# **Emission of singly and doubly charged light fragments from**  $C_{60}^{r+1}$  ( $r=4-9$ ) **in Xe**<sup>25+</sup> •  $C_{60}$  collisions

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Asymmetrical fission of  $C_{60}^{r+}$  ( $r=4-9$ ) ions are studied in Xe<sup>25+</sup>-C<sub>60</sub> collisions at 100 keV impact energy ( $v \approx 0.18$  a.u.). The branching ratios for the emission of a singly or a doubly charged light fragment,  $C_m^+$  or  $C_m^2$ , are measured for each initial charge state *r*. The measured *m*-dependent branching ratios for the singly charged  $C_m^+$  fragment emission channels are reproduced using a simple statistical model. The ionization energies  $I(C_{60-2n}^{q+})$  for even numbered fullerenes  $C_{60-2n}^{q+}(q=1-5, 8; n=1-4)$  and  $I(C_{2n}^{+})$  for singly charged light fragments  $C_{2n}$ <sup>+</sup> ( $n=1-4$ ) are estimated by the density-functional theory. The total branching ratio for the  $C_m^2$ <sup>+</sup> emission channels is found to increase from less than 2 to 25% when the charge *r* of the parent ion  $C_{60}^{r+}$  increases from 5 to 9.

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### **I. INTRODUCTION**

Fragmentation of highly charged clusters exhibits a rich complexity of dissociation channels and a large variety of dynamical processes  $[1-4]$ . C<sub>60</sub> fullerene is a highly stable system with strong bonds and constitutes an interesting case to study the fragmentation of clusters with large charge state  $[5-7]$ . Many experiments aimed at the observation of the coupling between the electronic excitation and vibronic degrees of freedom have been devoted to  $C_{60}$  molecules using laser excitation [8]. For ultrashort pulse duration ( $\sim$  femtoseconds), the ionization mechanism is a direct multiphoton ionization process, whereas for longer pulse duration (picoseconds), the coupling to the vibration occurs during the laser excitation time, and the fragmentation processes are observed. In collisions between highly charged ions (HCI) and  $C_{60}$  at low velocities ( $v \approx 0$ , 1 a.u.), the interaction time is very short (a few femtoseconds). Highly charged stable  $C_{60}^{r+}$  with *r* up to 10 can be produced by electron transfer from the  $C_{60}$  to the HCI at large impact parameters without excitation of the  $C_{60}$  molecules [9,10]. These processes are, to some extent, comparable to the ultrashort laser pulse excitations. However, for collisions at small impact parameters, the  $C_{60}$  molecules are not only ionized but also heated.

The excitation mechanism in these short-distance collisions is still a matter of discussion. In collisions with singly charged projectiles at impact parameters smaller than the size of  $C_{60}$ , nuclear and electronic stopping power produces hot  $C_{60}$  molecules undergoing asymmetrical fragmentation and multifragmentation [11]. In collisions with highly charged projectiles, only a small part of hot  $C_{60}$  molecules is related to rontal collisions. It is therefore necessary to propose another excitation mechanism for hot  $C_{60}^{r+}$  issued from outside  $C_{60}$  cage collisions. For impact parameters slightly larger than the size of the  $C_{60}$ , a large number of electrons are transferred simultaneously to the projectile at small interaction distances, leading to a sudden screening of the projectile nuclear charge. Fast energy rearrangement between the captured electrons occurs during the interaction time, and several electrons can occupy highly excited Rydberg states. These loosely bound electrons can be recaptured by the charged  $C_{60}$  in highly excited states, leading to a strong electronic excitation of the  $C_{60}$  molecule. A similar target excitation process via electron recapture in the preceding part of the collision has been already suggested in HCI-atom collisions to explain the Rydberg transition lines of the target  $[12]$ .

In collision experiments, the excitation energy of the target  $C_{60}^{r+}$  depends notably on the initial charge, core size, and collision velocity of the projectile as shown in several experiments devoted to excitation studies  $[13-15]$ . For a given  $C_{60}^{r+}$  charge state, lower excitation energy is obtained using projectiles with higher charge states and at higher velocities. In the  $Xe^{30+} + C_{60}$  collisions at 300 keV (*v*  $=0.3$  a.u.), the fragmentation ratio, i.e., the number of unstable  $C_{60}^{\prime\prime}$ <sup>+</sup> divided by the summation of the numbers of stable and unstable  $C_{60}^{\prime\prime}$ <sup>+</sup>, has been measured to be about 5% [7] for  $C_{60}^{4+}$  ions. Larger fragmentation ratio for the same ions  $C_{60}^{4+}$  has been measured to be about 50% in collisions with a projectile at lower charge state  $Ar^{8+} + C_{60}$  at 56 keV  $(v=0.24$  a.u.).

Other important factors that determine the fragmentation pattern are the charge state and the size of the cluster. In our previous experiments using  $Ar^{8+} + C_{60}$  collisions, detailed information concerning the asymmetrical fission of  $C_{60}^{3+}$ ,  $C_{60}^{4+}$ , and  $C_{60}^{5+}$  has been obtained by correlation measurements of the charged fragments. For  $C_{60}^{3+}$  parent ions, the evaporation of  $C_2$  is dominant while for  $C_6^{\phantom{5}5^+}$ , the asymmetrical fission is the major process. For  $C_{60}^{4+}$ , a competition between the evaporation and fission channels is observed [13] and the emissions of  $C_2^+$ ,  $C_4^+$ ,  $C_6^+$ , and  $C_8^+$ have been measured in coincidence with  $C_{58}^{3+}$ ,  $C_{56}^{3+}$ ,  $C_{54}^{3+}$ , and  $C_{52}^{3+}$  fullerene ions, respectively [16]. These singly charged light fragments are attributed to the loss of  $C_n^+$  chains from the  $C_{60}^{\prime\prime}$  cage via the so-called "unzipping'' mechanism. The odd-numbered light fragments, such as  $C^+$ ,  $C_3^+$ ,  $C_5^+$ , have been observed in coincidence with  $C_{58}^{3+}$ ,  $C_{56}^{3+}$ , and  $C_{54}^{3+}$  ions, respectively, showing that a

