Quartet system of CIV

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Theoretical and experimental investigations of the quartet system of CIv are reported. Twentyseven quartet-state energies are calculated. Based on this work, several lines observed for the first time in the extreme-ultraviolet beam-foil spectra of carbon (10—²⁰⁰ nm) are classified as 1s 2pnl⁴L-1s 2pn'l'⁴L' and 1s 2snl⁴L-1s 2sn'l'⁴L' (n = 2,3; n' = 4,5) transitions. The calculated fine structures for the quartet states are also reported. In addition, a list of new observed lines classified in CIII and CIV is given.

I. INTRODUCTION

Recently, the quartet states of the lithiumlike ions have received a fair amount of attention. For light ions such as 'Li I,^{1,2} Be II,³⁻⁶ and B III (Ref. 6) detailed studies have been made both theoretically and experimentally. However, for systems with nuclear charge $Z \ge 6$, only limited data are available.

Most of the theoretical results on quartet states of C Iv are limited to low-lying states and to a few angular symmetry states such as ${}^{4}S$, ${}^{4}P^{o}$, and ${}^{4}P$.⁷⁻¹² With the exception of $2s2p^{4}P^{o}$ and $2p2p^{4}P$ states, all theoretical calculations in the literature are nonrelativistic. Since relativistic effects contribute substantially to the energy of C Iv, they should be included if reliable results are to be obtained. Very recently, the energies of the CIV $2s 2p^4 P^o$ and $2p 2p⁴P$ states have been calculated to high accuracy with configuration-interaction wave functions.¹³

In the present work, the method used in Ref. 13, which is not limited to low-lying states, ¹⁴ is applied for calculating higher excited quartet states: ${}^{4}S$, ${}^{4}S^{o}$, ${}^{4}P^{o}$, ${}^{4}P$, ${}^{4}D^{o}$, ${}^{4}D$, ${}^{4}F^{o}$, and ${}^{4}F$. A nonrelativistic Hamiltonian and variational method are used as a first step. The relativistic corrections and mass polarization effect are calculated using first-order perturbation theory. The wave function and the computational procedure used are similar to those of Chung and Davis.

Experimental studies of the quartet system of C rv have been made previously using the beam-foil technique¹⁵⁻¹⁸ and transitions occurring nearly exclusively in the wavelength region $\lambda < 40$ nm were classified in this system.

In this work, beam-foil spectra of carbon are recorded using a grazing incidence spectrometer $(\lambda=10-40 \text{ nm})$ and a Seya-Namioka-type spectrometer (λ =30–200 nm). Transitions between quartet states are searched in these spectra on the basis of theoretical predictions.

II. THEORETICAL RESULTS

A. Center-of-gravity energy

The nonrelativistic energies (E_{nr}) obtained in this work are given in Table I. For comparison purposes, the results for the ${}^{4}S$ and ${}^{4}P^{o}$ states of Larsson *et al.*⁷ are also given. These are the most accurate theoretical calculations in which a large wave function and r_{ij} coordinates are explicitly employed. Their $2s2p^{4}P^{\circ}$ and $2s3s^{4}S$ energies are only slightly higher than those of the present work. However, for higher excited states, the deviation is much more substantial. Our results are lower than those of Lunell and Beebe⁸ and Holøien and Geltman.⁹

In Table I the sum of the expectation values for the mass correction term and Darwin term¹⁹ denoted as $\langle (H_1+H_2) \rangle$ is reported. The explicit forms for these operators are given in Ref. 13. For the CIv quartets, the energy contribution from this correction ranges from 0.25 to 0.30 eV, depending on whether the system has a $1s2s³S$ or $1s2p^3P^{\circ}$ core. The contribution from the ³S core is substantially larger than that of the ${}^{3}P^{o}$ core. This makes a term classification very straightforward: The $\langle (H_1+H_2) \rangle$ for states with a ³P^o core is about -0.0093 a.u. whereas that of the ${}^{3}S$ is about -0.0104 a.u.

The mass polarization effect $\langle H_3 \rangle$ is also tabulated in Table I. Although this effect is very small, nevertheless, it can be experimentally observed by measuring the isotope shift of ^{12}C and ^{14}C . The calculated result given in this table is obtained by approximating the ${}^{12}C$ nucleus with six protons and six neutrons. The retardation effect $\langle H_4 \rangle$ is somewhat larger than $\langle H_3 \rangle$ for C iv. In general, $\langle H_3 \rangle$ and $\langle H_4 \rangle$ are opposite in sign except for those states where both effects are very small.

