# Hyperfine quenching of the $1s^2 2s 2p^3 P_0$ level in berylliumlike ions

J. P. Marques and F. Parente

Centro de Física Atómica Instituto National de Investigação Científica e Departamento de Física da Universidade de Lisboa, Avenida Gama Pinto 2, P-1699 Lisboa Codex, Portugal

P. Indelicato

Laboratoire de Physique Atomique et Nucléaire, Boîte 93, Université Pierre et Marie Curie, 4 place Jussieu, F-75252 Paris CEDEX 05, France

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In this paper, we used the multiconfiguration Dirac-Fock method to compute with high precision the  $1s^22s2p$   ${}^3P_1-1s^22s2p$   ${}^3P_0$  separation energy in berylliumlike ions, including the relativistic contribution to electron-electron correlations and radiative corrections. The effect of the hyperfine interaction on both the energy and lifetimes of those levels has been evaluated. In the absence of nuclear magnetic moment the  ${}^3P_0$  level can decay to the ground state only by an E1-M1 transition, with a very low probability. We show that the hyperfine interaction increases dramatically the  ${}^3P_0$ transition probability.

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### I. INTRODUCTION

It has been found before, both theoretically and experimentally, that the hyperfine interaction plays a fundamental role in the lifetimes and energy separations of  $1s2p \ ^{3}P_{0}$  and  $1s2p \ ^{3}P_{1}$  levels in heliumlike ions [1-3]. In those systems, in the region  $Z \approx 45$ , these two levels undergo a level crossing [4] and are nearly degenerate because of magnetic interaction, which leads to the strong influence of the hyperfine interaction on the energy splitting and on the 2  $\ ^{3}P_{0}$  lifetime for isotopes with nonzero nuclear spin.

In this paper we extend our previous calculations to the influence of the hyperfine interaction on the  $1s^{2}2s^{2}p$ levels in berylliumlike ions. The energy level diagram for berylliumlike Xe is shown in Fig. 1. In these systems a level crossing of the  ${}^{3}P_{0}$  and  ${}^{3}P_{1}$  levels has not been found. One-photon transitions from the 2  ${}^{3}P_{0}$  to the ground state are forbidden, multiphoton transitions have been found to be negligible, and therefore the lifetime of this level may be considered infinite to a very good approximation. The energy separation between 2  ${}^{3}P_{0}$  and 2  ${}^{3}P_{1}$  levels is very small for low values of Z and increases very rapidly with Z. However, hyperfine interaction still has a strong influence on the energy splitting and on the 2  ${}^{3}P_{0}$  lifetime for isotopes with nonzero nuclear spin. On the other hand, the  ${}^{3}P_{2}$  level is very close to the  ${}^{3}P_{0}$  and  ${}^{3}P_{1}$  levels for low values of Z.

The different steps of this calculation are described in Refs. [1,5]. Here we will emphasize only the fundamental topics of the theory and the characteristic features of berylliumlike systems.

The multiconfiguration Dirac-Fock method [6, 7] (MCDF) is used to evaluate the  $1s^22s2p$  fine-structure separation  $\Delta E_{0;FS} = E_{^3P_1} - E_{^3P_0}$ . Several terms, such as the nonrelativistic contribution to the correlation, are the same for both levels. In this paper we calculate residual terms, including Breit interaction, one-particle

self-energy and vacuum polarization, and two-electron radiative corrections using the method described in [1, 6-8]. The MCDF method, in principle, allows for precise calculations, because it can include most of the correlation relatively easily, i.e., with a small number of configurations. Here correlation is important in the determination of transition energies to the ground state, which are used in the calculation of transition probabilities. The largest effect is obtained by using  $1s^22s^2$ ,  $1s^22p_{1/2}^2$ , and  $1s^22p_{3/2}^2$  as the configuration set for the ground state. For the  $1s^22s2p$   $^3P_J$  energy, no correlation was included because it has a very small contribution to the transition probability, and because  $\Delta E_{0;FS}$ , which is

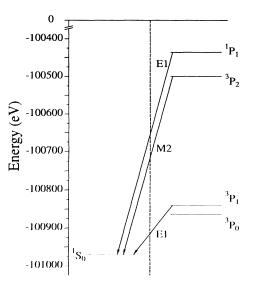


FIG. 1. Energy level and transitions diagram for berylliumlike xenon (Z = 54).

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the important parameter in the calculation of the hyperfine quenching, is not very sensitive to correlation: the main contribution to the correlation in that case is the nonrelativistic contribution, which is J invariant in the nonrelativistic case. Because of the preceding considerations, we have used respectively only three configuration state functions (CSF) ( $|1s^22s^2 J = 0\rangle$ ,  $|1s^22p_{1/2}^2 J = 0\rangle$ , and  $|1s^2 2p_{3/2}^2 J = 0\rangle$ ) for the ground state and only one CSF ( $|1s^22s2p_{1/2} J = 0\rangle$ ), and two ( $|1s^22s2p_{1/2} J = 1\rangle$ ,  $(|1s^22s^2p_{3/2} J = 1\rangle)$  for the excited states. The same set of CSF have been used for energy, transition probabilities, and for hyperfine matrix elements calculations. In our previous work on a heliumlike system we had also used single CSF for transition probabilities and hyperfine matrix elements calculations, but we did a very complete calculation of correlation energy for all three levels  $1s^2$ and  $1s2p {}^{3}P_{J}$ . This calculation has shown us that correlation contribution to the fine-structure separation  $\Delta E_{0;\text{FS}}$ was very small indeed. There are very recent calculations of correlation in  $1s^22s2p \ ^3P_1 \rightarrow 1s^22s^2 \ ^1S_0$  transitions in Fe and Mo [9], using relativistic many-body perturbation theory. Still, no evaluation of  $\Delta E_{0:FS}$  has been done in Ref. [9] that we could use to test more precisely the accuracy of our calculation.

Finally we would like to point out that all energy cal-

culations are done in the Coulomb gauge for the retarded part of the electron-electron interaction, to avoid spurious contributions (see, for example, Refs. [8, 10]). The lifetime calculations are all done using exact relativistic formulas. The length gauge has been used for all transition probabilities.