neutral carbon atom was also emitted. For the parent ions  $C_{60}^{5+}$  [17], events with three charged fragments C<sup>+</sup>, C<sub>3</sub><sup>+</sup>, and  $C_{56}^{3+}$  have been observed. The velocity correlation analysis of  $C^+$  and  $C_3^+$  shows that the two light fragments are emitted sequentially with an extremely short lifetime in the intermediate odd-numbered fullerene states  $C_{59}^{4+}$  or  $C_{57}^{4+}$ . This observation gives a tentative explanation why the odd-numbered fullerenes have been rarely observed in the TOF spectrum in fragmentation experiments. The emission of a doubly charged light fragment from a  $C_{60}^{5+}$  parent ion in the channels  $C_{60}^{5+} \rightarrow C_{60-m}^{3+} + C_m^{2+}$  has been also observed in  $Ar^{8+}-C_{60}$  collisions [18]. The population distribution of these channels has been measured as a function of the number *m* of carbon atoms of the light fragment  $C_m^2$ <sup>+</sup> ( $m=6-12$ ). A maximum has been found around  $m=8$ showing a shift towards higher mass compared to the *m* distribution of singly charged light fragments  $C_m^+$  in channels  $C_{60}^{5+} \rightarrow C_{60-m}^{4+}+C_m^+$ , for which the maximum is around  $m=2$ . This observation is in good agreement with a simple fission barrier analysis  $[4,18]$ .

Using projectiles at higher charge states, highly charged  $C_{60}^{r+}$  ions can be prepared. In  $Xe^{30+}$ -C<sub>60</sub> collisions, the fragmentation ratio and the branching ratios between  $C_2$ evaporation, asymmetrical fission, and multifragmentation processes have been measured as a function of the charge of  $C_{60}^{r+}$ , with *r* up to 9 [7]. In the present work, we report on the *m*-dependent relative branching ratios of  $C_m^+$  and  $C_m^2$ <sup>+</sup> light-fragment emission from asymmetrical fission of  $C_{60}^{\prime\prime}$ <sup>+</sup>  $(r=4-9)$  in Xe<sup>25+</sup>-C<sub>60</sub> collisions. The experimental data are compared with theoretical distributions obtained using a statistical model. To estimate the fission barrier for each reaction channel, the ionization energies  $I(C_{60-2n}^{q+})$  for the ionization reaction  $C_{60-2n}^{(q-1)+} \to C_{60-2n}^{q^2} + e^-$  (*q*  $=1-8$ ;  $n=1-4$ ) and  $I(C_{2n}^+)$  for  $C_{2n}^-\rightarrow C_{2n}^+ + e^-$  (*n*  $=1-4$ ) have been calculated using the density-functional theory (DFT) for the most stable isomers of the fullerenes and the  $C_{2n}$  chains, respectively.

## **II. EXPERIMENT**

The experimental setup [7] is presented in Fig. 1.  $Xe^{25+}$ projectile ions delivered by the ECR at AIM in Grenoble are accelerated to 100 keV and intercepted perpendicularly by a beam of  $C_{60}$  molecules. The outgoing projectiles  $Xe^{23+}$ , on which two captured electrons are stabilized  $(s=2)$ , are selected by an electrostatic analyzer in order to get a maximum initial population on  $C_{60}^{r+}$  ( $r=3-9$ ) parent ions (see Ref. [7], Fig. 4). Ejected electrons and charged  $C_{60}$  or fragments are extracted from the interaction region by a transverse electric field of 1 kV/cm. Electrons are accelerated towards a semiconductor detector (PIPS Canberra) polarized at 25 kV. The electron collection efficiency is optimized using an intermediate focusing electrode, and is estimated here to be 89%. The signal of the detector PIPS amplified and sent to an analog-digital converter (AD 811 Ortec) for pulse-height analysis therefore provides the information on the number *n* of emitted electrons in the collision.

On the other side of the extraction region, recoil ions are accelerated over a distance of 1 cm by an electric field of 2



FIG. 1. Experimental setup.

kV/cm, and sent through a time-of-flight (TOF) tube ( $\ell$  $=$  32 cm) to a detector composed of two multichannel plates (MCP). In order to increase the detection efficiency, the ions are postaccelerated towards the first MCP polarized at about  $-5$  kV. Behind the second MCP (5 mm), multianodes of 61 pixels  $(4.8 \text{ mm}^2 \text{ per pixel})$  are linked to 61 individual discriminators  $(2735 \text{ DC } \text{Lecroy})$ . The 61 signals are sent to two multihit  $32$ -channel time digital converters  $(TDC)$   $(3377)$ Lecroy). Under these experimental conditions, the detection efficiency of recoil ions is estimated to be 75% for singly charged fragments  $C_m^+$  ( $m=1-11$ ). Discriminator levels for signals from multianodes are set to get a balance between a good detection efficiency and a low probability for a singly charged light fragment to activate more than one neighboring anode. The relative probabilities for an ion  $C_m^+$  (*m*  $=1-11$ ) to activate one, two, and three anodes are measured to be 0.72, 0.22, and 0.06. On the contrary, for highly charged fullerene ions  $C_{60-2n}r^+$  ( $r>4$ ), the probability to activate three anodes is found maximum. This information is useful to differentiate two ions with the same mass over charge ratio for which the lines on a TOF spectrum are mixed, as for example, the stable  $C_{60}^{6+}$  and the singly charged fragment  $C_{10}$ <sup>+</sup> issued from multifragmentation process.

