

## Hyperfine structure of $N_2$ ( $B^3\Pi_g$ and $A^3\Sigma_u^+$ ): Oscillatory $J$ dependence of the $^3\Pi_{0,1}$ hyperfine structure

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Laser-induced fluorescence on a beam of metastable  $N_2$  ( $A^3\Sigma_u^+$ ) molecules has been used to study the hyperfine structure of the (10,6) band of the  $N_2$  ( $B-A$ ) transition. The hyperfine structure of the  $B^3\Pi_0$  and  $^3\Pi_1$  states was found to have an unusual, oscillatory  $J$  dependence. This was explained by perturbation theory, and hyperfine-structure constants for the  $B$  state were derived from a data fit. At the same time results from earlier, less-direct experiments on the  $A$ -state hyperfine structure were confirmed and extended.

Using sub-Doppler laser spectroscopy, the hyperfine structure (hfs) of molecular transitions can be resolved. We have done hfs measurements on the (10,6) band of the  $N_2$  ( $B^3\Pi_g$ - $A^3\Sigma_u^+$ ) system by laser-induced fluorescence (LIF), crossing a beam of metastable  $N_2$  ( $A$ ) molecules at right angles with a dye laser beam. A very unusual hfs of the  $B^3\Pi_0$  and  $^3\Pi_1$  states was found, exhibiting an oscillatory dependence on  $J$ . This contrasts with the much more regular hfs of the  $A$  state, which is known from earlier, Rabi-type experiments on a beam of  $N_2$  ( $A$ ) (Refs. 1 and 2), but was determined in the present work for a much greater number of  $J$  levels.

$N_2$  ( $A$ ) molecules were prepared by striking a dc discharge  $\sim 2$  A directly in an  $N_2$  nozzle beam, using the nozzle itself as an anode. With a nozzle temperature of 720 K, nozzle diameter of 1 mm, and a backing pressure of 30 Torr, a rotational temperature of 315 K for  $N_2$  ( $A, v=6$ ) was measured by LIF. About 300 lines of the (10,6) band of  $N_2$  ( $B-A$ ) were recorded on a strip chart and were identified using molecular constants from the literature.<sup>3</sup> Using very slow ( $\sim 1$  MHz/sec) laser scan speeds, the hfs of all lines was measured with a resolution of up to 15 MHz full width at half maximum (FWHM), and with very good  $S/N$  ratio. The hfs splittings were determined using an interferometer with a 62.5-MHz free spectral range.

As an example, Fig. 1 shows the hfs pattern of the  $Q_{33}(2)$  line; 11 of the expected 13 components are resolved.

All distinguishable hfs components of all measured lines were identified, on the basis of the  $\Delta F=0, \pm 1$  selection rule and the approximate proportionality between line intensities and  $F$  values. hfs level splittings of both the  $N_2$  ( $B$ ) and  $N_2$  ( $A$ ) states were then derived from the measured splittings of the lines.

Figures 2 and 3 show the results. The level separations, as a function of  $J$ , are plotted relative to the central component (having  $F=J$ ), which is shown as a horizontal line. The estimated accuracy of the data is  $\pm 2$  MHz. In the  $N_2$  ( $A$ ) state, Fig. 2, hfs splittings of the  $F_1$  and  $F_3$  fine-structure terms (regular and inverted, respectively) tend to a constant limit with increasing  $J$ , while the  $F_2$  term shows a measurable hfs only for the lowest  $J$ . The hfs of  $N_2$  ( $B, ^3\Pi_{0,1,2}$ ) Fig. 3, is very striking: the splitting decreases monotonically, and in the same way for *ortho*- $N_2$  and *para*- $N_2$ . For  $^3\Pi_0$ , levels with no detectable splitting alternate with levels which are split. For *ortho*- $N_2$ , levels with even  $J$  are split; for *para*- $N_2$ , those with odd  $J$  are split. Here the magnitude of the splitting increases with  $J$ . Finally,  $^3\Pi_1$  is intermediate between  $^3\Pi_2$  and  $^3\Pi_0$ .