### II. RELATIVISTIC CALCULATION OF HYPERFINE CONTRIBUTION TO FINE-STRUCTURE SPLITTING AND TO TRANSITION PROBABILITIES

In the case of a nucleus with nonzero spin, the hyperfine interaction between the nucleus and the electrons must be taken into account. The correspondent Hamiltonian can be written as

$$H_{\rm HFS} = \sum_{k} \mathbf{M}^{(k)} \cdot \mathbf{T}^{(k)}, \qquad (2.1)$$

where  $\mathbf{M}^{(k)}$  and  $\mathbf{T}^{(k)}$  are spherical tensors of rank k, representing, respectively, the nuclear and the atomic parts of the interaction. As in the case of heliumlike ions, the only sizable contribution from Eq. (2.1) is the magnetic dipole term (k = 1). The contribution of this interaction for the total energy has been evaluated through the diagonalization of the following matrix, for  $F = \frac{1}{2}$ :

$$H_{\text{tot}} = \begin{bmatrix} E_1 + \frac{1}{2}i\Gamma_1 + W(1,1) & W(1,2) & W(1,3) \\ W(2,1) & E_2 + \frac{1}{2}i\Gamma_2 + W(2,2) & W(2,3) \\ W(3,1) & W(3,2) & E_3 + \frac{1}{2}i\Gamma_3 + W(3,3) \end{bmatrix}.$$
(2.2)

Here,  $E_f$  is the unperturbed level energy and  $\Gamma_f$  is the radiative width of the unperturbed level  $(f = 1-3 \text{ stands}, \text{respectively, for } {}^3P_0, {}^3P_1, {}^1P_1)$ . A similar matrix must be diagonalized, for  $F = \frac{3}{2}$ , with the  ${}^3P_0$  level replaced by  ${}^3P_2$ .  $W(f, f') = \langle 1s^22s2p \ f | H_{\text{HFS}} | 1s^22s2p \ f' \rangle$  is the unperturbed hyperfine matrix element. This quantity may be written as

$$W(J_1, J_2) = \langle I, J_1, F, M_F | \mathbf{M}^{(1)} \cdot \mathbf{T}^{(1)} | I, J_2, F, M_F \rangle,$$
(2.3)

where I is the nuclear spin and F the total angular momentum of the atom, and may be set in the form

$$W(J_1, J_2) = (-1)^{I+J_1+F} \left\{ \begin{matrix} I & J_1 & F \\ J_2 & I & 1 \end{matrix} \right\} \\ \times \langle I || \mathbf{M}^{(1)} || I \rangle \langle J_1 || \mathbf{T}^{(1)} || J_2 \rangle.$$
(2.4)

The 6j symbol leads to W(0,0) = 0. Also the nuclear magnetic moment  $\mu_I$  in units of the nuclear magneton  $\mu_N$  may be defined by

$$\mu_I \mu_N = \langle I || \mathbf{M}^{(1)} || I \rangle \begin{pmatrix} I & 1 & I \\ -I & 0 & I \end{pmatrix}, \qquad (2.5)$$

with  $\mu_N = e\hbar/(m_p c)$ .

The electronic matrix elements were evaluated on the

basis set

$$|{}^3P_0
angle, |{}^3P_1
angle, |{}^1P_1
angle, |{}^3P_2
angle$$

with

$$\begin{split} |{}^{3}P_{0}\rangle &= |1s^{2}2s2p_{1/2} \ J = 0\rangle, \\ |{}^{3}P_{1}\rangle &= \alpha |1s^{2}2s2p_{1/2} \ J = 1\rangle + \beta |1s^{2}2s2p_{3/2} \ J = 1\rangle, \\ |{}^{1}P_{1}\rangle &= \beta |1s^{2}2s2p_{1/2} \ J = 1\rangle - \alpha |1s^{2}2s2p_{3/2} \ J = 1\rangle, \\ |{}^{3}P_{2}\rangle &= |1s^{2}2s2p_{3/2} \ J = 2\rangle. \end{split}$$

Electron correlation was neglected in the evaluation of matrix elements because its effect is small compared to available experimental precision. Upon diagonalization of the total energies matrix (2.2) for  $F = \frac{1}{2}$  and  $F = \frac{3}{2}$ , for a few values of Z, we found that the influence of the  ${}^{1}P_{1}$  and  ${}^{3}P_{2}$  levels on the lifetimes of the  ${}^{3}P_{0}$  and  ${}^{3}P_{1}$  is negligible; therefore, instead of the matrix (2.2) we limited ourselves to the following smaller matrix, replacing  ${}^{3}P_{0}$  by 0 and  ${}^{3}P_{1}$  by 1:

$$H_{\text{tot}} = \begin{bmatrix} E_0 + \frac{1}{2}i\Gamma_0 + W(0,0) & W(1,0) \\ W(0,1) & E_1 + \frac{1}{2}i\Gamma_1 + W(1,1) \end{bmatrix}.$$
(2.6)

The final result is then obtained by a diagonalization

of the  $2 \times 2$  matrix in Eq. (2.6), the real part of each eigenvalue being the energy of the correspondent level and the imaginary part its lifetime.

## **III. RESULTS AND DISCUSSION**

The method outlined in Sec. II has been used to evaluate the influence of the hyperfine interaction on both the  $1s^22s2p$   ${}^3P_0$  and  ${}^3P_1$  levels for all Z between 5 and 92 and for all stable and some quasistable isotopes of nonzero spin. Terms coming from higher multipoles have been found to be negligible.

A detailed list of the contributions to the theoretical  $1s^22s2p$   ${}^3P_0$  and  ${}^3P_1$  level energies is presented in Table I for Z = 6, 36, 54, 82. In Table II we present, for all possible values of the nuclear spin I, as a function of Z, the unperturbed separation energies  $\Delta E_0$ , the diagonal and off-diagonal hyperfine matrix elements W(1,1) and W(1,0), the magnetic dipole moments [11]  $\mu_i$ , and the separation energies  $\Delta E_{\rm HF}$  which are the difference of the eigenvalues of Eq. (2.6). In Fig. 2 is plotted the difference of  $E = \Delta E_{\rm HF} - \Delta E_0$  for the different nuclear spins. The influence of the hyperfine interaction on this energy is shown to increase slowly with Z.

