Dielectronic recombination and energy loss for He-like ⁷⁹Br ions channeled in a thin single crystal of Si

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Dielectronic recombination of He-like ⁷⁹Br ions channeled along the $\langle 110 \rangle$ axis of a thin Si crystal has been studied by the measurement of the charge-state distribution and x-ray production. The results of the charge-state measurements confirm that the probability of resonance capture is proportional to the valence electron density sampled by the ion. The energy-loss distributions of channeled ions are also in good agreement with theoretical estimates. [S1050-2947(96)02506-1]

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I. INTRODUCTION

Dielectronic recombination (DR) is a process in which an ion in an electron gas captures an electron with simultaneous excitation of a bound electron i.e., an inverse Auger process. The excited ion then stabilizes by emitting a photon. The process is resonant and has a maximum cross section when the velocity of the ion matches the velocity of an Auger electron. When the captured electron is initially bound in a target atom, the DR process is often denoted as resonant transfer and excitation (RTE).

Initial measurements of RTE were made by Tanis *et al.* [1] for collisions of S^{13+} ions in an Ar gas. More recently, Datz *et al.* [2] showed that RTE can be studied using channeling techniques, since heavy ions channeled in thin crystals interact mainly with loosely bound electrons and capture in close collisions with atoms is suppressed. Datz *et al.* [2] measured RTE cross sections for S^{15+} , Ca^{19+} , Ti^{20+} , and Ti^{21+} ions channeled in Si crystals by observing x rays emitted by the doubly excited ions.

In a similar experiment, Belkacem *et al.* [3] measured RTE for Ti¹⁹⁺ and Ti²⁰⁺ ions channeled along a $\langle 110 \rangle$ axis in an Au crystal. The best-channeled ions were selected as those ions with the lowest-energy loss. They observed the fraction of ions that captured one electron, as a function of energy, and reported a resonance width five times narrower than any previously observed for RTE. Dittner *et al.* [4] repeated this measurement for Ti²⁰⁺ ions channeled along a $\langle 100 \rangle$ axis in a thin Au crystal; they were unable to detect any resonance. We have recently measured DR for He-like ⁷⁹Br ions channeled along a $\langle 110 \rangle$ axis in a thin Au crystal [5] and observed a resonance strength and width compatible

with the predicted values for an electron gas with a density corresponding to the average electron density in a $\langle 110 \rangle$ channel in Au.

Finally, Andriamonje *et al.* [6] observed the *KLL* resonance for He-like Xe ions channeled along a $\langle 110 \rangle$ axis in Si. They observed the resonance both by detecting photons from the decay of the doubly excited state and by measuring the energy dependence of charge-state fractions of ions exiting the crystal with low-energy loss. A detailed analysis of the energy loss in these experiments was carried out by L'Hoir *et al.* [7].

We report here a similar experiment using a 17.9-MeV/u ⁷⁹Br beam from the Tandem Accelerator SuperConducting Cyclotron (TASCC) facility. Measurements of the distribution in energy and charge state of the exiting ions were made for 15 energies between 12.1 and 17.5 MeV/u for ions channeled along a $\langle 110 \rangle$ direction through a 1- μ m Si crystal. In addition, coincidence x-ray data were taken at 13.7, 15.3, and 17.5 MeV/u. A preliminary report [8] of this work appeared earlier.

The principle of the measurement is to use channeling to keep the ions away from rows of atoms, so that the charge-exchange processes in close collisions with Si atoms are negligible. The only close collisions are then with valence (M-shell) electrons and the probability for dielectronic recombination should be proportional to the average density of valence electrons along the trajectory. The energy loss of the channeled ions is reduced compared to the loss for ions penetrating a random medium and ions exiting the crystal with significantly different energies have sampled different regions of the channel. We could therefore study the variation of the capture probability with electron density by selecting windows in the energy-loss spectrum. The results are



FIG. 1. Schematic diagram of the experimental layout for heavy-ion channeling studies at the TASCC facility.

compared with calculations based on density profiles across the channels obtained from x-ray-diffraction measurements.

Since the analysis of these capture measurements is based on the reduction of the energy loss for channeled ions, we discuss in some detail the theoretical description of the energy-loss process. For Si atoms, the K, L, and M shells are well separated both in binding energy and in spatial extension and it is natural to consider separate contributions to the stopping as arising from different shells. We discuss the problems of such a separation and compare the resulting predictions with the measurements. A treatment of the random stopping of swift heavy ions, with reference to results obtained in this experiment, was given earlier [9].

In Sec. II we give experimental details, while Sec. III describes the analysis of the DR electron capture process. Section IV compares measurements and calculations of the resonance strength, energy, and width and Sec. V details energy-loss measurements. In Sec. VI the x-ray coincidence data are described and a summary and conclusions are given in Sec. VII.

II. EXPERIMENTAL DETAILS

The experimental layout is shown schematically in Fig. 1. A 17.9-MeV/u ⁷⁹Br²²⁺ beam from the TASCC facility superconducting cyclotron at Chalk River was stripped and degraded to ⁷⁹Br³³⁺ with a series of Al degrader foils. The foils ranged in thickness between 1 and 19 mg/cm², in steps of 1 mg/cm², corresponding to beam energies on target between 17.6 and 12.1 MeV/u. The 90° and 18.5° beam-transport magnets downstream of the degrader foil were used to select a narrow momentum bite of the 33⁺ charge-state component of the degraded beam. The beam divergence was controlled by two 0.5-mm apertures, separated by 1.6 m, directly ahead of the scattering chamber. The cyclotron beam energy was measured upstream of the stripper or degrader foil. Three accurately located time-pickoff detectors, separated by 6.755 m (1 and 2) and 22.540 m (2 and 3), determined the energy of the ⁷⁹Br²²⁺ beam to be 17.87 ± 0.03 MeV/u.

A Si crystal, with a $\langle 110 \rangle$ axis normal to its surface, was mounted on a three-axis goniometer in the scattering chamber; the crystal thickness was measured to be $0.99\pm0.02~\mu$ m with a mixed α source (²³⁹Pu, ²⁴¹Am, and ²⁴⁴Cm), using the TRIM stopping powers [10]. Before mounting the crystal in the chamber, we removed the native oxide layer on its surface by dipping the crystal into a 1% HF solution and then rinsing it in water. To align a $\langle 110 \rangle$ axis with the beam direction we used the fact that the ion energy loss is considerably lower for axial and planar channeling than for penetration in a random direction and searched for directions where a large fraction of the particles had low-energy loss.

