## Comments

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## Comment on "Molecular-dynamics simulation of excess-electron transport in simple fluids"

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A recent treatment of the saturation drift velocity  $v_{sat}$  of electrons in dense, supercritical argon [Leycuras and Levesque, Phys. Rev. A 32, 1180 (1985)] gives positive values of  $dv_{sat}/dn$  at  $n/n_c = 1.2 - 1.6$ , whereas the experimental values are negative in both the supercritical gas and the liquid at these densities [Jahnke, Meyer, and Rice, Phys. Rev. A 3, 734 (1971); Huang and Freeman, Phys. Rev. A 24, 714 (1981)]. Other difficulties are mentioned.

A recent treatment of the saturation drift velocities  $v_{sat}$  of extra electrons in dense, supercritical argon<sup>1</sup> does not fit certain features of the experimental data.<sup>2,3</sup> In particular, the change of  $v_{sat}$  with density,  $dv_{sat}/dn$ , is predicted to be positive in the density range  $n/n_c = 1.2 - 1.6$  ( $n_c$  is the density of the critical fluid),<sup>1</sup> whereas it is observed to be negative in both the supercritical gas<sup>2</sup> and the liquid<sup>3</sup> at these densities. Several comments are offered.

(1) At constant density, increasing the temperature to change from the liquid to the supercritical gas increases  $v_{sat}$  slightly but does not alter the value of  $dv_{sat}/dn$  (Fig. 1, experimental points from Refs. 2 and 3).

(2) Figure 3 of Ref. 1 displays calculated values of  $v_{sat} = 400-900$  m/s over the argon density range



FIG. 1. Saturation drift velocity of electrons in argon as a function of density:  $\nabla$ , supercritical gas, 155 ±3 K, experimental, Ref. 2;  $\blacktriangle$ , supercritical gas, ~155 K, theoretical, Ref. 1;  $\bullet$ , coexistence gas and liquid at indicated temperatures, experimental, Ref. 3; --, Ref. 2 as quoted in Ref. 1.  $2.69 \times 10^{25}$  molecule/m<sup>3</sup>=1 amagat (Leycuras and Levesque response).

n = 9.6 - 14.4  $(10^{27} \text{molecule/m}^3)$ . Experimentally, at n = 8.1 - 12.9  $(10^{27} \text{molecule/m}^3)$  a plateau in the drift velocity occurs at 900-600 m/s, at fields  $E \approx 10 - 30$  kV/m.<sup>3</sup> This appears to be the plateau to which Leycuras and Levesque<sup>1</sup> refer. At higher densities,  $n \ge 14.8 \times 10^{27}$  molecule/m<sup>3</sup>, this plateau does not exist;<sup>3</sup> it has collapsed into the long, gentle increase of drift velocity with field that occurs at high fields in argon at all densities.<sup>3-5</sup> The plateau at intermediate fields at  $n \le 13 \times 10^{27}$  molecule/m<sup>3</sup> is attributed to electron heating by the field and the rapid rise of the momentum-transfer cross section  $\sigma_m$  on the high-energy side of the Ramsauer-Townsend (RT) minimum.<sup>6</sup> At  $n > 13 \times 10^{27}$  molecule/m<sup>3</sup> the electron-molecule separation distance is continually too small to allow the RT effect to occur.<sup>3</sup>

(3) In argon at  $n < 13 \times 10^{27}$  molecule/m<sup>3</sup> the experimental value of  $dv_{sat}/dn$  is negative in both the supercritical gas and the liquid (Fig. 1), whereas that predicted by Leycuras and Levesque for the supercritical gas is positive.<sup>1</sup> Values of  $v_{sat}$  in the supercritical gas, displayed in Ref. 2, are included in Fig. 1. No velocity plateau was obtained at  $n < 10.6 \times 10^{27}$  molecule/m<sup>3</sup>;<sup>2</sup> the S curve attributed<sup>1</sup> to that reference seems to be in error, since there is not an experimental value  $v_{sat} = 600$  m/s at 0.0096 atoms/Å<sup>3</sup>.<sup>2</sup>

(4) The 10% dip in  $v_{sat}$  indicated in the calculated values at *n* near  $13.1 \times 10^{27}$  molecule/m<sup>3</sup> is within the reported 10% uncertainty of the calculations.<sup>1</sup> The dip is also too narrow to be credible (Fig. 1). The uncertainties in the calculated results can also be assessed from the earlier report.<sup>7</sup>

