

## Atomic $K$ -shell binding energies of multiply charged neon ions studied by zero-degree Auger-electron spectroscopy

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In this work we report an improved experimental determination of  $K$ -shell binding energies from Be-like  $\text{Ne}^{6+}$ , B-like  $\text{Ne}^{5+}$ , and C-like  $\text{Ne}^{4+}$  ground-state multiply charged ions using high-resolution Ne-K Auger-electron spectroscopy. The derived energy differences, namely,  $\text{Ne}^{6+} E(1s^2 2s^2)^1S - \text{Ne}^{7+} E(1s 2s^2)^2S$ ,  $\text{Ne}^{5+} E(1s^2 2s^2 2p)^2P^o - \text{Ne}^{6+} E(1s 2s^2 2p)^3P^o$ , and  $\text{Ne}^{4+} E(1s^2 2s^2 2p^2)^3P - \text{Ne}^{5+} E(1s 2s^2 2p^2)^4P$  are 1099.1, 1048.5, and 1001.8 eV, respectively. These energies are accurate to within  $\pm 0.1$  eV. Theoretically, we have studied relativistic binding energies of  $\text{Ne}^{q+}$  ( $q=6, 5,$  and  $4$ ) by using the (i) saddle-point technique, (ii)  $1/Z$  method, and (iii) multiconfiguration Dirac-Fock model. Excellent agreement with experiment is obtained.

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### I. INTRODUCTION

$K$ -shell binding energies of free atoms [1] and ions constitute important atomic data relevant to surface physics, fusion plasmas, x-ray laser design [2], astrophysics, and sophisticated ion sources such as the electron-cyclotron-resonance (ECR) source [3] and electron-beam ion trap (EBIT) [4]. These data are also of fundamental importance for a better understanding of electron correlation and relativistic interactions in autoionizing core-excited states which generally require computationally elaborate many-body theories [5–13]. Despite the fundamental importance of accurate inner-shell energy values, it was not until recently that free-atom  $K$ -shell binding energies of Be, B, and C have been studied both experimentally and theoretically [14–16]. Experimentally Bruch and co-workers applied the forward-angle ( $6.5^\circ$ ) projectile Auger-electron-spectroscopy method [14,15] to fast  $\text{Be}^+$ ,  $\text{B}^+$ , and  $\text{C}^+$  ion beams and Krause and Caldwell [16] made a study of the  $K$ -shell photoionization of atomic beryllium.

Highly accurate atomic data on binding energies of multiply charged ions are virtually nonexistent except for some recent results on the  $L$ ,  $M$ , and  $N$  shells of multiply charged krypton ions by internal-conversion-electron spectroscopy [17].

Here we report  $K$ -shell binding energies for charge states  $4+$  (C-like Ne),  $5+$  (B-like Ne), and  $6+$  (Be-like Ne). To our knowledge these measurements represent the most accurate  $K$ -shell binding energies for multiply charged Ne ions. Furthermore we have calculated precise Ne  $K$  energy values and shifts as a function of the number of  $2p$  orbitals by using relativistic many-body approaches. Our theoretical predictions are in excellent

agreement with experimental results and may serve as benchmark calibration points. The determination of experimental  $K$ -binding energies is discussed in the following.

### II. EXPERIMENTAL PROCEDURE

Zero-degree projectile Auger-electron spectroscopy [18–20] in conjunction with multiply charged energetic ion beams and light targets ( $\text{H}_2$ , He) has great potential for studying core-level binding energies, because (i) the excitation process is highly selective [21], similar to inner-shell photoionization [22–24], (i.e., mainly one inner-shell electron is removed), (ii) high-energy resolution is achieved due to drastic reduction of kinematic line broadening, and (iii) Auger spectra can be investigated individually, depending on the incident projectile charge state [25]. In this work Li-like, Be-like, and B-like core-excited configurations were selectively produced in 100-MeV  $\text{Ne}^{6+} + \text{He}$ , 100-MeV  $\text{Ne}^{5+} + \text{He}$ , and 70-MeV  $\text{Ne}^{4+} + \text{He}$  collisions (see Fig. 1). The experimental arrangement that has been used to study electron emission from selectively excited  $K$ -shell vacancy states of fast Ne ion beams has been described in detail previously [21] and will not be discussed here. However, the line assignment and absolute calibration for these Ne  $K$  Auger spectra have been considerably improved on the basis of refined theoretical computations using the saddle-point technique [26], the  $1/Z$  method [13], and the multiconfiguration Dirac-Fock (MCDF) mode [6].