At each beam energy, we made measurements for both random and aligned orientation of the crystal for two settings of the quadrupole and three dipoles (Q3D) magnetic spectrometer field, chosen to select either 31^+ , 32^+ , and 33^+ ions or 32^+ , 33^+ , and 34^+ ions in three resistive-wire counters positioned along the focal plane. Each resistive-wire counter had an active length of 35 cm. The dispersion of the Q3D spectrometer is 13 cm/%($\Delta p/p$) at the middle of the 2-m-long focal plane.

The resistive-wire counters were calibrated at the highest beam energy by removing the crystal and measuring the beam position in each counter for various settings of the magnetic field. For each position x on the counter the radius of curvature ρ in the spectrometer could be calculated from the magnetic field B and the accurately measured beam energy; in subsequent measurements the function $\rho(x)$ was 5000

4000

3000

2000

1000

32*





FIG. 2. Energy spectra of transmitted 32^+ and 33^+ ions for an incident beam of 15.6-MeV/u ⁷⁹Br³³⁺ ions. Spectra for random (----) and $\langle 110 \rangle$ alignment (—) are shown as a function of energy loss relative to the beam energy. The regions I, II, and III correspond to the regions of energy loss used in determining the ratio $I(32^+)/I[(32^+)+(33^+)]$. For the 1- μ m-thick Si crystal used in this experiment, the random energy loss is 4.5 MeV for 33⁺ ions at 15.6 MeV/u.

used to determine the energy of the transmitted ions from the magnetic-field setting.

Energy-loss spectra for 33^+ and 32^+ (one-electron pickup) ions are shown in Fig. 2 for random and aligned orientations at 15.6 MeV/u incident energy. The direct beam had a full width at half maximum (FWHM) of 306 keV, approximately half the width of the peak in random alignment.

A 200-mm² intrinsic Ge x-ray detector was mounted in the chamber at 127.5° to the beam direction and approximately 5.3 cm from the Si crystal as shown in Fig. 1. X rays were recorded in coincidence with 32⁺ ions detected in one of the focal plane detectors for incident energies of 13.7, 15.3, and 17.6 MeV/u, i.e., below, on, and above the KLL resonance, respectively. The incident flux of 33⁺ ions was determined from the measured charge-state ratio $I(32^+)/I[(32^+)+(33^+)]$ for channeled ions (see Sec. III).

The x-ray detector efficiency was measured with a calibrated 57 Co source that covered the region of x-ray energies of interest in this experiment. The detector efficiency was observed to change by 60% between 6.4 and 14.4 keV and, since we did not measure the effect of the Ge *K* absorption edge for the geometry of our detector at the time of the experiment (and the detector mount has since been modified), we estimate the uncertainty in efficiency to be ~15%



FIG. 3. Charge-state distribution for random (\blacksquare) and $\langle 110 \rangle$ alignment (\blacktriangle), with no window on the energy-loss spectra, for an incident beam of 15.3-MeV/u ⁷⁹Br³³⁺ ions.

in the region between these energies.

A measurement of the charge-state distribution was made for random and $\langle 110 \rangle$ alignment at each of the three beam energies where x-ray data were collected. The charge-state measurement at 15.3 MeV/u is shown in Fig. 3. We note the very strong reduction of electron capture for channeled ions. Were it not for this effect, it would be very difficult to experimentally identify the DR process directly as an increased yield of ions that captured an electron at the resonance energy.

III. ANALYSIS OF CAPTURE

At the resonance energy for KLL capture, the DR process is responsible for a large fraction of the charge exchange for channeled ions. This can be seen in Fig. 4(a), where the ratio $I(32^+)/I[(32^+)+(33^+)]$ is shown as a function of beam energy. Figure 4(b) shows the resonance contribution after the subtraction of a smooth background proportional to E^{-b} with b=2.94 determined empirically by fitting the three lowest-energy points and the highest-energy point.

In this analysis we include only well-channeled particles with low-energy loss (i.e., windows I, II, and III in Fig. 2). To calculate the capture ratio for a group of ions defined by a window in the 33^+ energy-loss spectrum, a corresponding window in the 32^+ spectrum must be identified, which contains ions with the same channeling properties, i.e., which corresponds to the same range of transverse energy. Furthermore, for determination of the dependence of the capture ratio on beam energy, the windows in the energy-loss spectra obtained for different incident-ion energies must also be chosen to correspond to the same range of transverse energy.

For the definition of these windows we have used the peak corresponding to random energy loss as a reference point. At the two extreme energies, 12.1 and 17.6 MeV/u, the energy of the 33^+ beam was measured by raising the crystal out of the beam. It was found that the ratio between random energy loss and the leading edge of the channeled energy-loss spectrum was the same at these two energies to within 1%. We have therefore defined window boundaries at definite fractions of random energy loss. An alternative proce-



FIG. 4. (a) Charge-state fraction $I(32^+)/I[(32^+)+(33^+)]$ for ions with energy loss encompassing regions I, II, and III in Fig. 2, plotted as a function of energy at the center of the crystal for $\langle 110 \rangle$ alignment. (b) Background-subtracted charge-state fraction $I(32^+)/I[(32^+)+(33^+)]$ for the data shown in (a) (see the text for details of background subtraction).

dure would be to define windows by the fraction of channeled 33^+ ions above the window boundary (i.e., with lowerenergy loss) in the energy-loss spectrum and indeed the constancy of this fraction, as a function of bombarding energy, served as a useful check on the consistency of our procedure.