In Table III we present, for all possible values of the nuclear spin I, as a function of Z, the perturbed  $1s^22s2p\ ^3P_0$  lifetime  $\tau_0$  (the unperturbed  $\tau_0$  is infinite in first approximation) and the  $1s^22s2p\ ^3P_1$  lifetime  $\tau_1$  which is not affected, within the precision shown by the hyperfine interaction. In Fig. 3 is plotted the perturbed  $1s^22s2p\ ^3P_0$  lifetime for the different nuclear spins I, as a function of Z. One can see that the opening of a new channel for the

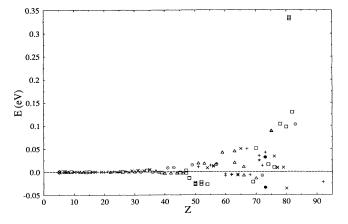


FIG. 2. Influence of the hyperfine interaction on the  $1s^2 2s 2p \ {}^{3}P_1 - 1s^2 2s 2p \ {}^{3}P_0$  energy separation, as a function of the nuclear spin I and the atomic number Z. The quantity  $E = \Delta E_{\rm HF,I} - \Delta E_0$  is the contribution of the hyperfine interaction to the fine-structure splitting  $\Delta E_0$ . The symbols  $\Box$ ,  $\times$ ,  $\Delta$ , +,  $\odot$ , \*,  $\diamondsuit$ ,  $\circ$ ,  $\star$ , and  $\bullet$  represent values for isotope with nuclear spin I of  $\frac{1}{2}$ ,  $\frac{3}{2}$ ,  $\frac{5}{2}$ ,  $\frac{7}{2}$ ,  $\frac{9}{2}$ , 1, 3, 5, 7, and 9, respectively. Some elements have several isotopes with identical spins but different  $\mu_i$ .

decay of the  $1s^22s2p$  <sup>3</sup> $P_0$  has a dramatic effect on its lifetime. This can be seen in the case of lead, for example. Using our transition probability code, we made a rough estimate of the E1-M1 transition rate. We included only the first few excited states and neglected possible resonant structure. The integrated rate we have obtained is

TABLE I. Contribution to the energy of the  $1s^2 2s 2p {}^3P_1$  and  $1s^2 2s 2p {}^3P_0$  levels (Z = 6, 36, 54, 82) and to the fine-structure separation  $\Delta E_0$ . All energies are in eV.

	${}^{3}P_{1}$	<sup>3</sup> P <sub>0</sub>	$\Delta E_0$	<sup>3</sup> P <sub>1</sub>	<sup>3</sup> P <sub>0</sub>	$\Delta E_0$
		Z = 6			Z = 36	
Coulomb energy	-986.418	-986.422	0.004	-43283.963	-43295.035	11.071
Magnetic energy	0.075	0.076	-0.001	21.956	22.495	-0.539
Lowest-order retardation $(\Delta \omega^2)$	-0.001	-0.001	0.000	-0.756	-0.755	0.000
High-order retardation $(\Delta \omega^n, n > 2)$	0.000	0.000	0.000	-0.003	0.001	-0.004
Self-energy	0.054	0.054	0.000	27.576	27.564	0.012
Self-energy screening	-0.007	-0.007	0.000	-0.750	-0.744	-0.005
Vacuum polarization $\alpha(Z\alpha)$	-0.002	-0.002	0.000	-2.816	-2.816	0.001
Vacuum polarization $\alpha(Z\alpha)^3$	0.000	0.000	0.000	0.032	0.032	0.000
Vacuum polarization $\alpha^2(Z\alpha)$	0.000	0.000	0.000	-0.023	-0.023	0.000
Total energy	-986.300	-986.303	0.003	-43238.747	-43249.282	10.535
		Z = 54			Z = 82	
Coulomb energy	-101009.779	-101034.668	24.889	-250750.523	-250795.364	44.841
Magnetic energy	78.288	79.965	-1.677	302.464	309.802	-7.338
Lowest-order retardation $(\Delta \omega^2)$	-2.727	-2.725	-0.002	-10.271	-10.268	-0.003
High-order retardation $(\Delta \omega^n, n > 2)$	0.012	0.016	-0.004	0.374	0.375	-0.001
Self-energy	109.782	109.776	0.007	494.333	494.332	0.001
Self-energy screening	-2.200	-2.174	-0.026	-8.225	-8.123	-0.102
Vacuum polarization $\alpha(Z\alpha)$	-15.418	-15.421	0.004	-109.010	-109.032	0.022
Vacuum polarization $\alpha (Z\alpha)^3$	0.347	0.347	0.000	4.608	4.609	-0.001
Vacuum polarization $\alpha^2(Z\alpha)$	-0.122	-0.122	0.000	-0.840	-0.841	0.000
Total energy	-100841.815	-100865.006	23.191	-250077.090	-250114.509	37.419

TABLE II. Influence of the hyperfine interaction on the  $1s^22s2p \, {}^{3}P_1 - 1s^22s2p \, {}^{3}P_0$  energy separation, as a function of the nuclear spin *I* and the atomic number *Z*. The unperturbed energy separation is  $\Delta E_0$  (eV) and  $\Delta E_{\rm HF}$  (eV) is the energy when the hyperfine interaction is taken into account. The hyperfine matrix elements W(1,0) and W(1,1) from Eq. (2.6) are given in eV and the nuclear magnetic moment  $\mu_i$  is given in nuclear magneton units.