For  $N_2$  ( $A$ ), the hfs coupling constants and matrix elements given in Refs. 1 and 2 show that, by far, the most important contribution comes from the magnetic interaction [Eq. (A12) in Ref. 1]. From this expression, one obtains the energy separations between levels  $F$  and  $F-1$  of the  $F_1, F_2, F_3$  terms [Eqs. (1), (2), and (3), respectively]

$$\Delta E = c_0^2 (F/J) [\alpha - \beta(2J-2)/(2J+1)] + 3c_0c_1 F [J(J+1)]^{-1/2} [\beta/(2J+1)] [(2J+3)/(2J+1)]^{1/2}, \quad (1)$$

$$\Delta E = F/[J(J+1)] (\alpha + 2\beta), \quad (2)$$

$$\Delta E = -c_0^2 [F/(J+1)] [\alpha - \beta(2J+4)/(2J+1)] + 3c_0c_1 F [J(J+1)]^{-1/2} [\beta/(2J+1)]. \quad (3)$$

The coefficients  $c_0 = [(R+\delta)/(2R)]^{1/2}$  and  $c_1 = [(R-\delta)/(2R)]^{1/2}$  describe the contributions of wave functions with  $N=J+1$  and  $N=J-1$  [Ref. 1, Eqs. (11)–(15)] to the wave function appearing in Ref. 1, Eq. (A12). Here,  $R = (\delta^2 + 4X^2)^{1/2}$ , with

$$\delta = 2B(2J+1) - 2\lambda/(2J+1)$$

and

$$X = 2\lambda [J(J+1)]^{1/2}/(2J+1),$$

where  $\lambda = -1.2935 \text{ cm}^{-1}$ ,  $B = 1.3345 \text{ cm}^{-1}$ . The constants  $\alpha = 12.657 \pm 0.013 \text{ MHz}$  and  $\beta = -12.540 \pm 0.009 \text{ MHz}$  for  $N_2$  ( $A, v=6$ ) are given in Ref. 2 and describe the Fermi contact and the dipolar interaction, respectively. The dashed curves in Fig. 2 were calculated from Eqs. (1)–(3), and are seen to fit our data very well, over a much wider range of  $J$  levels than were studied in Ref. 1.

In the  $B^3\Pi_g$  state, we again consider only magnetic hfs interactions. hfs formulas for Hund's case (a) are given in Ref. 4. One important conclusion is that a  $^3\Pi_0$  state should

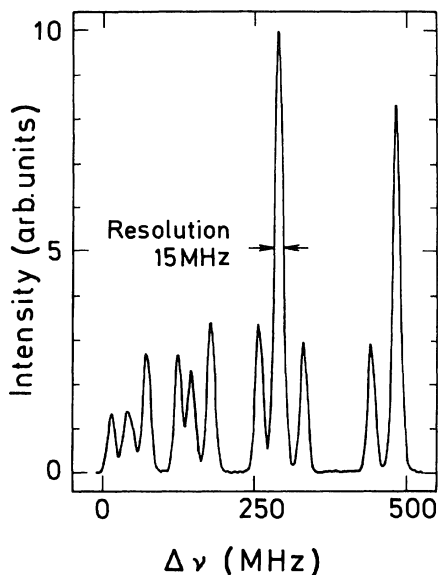


FIG. 1. Hyperfine splitting of the  $Q_{33}(2)$  line of the  $N_2$  ( $B-A$ ), (10,6) band at  $17145.03 \text{ cm}^{-1}$ .

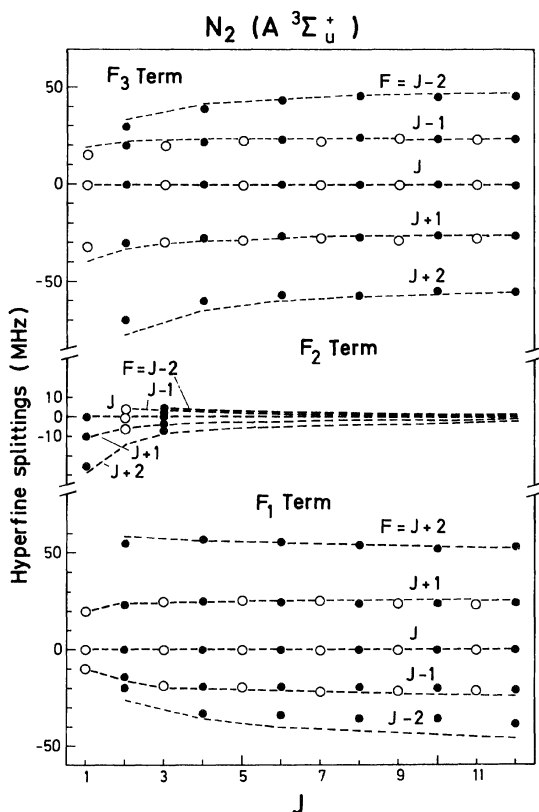


FIG. 2. Hyperfine splitting of the  $N_2$  ( $A, v=6$ ) levels. Dots ( $o-N_2$ ) and circles ( $p-N_2$ ) are measured, dashed lines are calculated.