(5) In liquid argon near the triple point, where  $n=21\times10^{27}$  molecule/m<sup>3</sup>, a much higher velocity plateau occurs at a much higher field strength:  $v_{sat}=8000$  m/s at E=7-9 MV/m.<sup>5</sup> This plateau does not occur at low densities and is due to a different mechanism than that discussed in the above item (2). The mechanism probably involves inelastic processes of relatively high-energy electrons. The Leycuras mechanism predicted a value of  $v_{sat}$  only 50% of the observed.<sup>7</sup>

(6) The model in Ref. 1 includes the assumption that the extra electron is localized on a single argon atom. It attributes the maximum electron-transfer rate, and hence the value of  $v_{sat}$ , to the molecule-molecule collision rate. This is contrary to the observation that  $v_{sat}$  is slightly higher in the low-density gas than in the dense gas or low-density liquid.<sup>3</sup> The localization model for electrons in supercritical or liquid argon, whether the electron is assumed to be localized on one or several molecules,<sup>8</sup> has been argued to be untenable.<sup>6,9</sup> The arguments need not be repeated here. Quasilocalization of electrons occurs in dense gases and low-density liquids at temperatures near the vapor-liquid coexistence curve, if the applied electric field is not too high.<sup>3,10-12</sup> At the field strengths required to attain  $v_{sat}$ , quasilocalization does not occur.<sup>3,10(b)</sup> Quasilocalization does not occur even at low field strengths in argon at  $n \ge 14 \times 10^{27}$  molecule/m<sup>3</sup>;<sup>3</sup> extra electrons reside in a conduction band.<sup>3,10,13-15</sup>

(7) The statement that "one can easily verify that for every gas the abrupt decrease of the mobility (less pronounced in methane) occurs at a density for which the onset of localization is predicted by the Mott expression  $\langle k\Lambda \rangle = k (n \langle \bar{\sigma}_m \rangle)^{-1}$ , where k is the wave number associated with the electron in thermal equilibrium with the fluid,  $\Lambda$  is the mean free path, n the number density of the fluid, and  $\langle \bar{\sigma}_m \rangle$  the thermal average of the momentum transfer cross section at the fluid temperature" has recently been shown to be untrue.<sup>16</sup> In helium at 2.7K  $\leq T \leq 293$  K, and in hydrogen at 78 K  $\leq T \leq 293$ K, the density-normalized mobility  $n\mu$  decreases at much lower densities than predicted by the Mott expression. The value of  $n\mu$  has decreased to 0.72 of the low-density gas limit  $(n\mu)_0$  at a density 6.3 times smaller than that,

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  (b) S. S.-S. Huang and G. R. Freeman, *ibid.* 68, 1355 (1978).
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 $n_M$ , predicted by the Mott expression.<sup>16</sup> Electron behavior in many dense gases has recently been assessed<sup>16</sup> with respect to the Mott expression<sup>17</sup> and that of Ioffe and Regel.<sup>18</sup> The latter applies cleanly to electrons in helium and hydrogen, where the electron-molecule interaction is repulsive. Neither expression applies cleanly to gases in which the interaction with thermal electrons is attractive (argon, xenon, ammonia, water, ethane, and so on).<sup>16</sup>

(8) The methane vibrational phase-relaxation results of Marsault cited in Ref. 19 display a maximum in bandwidth at the critical density  $n_c$  and a minimum near  $2n_c$ . They are reminiscent of the bulk viscosity of argon, which has a maximum at  $n_c$  and a minimum near  $2n_c$ .<sup>20</sup> While the vibrational bandwidth and the bulk viscosity reflect the molecular dynamics in the fluid, they do not support either the conduction-band model or the attachment model of electron transport, because they could be consistent with both types of model. In the deformation potential version<sup>14,15</sup> of the conduction-band model, electron mobility is determined by fluid-density fluctuations, as are the changes of vibrational bandwidth in methane<sup>19</sup> and bulk viscosity of argon.<sup>20</sup>

(9) The localization of an electron on a single argon atom proposed in Ref. 1 is very different from the quasilocalization of a thermal electron by a large density fluctuation in a dense gas near the vapor-liquid coexistence curve.<sup>10,21</sup> The latter has been demonstrated to occur in many gases, but under limited conditions.<sup>3,10,11,21,22</sup>

We are grateful to the Natural Sciences and Engineering Research Council of Canada for financial assistance.

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