

## Calculation of the weakly coupled 1 and 2 $^1\Pi$ twin states of KRb

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(Received 25 February 1994)

Spectroscopic properties of all excited states of KRb dissociating into  $4s(\text{K})+5s(\text{Rb})$ ,  $4s(\text{K})+5p(\text{Rb})$ , and  $4p(\text{K})+5s(\text{Rb})$  are studied, using quantum chemical calculations. Only the 1 and 2  $^1\Pi$  states showed a weak coupling between the  $4s(\text{K})+5p(\text{Rb})$  and the  $4p(\text{K})+5s(\text{Rb})$  components. The dipole moments, atomic orbital populations, and transition dipole moments of those two states showed a twin nature. Calculated Einstein coefficients for the  $1^1\Pi-X$  and  $2^1\Pi-X$  dipole transitions predict unusually rich band spectra. The intensity distributions of those two transitions showed a remarkable difference.

PACS number(s): 31.20.Di, 31.50.+w, 33.10.Gx

### I. INTRODUCTION

The electronic states of KRb are not well known among the alkali diatomic molecules. The ground-state characteristics were only very recently reported by Ross *et al.* [1], who analyzed laser-induced fluorescence spectra,  $A^1\Sigma^+ \rightarrow X^1\Sigma^+$ , to find the spectroscopic constants covering the ranges  $0 \leq v \leq 44$  and  $J \leq 141$ . Unresolved diffuse bands in the visible region originating from transitions between excited states have been reported by Beuc, Milosevic, and Pichler [2].

One aspect of the excited states of KRb is of particular interest, which is the energetic proximity of the dissociation channels  $4s(\text{K})+5p(\text{Rb})$  and  $4p(\text{K})+5s(\text{Rb})$ . As the energy levels for these two channels are separated by only from 0.028 ( $J=3/2$ ) to 0.050 eV ( $J=1/2$ ) [3], one might expect a strong coupling between these two components (two nonorthogonal basis functions) in the pair of electronically excited states of the same symmetry dissociating into these two channels.

We performed quantum chemical calculations for the ground state and the excited electronic states dissociating into  $4s(\text{K})+5p(\text{Rb})$  and  $4p(\text{K})+5s(\text{Rb})$ . The  $2,3^1\Sigma^+$  pair,  $2,3^3\Sigma^+$  pair, and  $1,2^3\Pi$  pair states showed strong coupling between these two components and this coupling led to large energetic separations within each pair. Only the 1 and 2  $^1\Pi$  states, which will be simply referred to as  $\underline{1}$  and  $\underline{2}$  states hereafter, showed a weak coupling between these two components. In this paper, we report the spectroscopic constants of all electronic states dissociating into  $4s(\text{K})+5s(\text{Rb})$ ,  $4s(\text{K})+5p(\text{Rb})$ , and  $4p(\text{K})+5s(\text{Rb})$  and we analyze the  $\underline{1}$  and  $\underline{2}$  states in particular.

### II. METHOD OF COMPUTATION

The small-core relativistic pseudopotentials of Christiansen and co-workers used to simulate the  $[1s^2/2s^22p^6]$

core of the potassium atom [4] and the  $[1s^2/2s^22p^6/3s^23p^63d^{10}]$  core of rubidium atom [5]. The restricted Hartree-Fock (RHF) calculations were done, using the ASTERIX program package [6]. The configuration-interaction (CI) calculation was done using a program originally written by Brooks and Schaefer [7] and a direct CI program with contractions by Siegbahn [8]. The molecular orbitals resulting from the RHF calculation of  $\text{KRb}^+$  were employed as one-electron basis functions for CI calculations. Only the two valence electrons were correlated for the excited states, because the valence-core effect for the excited states is much smaller than for the ground state. The population analysis was done using the natural molecular orbitals resulting from the CI.

The  $6s6p5d$  Gaussian-type orbitals (GTOs) to best describe the  $4s$ ,  $4p$ , and  $3d$  atomic states of potassium (and  $5s$ ,  $5p$ , and  $4d$  of rubidium) were obtained. Two  $s$  GTOs were added to describe the  $(n+1)s$  state, and one diffuse  $p$  GTO and one diffuse  $d$  GTO were also added. These  $8s7p6d$  GTOs were contracted to  $7s6p4d$  atomic basis functions. Then one  $f$  GTO was added to each atom with exponents 1.119 (K) and 0.8075 (Rb). The  $4s \rightarrow 4p$  (K) and  $5s \rightarrow 5p$  (Rb) excitation energies calculated in the RHF approximation, valence-core CI, the nine-electron ( $9e^-$ ) SDCI, and with Langhoff and Davidson's correction [9] are summarized in Table I. It shows the importance of the valence-core and core-core electron correlation effects for the atomic energies.