Multicoincidence measurements are performed in eventby-event mode and all data are recorded in list mode. The delayed  $Xe^{23+}$  ( $s=2$ ) outgoing projectile ion signal is used as trigger for the AD converter of the electron signal, and provides a common stop signal to the two units of TDC. The amplitude of the electron signal, the hit times on each pixel of the multianodes, and the pixel channels (spatial positions) activated in each event are recorded. From the electron number conservation law, the charge of the target  $C_{60}^{\prime\prime}$ <sup>+</sup> after the collision can be estimated by  $r=n+s$  (in fact,  $r=n+2$  with  $s=2$ ). Measurements under identical conditions were performed during 20 h with a flux of about 300 events per sec.



FIG. 2. Correlated two-fragment recoil ion (RI-RI) spectrum. Horizontal axis: the TOF of the heavy fragment; vertical axis: the TOF of the correlated light fragment. The activated pixel number associated with the heavy fragment is selected to be higher or equal to 3 to ensure the detection of a multiply charged fullerence.

#### **III. DATA ANALYSIS**

Figure 2 shows a two-dimensional  $(2D)$  spectrum of recoil ions (RI, RI) corresponding to events with two charged fragments. One of them is a multiply charged fullerene and the other one is a light fragment. The TOF  $(t_1)$  of the last detected fragment (the heavier one) is plotted along the horizontal axis, and the TOF  $(t_2)$  of the correlated light fragment along the vertical axis. Note that the TOF scales are reversed due to the common STOP data-acquisition mode of the TDC. The number *n* of detected electrons is selected in the range from 1 to 8, so that the charge *r* of the parent ions  $C_{60}^{r+1}$  is ranged from 3 to 10. The detection of a multiply charged fullerene ion in an asymmetrical fission process is assured by the selection of events for which at least three neighboring pixels were activated by the heavy fragment. The main spots  $(C_{60-m}^{q+1}$ -C<sub>m</sub><sup>+</sup>,  $q=3-8$ ,  $m=2, 4, 6, 8$ ) are characterized by the total number of carbon atoms on the two fragments, equal to 60. They are unambiguously attributed to the fission channels  $C_{60}^{r^+}\rightarrow C_{60-m}^{q^+}+C_m^{r^+}$   $(r=q+1=4-9; m$  $=$  2, 4, 6, 8), and the associated populations are given in the Table I. The long oblique tails that prolong the spots towards shorter flight time of  $\overline{C}_{60-m}q^+$  and longer flight time of  $\overline{C_m}^+$ are due to the delayed fission of  $C_{60}^{r+}$  ions all along the path<br>between the extraction grids. Other spots extraction grids. Other spots  $(C_{60-m}^{q+1}$ -C<sub>m'</sub><sup>+</sup>;  $m>m'$ ) with a total number of carbon atoms smaller than 60 are also observed in Fig. 2. Each of them cannot be associated to a fission channel unambiguously. For instance, two fission channels can be attributed to the spot  $(C_{58}^{4+}-C^+), C_{60}^{6+} \rightarrow C_{58}^{4+}+C_2^{2+},$  and  $C_{60}^{6+}$  $-C_{58}^{4+}+C^+ + C^+$  (when only one of the two C<sup>+</sup> fragments is detected in the last case). The possible contribution of another channel with a parent quintuply charged ion  $C_{60}^{5+}$ ,  $C_{60}^{5+} \rightarrow C_{58}^{4+} + C^+ + C$  is excluded by analyzing the tail of the spot  $(C_{58}^{4+}$ -C<sup>+</sup>). It is notable that the slope of this spot is very different from that of the spot  $(C_{58}^{4+}$ - $C_2^{\{+\}})$ , which is attributed to the fission of  $C_{60}^{5+}$  without doubt. In a delayed fission process, the slope of the tail depends sensitively on the charge difference between the parent ion and the fullerene fragment. A larger angle with respect to the vertical axis as shown by the spot  $(C^{4+}-C^+)$  compared to the spot  $(C_{58}^{4+}$ - $C_2^+$ ) is the typical signature of a fullerene ion  $C_{58}^{4+}$ carried at the beginning of the extraction field by a parent ion with two more charge units  $C_{60}^{6+}$ . The decay of  $C_{60}^{6+}$  to  $C_{58}^{4+}$  is possible by the loss of a doubly charged fragment  $C_2^2$ <sup>+</sup> or by the quasisimultaneous emission of two C<sup>+</sup> fragments [17]. This analysis is available for all other spots  $(C_{58}^{q+}, C^+)$  with  $q>4$ .

TABLE I. Event number counts of the spots  $(C_{60-m}^{(r-1)+} - C_m^{+})$ ,  $(C_{60-m}^{(r-2)+} - C_m^{2+})$ , and  $(C_{60-m}^{(r-2)+} - C_m^{+} - C_m^{+})$  measured in two-fragment or three-fragment (RI-RI) correlated spectra and the relative branching ratios  $R_b$  for the associated asymmetrical fission channels. The charge *r* of the parent ions  $C_{60}^{r+}$  ranges from  $r=4$  to 9.