In particular the line assignment of the boronlike states [Fig. 1(c)] has been completely revised. Figure 1 presents the basic results of this experiment. It clearly demonstrates that discrete selective Auger transitions can be ob-

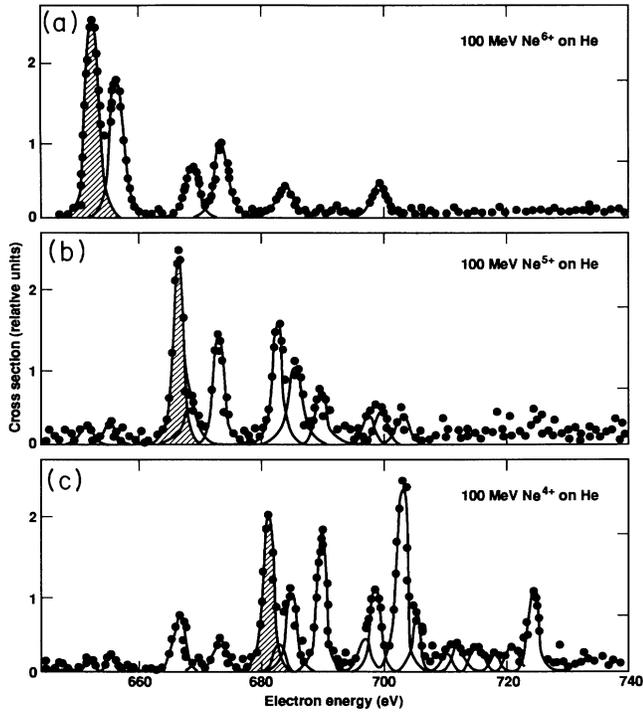


FIG. 1. High-resolution zero-degree electron spectra of neon, resulting from  $K$ -shell ionization following (a) 100-MeV  $\text{Ne}^{6+} + \text{He}$ , 100-MeV  $\text{Ne}^{5+} + \text{He}$ , and (c) 70-MeV  $\text{Ne}^{4+} + \text{He}$  collisions. The spectra are displayed after background subtraction and transformation to the projectile emitter frame.

served in energetic  $\text{Ne}^{q+}$  ( $q=6, 5$ , and  $4$ ) +  $\text{He}$  collisions. The majority of the Auger lines which are observed in Figs. 1(a) and 1(c) originate from Li-like, Be-like and B-like initial configurations. We have found striking evidence that the pronounced lines [see Figs. 1(a)–1(c)] can be uniquely identified as the

$$\text{Ne}^{7+}(1s2s^2)^2S \rightarrow (1s^2\epsilon s)^2S, \quad (1)$$

$$\text{Ne}^{6+}(1s2s^22p)^3P^0 \rightarrow (1s^22p\epsilon s \text{ or } \epsilon d)^3P^0, \quad (2)$$

$$\text{Ne}^{5+}[1s2s^22p^2(^3P)]^4P \rightarrow (1s^22p^2^3P\epsilon s \text{ or } \epsilon d)^4P \quad (3)$$

Auger transitions. A more detailed line identification and discussion of the branching ratios is given elsewhere [27].

According to Bisgaard *et al.* [14] we define the  $K$ -shell binding energies of Ne as the difference between the lowest-lying multiplet terms of the initial- and final-state configurations for the  $K$ -shell ionization process. For Be-, Be-, and C-like neon ions, the  $K$ -shell binding energies are therefore given as follows:

$$E_{1s}^B = \begin{cases} E(1s2s^2)^2S - E(1s^22s^2)^1S & \text{for } \text{Ne}^{6+} \end{cases} \quad (4)$$

$$E_{1s}^B = \begin{cases} E(1s2s^22p)^3P^0 - E(1s^22s^22p)^2P^0 & \text{for } \text{Ne}^{5+} \end{cases} \quad (5)$$

$$E_{1s}^B = \begin{cases} E[1s2s^22p^2(^3P)]^4P - E(1s^22s^22p^2)^3P & \text{for } \text{Ne}^{4+}. \end{cases} \quad (6)$$