	Z	A	$\Delta E_0$	$\Delta E_{ m HF}$		W(1,1)	$\mu_i$
	6	13	0.003	0.003	$-4.708 \times 10^{-06}$	$6.044 \times 10^{-06}$	0.7024118
	7	15	0.008	0.008	$3.384 \times 10^{-06}$	$-4.563 \times 10^{-06}$	-0.28318884
	9	19	0.032	0.032	$-7.700 \times 10^{-05}$	$1.105 \times 10^{-04}$	2.628868
	14	29	0.289	0.289	$7.322 \times 10^{-05}$	$-1.148 \times 10^{-04}$	-0.55529
	15	31	0.397	0.398	$-1.882 \times 10^{-04}$	$2.995 \times 10^{-04}$	1.13160
	26	57	3.862	3.863	$-9.926 \times 10^{-05}$	$1.868 \times 10^{-04}$	0.09044
	34	77	9.060	9.063	$-1.533 \times 10^{-03}$	$3.181 \times 10^{-03}$	0.5350422
	39	89	12.775	12.774	$6.466 \times 10^{-04}$	$-1.389 \times 10^{-03}$	-0.13741542
	45	103	17.160	17.159	$7.006 \times 10^{-04}$	$-1.540 \times 10^{-03}$	-0.08840
	47	103	18.563	18.561	$1.057 \times 10^{-03}$	$-2.334 \times 10^{-03}$	-0.113570
			18.563		$-1.215 \times 10^{-03}$	$2.683 \times 10^{-03}$	0.130563
	47	109		18.566	$5.986 \times 10^{-03}$	$-1.324 \times 10^{-02}$	
	48	111	19.251	19.238	$5.986 \times 10^{-03}$		-0.59488607
	48	113	19.251	19.237	$6.262 \times 10^{-03}$	$-1.385 \times 10^{-02}$	-0.62230092
	50	115	20.601	20.577	$1.077 \times 10^{-02}$	$-2.390 \times 10^{-02}$	-0.91883
	50	117	20.601	20.575	$1.174 \times 10^{-02}$	$-2.604 \times 10^{-02}$	-1.00104
	50	119	20.601	20.573	$1.228 \times 10^{-02}$	$-2.725 \times 10^{-02}$	-1.04728
	52	123	21.914	21.891	$1.002 \times 10^{-02}$	$-2.229 \times 10^{-02}$	-0.7369478
	52	125	21.914	21.887	$1.208 \times 10^{-02}$	$-2.687 \times 10^{-02}$	-0.88850513
	54	129	23.191	23.164	$1.222 \times 10^{-02}$	$-2.724 \times 10^{-02}$	-0.7779763
	69	169	31.681	31.658	$9.887 \times 10^{-03}$	$-2.225 \times 10^{-02}$	-0.2316
	70	171	32.179	32.230	$-2.244 \times 10^{-02}$	$5.054 \times 10^{-02}$	0.49367
	74	183	34.085	34.101	$-6.875 \times 10^{-03}$	$1.553 \times 10^{-02}$	0.11778476
	74	183	34.982	34.992	$-4.274 \times 10^{-03}$	$9.673 \times 10^{-03}$	0.06465189
					$-4.559 \times 10^{-02}$	$1.034 \times 10^{-01}$	
	78	195	35.838	35.942	-4.559×10		0.60952
	80	199	36.652	36.749	$-4.279 \times 10^{-02}$	$9.731 \times 10^{-02}$	0.50588549
	81	203	37.041	37.373	$-1.459 \times 10^{-01}$	$3.324 \times 10^{-01}$	1.62225787
	81	205	37.041	37.376	$-1.474 \times 10^{-01}$	$3.356 \times 10^{-01}$	1.63821461
	82	207	37.419	37.548	$-5.669 \times 10^{-02}$	$1.293 \times 10^{-01}$	0.592583
	5	11	0.001	0.001	$-6.498 \times 10^{-06}$	$3.461 \times 10^{-06}$	2.6886489
	10	21	0.056	0.056	$2.080 \times 10^{-05}$	$-1.365 \times 10^{-05}$	-0.661797
	11	23	0.090	0.090	$-9.654 \times 10^{-05}$	$6.457 \times 10^{-05}$	2.2175219
	16	33	0.532	0.532	$-9.915 \times 10^{-05}$	$7.161 \times 10^{-05}$	0.6438212
	17	35	0.696	0.696	$-1.553 \times 10^{-04}$	$1.138 \times 10^{-04}$	0.8218743
	17	37	0.696	0.696	$-1.293 \times 10^{-04}$	$9.473 \times 10^{-05}$	0.6841236
	19	39	1.125	1.125	$-1.079 \times 10^{-04}$	$8.145 \times 10^{-05}$	0.39146616
	19	41	1.125	1.125	$-5.920 \times 10^{-05}$	$4.470 \times 10^{-05}$	0.21487009
		53	2.876	2.876	$2.929 \times 10^{-04}$	$-2.391 \times 10^{-04}$	-0.47454
	24				$2.929 \times 10^{-04}$ 7.984×10 <sup>-04</sup>	$-6.914 \times 10^{-04}$	-0.75002
	28	61	4.999	4.998	7.984×10	$-0.914 \times 10$	
	29	63	5.616	5.618	$-2.687 \times 10^{-03}$	$2.359 \times 10^{-03}$	2.2273456
	29	65	5.616	5.619	$-2.873 \times 10^{-03}$	$2.522 \times 10^{-03}$	2.38161
	31	69	6.934	6.936	$-3.090 \times 10^{-03}$	$2.780 \times 10^{-03}$	2.016589
	31	71	6.934	6.937	$-3.926 \times 10^{-03}$	$3.532 \times 10^{-03}$	2.562266
	33	75	8.336	8.338	$-2.761 \times 10^{-03}$	$2.538 \times 10^{-03}$	1.439475
	35	79	9.794	9.798	$-4.996 \times 10^{-03}$	$4.675 \times 10^{-03}$	2.106400
	35	81	9.794	9.799	$-5.385 \times 10^{-03}$	$5.039 \times 10^{-03}$	2.270562
	54	131	23.191	23.199	$-8.099 \times 10^{-03}$	$8.075 \times 10^{-03}$	0.6918619
	56	135	24.433	24.444	$-1.130 \times 10^{-02}$	$1.128 \times 10^{-02}$	0.837943
	56	137	24.433	24.445	$-1.264 \times 10^{-02}$	$1.262 \times 10^{-02}$	0.937365
	64	155	29.059	29.054	$5.937 \times 10^{-03}$	$-5.957 \times 10^{-03}$	-0.25723
	64	157	29.059	29.052	$7.784 \times 10^{-03}$	$-7.811 \times 10^{-03}$	-0.33726
			29.600	29.650	$-4.961 \times 10^{-02}$	$4.980 \times 10^{-02}$	2.014
	65 76	159			$-4.961 \times 10$ $-3.252 \times 10^{-02}$	$4.980 \times 10$ $3.291 \times 10^{-02}$	2.014 0.659933
	76	189	34.982	35.015	-3.252×10	$3.291 \times 10^{-03}$ $8.003 \times 10^{-03}$	
	77	191	35.415	35.423	$-7.899 \times 10^{-03}$		0.1507
	77	193	35.415	35.424	$-8.580 \times 10^{-03}$	$8.693 \times 10^{-03}$	0.1637
	79	197	36.251	36.260	$-8.786 \times 10^{-03}$	$8.922 \times 10^{-03}$	0.148158
	80	201	36.652	36.616	$3.532 \times 10^{-02}$	$-3.592 \times 10^{-02}$	-0.56023