	$C_{60}^{4+}$		$C_{60}^{5+}$		$C_{60}^{6+}$		$C_{60}^{\ 7+}$		$C_{60}^{8+}$		$C_{60}^{9+}$	
Fission channels	Counts	$R_b$	Counts	$R_b$	Counts	$R_b$	Counts	$R_b$	Counts	$R_h$	Counts	$R_h$
$C_{58}^{r-1}$ + $C_2^+$	1243	0.335	7582	0.501	8212	0.527	4118	0.582	922	0.572	208	0.451
$C_{56}^{\ r-1}+C_4^{\ +}$	1659	0.447	3983	0.263	3197	0.205	929	0.131	62	0.038		0.000
$C_{54}^{\ r-1}+C_6^{\ +}$	307	0.082	809	0.053	444	0.028						0.000
$C_{52}^{\ r-1}+C_8^{\ +}$	156	0.042	188	0.012								0.000
$C_{58}^{\ r-2}+C_2^{\ 2+}$			18	0.001	363	0.023	325	0.046	122	0.076	90	0.195
$C_{56}^{\ r-2} + C_4^{\ 2+}$			78	0.005	255	0.016	229	0.032	160	0.099	32	0.070
$C_{54}^{r-2}+C_6^{2+}$			53	0.003	342	0.022	182	0.026				
$C_{52}^{\ r-2}+C_8^{\ 2+}$			63	0.004	354	0.023	119	0.017				
$C_{58}^{r-1}$ + $C^{+}$ + $C^{0}$	60	0.016	275	0.020								
$C_{56}^{\ r-1} + C_3^{\ r} + C_0^{\ 0}$	224	0.060	214	0.015								
$C_{54}^{r-1}$ + $C_5^{+}$ + $C_0^{0}$	59	0.015	86	0.006								
$C_{58}^{r-2} + C^+ C^+$			175	0.012	1071	0.069	715	0.101	206	0.133	130	0.284
$C_{56}^{r-2}+C_3^+$ + $C^+$			456	0.030	1347	0.086	392	0.056	131	0.085		
$C_{54}^{r-2}+C_3^+$ + $C_3^+$							66	0.009				



FIG. 3. (a) Electron number spectrum recorded in coincidence with  $Xe^{23+}$  outgoing projectiles. (b) Electron number spectrum for events with  $n=4$  ejected electrons, recorded in coincidence with  $Xe^{23+}$  ( $s=2$ ) and stable  $C_{60}^{6+}$  recoil ions.  $\circ$ , experimental data; continuous line, fit. The  $n=1, 2, 3$  peaks are due to the backscattered electron effect and the electron collection efficiency less than 100%. The fit allows us to estimate the electron collection efficiency to be about 89%.

In order to differentiate fragmentation channels issued from different parent ions  $C_{60}^{r+}$ , a straight way is to determine the initial charge  $r+$  by analyzing the number of ejected electrons. In Fig.  $3(a)$ , we present the electron number spectrum for all events, and in Fig.  $3(b)$  we present the  $n=4$  electron number spectrum. Events involving four ejected electrons are characterized by the detection of a stable  $C_{60}^{6+}$  ion. With  $r=6$ ,  $s=2$ , one obtains  $n=r-s=4$ . In Fig.  $3(b)$ , the one-, two-, and three-electron peaks are interpreted by the well-known backscattered electron effect of the electron detector PIPS and by a limited electron collection detection efficiency  $[19]$ . To reproduce precisely the measured four-electron spectrum, we have adjusted the electron collection detection efficiency and the backscattering probability to be 89% and 16%, respectively. Therefore, a peak in Fig. 3(a), for example  $n=3$ , is not only attributed to events where three electrons are ejected; it is also partially attributed to events where four, five, or more electrons are actually ejected. Two-fragment spectra of (RI, RI) similar to Fig. 2 are recorded for each selected electron number peak of Fig. 3(a). The obtained  $(RI, RI)$  spectrum for a given peak *n* is then contributed by the asymmetrical fission of the parent ions  $C_{60}^{r+}$  with mainly  $r=n+2$  and partially  $r>n+2$ .

A typical two-fragment (RI, RI) spectrum for a selected electron number peak,  $n=6$  ( $r=8$ ), is shown in Fig. 4. Three spots,  $(C_{58}^{7+} - C_2^+)$ ,  $(C_{58}^{6+} - C^+)$ , and  $(C_{56}^{6+} - C_2^+)$ , are attributed to the  $C_{60}^{8+}$  parent ions. The spot  $(C_{58}^{7+} - C_2^+)$  corresponds to the main fission channel  $C_{60}^{8+} \rightarrow C_{58}^{7+} + C_2^+$ . The spots  $(C_{58}^{6+} - C^+)$  or  $(C_{56}^{6+}$ - $C_2^{+})$  are attributed principally to the emission of a doubly charged fragment  $C_2^{2+}$  or  $C_4^{2+}$ , and partially to the



FIG. 4. Correlated two-fragment (RI-RI) spectrum associated with the  $n=6$  peak of the electron number spectrum, Fig. 3(a). The main spots  $(C_{58}^{7+} - C_2^+)$ ,  $(C_{58}^{6+} - C_1^+)$ , and  $(C_{56}^{6+} - C_2^+)$  are attributed to the parents  $C_{60}^{8+}$ . Contributions of parent ions at the higher charge state  $C_{60}^{9+}$  are also observed.

channels with the emission of two  $C^+$  fragments or two  $C_2^+$ fragments when only one of them is detected. The quasiabsence of the spot  $(C_{56}^{7+} - C_2^{+})$  shows that the channel  $C_{60}^{8+} \rightarrow C_{56}^{7+} + C_2^{+} + C_2$  can be neglected. It is in good agreement with the previous finding that the emission of a neutral fragment is negligible for fullerenes with a charge higher than 4 [13]. The spots  $(C_{58}^{8+} - C_2^{4})$  and  $(C_{58}^{7+} - C_1^{4})$ are attributed to channels of the  $C_{60}^{9+}$  parent ions,  $C_{60}^{9+}$  $\rightarrow C_{58}^{8}$ <sup>8+</sup> + C<sub>2</sub><sup>+</sup>, C<sub>6</sub><sup>9+</sup>  $\rightarrow$ C<sub>58</sub><sup>7+</sup> + C<sub>2</sub><sup>2+</sup>, and C<sub>6</sub><sup>9+</sup>  $\rightarrow$ C<sub>58</sub><sup>7+</sup>  $+C^+ + C^+$  (when only one  $C^+$  fragment is detected). Other weak spots like  $(C_{58}^{6+}, C_2^+)$  and  $(C_{58}^{5+} + C_2^+)$  are contributed by the parent ions  $C_{60}^{r+}$  at lower charge state *r*  $=7$  and 6. It is due to the one or two additional random electrons issued from double collision process. To get pure (RI-RI) spectra associated to each well-defined parent ion  $C_{60}^{r+}$ , the analysis began from the (RI-RI) spectrum of the highest charge state  $C_{60}^{9+}$  (*n*=7) which is practically pure (the fission of  $C_{60}^{10+}$  is not observed). The pure (RI-RI) spectrum of the parent ion  $C_{60}^{8+}$  is obtained by the (RI-RI) spectrum of the peak  $n=6$  subtracting the contribution of the spectrum of  $C_{60}^{9+}$ . The pure (RI-RI) spectrum of the parent ion  $C_{60}^{\pi}$ <sup>7+</sup> is obtained by the (RI-RI) spectrum of the peak  $n=5$  subtracting the contribution of the spectrum of  $C_{60}^{9+}$ and then that of the corrected spectrum of  $C_{60}^{8+}$ , etc.