The static and transition dipole moments were calculated also using the CI wave functions. The nonadiabatic terms neglected in the Born-Oppenheimer approximation

$$\left\langle \Phi_m(R) \left| -\frac{\hbar^2}{2I} \frac{\partial}{\partial R} R^2 \frac{\partial}{\partial R} \right| \Phi_n(R) \right\rangle,$$

where  $\Phi_m$  and  $\Phi_n$  are the wave functions of electronic states and  $I = \mu R^2$  is the moment of inertia of KRb, were calculated. The ground ( $X$ ) state was calculated in a 14-electron CI including the  $3p(\text{K})$  and  $4p(\text{Rb})$  core electrons. Four configuration-state functions  $(1\sigma)^2$ ,  $(1\sigma^*)^2$ ,  $(1\pi_x)^2$ , and  $(1\pi_y)^2$  were used as the zeroth-order reference. All single and double excitations from that refer-

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TABLE I. Calculated atomic excitation energies  $4s \rightarrow 4p$  (K) and  $5s \rightarrow 5p$  (Rb) in  $\text{cm}^{-1}$ .

	RHF	VCCI <sup>a</sup>	$9e^-$ SDCI	$+Q^b$	Experimental	
					$J = \frac{1}{2}$	$J = \frac{3}{2}$
K( $4s \rightarrow 4p$ )	11 462	12 626	12 696	12 800	12 985	13 043
Rb( $5s \rightarrow 5p$ )	10 833	12 204	12 252	12 381	12 579	12 817
$\Delta E^c$	629	422	444	419	406	226

<sup>a</sup>Valence-core correlation values.

<sup>b</sup> $9e^-$  SDCI with correlation energies according to Langhoff and Davidson [9].

<sup>c</sup>Energy difference between  $\text{K}(4p) + \text{Rb}(5s)$  and  $\text{K}(4s) + (\text{Rb})(5p)$ .

ence function were included in the CI. This multireference (MR) CI calculation gave  $R_e = 4.06 \text{ \AA}$  and  $\omega_e = 70 \text{ cm}^{-1}$ , which are in fairly good agreement with the values of Ross *et al.*,  $R_e = 4.0685 \text{ \AA}$  and  $\omega_e = 75.842 \text{ cm}^{-1}$ . The long-range part of the ground-state potential curve did not agree well with the RKR curve. This disagreement is

due to a size-consistency problem of the MRCI. Comparing the molecular MRCI energies to the atomic MRCI energies gave a dissociation energy of 0.47 eV. It is coincidentally in perfect agreement with an experimental estimate obtained using negative ion photoelectron spectroscopy [10].

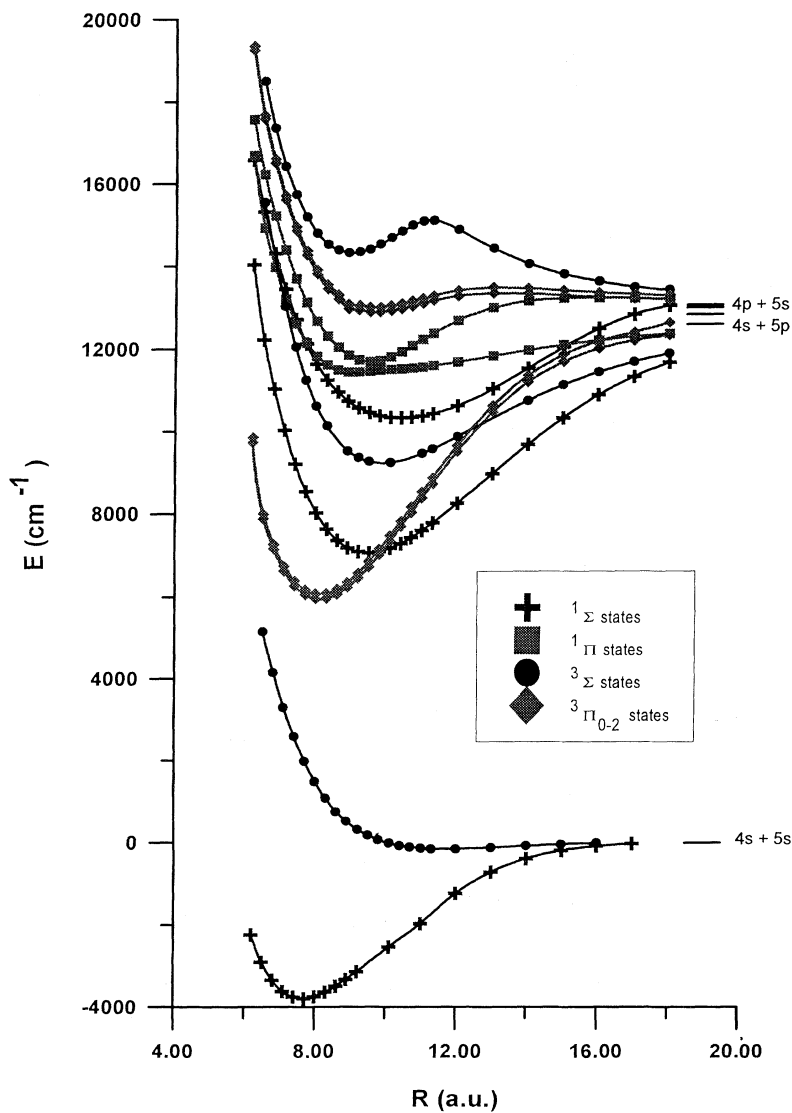


FIG. 1. Potential-energy curves for the electronic states of KRb dissociating into  $4s(\text{K}) + 5s(\text{Rb})$ ,  $4s(\text{K}) + 5p(\text{Rb})$ , and  $4p(\text{K}) + 5s(\text{Rb})$ .