	TABLE II. (Continued).								
Ι	Z	A	$\Delta E_0$	$\Delta E_{ m HF}$	W(1,0)	W(1,1)	$\mu_i$		
<u>5</u> 2	8	17	0.017	0.017	$2.503 \times 10^{-05}$	$-1.024 \times 10^{-05}$	-1.89379		
2	12	<b>25</b>	0.139	0.139	$4.587 \times 10^{-05}$	$-2.042 \times 10^{-05}$	-0.85545		
	13	27	0.204	0.204	$-2.556 \times 10^{-04}$	$1.156 \times 10^{-04}$	3.64150687		
	22	47	2.052	2.052	$3.294 \times 10^{-04}$	$-1.706 \times 10^{-04}$	-0.78848		
	25	55	3.349	3.351	$-2.264 \times 10^{-03}$	$1.229 \times 10^{-03}$	3.4687190		
	30	67	6.262	6.263	$-1.093 \times 10^{-03}$	$6.359 \times 10^{-04}$	0.8752049		
	37	85	11.281	11.283	$-3.595 \times 10^{-03}$	$2.235 \times 10^{-03}$	1.3533515		
	40	91	13.520	13.517	$4.593 \times 10^{-03}$	$-2.904 \times 10^{-03}$	-1.30362		
	42	95	14.995	14.993	$3.845 \times 10^{-03}$	$-2.452 \times 10^{-03}$	-0.9142		
	42	97	14.995	14.993	$3.926 \times 10^{-03}$	$-2.504 \times 10^{-03}$	-0.9335		
	44	99	16.446	16.444	$3.197 \times 10^{-03}$	$-2.052 \times 10^{-03}$	-0.6413		
	44	101	16.446	16.444	$3.583 \times 10^{-03}$	$-2.300 \times 10^{-03}$	-0.7188		
	46	105	17.866	17.863	$3.770 \times 10^{-03}$	$-2.432 \times 10^{-03}$	-0.642		
	51	121	21.262	21.281	$-2.902 \times 10^{-02}$	$1.888 \times 10^{-02}$	3.3634		
	53	127	22.557	22.575	$-2.810 \times 10^{-02}$	$1.832 \times 10^{-02}$	2.813273		
	59	141	26.231	26.273	$-6.494 \times 10^{-02}$	$4.253 \times 10^{-02}$	4.2754		
	63	151	28.510	28.555	$-6.881 \times 10^{-02}$	$4.517 \times 10^{-02}$	3.4717		
	63	153	28.510	28.530	$-3.038 \times 10^{-02}$	$1.995 \times 10^{-02}$	1.5330		
	66	161	30.133	30.125	$1.157 \times 10^{-02}$	$-7.607 \times 10^{-03}$	-0.4803		
	66	163	30.133	30.144	$-1.620 \times 10^{-02}$	$1.065 \times 10^{-02}$	0.6726		
	70	173	32.179	32.165	$2.112 \times 10^{-02}$	$-1.392 \times 10^{-02}$	-0.67989		
	75	185	34.538	34.627	$-1.353 \times 10^{-01}$	$8.955 \times 10^{-02}$	3.1871		
	75	187	34.538	34.628	$-1.367 \times 10^{-01}$	$9.047 \times 10^{-02}$	3.2197		
$\frac{7}{2}$	20	43	1.394	1.394	$3.799 \times 10^{-04}$	$-1.421 \times 10^{-04}$	-1.317643		
-	<b>21</b>	45	1.703	1.703	$-1.621 \times 10^{-03}$	$6.162 \times 10^{-04}$	4.7564866		
	22	49	2.052	2.052	$4.420 \times 10^{-04}$	$-1.706 \times 10^{-04}$	-1.10417		
	23	51	2.443	2.444	$-2.405 \times 10^{-03}$	$9.432 \times 10^{-04}$	5.14870573		
	27	59	4.413	4.415	$-3.800 \times 10^{-03}$	$1.584 \times 10^{-03}$	4.627		
	51	123	21.262	21.272	$-2.109 \times 10^{-02}$	$1.022 \times 10^{-02}$	2.5498		
	55	133	23.816	23.830	$-2.852 \times 10^{-02}$	$1.388 \times 10^{-02}$	2.5829128		
	57	139	25.041	25.058	$-3.533 \times 10^{-02}$	$1.722 \times 10^{-02}$	2.7830455		
	60	143	26.813	26.805	$1.658 \times 10^{-02}$	$-8.100 \times 10^{-03}$	-1.065		
	60	145	26.813	26.808	$1.022 \times 10^{-02}$	$-4.989 \times 10^{-03}$	-0.656		
	62	147	27.953	27.946	$1.449 \times 10^{-02}$	$-7.086 \times 10^{-03}$	-0.8148		
	62	149	27.953	27.947	$1.194 \times 10^{-02}$	$-5.841 \times 10^{-03}$	-0.6717		
	67	165	30.657	30.707	$-1.026 \times 10^{-01}$	$5.034 \times 10^{-02}$	4.173		
	68	167	31.173	31.166	$1.480 \times 10^{-02}$	$-7.259 \times 10^{-03}$	-0.56385		
	71	175	32.669	32.704	$-7.095 \times 10^{-02}$	$3.488 \times 10^{-02}$	2.23799		
	72	177	33.150	33.163	$-2.678 \times 10^{-02}$	$1.318 \times 10^{-02}$	0.7935		
	73	181	33.622	33.664	$-8.516 \times 10^{-02}$	$4.194 \times 10^{-02}$	2.3705		
	92	235	40.399	40.376	$4.395 \times 10^{-02}$	$-2.241 \times 10^{-02}$	-0.38		
<u>9</u> 2	32	73	7.626	7.626	$1.293 \times 10^{-03}$	$-4.580 \times 10^{-04}$	-0.8794677		
	36	83	10.535	10.534	$2.182 \times 10^{-03}$	$-8.011 \times 10^{-04}$	-0.970669		
	38	87	12.028	12.027	$2.989 \times 10^{-03}$	$-1.112 \times 10^{-03}$	-1.0936030		
	41	93	14.260	14.269	$-2.222 \times 10^{-02}$	$8.390 \times 10^{-03}$	6.1705		
	43	99	15.724	15.734	$-2.435 \times 10^{-02}$	$9.262 \times 10^{-03}$	5.6847		
	49	113	19.930	19.945	$-3.836 \times 10^{-02}$	$1.479 \times 10^{-02}$	5.5289		
	49	115	19.930	19.945	$-3.844 \times 10^{-02}$	$1.483 \times 10^{-02}$	5.5408		
	72	179	33.150	33.142	$2.109 \times 10^{-02}$	$-8.277 \times 10^{-03}$	-0.6409		
	83	209	37.784	37.886	$-2.669 \times 10^{-01}$	$1.061 \times 10^{-01}$	4.1106		
1	7	14	0.008	0.008	$-3.939 \times 10^{-06}$	$3.253 \times 10^{-06}$	0.40376100		
3	5	10	0.001	0.001	$-3.892 \times 10^{-06}$	$1.159 \times 10^{-06}$	1.80064475		
5	57	138	25.041	25.057	$-4.555 \times 10^{-02}$	$1.609 \times 10^{-02}$	3.713646		
7	71	176	32.669	32.693	$-9.472 \times 10^{-02}$	$2.470 \times 10^{-02}$	3.1692		
9	73	180	33.622	33.654	$-1.593 \times 10^{-01}$	$3.282 \times 10^{-02}$	+4.77		
9	73	180ª	33.622	33.558	$1.593 \times 10^{-01}$	$-3.282 \times 10^{-02}$	-4.77		