The populations of three-fragment channels with the quasisimultaneous emissions of two odd-numbered fragments such as  $C_{60}^{r+} \rightarrow C_{58}^{(r-2)+}+C^{+}+C^{+}$ ,  $C_{60}^{r+} \rightarrow C_{56}^{(r-2)+}$  $+C^+ + C_3^+$ , and  $C_{60}^{\prime\prime}$ <sup>+</sup>  $\rightarrow$   $C_{54}^{\prime\prime}$ <sup>(r-2)+</sup> +  $C_3^{\prime}$ +  $C_3^+$ ; and the successive emission of two even numbered fragments, such as  $C_{60}^{r^+} \rightarrow C_{56}^{(r-2)+} + C_2^{+} + C_2^{+}$ , are obtained from another type of 2D (RI, RI) spectrum showing the correlation between the two light fragments. An example is presented in Fig. 5, which shows a spectrum recorded by selecting events associated to a given electron number peak  $n=5$ , and characterized by the detection of a fullerene fragment  $C_{56}^{5+}$ . The TOF of the two light fragments are plotted in the 2D spec-



FIG. 5. Correlated three-fragment (RI-RI) spectrum between the two light fragments in coincidence with the selected heavy  $C_{56}^{5+}$ ions and the ejected electron number  $n=5$ . The main spots  $(C^{\dagger}$ -C<sub>3</sub><sup>+</sup>) and  $(C_2^{\dagger}$ -C<sub>2</sub><sup>+</sup>) are attributed to the reactions C<sub>60</sub><sup>7+</sup>  $\rightarrow C_{56}^{5+}+C^6+C_3^+$  and  $C_{60}^{7+}\rightarrow C_{56}^{5+}+C_2^+$  +  $C_2^+$ , respectively.

trum. The TOF of the heavier one is plotted along the horizontal axis and that of the lighter one along the vertical axis. From the spots  $(C_1^+, C_3^+)$  and  $(C_2^+, C_2^-)$ , we measured the populations of the corresponding channels  $C_{60}^{7+} \rightarrow C_{56}^{5+} + C^+ + C_3^+$  and  $C_{60}^{7+} \rightarrow C_{56}^{5+} + C_2^+ + C_2^+$ . Similar 2D spectra are recorded for  $n=5$ , in coincidence with the detection of a  $C_{58}^{5+}$  or a  $C_{54}^{5+}$ , respectively. The spots  $(C^+, C^+)$  and  $(C_3^+, C_3^+)$  on the two spectra allowed us to measure the populations of the other two channels,  $C_{60}^{7+} \rightarrow C_{58}^{5+} + C^+ + C^+$  or  $C_{60}^{7+} \rightarrow C_{54}^{5+} + C_3^+ + C_3^+$ . The contribution of these three-fragment channels in the two-fragment (RI, RI) spectrum is corrected using the detection efficiency of the monocharged fragments  $[18]$ . This correction allows us to determine the populations of the asymmetrical fission channels involving a doubly charged light fragment,  $C_{60}^{r^+} \rightarrow C_{60-m}^{(r-2)+} + C_m^{2+}$ .

#### **IV. RESULTS AND DISCUSSION**

The measured relative branching ratios of different fission channels  $R_b$  for parent ions  $C_{60}^{r+}$  with *r* ranging from 4 to 9 are presented in Table I. The dominant asymmetrical fission channels for all studied parent ions  $C_{60}^{r+}$  are the singly charged light-fragment emissions. The relative branching ratio as a function of the number *m* of carbon atoms on the light fragment  $C_m^+$  is presented in Fig. 6 for each charge state of the parent  $C_{60}^{r+}$ . Only data for even-numbered fragments and for the  $C^+$  fragment are considered, because the contributions of other odd-numbered fragments are very small. Difficulties arise in the determination of the population for the channels  $C_{60}^{r^+} \rightarrow C_{59}^{(r-1)+}+C^+$ . The emission of a  $C^+$  fragment from a  $C_{60}^{r+}$  parent ion is followed by a fast sequential emission of another odd-numbered charged fragment  $C^+$  or  $C_3^+$  leading to a contribution to the measured populations of the channels  $C_{60}^{r^+} \rightarrow C_{58}^{(r-2)+} + C^+$ 



FIG. 6. Relative branching ratios for the asymmetrical fission channels  $C_{60}^{r+} \rightarrow C_{60-m}^{(r-1)+} + C_m^{r+}$  as a function of the number of carbon atoms *m* on the light fragment. To guide the eyes, the data for each parent charge state  $C_{60}^{r+}$ ,  $4 \le r \le 9$ , are connected with a line and the associated charge  $r+$  is indicated.