TABLE II. Potential energies ( $\text{cm}^{-1}$ ) of the electronic states of KRb.

$R$ (bohrs)	$1^1\Sigma^+$	$2^1\Sigma^+$	$3^1\Sigma^+$	$1^3\Sigma^+$	$2^3\Sigma^+$	$3^3\Sigma^+$
6.2	-1769	14036	16571	6406	17712	20550
6.5	-2584	12219	15314	5155	15546	18489
6.8	-3162	11030	14302	4148		17352
7.1	-3535	10027	13442	3294	13020	16414
7.4	-3735	9199	12717	2577	12039	15730
7.7	-3792	8534	12118	1977	11240	15188
8.0	-3735	8018	11633	1486	10610	14795
8.3	-3590	7632	11247	1089	10125	14532
8.6	-3381	7360	10950	768		14381
8.9	-3126	7184	10727	516	9515	14319
9.2	-2843	7092	10562	320	9350	14335
9.5	-2546	7066	10450	171	9256	14409
9.8	-2247	7097	10375	59		14530
10.1	-1953	7171	10334	-21	9232	14684
10.4	-1672	7285	10323	-79		14842
10.7	-1410	7426	10334	-116		14989
11.0	-1169	7590	10364	-140	9449	15087
11.3	-947	7773	10417	-154	9561	15103
11.65				-158	9706	15022
12.0	-700	8242	10608	-153	9859	14877
13.0	-414	8958	11019	-121		14416
14.0	-223	9664	11521	-79	10739	14047
15.0	-113	10312	12032	-42	11113	13786
16.0	-50	10869	12478	-13	11426	13608
17.0	-14	11317	12816		11679	13487
18.0		11659	13033		11878	13406
$\infty$	0	12579	12985	0	12579	12985

$R$ (bohrs)	$1^1\Pi$	$2^1\Pi$	$1^3\Pi_0$	$1^3\Pi_2$	$2^3\Pi_0$	$2^3\Pi_2$
6.2	16685	17563	9734	9850	19234	19334
6.5	14932	16216	7877	7993	17571	17671
6.8	13975	15226	7154	7272	16495	16595
7.1	13202	14394	6628	6746	15595	15695
7.4	12599	13698	6268	6386	14855	14957
7.7	12142	13125	6053	6171	14262	14364
8.0	11820	12699	5996	6078	13799	13901
8.3	11609	12311	5966	6090	13450	13552
8.6	11488	12041	6063	6187	13201	13305
8.9	11438	11850	6230	6354	12970	13076
9.2	11438	11734	6451	6579	12937	13043
9.5	11457	11690	6719	6847	12891	13001
9.8	11482	11719	7017	7147	12889	12999
10.1	11493	11806	7339	7469	12917	13041
10.4	11508	11932	7688	7810	12967	13083
10.7	11528	12074	8024	8158	13018	13144
11.0	11554	12223	8374	8510	13092	13212
11.3	11587	12368	8720	8858	13154	13278
12.0	11677	12676	9497	9639	13269	13399
13.0	11820	12983	10456	10606	13332	13464
14.0	11960	13145	11179	11341	13320	13446
15.0	12087	13207	11679	11851	13280	13398
16.0	12193	13220	11999	12181	13238	13348
17.0	12281	13209	12195	12389	13206	13304
18.0	12351	13194	12317	12521	13181	13273
$\infty$	12579	12985	12579	12817	12985	13043

The potential-energy curves, static dipole moment curves, and transition dipole moment curves were fitted with cubic spline functions to find equilibrium spectroscopic constants. The vibrational wave functions for the ground state were calculated using the Rydberg-Klein-Rees (RKR) potential curve of Ross *et al.* [1]. The products of the vibrational wave functions  $W_{(m,v')}(R)$  and  $W_{(n,v'')}(R)$  and the transition dipole moment as a function of the internuclear distance  $\bar{\mu}_{(m \leftarrow n)}(R)$  were numerically integrated to obtain the vibronic transition dipole moment

$$p_{(mv' \leftarrow nv'')}^u = \int_0^\infty dR W_{(n,v'')}^*(R) W_{(m,v')}(R) \bar{\mu}_{(m \leftarrow n)}^u(R),$$

where  $n$  and  $m$  designate the lower and the upper electronic states, respectively,  $v''$  and  $v'$  designate the corresponding vibrational states, and  $u$  represents the  $x, y$ , and  $z$  components. Then the Einstein coefficients of stimulated absorption for vibronic transitions [11] were obtained according to

$$B_{(mv' \leftarrow nv'')} = \frac{\mu_0 c^2}{6\hbar^2} \sum_u \left| p_{(mv' \leftarrow nv'')}^u \right|^2.$$

### III. RESULTS AND DISCUSSION

The calculated potential-energy curves for the  $1^1, 3\Sigma^+$  states dissociating into  $4s(K) + 5s(Rb)$ , the  $2^1, 3\Sigma^+$  and  $1^1, 3\Pi$  states dissociating into  $4s(K) + 5p(Rb)$  and the  $3^1, 3\Sigma^+$  and  $2^1, 3\Pi$  states dissociating into  $4p(K) + 5s(Rb)$  are reported in Table II and Fig. 1. The  $2, 3^1, 3\Sigma^+$  and  $1, 2^3\Pi$  pair states show large splittings in energy. Their wave functions at short and intermediate internuclear distances showed mixtures in large extent of those two atomic characters.