TABLE II. (Continued).

<sup>a</sup>The sign of  $\mu_i$  for <sup>180</sup>Ta is not known; therefore, calculation has been done for both signs.

TABLE III. Lifetime of the perturbed  $1s^2 2s 2p \ ^3P_0 \ (\tau_0 \ _{\rm HF})$  (the unperturbed lifetime  $\tau_0 = \infty$ )(in s). The lifetime of the  $1s^2 2s 2p \ ^3P_1 \ (\tau_1)$  is the same with or without perturbation to the decimal figures shown.

Z	A	$ au_{0~\mathrm{HF}}$	$ au_1$	Z	A	$ au_{0~\mathrm{HF}}$	$ au_1$
				$I=\frac{1}{2}$			
6	13	$4.340 \times 10^{+03}$	$1.258 \times 10^{-02}$	50	117	$1.832 \times 10^{-03}$	$5.960 \times 10^{-10}$
7	15	$1.056 \times 10^{+04}$	$2.123 \times 10^{-03}$	50	119	$1.673 \times 10^{-03}$	$5.960 \times 10^{-10}$
9	19	$2.778 \times 10^{+01}$	$1.610 \times 10^{-04}$	52	123	$2.501 \times 10^{-03}$	$5.235 \times 10^{-10}$
14	29	$4.625 \times 10^{+01}$	$2.970 \times 10^{-06}$	52	125	$1.720 \times 10^{-03}$	$5.235 \times 10^{-10}$
15	31	$7.381 \times 10^{+00}$	$1.653 \times 10^{-06}$	54	129	$1.668 \times 10^{-03}$	$4.640 \times 10^{-10}$
26	57	$3.059 \times 10^{+01}$	$2.020 \times 10^{-08}$	69	169	$2.306 \times 10^{-03}$	$2.249 \times 10^{-10}$
34	77	$1.174 \times 10^{-01}$	$3.359 \times 10^{-09}$	70	171	$4.450 \times 10^{-04}$	$2.158 \times 10^{-10}$
39	89	$6.320 \times 10^{-01}$	$1.619 \times 10^{-09}$	74	183	$4.523 \times 10^{-03}$	$1.839 \times 10^{-10}$
45	103	$5.234 \times 10^{-01}$	$8.725 \times 10^{-10}$	76	187	$1.140 \times 10^{-02}$	$1.701 \times 10^{-10}$
47	107	$2.284 \times 10^{-01}$	$7.408 \times 10^{-10}$	78	195	$9.803 \times 10^{-05}$	$1.577 \times 10^{-10}$
47	109	$1.729 \times 10^{-01}$	$7.408 \times 10^{-10}$	80	199	$1.082 \times 10^{-04}$	$1.467 \times 10^{-10}$
48	111	$7.092 \times 10^{-03}$	$6.867 \times 10^{-10}$	81	203	$9.276 \times 10^{-06}$	$1.415 \times 10^{-10}$
48	113	$6.481 \times 10^{-03}$	$6.867 \times 10^{-10}$	81	205	$9.098 \times 10^{-06}$	$1.415 \times 10^{-10}$
50	115	$2.175 \times 10^{-03}$	$5.960 \times 10^{-10}$	82	207	$5.992 \times 10^{-05}$	$1.366 \times 10^{-10}$
				$I = \frac{3}{2}$			
5	11	$1.567 \times 10^{+03}$	$1.417 \times 10^{-01}$	33	75	$3.658 \times 10^{-02}$	$4.011 \times 10^{-09}$
10	21	$4.226 \times 10^{+02}$	$5.921 \times 10^{-05}$	35	79	$1.095 \times 10^{-02}$	$2.846 \times 10^{-09}$
11	23	$2.161 \times 10^{+01}$	$2.468 \times 10^{-05}$	35	81	$9.423 \times 10^{-03}$	$2.846 \times 10^{-09}$
16	33	$2.769 \times 10^{+01}$	$9.617 \times 10^{-07}$	54	131	$3.807 \times 10^{-03}$	$4.640 \times 10^{-10}$
17	35	$1.169 \times 10^{+01}$	$5.813 \times 10^{-07}$	56	135	$1.940 \times 10^{-03}$	$4.146 \times 10^{-10}$
17	37	$1.686 \times 10^{+01}$	$5.813 \times 10^{-07}$	56	137	$1.551 \times 10^{-03}$	$4.146 \times 10^{-10}$
19	39	$2.543 \times 10^{+01}$	$2.338 \times 10^{-07}$	64	155	$6.692 \times 10^{-03}$	$2.794 \times 10^{-10}$
19	41	$8.439 \times 10^{+01}$	$2.338 \times 10^{-07}$	64	157	$3.892 \times 10^{-03}$	$2.794 \times 10^{-10}$ $2.794 \times 10^{-10}$
24	53	$3.555 \times 10^{+00}$	$3.687 \times 10^{-08}$	65	159	$9.543 \times 10^{-05}$	$2.672 \times 10^{-10}$
28	61	$4.634 \times 10^{-01}$	$1.182 \times 10^{-08}$	76	189	$1.972 \times 10^{-04}$	$1.701 \times 10^{-10}$
29	63	$4.049 \times 10^{-02}$	$9.261 \times 10^{-09}$	77	191	$3.294 \times 10^{-03}$	$1.638 \times 10^{-10}$
29	65	$3.542 \times 10^{-02}$	$9.261 \times 10^{-09}$	77	193	$2.792 \times 10^{-03}$	$1.638 \times 10^{-10}$ $1.638 \times 10^{-10}$