The same fractions of random energy loss were used to define the regions in the 32^+ spectra. The dependence of energy loss on the charge state was ignored. For convenience, we may assume that the capture occurs in the middle of the crystal and therefore the energy loss, for a fixed trajectory, should be reduced by about 3% because of the Q^2 dependence of the stopping. However, the random energy loss, which is used as a reference, should also be slightly smaller for exiting 32^+ ions than for 33^+ ions. This difference may be estimated from the observation that the charge-state distribution after the crystal had a small dependence on incident charge state consistent with an exponential approach to equilibrium with a decay length of $\frac{1}{4} \mu m$. This would give the same energy-loss difference for the random 32^+ and 33^+



FIG. 5. Background-subtracted charge-state fraction $I(32^+)/I[(32^+)+(33^+)]$ for the regions in energy loss, shown in Fig. 2, corresponding to windows I (\blacktriangle), II (\times), and III (\blacksquare).

ions as for channeled ions, since the random stopping power is about twice as large and the decay length is $\frac{1}{4}$ of the crystal thickness. Semiclassical calculations of the cross section for loss of a Br *L*-shell electron in a collision with a Si nucleus [11] lead to a mean free path for this process of about $\frac{1}{2} \mu m$ (and hence to a decay length of about $\frac{1}{4} \mu m$), in agreement with the charge-state observations. This estimate may also be applied to set a limit for the correction to the capture ratio for loss of the captured electron in Br³²⁺ in collisions with electrons in the channel. The cross section for this process must be smaller by a factor of ~14² and, since the electron density in the channel is only a few electrons per atom, the correction cannot be larger than ~2%.

In order to obtain information on the variation of the capture probability with electron density, the peak in the energyloss spectrum for channeled Br^{33+} ions was subdivided into three intervals as shown in Fig. 2. As discussed in Sec. V B 4, the spread in energy-loss results mainly from a variation of the particle trajectory associated with the point of impact on the crystal surface, with only a small contribution from straggling in energy loss for a fixed trajectory. Hence larger energy loss should correspond to larger transverse energy and higher average electron density along the trajectory. For the three selected energy-loss windows, the charge-state distributions were analyzed as before (see Fig. 4) and the results are shown in Fig. 5.

The calculated energy-integrated cross section for dielectronic recombination of He-like ⁷⁹Br ions [12] is 5.6×10^{-19} eV cm². With this value it is possible to deduce the average electron density seen by the channeled ions from the area of the background-corrected distributions shown in Figs. 4(b) and 5. The energy scale must be converted to the equivalent energy (in the ion rest frame) of electrons at rest in the target; the area is then equal to the cross section multiplied by the number of electrons per unit area of the crystal. The results of this analysis are summarized in Table I. The errors include an estimated 4% systematic error (added linearly to the statistical error) resulting from the method used to determine

| Window | Random energy-loss fraction | Channeled fraction ^a | $ ho_e$ (electrons/ atom) ^b | $\Delta E_{\text{FWHM}}/E_r$ (%) | |
|--------|-----------------------------------|---------------------------------|--|----------------------------------|------------------|
| | | | | Predicted | Measured |
| I | 0.41-0.48 | 0.07-0.28 | 2.0 ± 0.1 | 8.5 | 8.2±0.5 |
| II | 0.48 - 0.55 | 0.28 - 0.57 | 3.1 ± 0.1 | 9.9 | 10.9 ± 0.4 |
| III | 0.55 - 0.62 | 0.57 - 0.76 | $3.8 {\pm} 0.2$ | 10.6 | $11.8 {\pm} 0.5$ |
| I–III | 0.41-0.62 | 0.07 - 0.76 | 2.8±0.1 | 9.6 | 10.5 ± 0.2 |

TABLE I. Electron densities determined from resonance yields and a comparison of calculated and measured resonance widths.

^aFraction of channeled ions in the region determined by the random energy-loss window.

^b1 electron/atom=0.05 $e^{-}/\text{Å}^{3}$.

I I I I

the nonresonant background. In contrast to an earlier study [6] there is a clear variation of derived electron density with energy loss.¹

IV. COMPARISON OF MEASURED AND CALCULATED **ELECTRON DENSITIES**

Experimentally, the electron density is better known in silicon than in any other material owing to extremely accurate x-ray-diffraction measurements. An analytical fit to these measurements, based on the Doyle-Turner representations [13] of x-ray form factors for Si and for Si⁴⁺ and a Gaussian blob of charge in the bonds, has been made by Scheringer [14] and we shall base our calculations on this model.

Ions with energy loss much smaller than the "random" value (i.e., for an amorphous target) have been channeled through the crystal. The motion of channeled ions is governed by the transverse potential U(x,y), i.e., the crystal potential averaged over the coordinate z along the (110) direction. Since the ion is nearly fully stripped, it may be treated as a point charge Qe interacting with the electrostatic potential ϕ in the crystal $U(x,y) = Qe \phi(x,y)$. It is then convenient to define a reduced transverse energy ϵ of channeled ions as

$$\epsilon = \frac{p_{\perp}^2}{2MQ} + e\,\phi(x,y),\tag{1}$$

where p_{\perp} is the projection of the ion momentum on the transverse (x,y) plane and M is the ion mass.

The calculation of the average electron density along the trajectory of an ion that experiences a given energy loss is based on the following assumptions:

(i) The reduced transverse energy ϵ is conserved.

(ii) The transverse distribution of ion trajectories for fixed ϵ is uniform in the allowed area, corresponding to a statistical equilibrium for transverse motion in the potential U(x,y).

(iii) The energy loss ΔE is an increasing function of ϵ .

The first assumption should be quite accurate for our case. In particular, the average increase in reduced transverse energy resulting from multiple scattering due to electronic collisions may be estimated from the energy loss,

$$\langle \Delta \epsilon \rangle = \Delta E \, \frac{m}{2M} \, \frac{1}{Q},$$
 (2)

where *m* is the electron mass. In the middle of the crystal, $\langle \Delta \epsilon \rangle$ is half this amount, which in the present case is negligible, $\langle \Delta \epsilon \rangle / 2 \simeq 0.1$ eV. Note, however, that if the crystal thickness is increased by an order of magnitude as in the work by Andriamonje et al. [6], this correction becomes significant. The validity of assumptions (ii) and (iii) is discussed in Sec. IV C and V, respectively.

A. Distribution in ϵ

It is convenient to discuss the integrated distribution

$$G(\boldsymbol{\epsilon}) = \int_{0}^{\boldsymbol{\epsilon}} d\boldsymbol{\epsilon}' g(\boldsymbol{\epsilon}'), \qquad (3)$$

where $g(\epsilon')$ is the distribution in transverse energy. If the beam is incident parallel to the crystal axis, $G(\epsilon)$ is simply the normalized area function

$$G_0(\boldsymbol{\epsilon}) = A(\boldsymbol{\epsilon}) / A_0, \qquad (4)$$

i.e., the fraction of the transverse plane available for the motion of particles with reduced transverse energy ϵ . This function is shown in Fig. 6.