However, the  $\underline{1}, \underline{2}$  pair states show a small splitting in potential energy. The vibrational energy levels of these two states are reported in Fig. 2. These vibrational energy

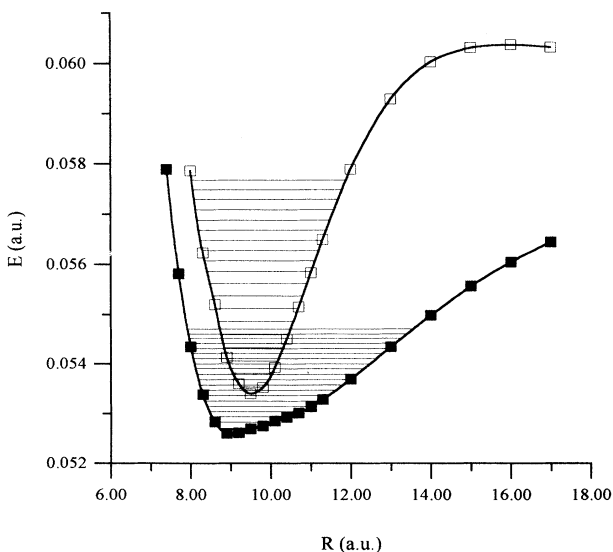


FIG. 2. Potential-energy curves and vibrational energy levels of the  $1$  and  $2^1\Pi$  states.

levels are quite irregular. The lowest vibrational energy levels of the  $\underline{1}$  state are  $G(0)=21$ ,  $G(1)=50$ ,  $G(2)=75$ ,  $G(3)=98$ ,  $G(4)=120$ , and  $G(5)=144 \text{ cm}^{-1}$  and those of the  $\underline{2}$  state are  $G(0)=31$ ,  $G(1)=89$ ,  $G(2)=144$ ,  $G(3)=203$ ,  $G(4)=262$ , and  $G(5)=321 \text{ cm}^{-1}$ . The Dunham-type analyses for these states are rather meaningless. The small splitting of the potential-energy curves for these states over a wide range of internuclear distances implies a weak coupling between these two states. The nonadiabatic correction (see Sec. II) proved to be so small [the diagonal ( $m=n$ ) and coupling ( $m \neq n$ ) terms being less than  $10^{-5}$ ] that it could be neglected. This means that vibrations do not mix these two adiabatic electronic states.

The molecular spectroscopic constants are listed in Table III. Dunham analysis for the  $2^3\Pi$  state did not converge because of its extremely shallow potential-energy well. The CI wave functions analyzed in terms of the atomic-orbital (AO) populations in Figs. 3(a) and 3(b) clearly show the complementary nature of these two  $^1\Pi$  states. The  $\underline{1}$  state is essentially composed of the  $s$  AO of potassium and the  $p_\pi$  AO of rubidium, while the  $\underline{2}$  state is essentially composed of the  $s$  AO of rubidium and the  $p_\pi$  AO of potassium. At  $R \leq 8$  bohrs and  $R \approx 13$  bohrs, however, there occurs substantial mixing between these two basis components.

In contrast, the  $2, 3^1, 3\Sigma^+$  and  $1, 2^3\Pi$  states show mixtures in larger extent (approximately half and half) of the  $4s(K) + 5p(Rb)$  and  $4p(K) + 5s(Rb)$  characters and the AO populations change rather monotonously as a function of the internuclear distance (see Fig. 4).

To understand the strange behavior of the  $\bar{1}$  and  $\bar{2}$  states, one configuration state function (CSF) valence-band (VB) description for these states, i.e., the nonorthogonal  $|4s5p_\pi\rangle$  and  $|5s4p_\pi\rangle$  states, was analyzed. Then the coupling between those states  $\langle 4s5p_\pi | H | 5s4p_\pi \rangle$  reduces to a single integral  $\langle 4s(1)5p_\pi(2) | r_{12}^{-1} | 5s(1)4p_\pi(2) \rangle$ . That integral varies as

TABLE III. Molecular spectroscopic constants.