31	69	$2.991 \times 10^{-02}$	$5.933 \times 10^{-09}$	79	193	$2.792 \times 10^{-03}$ $2.589 \times 10^{-03}$	$1.538 \times 10^{-10}$ $1.520 \times 10^{-10}$
31	71	$1.853 \times 10^{-02}$	$5.933 \times 10^{-09}$	80	201	$1.576 \times 10^{-04}$	$1.320 \times 10^{-10}$ $1.467 \times 10^{-10}$
01		1.000×10	0.000 10	00	201	1.370×10	1.407 × 10
				$I = \frac{5}{2}$			
8	17	$2.280 \times 10^{+02}$	$5.185 \times 10^{-04}$	46	105	$1.801 \times 10^{-02}$	$8.023 \times 10^{-10}$
12	25	$1.036 \times 10^{+02}$	$1.133 \times 10^{-05}$	51	121	$2.999 \times 10^{-04}$	$5.578 \times 10^{-10}$
13	27	$3.582 \times 10^{+00}$	$5.622 \times 10^{-06}$	53	127	$3.176 \times 10^{-04}$	$4.922 \times 10^{-10}$
22	47	$2.812 \times 10^{+00}$	$7.244 \times 10^{-08}$	59	141	$5.799 \times 10^{-05}$	$3.543 \times 10^{-10}$
25	55	$5.924 \times 10^{-02}$	$2.705 \times 10^{-08}$	63	151	$5.036 \times 10^{-05}$	$2.924 \times 10^{-10}$
30	67	$2.419 \times 10^{-01}$	$7.361 \times 10^{-09}$	63	153	$2.578 \times 10^{-04}$	$2.924 \times 10^{-10}$ $2.924 \times 10^{-10}$
37	85	$2.076 \times 10^{-02}$	$2.107 \times 10^{-09}$	66	161	$1.732 \times 10^{-03}$	$2.524 \times 10$ $2.555 \times 10^{-10}$
40	91	$1.245 \times 10^{-02}$	$1.437 \times 10^{-09}$	66	163	$8.844 \times 10^{-04}$	$2.555 \times 10^{-10}$
42	95	$1.758 \times 10^{-02}$	$1.156 \times 10^{-09}$	70	173	$5.007 \times 10^{-04}$	$2.535 \times 10^{-10}$ $2.158 \times 10^{-10}$
42	97	$1.686 \times 10^{-02}$	$1.156 \times 10^{-09}$	75	185	$1.158 \times 10^{-05}$	$1.767 \times 10^{-10}$
44	99	$2.522 \times 10^{-02}$	$9.534 \times 10^{-10}$	75	185	$1.135 \times 10^{-05}$	$1.767 \times 10^{-10}$
44 55 44 101		$2.0022 \times 10^{-02}$ $2.008 \times 10^{-02}$	$9.534 \times 10^{-10}$	10	107	1.135 × 10	1.767×10
				$I = \frac{7}{2}$			
	40	0.00110+00	1 7 17 10-07			02	10
20	43	$2.081 \times 10^{+00}$	$1.545 \times 10^{-07}$	60	145	$2.322 \times 10^{-03}$	$3.371 \times 10^{-10}$
21	45	$1.155 \times 10^{-01}$	$1.046 \times 10^{-07}$	62	147	$1.140 \times 10^{-03}$	$3.064 \times 10^{-10}$
22	49	$1.562 \times 10^{+00}$	$7.244 \times 10^{-08}$	62	149	$1.678 \times 10^{-03}$	$3.064 \times 10^{-10}$
23	51	$5.286 \times 10^{-02}$	$5.118 \times 10^{-08}$	67	165	$2.194 \times 10^{-05}$	$2.450 \times 10^{-10}$
27	59	$2.069 \times 10^{-02}$	$1.533 \times 10^{-08}$	68	167	$1.040 \times 10^{-03}$	$2.344 \times 10^{-10}$
51	123	$5.677 \times 10^{-04}$	$5.578 \times 10^{-10}$	71	175	$4.400 \times 10^{-05}$	$2.071 \times 10^{-10}$
55	133	$3.059 \times 10^{-04}$	$4.382 \times 10^{-10}$	72	177	$3.052 \times 10^{-04}$	$1.990 \times 10^{-10}$
57	139	$1.976 \times 10^{-04}$	$3.928 \times 10^{-10}$	73	181	$2.986 \times 10^{-05}$	$1.911 \times 10^{-10}$
60	143	$8.806 \times 10^{-04}$	$3.371 \times 10^{-10}$	92	235	$8.562 \times 10^{-05}$	$1.014 \times 10^{-10}$
				$I = \frac{9}{2}$			
32	73	$1.685 \times 10^{-01}$	$4.847 \times 10^{-09}$	49	113	$1.727 \times 10^{-04}$	$6.387 \times 10^{-10}$
36	83	$5.679 \times 10^{-02}$	$2.437 \times 10^{-09}$	49	115	$1.720 \times 10^{-04}$	$6.387 \times 10^{-10}$
38	87	$2.977 \times 10^{-02}$	$1.839 \times 10^{-09}$	72	179	$4.915 \times 10^{-04}$	$1.990 \times 10^{-10}$
41	93	$5.298 \times 10^{-04}$	$1.285 \times 10^{-09}$	83	209	$2.661 \times 10^{-06}$	$1.320 \times 10^{-10}$
43	99	$4.372 \times 10^{-04}$	$1.047 \times 10^{-09}$				