+ C<sup>+</sup> or  $C_{60}^{r+} \rightarrow C_{56}^{r-2} + C^+ + C_3^+$ . However, the measured population of the last channel is partially contributed by another fission path,  $C_{60}^{r+} \rightarrow C_{57}^{(r-1)+} + C_3^+ \rightarrow C_{56}^{(r-2)+}$  $+C^+ + C_3^+$ , where the  $C_3^+$  fragment is lost at the first step. The relative contributions of these two paths can be estimated by analyzing the kinetic energy of the light fragment, which depends on the charge of its fission partner. If  $C^+$  is ejected at the first step, the Coulomb repulsion between  $C_{59}^{(r-1)+}$  and C<sup>+</sup> is higher than that between  $C_{56}^{(r-2)+}$  and  $C^+$  when it is ejected at the second step. For parent ions  $C_{60}^{5+}$ , the contributions of the two paths have been estimated to have equal probabilities  $[17]$ . In this study, we assume roughly that the contribution of the path where the  $C^+$ is ejected at the first step increases linearly from 50% to 90% as the charge of the parent ion  $C_{60}^{r+}$  varies from 5 to 8. For the  $C_{60}^{8+}$  parent ions, the emission of C<sup>+</sup> is dominant over that of  $C_3^+$ . A population shift towards lighter fragments  $C^+$ and  $C_2^+$  is noted as the charge of the parent  $C_{60}^{\prime\prime}$ <sup>+</sup> increases. The same shift is remarkable from Table I for doubly charged light fragments.

In order to reproduce theoretically the relative population distribution as a function of *m* of the singly charged light fragment  $C_m^+$  for each  $C_{60}^{r+}$  ion ( $r=4-9$ ), a statistical model based on the Rice, Ramsperger, and Kassel theory is employed [20,13]. We consider a fullerene ion  $C_{60}^{r+}$  with internal energy  $\epsilon$  which is statistically distributed among all vibrational modes. A fission channel is opened as long as a critical energy higher than the inner part of the associated fission barrier *B* is accumulated in at least one vibrational mode. The relative branching ratio of such a fission channel is then estimated as proportional to  $(1-B/\epsilon)^{3p-7}$ , with *p*  $=60$  for C<sub>60</sub>. The fission barrier *B* for each reaction channel  $C_{60}^{r^+} \rightarrow C_{60-m}^{(r-1)+} + C_m^{+}$  is obtained by summing up the

energy change  $\Delta_m^r$  of the reaction and the outer part of the barrier  $B'_{m}$ <sup>r</sup> due to the Coulomb repulsion between the two fission partners. The energy change  $\Delta_m^r$  is calculated as following:

$$
\Delta_m^{\prime\prime} = E_{\text{at}}(C_{60}) - V_{\text{ion}}^{(r)'}(C_{60}) - [E_{\text{at}}(C_{60-m}) - V_{\text{ion}}^{r'-1}(C_{60-m}) + E_{\text{at}}(C_m) - V_{\text{ion}}^{(1)}(C_m)],
$$
\n(1)

where  $E_{at}(C_p)$  stands for the atomization energy of the clusters  $C_p$  [5] and  $V_{\text{ion}}^{(z)}(C_p)$  for the *z* ionization potential of  $C_p$ . The atomization energies  $E_{at}(C_p)$  for fullerenes (50  $\leq p$  $\leq 60$ ) and for light chains (2 $\leq p \leq 10$ ) are calculated using the binding energy per atom of Campbell, Raz, and Lovine [21]. The *z* ionization potential  $V_{\text{ion}}^{(z)}(C_p)$  is the sum of the successive ionization energies  $I(C_p^{q+})$  for the reactions  $C_p^{(q-1)+} \rightarrow C_p^{q+} + e^-$  with *q* varying from 1 to *z*.  $I(C_p^{q+})$  is obtained by calculating the energy-level difference between the final and the initial states of each ionization reaction.

The energy levels of fullerenes  $C_{60-2n}^{q+}$  are calculated with the DFT [22] using the GAUSSIAN code with *B*3LYP base. The closed-cage geometry of each fullerene  $C_{58}$ ,  $C_{56}$ ,  $C_{54}$ , and  $C_{52}$  is obtained using a successive Stone-Wales rearrangement following  $C_2$  extrusions as described in Ref.  $[16]$ . The ring spirals, describing how the pentagons are distributed on these cages, are given in the following:

58:~1,2,9,11,13,15,17,20,23,25,27,29!, 56:~1,2,4,9,12,16,19,22,23,24,26,28!, 54:~1,2,4,9,12,14,16,19,23,25,27,28!, 52:~1,2,4,9,12,14,16,19,21,23,25,28!.

The C—C bond distances of each fullerene have been optimized using a semi-empirical method, i.e., modified neglect of differential overlap. Another isomer of  $C_{56}$  obtained from  $C_{60}$  by direct extrusion of a  $C_4$  carbon chain has been also studied. The energy level of this second isomer is slightly lower  $(-0.4 \text{ eV})$  than that of the first isomer for the neutral molecule and is higher for the multicharged molecule  $C_{56}^{5+}$  $(0.7 \text{ eV})$ . The ionization energy  $I(C_{56}^{q+})$  for the ionization reaction  $C_{56}^{(q-1)+} \rightarrow C_{56}^{q+} + e^-$  is then the difference between the energy levels associated to the most stable isomers of  $C_{56}^{(q-1)+}$  and  $C_{56}^{q+}$ . The obtained  $I(C_{56}^{q+})$  values are very near to those calculated using only the first isomers within a dispersion range of 0.1 eV. So, in the following, for other fullerenes only isomers achieved by successive  $C_2$  extrusions are considered. The results of calculations are shown in Fig. 7 for  $I(C_{60-2n}^{q+})$  for  $n=1-4$ , and  $q=1-5$  and *q*  $=$ 8. As expected, the ionization energy increases with decreasing size of the fullerene. Fits were performed to reproduce the theoretical data using the following equation:

$$
I(C_{60-2n}^{q+}) = W_{\infty} + \frac{q}{R_0 \left(\frac{60-2n}{60}\right)^{1/2}} \times 27.21 \text{(eV)}, \quad (2)
$$