States	$T_e^a$ ( $\text{cm}^{-1}$ )	$\omega_e$ ( $\text{cm}^{-1}$ )	$R_e$ (pm)
$1^1\Sigma^+$	-3 792	65	405
$2^1\Sigma^+$	7 066	53	502
$3^1\Sigma^+$	10 322	34	549
$1^1\Pi$	11 430	22 <sup>b</sup>	504
$2^1\Pi$	11 690	59 <sup>b</sup>	478
$2^3\Sigma^+$	9 220	47	522
$3^3\Sigma^+$	14 316	62	473
$1^3\Pi_0$	5 951	69	426
$1^3\Pi_1$	6 012	69	426
$1^3\Pi_2$	6 073	69	426
$2^3\Pi_0$	12 886	c	511
$2^3\Pi_1$	12 940	c	511
$2^3\Pi_2$	12 994	c	511

<sup>a</sup>With respect to the energy of  $K(4s) + Rb(5s)$ .

<sup>b</sup>See the text for the  $G_{(v)}$  values.

<sup>c</sup>Dunham's analysis did not converge.

0.025 33, 0.020 49, 0.015 20, 0.008 70, 0.004 77, 0.002 70, and 0.001 40 (in hartree) at 3, 5, 7, 10, 13, 16, and 20 bohrs, respectively. In two-states approximation, the adiabatic electronic states  $|\Phi_1\rangle$  and  $|\Phi_2\rangle$  can be written as

$$|\Phi_1\rangle = c|4s5p_\pi\rangle + d|5s4p_\pi\rangle,$$

$$|\Phi_2\rangle = -d|4s5p_\pi\rangle + c|5s4p_\pi\rangle.$$

The angle defined by  $\varphi = -\arctan(d/c)$  varies as  $51^\circ$ ,  $44^\circ$ ,  $41^\circ$ ,  $39^\circ$ ,  $34^\circ$ ,  $27^\circ$ , and  $18^\circ$  at 3, 5, 7, 10, 13, 16, and 20 bohrs, respectively. It shows the coupling between  $|4s5p_\pi\rangle$  and  $|5s4p_\pi\rangle$  becoming progressively stronger as

the two atoms approach each other. That seems quite contrary to the population analysis. One answer to that disagreement may be found in the inadequacy of representing each of the  $\underline{1}$  and  $\underline{2}$  states by a single VB CSF. A qualitatively identical conclusion is reached when the effective Hamiltonian [12] and the perturbation method up to the second order are used. We are unable to give here a plausible explanation for this strange character of the  $\underline{1}$  and  $\underline{2}$  states.

The dipole moment functions in Fig. 3(c) show that the  $\underline{1}$  state is  $K^{\delta+}Rb^{\delta-}$ , while the  $\underline{2}$  state is  $K^{\delta-}Rb^{\delta+}$  for a wide range of internuclear distances. This is parallel to the analysis of the total populations (the net charge of ei-