I

3

1

 $\mathbf{5}$ 

7

9

9

73

180°

 $1.911 \times 10^{-10}$ 

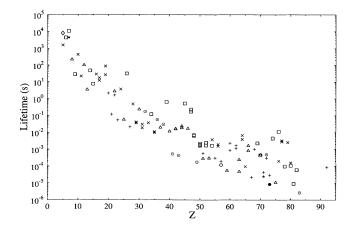


FIG. 3. Influence of the hyperfine interaction on the lifetime of the  $1s^22s2p$   ${}^{3}P_{0}$  state, as a function of Z (the unperturbed lifetime is infinite). The symbols  $\Box$ ,  $\times$ ,  $\triangle$ , +,  $\odot$ , \*,  $\diamond$ ,  $\circ$ ,  $\star$ , and  $\bullet$  represent  $\tau_{0}$  <sub>HF</sub> for isotope with nuclear spin I of  $\frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \frac{7}{2}, \frac{9}{2}, 1, 3, 5, 7$ , and 9, respectively.

 $10^{-7}$  s<sup>-1</sup>. In contrast the hyperfine-quenched transition rate for <sup>207</sup>Pb is  $1.7 \times 10^4$  s<sup>-1</sup>, i.e., 11 orders of magnitude larger. This is very different from the heliumlike case, because here the  $1s^22s2p$   ${}^3P_0-1s^22s^2$   ${}^1S_0$  transition energy is of a few hundred eV at Z = 82, while the 1s2p  ${}^3P_0-1s^2$   ${}^1S_0$  transition energy is  $\approx 70$  keV for the corresponding heliumlike ion.

One of the most interesting practical implications of these calculations is due to the relation between the  $1s^22s2p$   ${}^{3}P_0 - 1s^22s2p$   ${}^{3}P_1$  energy separation and the  $1s^22s2p$   ${}^{3}P_0$  lifetime [Eq. (2.6)]. As in the heliumlike case, this energy separation is not easy to measure directly in spectroscopy. The perturbed energy is not easily measured either. It is mostly the sum of the unperturbed energy and of W(1, 1), and W(1, 0) does not play any role in its value. The  $1s^22s2p$   ${}^{3}P_0$  lifetime in contrast is very sensitive to both the separation energy  $\Delta E_0$  and W(1, 0).

It could thus be possible to estimate  $\Delta E_0$  through a

TABLE III. (Continued). ZA  $au_0$  hf  $au_1$  $\mathbf{5}$ 10  $4.340 \times 10^{+03}$  $1.417 \times 10^{-01}$ 7  $7.806 \times 10^{+03}$ 14  $2.123 \times 10^{-03}$  $1.189 \times 10^{-04}$ 57138  $3.928 \times 10^{-10}$  $2.467 \times 10^{-05}$ 71176  $2.071 \times 10^{-10}$  $8.530 \times 10^{-06}$  $1.911 \times 10^{-10}$ 73 180

 $8.496 \times 10^{-06}$ 

<sup>a</sup>The sign of  $\mu_i$  for <sup>180</sup>Ta is not known; therefore, calculation has been done for both signs.

measurement of the hyperfine-quenched  $1s^2 2s 2p {}^3P_0$  lifetime of berylliumlike ions with nuclear spin  $I \neq 0$ . The method has been demonstrated in heliumlike  $Ag^{45+}$  [2] and  $\mathrm{Gd}^{62+}$  [3]. The berylliumlike ions case is rather different, because, even for the highest Z the lifetimes involved are much longer than in heavy heliumlike ions. However, because of recent progress in ion sources and ion trap technology, lifetimes between 0.1 s and 10  $\mu$ s could be measured with some accuracy, by directly looking at the light emitted by the ions as a function of time, after the trap has been loaded. Obviously it means that the vacuum inside the trap has to be very good if long lifetimes have to be measured. Whether this method will work remains to be experimentally demonstrated. But such experiments would provide for different isotopes. the unperturbed energy separation, since nuclear magnetic moments are well known. This would be a very interesting test of our relativistic calculations.

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