The collimation of the incident beam corresponds to a distribution f in ϵ and, taking this into account, we obtain

$$G(\boldsymbol{\epsilon}) = \int_0^{\boldsymbol{\epsilon}} d\boldsymbol{\epsilon}' f(\boldsymbol{\epsilon}') G_0(\boldsymbol{\epsilon} - \boldsymbol{\epsilon}').$$
 (5)

For large values of ϵ , where $G_0(\epsilon - \epsilon')$ is approximately linear over the range of $f(\epsilon')$, we obtain

$$G(\boldsymbol{\epsilon}) \simeq G_0(\boldsymbol{\epsilon} - \langle \boldsymbol{\epsilon}' \rangle), \tag{6}$$

with

$$\langle \boldsymbol{\epsilon}' \rangle = \int_0^\infty d\boldsymbol{\epsilon}' \, \boldsymbol{\epsilon}' f(\boldsymbol{\epsilon}')$$

¹In a preliminary report on this experiment [8], it was stated that we saw no variation in electron density with energy loss; this resulted from an error in that data analysis, which has since been corrected.



FIG. 6. Normalized area function $G_0(\epsilon)$ as a function of reduced transverse energy ϵ (---). The modified function $G(\epsilon)$ (—) takes into account the increase in transverse energy introduced by the finite collimation used in the experiment. The --- lines represent values of $G(\epsilon)$ and the corresponding value of $G_0(\epsilon)$ (with the same ϵ) for the boundaries of the energy-loss windows I, II, and III in Fig. 2.

i.e., the function G is just shifted by the average reduced transverse energy of the incident beam. With the collimation used in this experiment, we have $\langle \epsilon' \rangle = 1.24$ eV at 15.6 MeV/u. The modified function $G(\epsilon)$ is shown as a solid line in Fig. 6.

We now use assumption (iii) above to calculate the available area for ions in the three windows on the energy-loss spectra (see Fig. 2). Via the modified $G(\epsilon)$ curve, each window boundary, represented by the fraction of ions with energy loss lower than that boundary, may be associated with a particular transverse energy. The function $G_0(\epsilon)$ then gives the corresponding available area of the transverse plane as illustrated in Fig. 6. The increase in available area caused by the angular spread of the beam is clearly a significant correction.

B. Electron density

The calculated average electron density in a Si $\langle 110 \rangle$ channel as a function of the available area in the transverse plane $x = A(\epsilon)/A_0$ is shown in Fig. 7. The solid curve with 0.56 electrons in each bond corresponds to the best fit to the x-ray-diffraction data [14], while the dashed curve gives the atomic charge density without correction for bonding. The average density of valence electrons $\overline{\rho}$ is close to $\overline{\rho}=1+3x$ electrons/atom and this is a useful approximation. The corresponding approximation for the local density at the boundary of the area $A(\epsilon)$ is $\rho=1+6x$. The steep rise for x>0.8 is due to L electrons.

The intervals in *x*, derived from Fig. 6, are given by dashed lines. For the lowest window in ϵ , the measured density of 2.0 ± 0.1 electrons/atom is in very good agreement with the calculation. For the two higher windows, the experimental values of 3.1 ± 0.1 and 3.8 ± 0.2 are $\sim10-15$ % higher than the calculated values, i.e., only slighly outside our experimental uncertainties.

For this comparison we have assumed that resonant electron capture is a local process and hence the capture probability is proportional to the local electron density averaged along the projectile trajectory. The impact-parameter dependence may be estimated from the angular momenta involved



FIG. 7. Calculated average electron density $\overline{\rho}$ for a Si $\langle 110 \rangle$ axis as a function of the available area in the transverse plane $x=A(\epsilon)/A_0$ (---). The correction for 0.56 electrons in each bond is also shown (—). The (---) lines represent the values of x corresponding to the boundaries of regions I, II, and III of the energyloss spectra in Fig. 2, including the correction for beam divergence illustrated in Fig. 6.

and conservation of angular momentum restricts the *l* values for the electron to be captured to $l \le 2$. The largest value corresponds to a classical impact parameter b=0.1 Å, which is small on the scale of the variation of ρ . Hence there seems to be no reason to suspect an important correction for nonlocality as has been suggested by Andriamonje *et al.* [6].

C. Spatial average

The assumption of a uniform distribution of ion trajectories in the available transverse area, which corresponds to a statistical equilibrium for two-dimensional motion, may be questioned for such a thin crystal (1 μ m). In the middle of the channel, the potential is nearly axially symmetric and angular momentum along the axis is approximately conserved. Hence the establishment of full two-dimensional equilibrium requires each channeled trajectory to undergo many oscillations.

Consider for simplicity a harmonic potential U(x,y) corresponding to the average valence electron density of 4 electrons/atom. The oscillation frequency ω for the transverse motion of an ion with charge Qe may, through Poisson's equation, be related to the plasma frequency in silicon, $\omega_{pl}=16.6 \text{ eV}/\hbar$, by

$$\Delta U = 4 \pi \rho e^2 Q = 2M \omega^2, \tag{7}$$

leading to $\omega = (Qm/2M)^{1/2}\omega_{\rm pl}$.

The number of oscillations during the time spent traversing the crystal ($T=1 \ \mu m/v$, where v is the ion velocity) is then close to unity and for the lower density in the $\langle 110 \rangle$ channel the ions will perform less than one full oscillation. Thus the crystal thickness is far too small for a full equilibrium in phase space to be established.

Nevertheless, we may argue that our estimates of average electron densities seen by the ions should be reasonable. As seen in Fig. 7, the electron density is nearly linear in the square of the displacement from the channel center. All we require, therefore, is that for ion trajectories at a given transverse energy, the mean-square displacement from the center is the same as in two-dimensional equilibrium.

This is a much weaker assumption. Consider ions incident parallel to the axis near the center of the channel. The potential has approximate azimuthal symmetry in this region and the ions will therefore in their transverse motion oscillate with zero angular momentum, in one-dimensional, nearly harmonic motion. In such motion, an average spatial distribution corresponding to equilibrium is established already after a quarter of an oscillation from the extremum and, moreover, the mean-square displacement from the center is for a harmonic oscillator the same in one- and twodimensional equilibrium. We may conclude that even for the lower transverse energies, the calculation of the mean electron density seen by ions should be fairly accurate. For higher transverse energies, the ions move further in the transverse plane. There is no conservation of angular momentum around the channel center and only one collision with a string is required to establish a spatial distribution corresponding approximately to equilibrium (constant in the allowed area). This has been shown previously by Monte Carlo simulation of channeling. A quantitative test of the accuracy of our density estimates would require simulations for our specific case and are outside the scope of this work.