The center-of-gravity energies given by

$$
E_{\rm CG} = E_{\rm nr} + \langle (H_1 + H_2) \rangle + \langle H_3 \rangle + \langle H_4 \rangle
$$

are quoted in Table I. The wavelengths calculated from the E_{CG} energies are given in Table II. The conversion factor used is 45.5656 nm/a. u.

B. Fine structure

Recent spectroscopic measurements of the finestructure wavelengths of the 1s $2s2p^4P^o-1s2p^2P^4P$ tranition in the Li_I sequence^{17,20–23} have stimulated consid-
rable amount of theoretical interest.^{10–13} However, to our knowledge, the only fine-structure data available for

TABLE I. The energies of quartet system of CIV (in a.u.). E_{nr} , nonrelativistic energy; $\langle (H_1 + H_2) \rangle$ mass correction term and Darwin term; $\langle H_3 \rangle$, mass polarization term; $\langle H_4 \rangle$, retardation term. E_{CG} center $(E_{CG} = E_{nr} + \langle (H_1 + H_2) \rangle + \langle H_3 \rangle + \langle H_4 \rangle).$

	$-E_{\rm nr}$				$-E_{\rm CG}$	$-E_{\rm nr}$	$-E_{\rm exp}$
Term	This work	$-10^2 \langle (H_1 + H_2) \rangle$	$-10^5 \langle H_3 \rangle$	$-10^4 \langle H_4 \rangle$	This work	Other works	This work
$1s$ 2s 3s ${}^{4}S$	22.520 631	1.0924	-0.166	-0.069	22.531 546	22.51993 ^a	22.531996
1s 2p 3p 4S	22.194079	0.9533	$+9.654$	-2.125	22.203 496	22.18851 ^a	22.203 596
1s2s4s ⁴ S	21.997711	1.0657	$+0.074$	-0.034	22.008 366	21.99678 ^a	22.008 402
$1s$ 2s 5s ${}^{4}S$	21.784968	1.0405	$+1.037$	-0.287	21.795 354	21.78177 ^a	
1s 2p 4p 4S	21.748218	0.9394	$+7.805$	-1.664	21.757 524	21.73375 ^a	
$1s$ 2s 6s ${}^{4}S$	21.663938	1.0550	-0.031	-0.015	21.674486		
$1\,s\,2s\,2p\;^4P^o$	23.969309	1.0821	$+7.609$	-1.693	23.980037	23.969 19 ^a	
$1s$ 2s $3p\ ^4P^o$	22.422 499	1.0604	$+2.597$	-0.486	22.433081	22.42098 ^a	22.433 260
$1\,s\,2p\,3s\,^4P^o$	22.279 031	0.9670	$+8.613$	-1.850	22.288 602	22.27751 ^a	22.288885
$1s 2p 3d 4P^o$	22.112594	0.9374	$+8.823$	-1.912	22.121865	22.054 67 ^a	22.122 129
$1s2p4d4p^o$	21.722 642	0.9405	$+8.408$	-1.794	21.731951		21.731309
1s 2p 2p 4P	23.631 579	0.9619	$+14.80$	-3.408	23.641 006	23.62843^{b}	
1s 2p 3p 4P	22.182004	0.9366	$+10.21$	-2.273	22.191245		22.191612
1s 2p 4p 4P	21.751345	0.9294	$+9.448$	-2.041	21.760 529		21.760 598
1s2p5p4P	21.556585	0.9272	$+9.213$	-1.966	21.565753		21.565969
1s 2p 6p 4P	21.451948	0.9264	$+9.115$	-1.934	21.461 110		
$1s$ 2s $3d$ ⁴ D	22.364027	1.0440	-0.528	-0.110	22.374451		22.374 539
1s 2p 3p 4D	22.220369	0.9498	$+10.63$	-2.097	22.229763		22.230903
$1s2s4d^{4}D$	21.939 651	1.0511	-0.300	$+0.005$	21.950 160		21.950424
1s 2p 4p 4D	21.765 503	0.9393	$+8.883$	-1.895	21.774796		21.775 512
$1s2s5d^{4}D$	21.748 642	1.0410	$+0.737$	-0.148	21.759045		21.759 614
1s2p3d4D°	22.132368	0.9278	$+7.130$	-1.834	22.141534		22.141 640
1s2p4d4D°	21.730712	0.9264	$+8.360$	-1.866	21.739873		21.739 433
$1s$ $2p$ $5d$ $^4D^o$	21.546 101	0.9247	$+8.686$	-1.877	21.555246		21.554961
1s 2p 4f 4F	21.727519	0.9267	$+8.951$	-1.885	21.736 687		21.736717
$1s2p3d4P^o$	22.171 137	0.9292	$+12.22$	-1.889	22.180362		22.180954
$1s 2s 4f$ ⁴ Fo	21.921072	1.0509	-0.137	-0.011	21.931 579		21.931 683