not have any magnetic hfs at all. Our observation (Fig. 3), therefore, indicates that the  $^3\Pi_0$  wave functions are not purely case (a), but are perturbed by the molecular rotation. The rotation Hamiltonian  $B(\vec{J}-\vec{L}-\vec{S})^2$  perturbs the "pure" Hund's case (a) wave functions  $|\Omega\rangle$ , to give in first order<sup>5</sup> [with  $x=J(J+1)$ ],

$$|\psi^\pm\rangle_{\Omega=0} = |0^\pm\rangle - (B/A)(2x)^{1/2}|1^\pm\rangle, \quad (4)$$

$$|\psi^\pm\rangle_{\Omega=1} = |1^\pm\rangle + (B/A)(2x)^{1/2}|0^\pm\rangle - (B/A)(2x-4)^{1/2}|2^\pm\rangle, \quad (5)$$

$$|\psi^\pm\rangle_{\Omega=2} = |2^\pm\rangle + (B/A)(2x-4)^{1/2}|1^\pm\rangle. \quad (6)$$

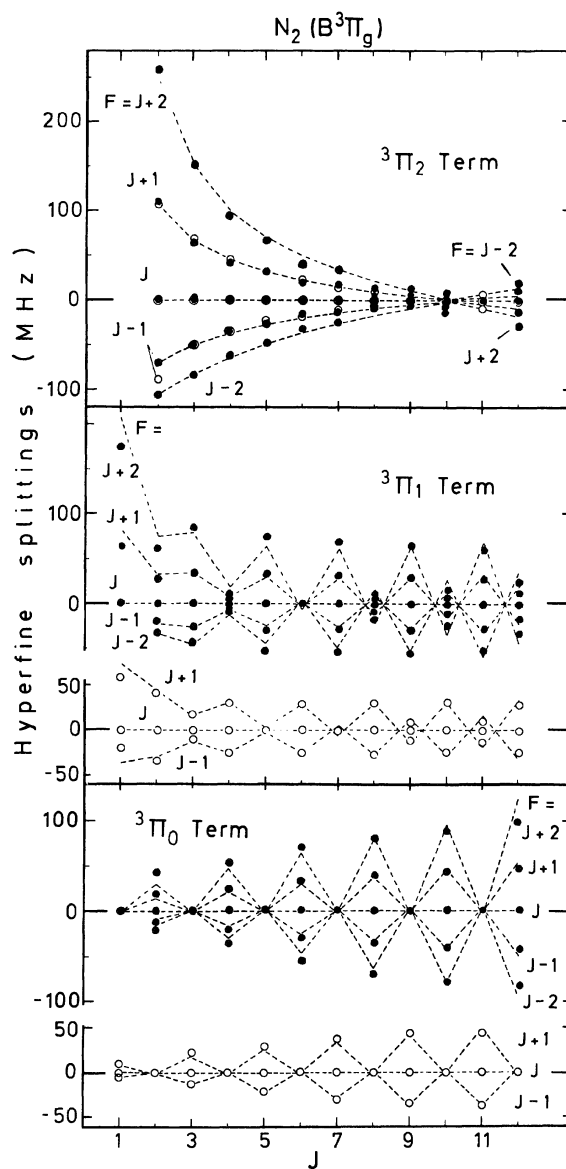


FIG. 3. Same as Fig. 2, for  $N_2$  ( $B, v=10$ ). In the  $^3\Pi_2$  term the hfs is almost identical for  $o-N_2$  and  $p-N_2$ .

$B = 1.44098 \text{ cm}^{-1}$  is the rotational constant and  $A = 41.525 \text{ cm}^{-1}$  is the spin-orbit coupling constant of N<sub>2</sub> ( $B, v = 10$ ) (Ref. 3), and  $|\Omega^\pm\rangle = [|\Omega\rangle \pm |-\Omega\rangle]/\sqrt{2}$ . In Ref. 4, hyperfine matrix elements for the nonparity states  $|\Omega\rangle$  and  $|-\Omega\rangle$  are given. From Ref. 4, Eq. (3) and Table II, one obtains the following matrix elements between the parity states  $|\Omega^\pm\rangle$ :