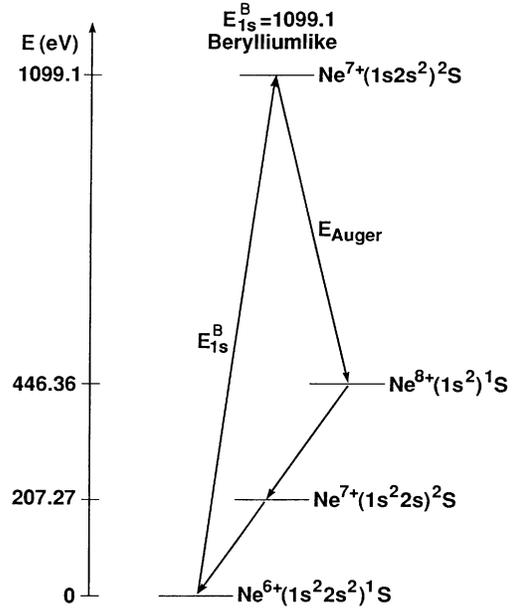


FIG. 2. Energy-level diagram for establishing the  $K$ -shell binding energy of berylliumlike neon.

The procedure for extracting the berylliumlike, boron-like, and carbonlike  $K$ -shell binding energies is illustrated schematically in Figs. 2, 3, and 4, respectively. In these energy-level diagrams  $E_{\text{Auger}}$  is the experimentally determined Auger transition energy. In this connection we note that the necessary additional  $L$ -shell ionization energies of the Ne can be deduced with high accuracy from spectroscopic data [28]. The  $K$ -binding energies thus derived are summarized in Table I along with theoretical calculations which are discussed in the next section.

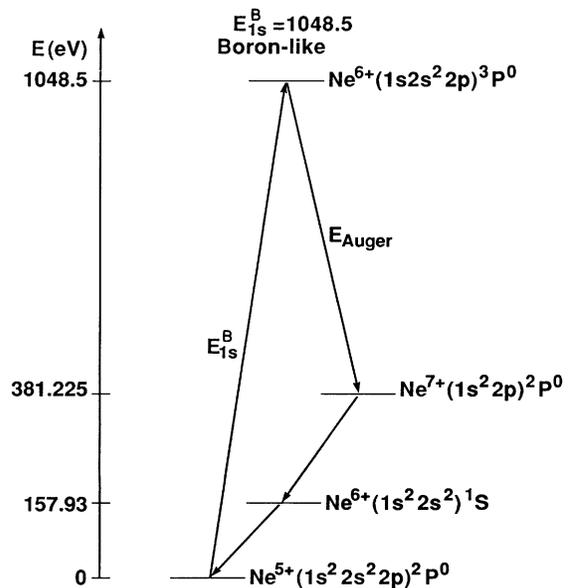


FIG. 3. Energy-level diagram for establishing the  $K$ -shell binding energy of boronlike neon.

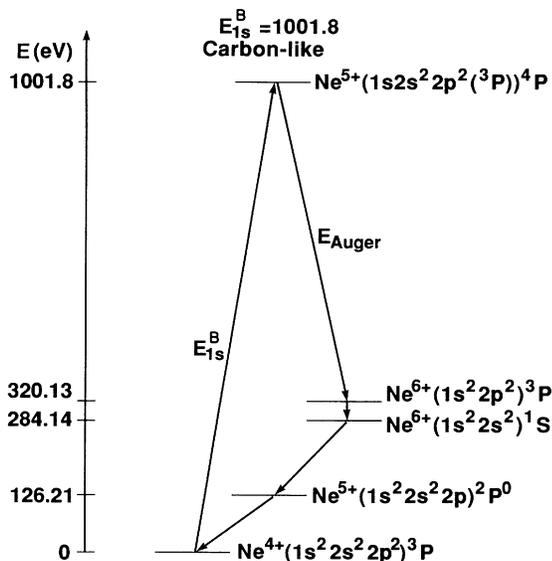


FIG. 4. Energy-level diagram for establishing the  $K$ -shell binding energy of carbonlike neon.

### III. THEORETICAL COMPUTATION

In 1979, a saddle-point variation method was developed for dealing with resonances arising from

inner-shell excitation [26]. This method has been applied to numerous two- and three-electron resonances. Here we have applied this technique to the lowest three-electron state, i.e.,  $(1s2s^2)^2S$  in  $\text{Ne}^{7+}$  and the lowest four-electron state, i.e.,  $(1s2s^22p)^3P^0$  in  $\text{Ne}^{6+}$ . The details of the calculations are reported by Chung and Bruch [7]. We note that the saddle-point method for a four-electron system [29] is very similar to that for a three-electron system. The nonrelativistic part of the calculation follows the same procedure as in Chung [30] in which an  $LS$ -coupling scheme was used. The relativistic corrections are calculated with the Breit-Pauli approximation [31] using first-order perturbation theory. The mass polarization effect is also included. The explicit forms of the operators are given by Chung [32].