^aLarsson et al., Ref. 7.

^bLunell and Beebe, Ref. 8.

quartets in the literature are those of the $2p2p^{4}P$ and $2s 2p$ ⁴P^o states. In the present work, the fine-structure splittings for several quartet states are calculated. The results are quoted in Table III together with the energy for

the $J_1 = L + 1.5$ state. It is apparent from this table that states with a $2p$ electron have a considerably larger splitting as compared with other states. A very illustrative example is the ${}^{4}D$ states. The 1s 2snd ${}^{4}D$ states have very

		This work		
Experiment ^a	$I^{\rm b}$	Theory	Assignments	Other experiments
		18.089	$2s 2p^{4}P^{o}-2p 6p^{4}P$	
		18.873	$2s 2p$ ⁴ P^o -2p5p ⁴ P	
		19.763	$2s 2p^{4}P^{0}-2s 6s^{4}S$	
		20.502	$2s 2p$ ⁴ P^o -2p4p ⁴ S	
		20.516	$2s 2p^{4}P^{o}-2s 5d^{4}D$	
20.529 ± 0.005	w	20.529	$2s 2p$ ⁴ P^o -2p4p ⁴ P	20.521 ^g
20.67 ± 0.01	(b1)	20.662	$2s 2p$ ⁴ P^o -2p4p ⁴ D	20.66^{d} , $20.62(\text{b1})^{\text{e}}$
		20.857	$2s2p^{4}P^{o}-2s5s^{4}S$	
21.843 ± 0.005	vw	21.846	$2p 2p 4P - 2p 5d 4D^o$	21.8 ^d ,21.83 ^e ,21.843 ^g
22.451 ± 0.005	m	22.447	$2s 2p^{4}P^{o}-2s 4d^{4}D$	22.44 ^{d,e} ,22.45 ^g
23.110 ± 0.005	vw	23.110	$2s 2p^{4}P^{o}-2s 4s^{4}S$	23.08°, 23.14 ^g
23.860 ± 0.015	VW	23.868	$2p 2p 4P - 2p 4d 4P^o$	
23.962 ± 0.005	m	23.967	$2p 2p 4P - 2p 4d 4D^o$	24.05 ^d , 24.00 ^e , 23.972 ^g
25.478 ± 0.005	m	25.473	$2s 2p$ ⁴ P^o -2p3p ⁴ P	25.43d,h,25.46e,25.475g
25.650 ± 0.005	vw	25.648	$2s2p^{4}P^{o}-2p3p^{4}S$	25.656 ⁸ ,25.66 ^h
		26.033	$2s2p^{4}P^{o}-2p3p^{4}D$	

TABLE II. Wavelengths (in nm) associated with quartet states in CIV.

^aThe quoted uncertainties represent the error on the position of the line maximum (except for the 134.42-nm transition-see text). bObserved intensity. vw, very weak; w, weak; m, mean; s, strong; vs, very strong; bl, blended line.

^cValue obtained by taking into account the radiative correction of Ref. 12 (see Ref. 13).

^dBerry et al., Ref. 15.

^eBuchet-Poulizac, Ref. 16.

^fLivingston and Berry, Ref. 17.

^gTo et al., Ref. 18.

hJacques et al., Ref. 26.