D. Resonance energy and width

The resonance condition for *KLL* capture of a free electron with velocity v_e by an ion with velocity v may be expressed as energy conservation in the ion frame,

$$\frac{1}{2}m(\bar{v}_{e}-\bar{v})^{2} = E_{K}-2E_{L}, \qquad (8)$$

where E_K and E_L are the K- and L-shell binding energies.

The right-hand side of Eq. (8) can be obtained from a purely atomic calculation since at the small distances of binding, the screening by electrons in the solid can be neglected. A number of final states with slightly different binding energy contribute and the average, weighted by the partial capture cross section, becomes 8.50 keV [12].

The main term on the left-hand side of Eq. (8) is $\frac{1}{2}mv^2$ and hence Er=8.50 keV is a first estimate of the resonance energy; modifications we move to the right-hand side as corrections to E_r . We first note that relativistic corrections to the kinetic energy are less than 1% so we may use the nonrelativistic expression for calculation of corrections. After averaging over directions of v_e we obtain as the first correction to E_r , $-\langle \frac{1}{2}mv_e^2 \rangle$. For a Fermi gas the average kinetic energy is $\frac{3}{5}$ of the Fermi energy, which is given by in units of a Rydberg, $e^2/2a_0=13.6$ eV, where $a_0=0.529$ Å is the Bohr radius. With the electron density corresponding to window I (see Table I), the correction to E_r from the kinetic energy of the captured electron becomes -5 eV.

Is there a corresponding correction for potential energy? If the collision with the ion is viewed in the laboratory frame, the electron moves only a very small distance of order $b_0 < 0.1$ Å before capture [see Eq. (18)] and hence we can neglect the influence of the lattice potential. (Note that a significant correction for potential energy was erroneously included by Pitharke, Ritche, and Echenique [15].) However, there is another potential-energy correction that can be significant.

The scattering of target electrons on the ion builds up a polarization potential, which repels the electron to be captured and reduces the energy release [left-hand side of Eq. (8)]. For a uniform Fermi gas in the high-velocity limit, the magnitude of this potential energy at the position of the ion may be written [16] as [the expression (4.27) in Ref. [16] for the self-energy of the ion should be multiplied by $2/Z_1e$ to obtain the induced electrostatic potential at the position of the ion]

$$V = \frac{\pi}{2} \frac{v_0}{v} Q\hbar \omega_{\rm pl}, \qquad (10)$$

where v_0 is the Bohr velocity, Qe the ion charge, and $\hbar \omega_{pl}$ the plasmon energy, which in Rydberg units is given by

$$\hbar \omega_{\rm pl} = (16\pi \rho_e a_0^3)^{1/2}.$$
 (11)

The potential builds up over distances from the ion up to $v/\omega_{\rm pl}$, which for our case is tens of angstroms. Hence, for the contribution from valence electrons we may use Eq. (10) with the plasmon energy in Si, $\hbar\omega_{\rm pl}=17$ eV, which leads to V=35 eV and a positive correction of this magnitude to E_r .

Since the polarization potential is not very local, the contribution from *L* electrons should also be considered. For a simple estimate, we may again use the formula (10) for a homogeneous electron gas. The proportionality of *V* to ω_{pl} results from a combination of a proportionality to electron density, i.e., to ω_{pl}^2 according to Eq. (11), and a proportionality to the reciprocal response frequency ω_{pl}^{-1} . For the *L* electrons, the average density is higher by a factor of 2 compared to *M* electrons, but the response frequency is higher by more than an order of magnitude (see Table I). Hence the contribution from *L* electrons cannot increase the polarization potential by more than about 15%.

The combined correction to E_r will then be of order 35 eV, leading to a predicted resonance energy of E_r =8.54 keV. For the interval I, the centroid of the resonance peak shown in Fig. 5 is 8.50±0.02 keV, in reasonable agreement with the prediction; the uncertainty on the resonance centroid includes uncertainty on the determination of the centroid of the distribution and on the energy calibration of the Q3D spectrometer.

The width of the resonance, resulting from the motion of captured electron results from the term $-mv_ev$ in Eq. (8) and can be expressed as

$$\Delta E_{\rm FWHM} / E_r = 2(2E_f / E_r)^{1/2}.$$
 (12)

The measured resonance widths for regions I, II, and III and the predictions, based on Eq. (12), with the measured electron densities are summarized in Table I. Good agreement (\sim 10%) is obtained considering the fact that the electron density in a channel varies considerably with the *z* coordinate.

V. ENERGY LOSS

The analysis of the experiment is based on the measurement of energy loss and it is therefore important to understand the ΔE spectra in Fig. 2. We first briefly summarize the discussion in Ref. [9] of the energy loss and straggling for random incidence.

A. Random energy loss

For particles with charge Qe and high but still nonrelativistic velocity v, the stopping is approximately given by [17]

$$\frac{dE}{dx} = \frac{4\pi Q^2 e^4}{mv^2} \rho L_e, \qquad (13)$$

where ρ is the average electron density $\rho = NZ_2$ and N is the atomic density. The stopping logarithm may be written as

$$L_e \simeq \ln \frac{b_{\max}}{b_{\min}},\tag{14}$$

where b_{max} and b_{min} are effective limits in the integration over impact parameters *b* of the energy transfer to electrons, which for small scattering angles is proportional to b^{-2} . Such a classical description of electron-ion collisions is permitted when Bohr's parameter κ is larger than unity,

$$\kappa = 2Qv_0/v, \tag{15}$$

where v_0 is the Bohr velocity. For Br³³⁺ at 17.6 MeV/u we have $\kappa = 2.5$.

In distant collisions, an atom responds like a collection of harmonic oscillators. For a single oscillator with frequency ω , the effective upper cutoff in *b*, due to adiabaticity of the interaction, is given by

$$b_{\rm max} = 1.123 v / \omega.$$
 (16)

For an atom, b_{max} is given by Eq. (13) with a weighted average frequency

$$\ln(\omega) = Z_2^{-1} \sum_i f_i \ln(\omega_i), \qquad (17)$$

where f_i are dipole oscillator strengths fulfilling the sum rule $\sum_i f_i = Z_2$. The energy $I = \hbar \omega$ is denoted the *I* value.