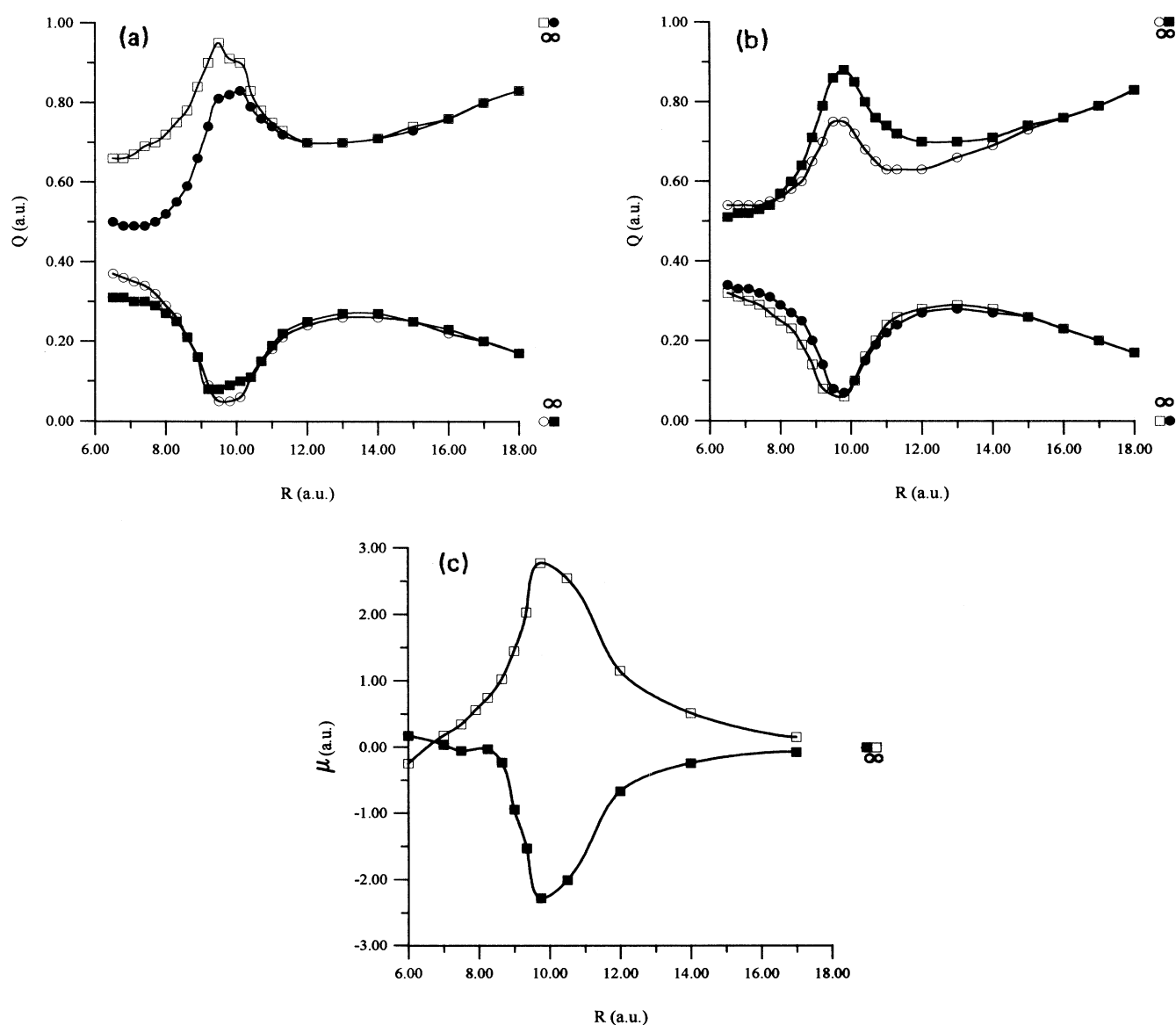


FIG. 3. (a) Population analysis of the wave functions for the  $1^1\Pi$  state and the  $2^1\Pi$  state: filled circle,  $s(K)$ ; filled square,  $p_\pi(K)$ ; empty circle,  $s(Rb)$ ; empty square,  $p_\pi(Rb)$ . (b) Population analysis of the wave functions for the  $2^1\Pi$  state: same as in (a). (c) Dipole moment curves of the  $1^1\Pi$  (filled square) and the  $2^1\Pi$  (empty square).

ther atom is very small). The transition dipole moments  $\underline{1-X}$  and  $\underline{2-X}$ , shown as functions of the internuclear distance in Fig. 5, exhibit remarkably contrasting behavior. As the ground state is principally made of  $4s(\text{K})+5s(\text{Rb})$ , the  $\underline{1-X}$  and  $\underline{2-X}$  transition dipole moments can be decomposed into  $4s(\text{K})\rightarrow 4p_{\pi}(\text{K})$ ,  $5s(\text{Rb})\rightarrow 5p_{\pi}(\text{Rb})$ , and other minor terms. The  $\langle 4s(\text{K})|er_i|4p_i(\text{K})\rangle$  is 3.215 a.u. and the  $\langle 5s(\text{Rb})|er_i|5p_i(\text{Rb})\rangle$  is 3.396 a.u. The largest contributions among the minor terms are the cross integrals  $\langle 4s(\text{K})|er_i|5p_i(\text{Rb})\rangle$  and  $\langle 5s(\text{Rb})|er_i|4p_i(\text{K})\rangle$ . These are about  $\frac{1}{3}$  of the major terms at  $R = 10$  bohrs and about  $\frac{1}{10}$  at  $R = 15$  bohrs. Due to a destructive combination of