The main advantage of this saddle-point method is the simplicity with which computations can be carried out to yield high-precision results, which can be used for calibration in high-resolution electron spectroscopy. Our theoretical predictions for  $K$ -shell binding energies deduced from the saddle-point method are listed in Table I.

Since the saddle-point method is limited so far to calculations of two-, three-, and a few four-electron systems, we have determined additional  $K$ -shell binding energies in beryllium and boronlike neon ions with  $1s2s^22p$  and  $1s2s^22p^2$  initial configurations. These calculations have been performed relativistically in terms of the multiconfiguration Dirac-Fock model in optimum-level

TABLE I. Experimental  $K$ -shell binding energies of Be-, B-, and C-like multiply charged neon ions in comparison with theoretical predictions.

System	Ionization process	Experimental		Saddle-point method	Theoretical	
		Projectile	Target		1/Z expansion	MCDF model
$\text{Ne}^{6+}$ Be-like	$(1s^22s^2)^1S \rightarrow (1s2s^2)^2S$	$1099.1 \pm 0.1^a$	$1099.4^b$ $1098.8^f$ $1098.4^g$	$1099.02^c$		$1099.26^d$
$\text{Ne}^{5+}$ B-like	$(1s^22s^22p)^2P^0 \rightarrow (1s2s^22p)^3P^0$	$1048.5 \pm 0.1^a$	$1048.1^f$	$1048.495^c$	$1048.17^h$	$1048.47^d$ $1049.02^i$
$\text{Ne}^{4+}$ C-like	$(1s^22s^22p^2)^3P \rightarrow [1s2s^22p^2(^3P)]^4P$	$1001.8 \pm 0.1^a$	$1002.0^f$		$1001.95^h$	$1001.87^d$

Energy difference  $\text{Ne}^{5+}(1s^22s^22p)^2P^0 - \text{Ne}^{7+}(1s^22p)^2P^0$ : 381.225 eV  
 Bashkin and Stoner (Ref. [28])  
 Energy difference  $\text{Ne}^{4+}(1s^22s^22p^2)^3P - \text{Ne}^{6+}(1s^22p^2)^3P$ : 320.13 eV  
 Bashkin and Stoner (Ref. [28])  
 Energy difference  $\text{Ne}^{6+}(1s^22s^2)^1S - \text{Ne}^{8+}(1s^2)^1S$ : 446.36 eV  
 Bashkin and Stoner (Ref. [28])

<sup>a</sup>Zero-degree projectile electron spectroscopy, this work.

<sup>b</sup>Target Auger-electron spectroscopy, Schneider, Moore, and Johnston (Ref. [37]).

<sup>c</sup>Saddle-point technique including relativistic corrections, this work.

<sup>d</sup>Multiconfiguration Dirac-Fock calculation, this work.

<sup>e</sup>Beam-foil Auger-electron spectroscopy, Schumann and co-workers (Refs. [35,36]).

<sup>f</sup>Target Auger-electron spectroscopy, Kádár *et al.* (Ref. [40]).

<sup>g</sup>Target Auger-electron spectroscopy, Stolterfoht *et al.* (Ref. [38]).

<sup>h</sup>1/Z-expansion method including relativistic corrections, this work (Ref. [13]).

<sup>i</sup>Multiconfiguration Dirac-Fock calculation, Schumann, Groeneveld, and Nolte (Ref. [35]).

scheme [33], where the Breit interaction and quantum-electrodynamic corrections are taken into account. In addition, the ground-state correlation corrections are also included [34].

In a third method we have applied the  $S$ -matrix formalism [13] as developed by Ivanov and Safronova to the nonrelativistic and relativistic energies of the  $\text{Ne}^{6+}(1s2s^22p)^3P^0$  and  $\text{Ne}^{5+}[1s2s^22p^2(^3P)]^4P$  states. This  $1/Z$  expansion yields  $K$ -shell binding energies which are listed in Table I along with the MCDF values.

#### IV. RESULTS AND DISCUSSIONS

It is interesting to compare the experimental and theoretical  $K$ -binding energies for the different Ne charge states (see Table I). In the column labeled “Projectile” we compare our results with earlier beam-foil measurements of Schumann and co-workers [35,36]. It is evident that we have increased the accuracy of Ne  $K$  Auger energies by one order of magnitude. In this connection we note that for the  $\text{Ne}^{5+}$  case our projectile energy value deviates from the corresponding beam-foil result by 2.3 eV.