Term	$-E_{J_{1}}$ (a.u.)	E_J - E_J	E_J - E_J	$E_{J_3} - E_{J_4}$
ls 2s 2p ⁴ P°	23.979819	94.27	3.778	
$1s$ $2s$ $3p$ $^4P^o$	22.433026	23.50	1.523	
1s 2p 3s 4P ^o	22.288355	104.82	11.41	
$1s2p3d4p^o$	22.121974	-37.09	-32.08	
1s 2p 4d ⁴ P°	21.732083	-46.22	-35.38	
ls 2p 2p ⁴ P	23.640857	39.91	76.01	
1s 2p 3p 4P	22.191 127	34.09	53.50	
ls 2p 4p ⁴ P	21.760414	33.94	49.44	
1s2p5p4P	21.565 639	33.82	48.09	
l s 2p 6p ⁴ P	21.460998	33.57	47.38	
l s 2s 3d 4D	22.374421	9.522	2.706	-0.014
ls 2p 3p ⁴ D	22.229 472	86.17	36.81	12.19
ls 2s 4d 4D	21.950155	1.917	0.246	-0.301
1 s 2p 4p ⁴ D	21.774 528	78.90	33.93	11.38
$1s$ 2s 5d 4D	21.759024	6.496	2.371	0.515
$1s$ $2p$ $3d$ 4 D^o	22.141468	6.979	26.51	24.52
$1s2p4d4^D$	21.739 809	6.198	26.25	24.48
$1s$ 2p 4 f 4F	21.736 650	-2.807	18.07	23.75
$1s 2p 3d ~^4F^o$	22.180110	64.64	32.82	14.09
l s $2s$ 4 f ^{4Fe}	21.931 575	1.156	0.309	-0.096

TABLE III. The fine structure of quartet system of CIV. $J_1 = L + 1.5$; $J_2 = L + 0.5$; $J_3 = L - 0.5$; $J_4 = L - 1.5$ (in cm⁻¹).

small splittings whereas those of the 1s $2pnp \,^4D$ states are much larger.

III. EXPERIMENTAL TECHNIQVE AND RESULTS

 C^+ beams of about 1 μ A (diameter 5 or 10 mm) are supplied by a 2- or a 3-MV Van de Graaff accelerator equipped with an rf source into which CO gas was admi'tted. Beam light emitted after the carbon foil $(\simeq 10$ μ g/cm²) is observed with a grazing-incidence spectrometer $(\lambda = 10 - 40$ nm) or with a Seya-Namioka-type spectrometer $(\lambda = 30 - 200 \text{ nm})$. The grazing-incidence spectrometer is equipped with a curved exit slit and five channeltron detectors; the Seya-Namioka with three channeltron detectors (λ < 125 nm) or with an EMR542G

TABLE IV. Newly observed lines in C III.

λ (nm)	Intensity ^a	Assignment	
172.54	w	$2p 3p 3P_2 - 2p 4d 3D_3^o$	TAI
170.33	m	$2s4p^{1}P_{1}^{o}-2p4p^{1}P_{1}$	λ (nm)
162.32	w	$2s4d^{1}D_{2}-2p4d^{1}D_{2}^{o}$	
154.58	m	$2s5p^{3}P_{1,2}^{0}-2p5p^{3}P_{2}$	165.44
150.16	s	2s 4p ${}^3P^o_{0,1,2}$ -2p 4p ${}^3P_{1,2}$	165.39
149.37	s	$2s4s3S_1 - 2p4s3P_2^o$	163.77
149.14	vw	2s 4d ${}^3D_{1,2,3}$ - 2p 4d ${}^3P_2^o$	144.01
140.36	vw	$2p$ 3d ${}^3D_{1,2,3}^o$ -2p 5p 3P_2	135.30^{b}
135.66	s	$2p\,3s\,{}^{3}P^{\circ}_{1,2}$ - 2p 4p ${}^{3}D_{2,3}$	135.14
131.43	(b1)	$2p 3s \frac{3p}{2} - 2p 4p \frac{3p}{2}$ _{1.2}	131.56
131.33	(b1)	$2p$ 3s ${}^3P^o_{0,1}$ - 2p 4p ${}^3P_{1,2}$	121.38
130.18	vw	$2p$ 3d ${}^{1}D_{2}^{\circ}$ - 2p 5p ${}^{1}D_{2}$	121.06
129.15	vw	$2p$ 3d ${}^{3}F^{o}_{3,4}$ - 2p 5f ${}^{3}F_{4}$	118.44
114.35	vw	$2p\,3p\,3D_{2,3} - 2p\,5d\,3D_3^o$	^a vw. verv weak:

 v^* ww, very weak; w, weak; m, mean; s, strong; bl, blended line.

photomultiplier tube $(\lambda > 105 \text{ nm})$. These two beam-foil spectroscopy arrangements are described in detail in Refs. 24 and 25, respectively.