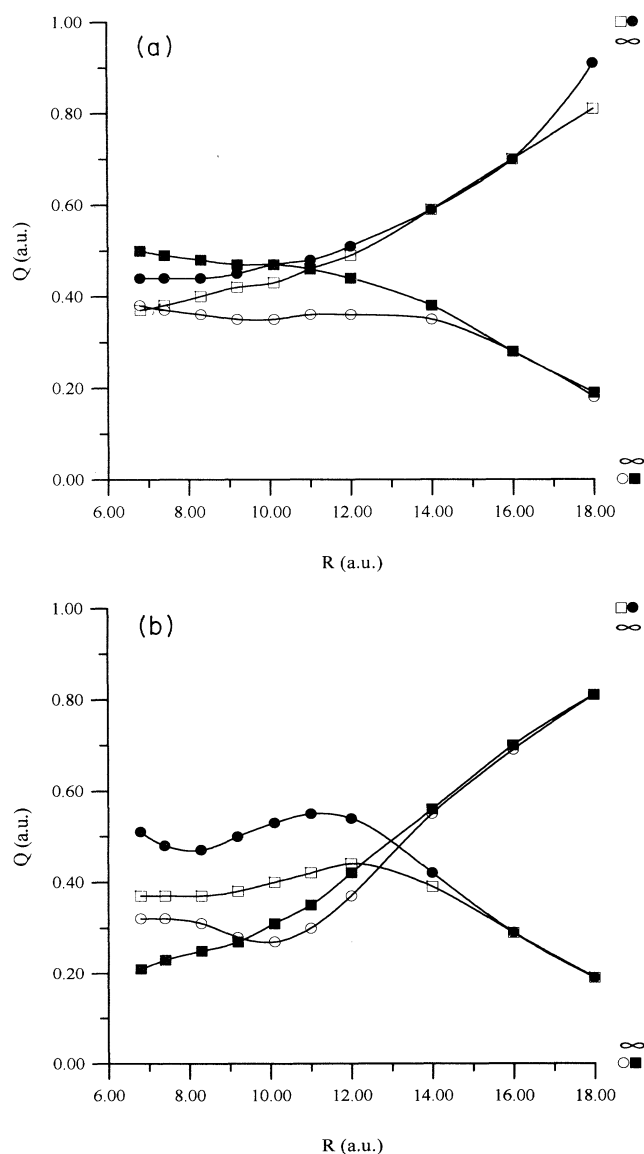


FIG. 4. Population analysis of the wave function for (a) the  $1^3\Pi$  state and (b) the  $2^3\Pi$  state: filled circle,  $s(\text{K})$ ; filled square,  $p_{\pi}(\text{K})$ ; empty circle,  $s(\text{Rb})$ ; empty square,  $p_{\pi}(\text{Rb})$ .

these terms with opposite relative phases, the  $\underline{2-X}$  transition dipole moment is practically zero at short internuclear distances. It increases in the weakly coupled region, then remains nearly constant at longer internuclear distances, and finally converges to the  $4s(\text{K})-4p(\text{K})$  value at long distances. In contrast, the  $\underline{1-X}$  transition dipole moment has relatively large values at short internuclear distances, then decreases in the weakly coupled region, and then slowly converges to the  $5s(\text{Rb})-5p(\text{Rb})$  value at very long (not appearing in Fig. 5) distances due to a much more diffuse nature of the  $5p$  AO in comparison with that of  $4p$ .

The Einstein coefficients for the vibronic transitions  $v'\rightarrow v''$ , where  $v'$  belongs to  $\underline{1}$  or  $\underline{2}$  states and  $v''$  belongs to the  $X^1\Sigma^+$  state, are reported in Fig. 6. This figure shows an unusual characteristic of these transitions. Indeed, both types of transition appear to have significant intensity for a wide range of  $\Delta v = v' - v''$ . The resolution of the (ro)vibronic transition spectra between the  $X$  state and the  $\underline{1}$  and  $\underline{2}$  states may seem extremely complicated due to the proximity of these two states, even though the  $\Delta G_v$  values of the  $\underline{1}$  and  $\underline{2}$  states are quite different. Nevertheless, the two types of transition,  $\underline{1-X}$  and  $\underline{2-X}$  differ in a very striking way. The  $\underline{1-X}$  transition has significant intensities for transitions from or to low  $v''(X)$  vibrational states, except  $v''=0-5$ . In contrast, the  $\underline{2-X}$  transition probabilities from or to low  $v''(X)$  vibrational states are negligible. This is due to different behavior of the two transition dipole moments as functions of internuclear distance (Fig. 5) and the vibrational wave functions of the ground state (Franck-Condon principle), which are concentrated around 7.688 bohrs. It is worth noticing the contrasting patterns between Figs. 6(a) and 6(b) and the presence of a series of belts (set of high-intensity bands) in Fig. 6(a). As a consequence, the most intense bands for

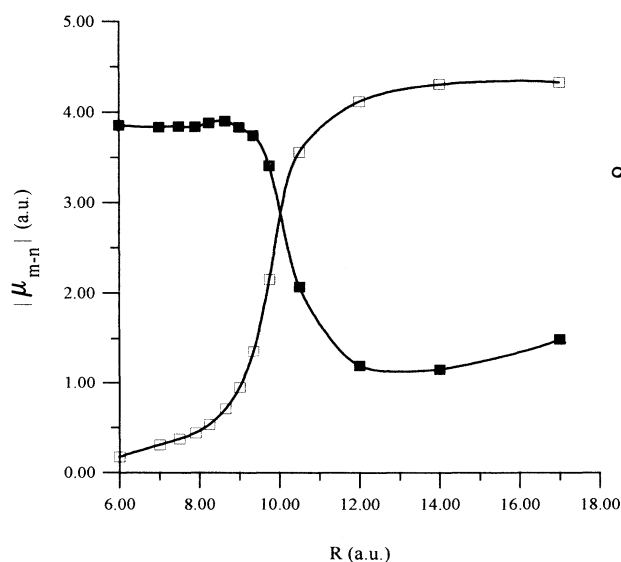


FIG. 5. Transition dipole moment curves:  $1^1\Pi-X$ , filled square;  $2^1\Pi-X$ , empty square.