FIG. 7. Ionization energy  $I(C_{60-2n}q^+)$  for the reaction  $C_{60-2n}$ <sup>(q-1)+</sup> $\rightarrow$ C<sub>60-2n</sub><sup>q+</sup>+e<sup>-</sup> calculated using the densityfunctional theory, versus the number of carbon atoms of the fullerene  $(60-2n)$  for charge state *q* varying from 1 to 8. The curves result from the fitted equation  $(2)$ .

where  $W_\infty$  stands for the work function to remove an electron from a neutral fullerene cage and  $R_0$  for the radius of the C<sub>60</sub> molecule. The term  $R_0[(60-2n)/60]^{1/2}$  corresponds to the radius of a fullerene  $C_{60-2n}$ , under the assumption that the surface density of the carbon atoms is conserved for all fullerene cages. The best fit is found with  $W_\infty = 3.69$  eV and  $R_0$ =8.34 a.u. The ionization energies for odd-numbered fullerenes and for even-numbered fullerenes  $I(C_{60-2n}^{q+})$ with  $n>4$  and for  $q=5-7$  are estimated with this relation. The first ionization energies  $I(C_{2n}^+)$  of even-numbered carbon chains are calculated using the same method with a complete geometry optimization for each molecule. The values, 12.15, 11.25, 10.11, and 9.53 eV for  $C_2^+$ ,  $C_4^+$ ,  $C_6^+$ , and  $C_8^+$ , respectively, are in good agreement with the data of the Ref. [23]. For the odd-numbered carbon chains, we use the first ionization energies given in the same reference  $[23]$ , 11.26, 11.4, 10.7, 10, and 9.4 eV for  $C^+$ ,  $C_3^+$ ,  $C_5^+$ ,  $C_7^+$ , and  $C_9^+$ , respectively.

The energy change  $\Delta_m^r$  has been calculated for the reactions  $C_{60}^{r+} \rightarrow C_{60-m}^{(r-1)+}+C_m^+$  with *m* ranging from 1 to 8 and for *r* from 4 to 9. The outer part of the Coulomb barrier  $B'_{m}$ <sup>r</sup>, depending on the charge of the two fission partners and the fission distance *R*, is estimated as  $B'_{m}^{r} = (r-1)/R$ . Under the multistep assumption for the fission process  $[24]$ , *R* is considered as the critical distance for single-electron transfer from the initially evaporated neutral fragment C*<sup>m</sup>* to



FIG. 8.  $\Box$  connected by broken lines, experimental *m*-dependent branching ratios for the fission channels  $C_{60}^{r^+} \rightarrow C_{60-m}^{(r-1)+}$  $+C_m^+$  with *r* ranging from 4 to 9.  $\circ$  connected by continuous lines, branching ratios calculated with the statistical model.

the residual fullerene  $C_{60-m}$ <sup>*r*+</sup>. It increases linearly from 17 to 18.5 a.u. as the number of carbon atoms of the light fragment increases from 2 to 8. These values are extrapolated from measurements of the kinetic-energy release in the fission processes  $C_{60}^{5+} \rightarrow C_{60-m}^{4+} + C_m^+$ ,  $m=2, 4,$  and 6 [ $24,25$ ]. The inner part of the fission barrier *B* for the emission of a  $C_2^+$  fragment is found to be 11.2, 9.8, 8.4, 7.1, 5.8, and 4.5 eV for  $C_{60}^{r+}$  with *r* ranging from 4 to 9. A critical charge state, corresponding to the vanishing of the fission barrier, can be extrapolated for the reaction  $C_{60}^{r+1}$  $\rightarrow$ C<sub>58</sub><sup>( $r-1$ )+</sup> + C<sub>2</sub><sup>+</sup> at  $r=12$ .

A detailed comparison between the theoretical branching ratios obtained with the statistical model and the experimental population distributions for the fission channels  $C_{60}^{\rightharpoonup r+1}$  $\rightarrow$ C<sub>60-m</sub><sup>( $r-1$ )+</sup> + C<sub>m</sub><sup>+</sup> is presented in Fig. 8, as a function of the number *m* of the light fragment for each  $C_{60}^{r+}$  parent ion  $(4 \le r \le 9)$ . In the calculation for  $r=4-9$  values, the excitation energy was taken to  $\varepsilon = 80$  eV according to Ref. [7], where this value has been adjusted in order to fit the measured fragmentation ratio of  $C_{60}^{r+}$  parents ions in Xe<sup>30+</sup> -C<sub>60</sub> collisions. On the contrary to the relative branching ratios, the fragmentation ratios are more sensitive to the excitation energy. The global agreement between the calculation and the experiment shows that the statistical model gives a satisfactory description for the asymmetrical fission of multiply

charged  $C_{60}$ , with the charge of parent ion up to 9 and the mass of the light fragment from 1 to 8. For higher charge states  $r > 5$ , the multifragmentation channels are opened. These channels, probably due to  $C_{60}^{r+}$  parent ions with an initial energy much higher than 80 eV, are not considered in the simulation.

Based on the statistical model, for a given parent ion  $C_{60}^{r+}$ , the maximum of the branching ratio is associated to the fission channel with the lowest fission barrier. The population shift (Fig. 6) towards lighter fragments  $C^+$  and  $C_2^+$ with increasing charge of the  $C_{60}^{r+}$  can be then understood qualitatively in terms of the fission barrier variation as a function of the number *m*. The energy change  $\Delta_m^r$  of the fission reaction  $C_{60}^{r+} \rightarrow C_{60-m}^{(r-1)+} + C_m^+$  can be considered as the summation of two terms, a positive term contributed by the atomization energy change and a negative term, called Coulomb term  $\Lambda$ , which is associated with the ionization potential change. The positive term decreases with decreasing *m* value of the light fragment, which favors the very asymmetrical mass division process. In the negative term  $\Lambda$ , the ionization potential of the light fragment  $V_{\text{ion}}^{(1)}(C_m)$  decreases with increasing *m* and that of the fullerene heavy fragment  $V_{\text{ion}}^{(r-1)}(C_{60-m})$  increases with *m*. For fission reactions with a parent ion  $C_{60}^{r+}$  at low charge state ( $r$ <4), the variation of the negative term as a function of *m* is dominated by  $V_{\text{ion}}^{(1)}(C_m)$ , because the variation of  $V_{\text{ion}}^{(r-1)}(C_{60-m})$ with *m* is negligible compared to that of  $V_{\text{ion}}^{(1)}(C_m)$  (Fig. 7). The negative term  $\Lambda$  favors then the fission channels with a heavier fragment  $C_m^+$ . When the charge of the parent ion  $C_{60}^{r+}$  increases, the variation of  $V_{\text{ion}}^{(r-1)}(C_{60-m})$  as a function of *m* plays a more and more important role in the term  $\Lambda$  and becomes dominant for  $r > 5$ . So, for  $C_{60}^{r+1}$  at high charge state, both the negative and the positive terms favor the asymmetrical mass division channels, leading to the measured branching ratio  $R<sub>b</sub>$  shifted towards lighter fragments  $C^+$  and  $C_2^+$ .