In the classical regime $\kappa > 1$, the effective lower limit in the integration over *b* corresponds to a scattering angle of $\pi/2$ in the relative ion-electron motion and the impact parameter is given by

$$b_{\min} = b_0/2 = Qe^2/mv^2.$$
 (18)

The main correction to this description is the so-called Barkas effect, which may be explained as an effect of dynamic

TABLE II. Oscillator strengths and ionization values for silicon.

| Shell | Dipole oscillator strength | <i>I</i> value ^a (eV) | <i>I</i> value ^b (eV) |
|-------|----------------------------|-------------------------------------|-------------------------------------|
| K | 1.5 | 3200 | 3200 |
| L | 8.5 | 240 | 310 |
| М | 4.0 | 11 | 17 |

^aEstimated from Fig. 8 of Ref. [16].

^bCollective effects included (see the text).

(adiabatic) screening of the interaction at large electron-ion distances. For the present experiment, the correction is $\sim 5\%$ and with the above description the measured stopping is then reproduced within a few percent (Table I of Ref. [9]).

The straggling in energy loss was shown in Ref. [9] to have about equal contributions from fluctuations in ion charge (charge-exchange straggling) and from fluctuations in the large-energy transfers in collision with electrons (Bohr straggling). Furthermore, the calculated width of the random energy-loss distribution was in good agreement with the measured width.

B. Channeled energy loss

1. Separation of shells

For channeled ions, the theoretical treatment of energy loss is much more complicated because of the imposed selection of impact parameters with atoms. Both the spatial distribution of the electrons and the frequency distribution of the dipole oscillator strengths f_i become important.

A reasonable description of the stopping may be obtained by the customary separation into contributions from different electron shells. For Si there are three shells: the K, L, and Mshells. While the K and L shells are localized near atomic positions, the M electrons are delocalized in the solid and form the valence band. The binding energies differ by about an order of magnitude and are of order 10^3 , 10^2 , and 10 eV, respectively.

There are two main complications in this description: the Pauli principle and collective effects. For the first we may refer to the calculation by Dehmer, Inokuti, and Saxon [18] in the independent-electron model with Herman-Skillman wave functions. The Pauli principle blocks transitions to filled states and transfers oscillator strength from lower to higher shells. Without this effect, the total oscillator strength for a shell would be equal to the number of electrons it contains. In Si, the main effect is a transfer from the *K* shell to the filled *L* shell (Fig. 7 of Ref. [18]) of about 0.5, as given in Table II. The *I* values in the third column of Table II are estimated from Fig. 8 of Ref. [18], and with these values we reproduce closely the atomic *I* value given in Ref. [18], I=131.5 eV.

This *I* value is much smaller than the empirical value [19] of I=174.5 eV. The main reason is that the calculation ignores collective effects, which, according to the estimate by Lindhard and Scharff [20], should increase the characteristic response frequencies by an average factor of about $\sqrt{2}$. Semi-empirical estimates of shell *I* values are given in the fourth column of Table II. Because of the large differences between the shells in both spatial extension and binding, the collec-



FIG. 8. Diagram of the transverse plane for a Si $\langle 110 \rangle$ axis showing positions of the atomic string (\bullet). The dashed curves indicate potential-energy contours corresponding to the boundaries of energy-loss windows I, II, and III in Fig. 2. The circle in the center is a convenient approximation to the innermost contour line.

tive effects are mainly confined to interactions between electrons in one shell. For the *K* shell, this effect should be small and, for the *M* shell, the increase to about 17 eV is known empirically from the observed plasma frequency in Si. The *I* value for the *L* shell is then determined from the total *I* value through Eq. (17) and the increase by a factor ~ 1.3 from the independent-electron result is not too far from $\sqrt{2}$. The effective *I* value for the *L* shell is an important parameter for the following estimates of energy loss for channeled ions.

2. Energy loss to K and L shells

We consider now the energy loss for well channeled ⁷⁹Br³³⁺ ions at 15.6 MeV/u. For both the *K* and *L* shells, the ion trajectories are well outside the shell radius, so only energy loss in distant collisions remains. We may then estimate the energy loss from the result for a classical harmonic oscillator with frequency $\omega = I/\hbar$ [21], where *I* is the shell *I* value. At impact parameters comparable to the adiabatic distance $b_{ad} = v/\omega$, the energy loss ΔE is reduced compared to the energy transfer ΔE_{free} to a free electron at the same impact parameter *b* because the electron adjusts adiabatically to the slowly varying external field. The reduction factor is approximately [21,22]

$$R(\xi) = \xi^2 [K_0^2(\xi) + K_1^2(\xi)], \qquad (19)$$

where $\xi = b/b_{ad}$ and K_0 and K_1 are modified Bessel functions [23].

For the two shells, the adiabatic distances are $b_{ad}^{K} = 0.11$ Å and $b_{ad}^{L} = 1.16$ Å and for a trajectory in the middle of a $\langle 110 \rangle$ channel the distance to the nearest strings is about 2 Å (see Fig. 8). The factor $R(\xi)$ is about 0.5 for $\xi \sim 1$ and decreases as $\exp(-2\xi)$ for large ξ . The energy loss to the K shell, which is \sim 6% of the total loss for random stopping, is therefore completely negligible for channeled ions.

The energy loss to the *L* shell is also strongly reduced by adiabaticity and we shall try to estimate the magnitude of this loss. The minimum contribution from the *L* shells, ΔE_{\min}^{L} , is obtained for an ion moving along the center of a $\langle 110 \rangle$ channel. As seen in Fig. 8, the ion is then surrounded by six strings, each at a distance of $r_{ch} \approx 2$ Å. Adiabaticity makes the energy loss negligible to *L* electrons in strings further away.

Each time the ion moves through a $\langle 110 \rangle$ lattice spacing d=3.84 Å it collides with $6\times8=48$ L electrons at impact parameter $b \approx r_{\rm ch}$. The small transfer of oscillator strength from the K shell (see Table II) in effect increases this number to 51 electrons. The energy loss to free electrons would be

$$\Delta E_{\text{free}} = n \left[\frac{b_0}{b} \right]^2 \left[\frac{1}{2} m v^2 \right] \left[\frac{t}{d} \right], \tag{20}$$

which with n=51, $b=r_{\rm ch}$ and $t=1 \ \mu {\rm m}$ gives $\Delta E_{\rm free}=0.88$ MeV. The adiabaticity parameter is $\xi=1.72$ and the reduction factor $R(\xi)$ is then 0.20, leading to $\Delta E_{\rm min}^L=0.18$ MeV.