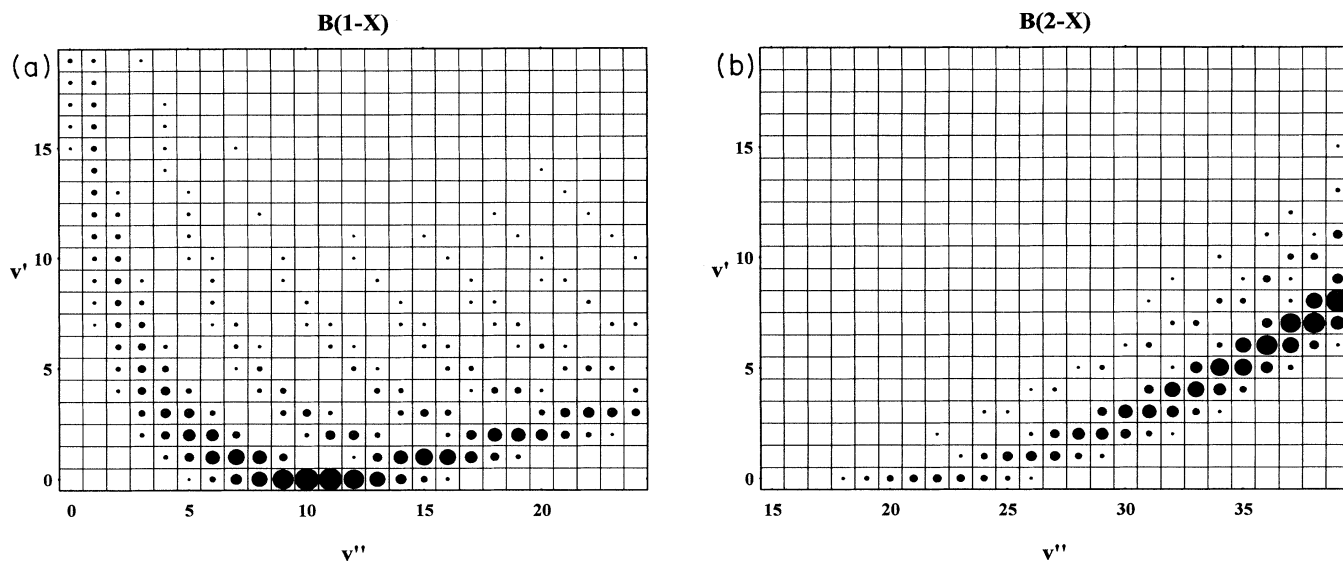


FIG. 6. Einstein coefficients for stimulated emission in  $J^{-1} m^3 s^{-2}$ : (a)  $1^1\Pi-X$ , the largest dot represents  $2.51 \times 10^{20}$  and the smallest represents  $0.302 \times 10^{20}$ ; (b)  $2^1\Pi-X$ , coefficients vary from  $2.12 \times 10^{20}$  to  $0.254 \times 10^{20}$ .

the  $2-X$  transitions appear in longer wavelengths than those of the most intense  $1-X$  transitions, contrary to the order of  $T_e$ 's for these states [13].

Considering limitations of the present calculation, our  $2-1$  transition energies may be off by up to  $300 \text{ cm}^{-1}$  with respect to the real values. However, we believe that the qualitative conclusion regarding the  $1-X$  and  $2-X$  transition intensities remains valid. Unfortunately, no experimental data are available to verify this.

#### ACKNOWLEDGMENTS

The calculation presented in this work was done with the IBM-3090 machine of the CCSC near Strasbourg and the CRAY-2 machine of the CCVR at Palaiseau through a grant from the CNRS. Many interesting discussions with Dr. Amanda Ross are gratefully acknowledged. Laboratoire de Chimie Quantique is UPR-193 of the CNRS.

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- [1] A. J. Ross, C. Effantin, P. Crozet, and E. Boursey, *J. Phys. B* **23**, L247 (1990).  
 [2] R. Beuc, S. Milosevic, and G. Pichler, *J. Phys. B* **17**, 739 (1984).  
 [3] C. E. Moore, *Atomic Energy Levels*, Natl. Bur. Stand. (U.S.) Circ. No. 467 (U.S. GPO, Washington, DC, 1971), Vols. 1-3.  
 [4] M. M. Hurley, L. F. Pacios, P. A. Christiansen, R. B. Ross, and W. C. Ermler, *J. Chem. Phys.* **84**, 6840 (1986).  
 [5] L. A. LaJohn, P. A. Christiansen, R. B. Ross, T. Atashroo, and W. C. Ermler, *J. Chem. Phys.* **87**, 2812 (1987).  
 [6] M.-M. Rohmer, R. Ernenwein, M. Ulmschneider, R. West, and M. Bénard, *Int. J. Quantum Chem.* **40**, 723 (1991); T. Leininger, G. H. Jeung, M. M. Rohmer, and M. Pélissier, *Chem. Phys. Lett.* **190**, 342 (1992).  
 [7] B. R. Brooks and H. F. Schaefer III, *J. Chem. Phys.* **70**, 5092 (1979).  
 [8] P. E. M. Siegbahn, *J. Chem. Phys.* **72**, 1647 (1980).  
 [9] S. R. Langhoff and E. R. Davidson, *Int. J. Quantum Chem.* **8**, 61 (1974).  
 [10] J. G. Eaton, H. W. Sarkas, S. T. Arnold, K. M. McHugh, and K. H. Bowen, *Chem. Phys. Lett.* **193**, 141 (1992).  
 [11] E. Durand, *Mécanique Quantique* (Masson, Paris, 1970), Vol. 1, pp. 572-576.  
 [12] G. Nicolas and P. Durand, *J. Chem. Phys.* **72**, 453 (1980).  
 [13] A. Yiannopoulou, T. Leininger, A. M. Lyyra, and G.-H. Jeung, *Int. J. Quantum Chem.* (to be published).