Complementary  $K$ -binding energies resulting from Ne  $K$ -target spectra following bombardment of fast multiply charged ions on Ne are also included in Table I (see column “Target”). The strong Coulomb field induced by the highly charged ions results in the removal of several electrons from the Ne  $L$  shell whenever a vacancy is produced in the  $K$  shell [37–40]. This causes the production of recoil charge states which correspond mainly to Li-, Be-, B-, and C-like electron configurations. As can be seen from Table I the  $K$ -shell binding energies derived from the work of Kádár *et al.* [40] agree within a few tenths of an eV with our experimental projectile results.

In our MCDF calculations of  $K$ -shell binding energies, the ground-state-correlation corrections which arise from the broken pairs in the ionization were estimated to be 1.17, 1.23, and 1.27 eV for  $\text{Ne}^{6+}$ ,  $\text{Ne}^{5+}$ , and  $\text{Ne}^{4+}$ , respectively, by using the calculated nonrelativistic pair energies [41]. For  $\text{Ne}^{5+}$ , the present MCDF results differ slightly with the corresponding value given by Schumann, Groeneveld, and Nolte [35] due to the use of optimum-level scheme [33] and the inclusion of the

ground-state-correlation correction in our calculation.

To our knowledge, the best theoretical data for  $K$ -shell binding energies are by Chung and Davis. Indeed, our experimental values for  $\text{Ne}^{6+}$  and  $\text{Ne}^{5+}$  are in excellent agreement with the saddle-point calculation. In the case of  $\text{Ne}^{5+}$  the  $1/Z$ -expansion method predicts  $K$ -binding energies outside our experimental uncertainty, whereas the saddle-point and MCDF calculations are in perfect agreement with our experimental value. For  $\text{Ne}^{4+}$  our MCDF result lies inside the experimental uncertainty quoted, whereas the  $1/Z$  expansion predicts a binding energy which is slightly higher than our experimental energy.

There is another interesting point worth mentioning. It is apparent from Figs. 2–4 and Table I that the  $K$ -binding energies dramatically increase with decreasing number of  $2p$  electrons. The corresponding binding-energy shifts derived from Table I are summarized in Table II. This effect can be explained qualitatively as a screening effect [22] of the nuclear potential owing to the  $2p$  orbitals.

#### V. CONCLUSION

In summary, we have determined accurate  $K$ -binding energies for free neon ions of Be-, B-, and C-like configurations from high-resolution projectile-Auger-electron spectra. Our theoretical calculations agree very well with these data. In particular the present study provides insight into the role of  $2p$  electron correlation and screening effects in the inner-shell ionization process of neon ions. The zero-degree projectile-Auger-electron-spectroscopy method can be extended to other studies of  $K$ -,  $L$ -, and  $M$ -shell binding energies along isoelectronic sequences, depending on the availability of intense fast-ion beams [42]. On the other hand, multiply charged inner-hole states can also be populated efficiently in slow collisions following selective multiple electron capture in ion-atom, ion-molecule, and ion-surface collisions [43]. The wealth of such Auger spectroscopic information may not only lead to a better understanding of the relativistic many-body problem in highly charged ions but may also help to unravel the complex physics in high-temperature dense plasmas as they are important for fusion, material processing, and x-ray laser research.

TABLE II. Ne  $K$ -shell binding-energy shifts in eV compared with theoretical calculations.

Charge state	Experimental		Theory		
	Projectile	Target	Saddle-point method	$1/Z$ expansion	MCDF model
5→6	50.6 <sup>a</sup> 52.2 <sup>c</sup>	50.7 <sup>b</sup>	50.53 <sup>c</sup>		50.79 <sup>d</sup>
4→5	46.7 <sup>a</sup>	46.1 <sup>b</sup>		46.22 <sup>f</sup>	46.60 <sup>d</sup>

<sup>a</sup>Zero-degree projectile electron spectroscopy, this work.

<sup>b</sup>Target electron spectroscopy, Kádár *et al.* (Ref. [40]).

<sup>c</sup>Saddle-point technique including relativistic corrections, this work.

<sup>d</sup>Multiconfiguration Dirac-Fock calculation, this work.

<sup>e</sup>Beam-foil Auger-electron spectroscopy (Ref. [35]).

<sup>f</sup> $1/Z$ -expansion method including relativistic corrections, Ivanov and Safronova (Ref. [13]), this work.

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