For comparison with the experimental spectrum in Fig. 2, we select the upper boundary of window I, corresponding to a measured energy loss of 0.41 times random, or $\Delta E_{\text{expt}}=1.83$ MeV. According to Fig. 6, the channeled ions with this energy loss have a transverse energy corresponding to an allowed area $A(\epsilon)/A_0=0.19$. A circle with this area and radius $\Delta r=0.79$ Å is illustrated in Fig. 8 and an average of the energy loss to *L* electrons must be estimated over this circle.

First we estimate the average of ΔE_{free} given by Eq. (20). For a displacement r of the ion from the center, the square of the distance to one of the six surrounding strings becomes $b^2 = r_{\text{ch}}^2 + r^2 - 2r_{\text{ch}}r\cos\theta$, where θ is the angle between the displacement and the direction towards the string. The averaging of b^{-2} over θ and over r can be carried out analytically and we obtain

$$\langle b^{-2} \rangle = \frac{1}{\Delta r^2} \int_0^{\Delta r^2} dr^2 \frac{1}{2\pi} \int_0^{2\pi} d\theta (r_{\rm ch}^2 + r^2 - 2r_{\rm ch}r \, \cos\theta)^{-1}$$
$$= -\Delta r^{-2} \ln(1 - \Delta r^2 / r_{\rm ch}^2). \tag{21}$$

For $\Delta r = 0.79$ Å, we obtain $\langle b^{-2} \rangle = 1.09 r_{\rm ch}^{-2}$ and hence the average of $\Delta E_{\rm free}$ is 9% larger than the minimum value.

However, the adiabatic reduction factor $R(\xi)$ should be included. It turns out that for the range of ξ values in question, $R(\xi)$ can be approximated well by $R(\xi) \propto \xi^{-2}$. An average of $R(\xi) \Delta E_{\text{free}}$ analogous to Eq. (21) can then be carried out analytically and we obtain $\Delta E^L \simeq 1.4 \Delta E_{\min}^L = 0.25$ MeV.

3. Energy loss to M shells

According to Eqs. (13), (14), (16), and (18) with $\hbar\omega$ =17 eV, the energy loss in a 1- μ m crystal for ⁷⁹Br³³⁺ at 15.6 MeV/u to the valence electrons is 2.25 MeV for a uniform flux distribution and this is therefore the limit for high transverse energy. In a (110) channel, the density of valence electrons is lower than average and hence the energy loss is

lower. The average electron density, as a function of the fraction x of the transverse area available, is shown in Fig. 7 and, as discussed before, the dependence may be approximated by $\overline{\rho}(x) = 1 + 3x$ (electrons/atom), corresponding to the density variation $\rho(x) = 1 + 6x$.

We use this approximation to estimate the reduction for a trajectory in the center of a $\langle 110 \rangle$ channel. The area of a $\langle 110 \rangle$ channel is $\pi r_0^2 = 2 \text{ (Nd)}^{-1}$, since along the $\langle 110 \rangle$ direction there are two strings associated with each channel. The corresponding value of r_0 is 1.82 Å. If we assume the *M*-electron density to be in effect uniform outside this radius, the stopping logarithm is modified to

$$L_e^M = \ln \frac{1.123\hbar v/I_M}{r_0} + \int_0^{r_0^2} \frac{db^2}{8(b^2 + b_0^2/4)} \rho \frac{b^2}{r_0^2} \quad (22)$$

and the reduction in the logarithm becomes

$$\delta L_e^M = -\frac{3}{4} \left[\ln \frac{2r_0}{b_0} - 1 \right], \tag{23}$$

which for 15.6-MeV/u ⁷⁹Br³³⁺ gives $\delta L_e^M = -2.38$ and $\Delta E_{\min}^M \approx 1.46$ MeV. This value is not very sensitive to the approximation for $\rho(x)$ and the same result is obtained with a linear dependence of ρ on $r \propto x^{1/2}$, as applied by L'Hoir *et al.* [7]. If we assume L_e^M to increase linearly with the available area towards the random value, we obtain for $A(\epsilon)/A_0=0.19$ a value $\Delta E^M \approx 1.61$ MeV. Adding the contribution from the *L* shell, we obtain $\Delta E \approx 1.86$ MeV, in almost exact agreement with the experimental value of $\Delta E_{expt}=1.83$ MeV.

We note that the inclusion of the energy loss to L electrons is important for this agreement and that this contribution becomes even more important at higher velocities, where the adiabaticity parameter is smaller. In the analysis of similar experiments with 27-MeV/u Xe ions, L'Hoir et al. [7] disregarded the energy loss to L electrons. The authors of Ref. [7] argued that energy loss to L electrons was unimportant for well-channeled ions because the impact parameters with Si atoms are large compared to the value at which the classical energy transfer to an electron [Eq. (20) with n = t/d=1] equals the L-shell binding energy ($E_L=112$ eV). As discussed by Bohr [21], this argument is incorrect. The classical formula gives the average energy transfer correctly at large impact parameters, also when it is small compared to the minimum energy quantum that can be absorbed by the system. The correct cutoff of energy transfers is at impact parameters $b \sim \hbar v / I$ due to adiabaticity, as discussed above.

4. Energy-loss distribution

The two dominant contributions to straggling in random energy loss (i.e., charge exchange and close collisions with electrons) are both strongly reduced for channeled ions. The charge state is frozen and the electron density experienced by the ions is reduced by nearly an order of magnitude. Hence the width of the energy-loss distribution is completely dominated by the variation in channeling trajectories associated with the uniform distribution of the point of ion impact on the crystal surface. Our assumption that ΔE is a function of transverse energy should be reasonable. We now examine whether the width of the observed ΔE spectrum (Fig. 2) is consistent with this assumption.

We use the random energy-loss windows defined in Fig. 2. With the corrections illustrated in Fig. 6, the energy losses corresponding to the boundaries of the windows are associated with allowed areas for transverse motion of channeled ions and analytical estimates analogous to those discussed above can be carried out. For the intervals I and II, these estimates give widths of ~0.3 MeV, with equal contributions from the *L* and *M* shells to the change in ΔE , in good accord with the experiment. It should be noted, however, that the assumption in these estimates of a circular geometry to the allowed area becomes increasingly unrealistic for increasing transverse energy.