The emission of a doubly charged light fragment from a  $C_{60}^{r+}$  parent ion is a relatively weak channel. However, it becomes more important with increasing charge *r*. The total branching ratios for the emission of singly charged light fragments  $(C_m^+)$  and that of doubly charged light fragments  $(C_m^{2+})$  are presented in Fig. 9 as a function of the charge *r*. They are obtained from Table I by the summations  $\sum_{m} R_b(C_m^{\tbinom{m}{2}})$  and  $\sum_{m} R_b(C_m^{\tbinom{m}{2}})$ , respectively, for each parent ion  $C_{60}^{r+}$ . The total branching ratio for the emission of doubly charged light fragments  $\sum_m R_b (C_m^{2+})$  increases from less than 2% to 25% with the increasing charge of the parent ion *r* from 5 to 9. This tendency can be interpreted by analyzing the fission barrier variation of these two types of channels versus the charge of  $C_{60}$ . The fission barrier for the emission of a  $C_2$ <sup>+</sup> fragment, for example, is found to decrease with increasing charge *r*. This variation is mainly due to the negative Coulomb term  $[\Lambda = -V_{\text{ion}}^{(r)}(C_{60}) + V_{\text{ion}}^{(r-1)}$  $\times (C_{58}) + V_{\text{ion}}^{(1)}(C_2)$ ] in the energy change calculation of the reaction  $C_{60}^{r+} \rightarrow C_{58}^{(r-1)+} + C_2^+$ . If the difference between  $V_{\text{ion}}^{(r-1)}(C_{60})$  and  $V_{\text{ion}}^{(r-1)}(C_{58})$  is neglected, this term is approximated as  $\Lambda \approx -\Gamma(C_{60})+V_{\text{ion}}^{(1)}(C_2)$ , which decreases ac-



FIG. 9.  $\bigcirc$ : total branching ratio  $\Sigma_m R_b(C_m^+)$  of the singly charged light-fragment emission channels versus the charge state *r* of the parent ions  $C_{60}^{r+}$ .  $\Box$ : total branching ratio  $\Sigma_m R_b(C_m^{2+})$  of the doubly charged light-fragment emission channels versus *r*.

tually with increasing charge *r*. In a similar way, for the fission channel  $C_{60}^{r^+} \rightarrow C_{58}^{(r-2)+} + C_2^{2+}$ , the Coulomb term is approximated as  $\Lambda' \approx -I^r(C_{60}) - I^{r-1}(C_{60}) + V_{ion}^{(2)}(C_2)$ , which decreases more rapidly with increasing charge *r*. At low charge state  $C_{60}^{5+}$ , the very different branching ratios of the two types of fission channels suggest that the barrier for the  $C_m^2$ <sup>+</sup> emission channel is much higher than that of the  $C_m^+$  emission channel. As the charge *r* becomes higher, the barrier for the emission of a doubly charged fragment  $C_m^2$ <sup>+</sup> decreases faster than that for the  $C_m^+$  emission channel. At high charge state  $C_{60}^{9+}$ , the barriers for the two types of fission channels are so close that the relative branching ratios become comparable.

### **V. CONCLUSION**

By multicoincidence analyses of the projectile final charge state, the ejected electron number, the TOF, and the activated pixel numbers of the charged fragments, we have measured the light-fragment mass-dependent branching ratios of the asymmetrical fission of  $C_{60}^{r+}$  parent ions with the charge *r* ranging from 4 to 9. The measured *m*-dependent population distributions for the singly charged fragment emission channels  $C_{60}^{r+} \rightarrow C_{60-m}^{(r-1)+} + C_m^{r-}$  are relatively well reproduced with a simple statistical model showing that the asymmetrical fission of  $C_{60}^{r+}$  with a charge state *r* up to 9 can be described by similar thermally activated evaporative process. To estimate the fission barriers, the ionization potentials of multiply charged fullerenes and light singly charged C*<sup>m</sup>* chains are calculated with the density-functional theory. A population shift towards lighter fragments  $C^+$  and  $C_2^+$  is observed with the increasing charge of the  $C_{60}^{r+}$ . It is interpreted qualitatively in terms of the fission barrier variation as a function of the number *m*. The doubly charged lightfragment emission channels  $C_{60}^{r^+} \rightarrow C_{60-m}^{(r-2)+} + C_m^{2+}$ are also observed. The total branching ratio of these channels increases from less than 2% to 25% with the charge of the parent ion varying from 5 to 9. This tendency is due to the fact that the fission barrier of the  $C_m^2$ <sup>+</sup> emission channel decreases faster than that of the  $C_m^+$  emission channel as the charge of the  $C_{60}^{r+}$  parent ion increases. The multifragmentation channels become important for  $C_{60}^{r+}$  parent ions with  $r$   $>$  6. Studies taking account of both asymmetrical fission and multifragmentation of  $C_{60}^{r+}$  will be performed in the near future.

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