser field was used for these measurements. The peak intensities were 2  $\times 10^{15}$  W/cm<sup>2</sup> for linear polarization and  $4\times 10^{15}$  W/cm<sup>2</sup> for circular polarization.

the laser field at least to some extent. If it does, then the alignment might decrease as the ellipticity increases. If it does not, then those effects that depend on the alignment of the molecule to the field will become more important with  $circular$  polarization  $[26]$ . By studying yields using linear and circular polarized light  $[26]$ , we will show below that neither  $D_2$  nor  $D_2^+$  aligns.

None of the effects described above can influence the results for small ellipticities since the field strength along the major axis hardly changes. The high-kinetic-energy fragment signal has fallen to less than 40% of the peak value and the cutoff energy is almost unchanged for an ellipticity of 0.25. By ellipticity  $\sim 0.5$ , where the electric field  $\sim 89\%$  of its maximum value, the high-energy component is almost unobservable. The only mechanism compatible with such strong ellipticity dependence is recollision.

We now confirm this interpretation by comparing the kinetic-energy distributions of  $D^+$  ions for linear and circular polarizations where the field amplitude is kept constant. Keeping the field constant eliminates the influence of the first two processes mentioned above and allows us to evaluate the third process. Concerning the first two processes one can say the following.

 $(1)$  Since the ionization rate depends on the field strength in the tunneling regime  $[27]$ , the ionization rate should be essentially the same if the field is the same.

(2) With circular polarization, the polarization becomes parallel to the detector surface twice in an optical period. The cutoff kinetic-energy comes from those molecules that are aligned parallel to the detector plane irrespective of the polarization.

Combining these two facts, the effect caused by rotation of the major axis in Fig. 2 can be completely eliminated.

The result is shown in Fig. 4, where the peak intensity was  $2 \times 10^{15}$  W/cm<sup>2</sup> for linear polarization and thus 4  $\times$ 10<sup>15</sup> W/cm<sup>2</sup> for circular polarization. It can be seen that the enhanced ionization yield (the number of  $D^+$  ions) for circularly polarized light increases by a factor of 3.8 compared to that for linearly polarized light. This shows that

there is little dynamic alignment of  $D_2$  and/or  $D_2^+$  [26]. This conclusion is consistent with our numerical simulations where the dynamic alignment of  $D_2$  and  $D_2$ <sup>+</sup> has been studied by solving the time-dependent Schrödinger equation. In contrast to the increased strength of the enhanced ionization peak, the high-kinetic-energy fragments are not observable with the circular polarization used, as expected for any recollision process [15]. A recent experimental study, with  $H_2^+$ ions as the target  $[28,29]$ , suggests that the neutral parent plays an important precursor role in the laser-induced fragmentation dynamics of  $H_2$ , corroborating the present results and considerations.

Before concluding, it is important to show how recollision can be responsible for the high-kinetic-energy fragments that we, and others  $[3,4]$  observe. Nonsequential double ionization is really a ''sub-laser-cycle'' process. Following single ionization, the newly ionized electron is pulled away from the ion, only to be driven back. The typical time required before the electron makes its first attempt at recollision is  $\sim$  2/3 of a laser period. During this time, the D<sub>2</sub><sup>+</sup> wave packet is able to move a bit. If the electron recollides with sufficient energy, it can excite the molecule to any of the numerous states, or further ionize the singly charged molecular ion by inelastic scattering. Consistent with our observations, the high-energy cutoff of the fragment kinetic-energy distribution will be slightly lower than that observed for true Coulomb explosion. We refer the reader to Ref.  $|12|$  for a detailed calculation.

In addition, Coulomb focusing and non-hard-sphere collisions  $[17,18]$  provide the electron wave packet with significant probability of subsequent recollisions. These occur in the few laser cycles following ionization  $[17]$  and will contribute lower-energy deuterons to the spectrum. In Ref.  $|12|$ this dynamics is measured at low intensity. Our measurements of the kinetic-energy spectrum of the  $D^+$  ions indirectly measure this dynamics at high intensity in the order of  $10^{15}$  W/cm<sup>2</sup>.

In summary, the kinetic-energy distributions of  $D^+$  fragments obtained from the Coulomb explosion of  $D_2$  molecules with intense 20-fs pulses included a fractional contribution with a high kinetic-energy extending up to  $\sim$  10 eV. All our results are consistent with the interpretation that the energetic  $D^+$  fragments are caused by nonsequential double ionization caused by recollision. We expect similar behavior for any two-electron dimer, for example  $Na<sub>2</sub>$ . Ionization can be controlled to allow only a small range of times for recollision  $[30]$ . Thus, the recollision electron can excite the ion at a well-defined (short) time after ionization. Coulomb explosion then images the nuclear position.

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