At high transverse energy, the energy loss increases rapidly, mainly due to the energy loss to L electrons, which for random incidence is more than half the total energy loss. The spectrum in Fig. 2 stretches to energy losses considerably larger than for random incidence. This can be understood as an effect of planar blocking: ions with high transverse energy are incident near a string and are blocked by planes containing the string. Hence they are confined to the shoulder regions (relative to planes) and their flux will be higher near strings than would be the case for random incidence.

VI. X-RAY COINCIDENCE DATA

Coincident x-ray spectra for the three $^{79}\text{Br}^{33+}$ bombarding energies 13.7, 15.3, and 17.6 MeV/u (i.e., below, on, and above the KLL resonance, respectively) are shown in Fig. 9. The Br x-rays correspond to well-channeled ions, i.e., to the sum of regions I, II, and III in Fig. 2(a). The spectra have been normalized to the same number of incident 33⁺ ions.

Inspection of Fig. 9 shows that at 17.5 and 13.7 MeV/u [Figs. 9(a) and 9(c), respectively] the $K\alpha$ line is clearly separated from the *L* and *M* radiative electron capture (REC) peaks. At 15.3 MeV/u [Fig. 9(b)] the *L* REC and $K\alpha$ energies coincide and cannot be distinguished experimentally. The three spectra also show that the x-ray yield associated with charge exchange is lower by an order of magnitude above and below the resonance and thus that a considerable amount of the background in the $I(32^+)/I[(32^+)+(33^+)]$ ratio [Fig. 4(a)] is from nonradiative capture.

During replay of the x-ray data we also generated 32^+ particle spectra for those ions which were in coincidence with a Br $K\alpha$ x ray. The results for the three bombarding energies are shown in Fig. 10, again normalized to the same number of incident ions. At 17.6 and 13.7 MeV/u the $K\alpha$ x rays are associated with poorly channeled ions as can be seen in Figs. 10(a) and 10(c), while near the peak of the DR resonance [Fig. 10(b)] the majority of the $K\alpha$ x rays are associated with well-channeled ions.

From the intensities of the lines in the x-ray spectra shown in Fig. 9 we can calculate electron densities using the calculated flux of incident ions and the measured efficiency of the x-ray detector. From the intensities of the REC lines in the spectra taken at the three energies we derive electron densities for well-channeled ions along the $\langle 110 \rangle$ axis of Si as shown in Table III. The Bethe-Salpeter [24] cross section



FIG. 9. X-ray spectra in coincidence with well-channeled $^{79}\text{Br}^{32+}$ ions corresponding to the region encompassed by windows I, II, and III in Fig. 2 for (a) 17.5 MeV/u, (b) 15.3 MeV/u, and (c) 13.7 MeV/u. The spectra have been normalized to the same number of incident $^{79}\text{Br}^{33+}$ ions.

was used in the calculations and we included the sum of the M, N, and O REC calculated cross sections for the lowerenergy REC line. Inspection of Table III shows that good agreement is obtained among the derived values of the electron densities, but the value is about 30% lower than the electron density value of 2.8 ± 0.1 electrons/atom derived from the charged-particle data.

From the intensities of the $K\alpha$ x rays at the three energies we can derive a value for the DR capture probabilities. The values obtained are $(4.6\pm2.0)\times10^{-4}$, $(5.4\pm1.1)\times10^{-3}$, and $(3.0\pm0.6)\times10^{-4}$ at 13.7, 15.3, and 17.5 MeV/u, respectively. The $K\alpha$ yield at 15.3 MeV was corrected for *L* REC by scaling the *M* REC intensity by the ratio of the Bethe-Salpeter [24] REC cross sections. Comparisons of these numbers with the directly measured capture probabilities shown in Fig. 4(b) show that at 15.3 MeV/u, the x-ray data are again about 30% lower. In the work of Andriamonje *et al.* [6] the x-ray data also yielded a value about 30% lower than the particle data. However, because of the uncertainties in efficiency calibration, we, like Andriamonje *et al.*, do not ascribe any significance to these differences.

VII. SUMMARY

We have measured the KLL, DR resonance in electron capture for He-like ⁷⁹Br³³⁺ ions, as an enhancement in the $I(32^+)/I[(32^+)+(33^+)]$ ratio for channeled ions in a thin Si crystal. Through x-ray coincidence measurements below, on, and above the KLL resonance it was confirmed that this

TABLE III. Electron densities (e^{-} /atom) in the Si(110) channel derived from REC x-ray yields assuming the Bethe-Salpeter cross section.

| E (MeV/u) | L REC ^a | M+N+0 REC ^a |
|-----------|--------------------|------------------------|
| 17.5 | 1.9±0.4 | 2.1±0.4 |
| 15.3 | b | 2.1±0.6 |
| 13.7 | 1.5 ± 0.6 | 2.2 ± 0.9 |

^aThe errors include an estimated 15% systematic error (added linearly to the statistical error) in the absolute efficiency calibration (see Sec. II).

^bL REC and $K\alpha$ are unresolved at this energy.

is associated with resonance enhancement in *L* REC when the x-ray energy matches the $K\alpha$ atomic transition.

Using a calculated DR cross section, we determined that the electron density for well-channeled ions along a Si $\langle 110 \rangle$ axis is 2.8±0.1 e^{-1} /atom. Through a detailed study of the energy loss of channeled ions, a variation in electron density across the channel was observed that agrees well with predictions based on x-ray-diffraction measurements.

An analysis of energy-loss processes showed that the measured spectra can be understood from a separation of contributions to the stopping arising from the K, L, and M shells of the Si atoms. Although the M-shell electrons dominate the stopping of well-channeled ions, there is a significant contribution from distant collisions with L-shell electrons.



FIG. 10. Energy-loss spectra for $^{79}\text{Br}^{32+}$ ions in coincidence with Br $K\alpha$ x rays for incident $^{79}\text{Br}^{33+}$ bombarding energies of (a) 17.5 MeV/u, (b) 15.3 MeV/u, and (c) 13.7 MeV/u. The spectra have been normalized to the same number of incident $^{79}\text{Br}^{33+}$ ions.

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