Typical spectra of carbon between 22 and 26 nm and between 119 and 137 nm are shown in Figs. ¹ and 2, respectively. The experimental linewidths [full width at half-maximum (FWHM)] are about 0.04 nm with the grazing-incidence spectrometer and 0.07 nm with the Seya-Namioka spectrometer.

The wavelengths of the lines appearing in our spectra and assigned to transitions between quartet states in CIV on the basis of theoretical predictions are reported in Table II together with rough estimations of the observed line intensities. This table shows that an excellent agreement exists between our theoretical and experimental wavelengths.

TABLE V. Newly observed lines in CIV.

 α ^avw, very weak; w, weak; m, mean; vs, very strong. b Previously observed in Ref. 26 but at 135.20 nm.

INTENSITY (COUNTS/CHANNEL)

FIG. 1. A section of the beam-foil spectrum of carbon between 22 and 26 nm (grazing-incidence spectrometer). Assignments of newly classified lines are indicated.

Due to the wavelength resolution of the beam-foil spectra, the fine structure of the multiplets cannot generally be resolved. However, for the 134.4-nm transition two finestructure components are observed and the wavelength quoted is that of their center of gravity. Moreover, some predicted lines which are blended with other carbon lines cannot be observed.

The experimental wavelengths of the lines reported previously by other authors^{15–18,26} are quoted in Table II. However, some classifications based on earlier theoretical data have been changed. We note that eleven lines are observed for the first time in this work.

The term energies (E_{exp}) derived by a least-squares calculation from our observed wavelengths are listed in Table I. (The energies of the 1s 2s $2p^{4}P^{\circ}$ and 1s $2p 2p^{4}P$ terms have been kept constant and equal to the theoretical values). There is a very good agreement between our experimental and theoretical term energies. A11 the theoretical energies ($-E_{CG}$) lie slightly above their corresponding experimental values $(-E_{exp})$ except for the $1s2p4d^{4}P^{\circ}$ term. Let us note that the error for this term energy is larger than for the other terms due to the error on the wavelength determination for the $1s2p^2P-1s2p4d^4P^o$

transition which is blended with a C Iv line (see Table II).

We show in Fig. 3 the transitions observed in the quartet system of CIV on a partial term diagram. In this figure the absolute scale for the $2s2p^{4}P^{\circ}$ energy is set to be 294.084 eV above the $1s²2s²S$ energy of CIV. It is obtained by a direct calculation of this $2S$ state. This result agrees with a recent $2s 2p^4P^o - 1s^22s^2S$ transition measurement of Brenn²⁷ where $a \pm 0.1$ -eV experimental uncertainty is quoted. It is very different from the 294.72 eV of Berry et al.¹⁵ and the 294.552 eV of To et al.¹⁸

IV. NEW OBSERVED LINES IN C III AND CIy

Many lines appearing in our beam-foil spectra remain unidentified. We have classified twenty-four among them in CIII and CIV from known level energies.²⁸ In Tables IV and V, these new observed lines in CiII and CIv are quoted together with their classifications and estimations of their intensities. Some new observed lines can be seen in the spectrum shown in Fig. 2.

V. CONCLUSION

The present theoretical and experimental studies of the C IV quartet system lead to a term diagram for this system

FIG. 3. Term diagram of the quartet system of C IV.

more reliable and complete than those previously reported. Twenty-seven quartet states have been calculated together with 20 fine-structure splittings which are significant for many of these quartets. Twenty-seven lines appearing in the beam-foil spectra of carbon (11 observed for the first time) have been classified in the quartet system of Civ. The wavelengths observed for these transitions are in very good agreement with our theoretical predictions and with the other experimental data available.

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Twenty-four new lines appearing in our spectra have also been identified as transitions between known energy levels in C III and C Iv.

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