$$\langle 2^\pm | H | 2^\pm \rangle = y(2/\sqrt{6})[2D_{11}/\sqrt{30} + \sqrt{6}G_{11} + K_{11}] , \quad (7)$$

$$\langle 2^\pm | H | 1^\pm \rangle = y[(x-2)/12]^{1/2}[D_{11}/\sqrt{30} - K_{11}] , \quad (8)$$

$$\langle 1^\pm | H | 1^\pm \rangle = yG_{11} , \quad (9)$$

$$\langle 1^\pm | H | 0^\pm \rangle = y(x/12)^{1/2}[D_{11}/\sqrt{30} - K_{11} \mp D_{1-1}/\sqrt{5}] , \quad (10)$$

$$\langle 0^\pm | H | 0^\pm \rangle = 0 . \quad (11)$$

$H$  is the hyperfine Hamiltonian including only magnetic dipole terms [the quadrupole interaction would, e.g., give a nonvanishing term in Eq. (11)], and

$$y = [F(F+1) - I_T(I_T+1) - J(J+1)]/[2J(J+1)] ,$$

with the total nuclear spin  $I_T$ .  $G_{11}$ ,  $K_{11}$ ,  $D_{11}$ , and  $D_{1-1}$  are molecular parameters describing the nuclear spin-orbit interaction ( $G_{11}$ ), the Fermi contact interaction ( $K_{11}$ ), and the dipolar interaction ( $D_{11}$  and  $D_{1-1}$ ) for each nucleus separately, as defined in Ref. 4, Table II [the label (1) used in Ref. 4 to indicate nucleus 1 has been dropped for brevity]. The energies (7)–(11) include factors of 2 from the summation over both nuclei.

The diagonal matrix elements of the perturbed states,  $\langle \psi^\pm |_{\Omega=0,1,2} H | \psi^\pm \rangle_{\Omega=0,1,2}$ , are obtained from the expressions (4)–(6), using (7)–(11). Keeping only terms linear in  $B/A$ , we then find the energy differences between terms  $F$  and  $F-1$ , in the  $\Omega = 2$  case,

$$\begin{aligned} \Delta E = (F/x) \{ & 2G_{11} + 4D_{11}/(3\sqrt{20}) + \sqrt{6}K_{11}/3 \\ & + (B/A)(x-2)[2D_{11}/(3\sqrt{20}) - \sqrt{6}K_{11}/3] \} . \end{aligned} \quad (12)$$

This splitting obeys the Landé interval rule, and decreases essentially as  $1/J$  in the limit of large  $J$ , in agreement with the observation (Fig. 3, top).

Similarly for the <sup>3</sup>Π<sub>0</sub> state, one finds the energy differences between the diagonal elements  $F$  and  $F-1$ :

$$\Delta E = (FB/A) [ \pm 2D_{1-1}/\sqrt{30} - 2D_{11}/(3\sqrt{20}) + \sqrt{6}K_{11}/3 ] . \quad (13)$$

Thus the zero-order term makes no contribution to the hfs. The splitting results solely (in our approximation) from the perturbation of <sup>3</sup>Π<sub>0</sub> by <sup>3</sup>Π<sub>1</sub>. It has the interesting property of being of different magnitude for the  $|\psi^+\rangle$  and  $|\psi^-\rangle$  states. These correspond to the two  $\Lambda$  doublet components of each <sup>3</sup>Π<sub>0</sub> $J$  level. The extremely small hfs splitting for alternate  $J$  levels, of a given N<sub>2</sub> modification (Fig. 3, bottom) can then be associated with the subtractive combination of the constants in Eq. (13). [The constants given in Eq. (15) happen to be such that for these levels, an overall  $\Delta E \leq 3$  MHz results.] The other levels of the same modification will then have an additive combination of terms and a large splitting, as is in fact observed. For a given  $J$ , the two modifications are associated with opposite signs in  $|\Omega^\pm\rangle$  and  $|\psi^\pm\rangle$ , which explains the out-of-phase oscillation of the hfs for *ortho*-N<sub>2</sub> and *para*-N<sub>2</sub>.

Finally, for the <sup>3</sup>Π<sub>1</sub> state, the hfs energy differences are

$$\begin{aligned} \Delta E = (F/x) [ & G_{11} + (B/A)(4D_{11}/(3\sqrt{20}) \\ & - 2\sqrt{6}K_{11}/3) ] \mp (F2B/A)D_{1-1}/\sqrt{30} . \end{aligned} \quad (14)$$

This shows clearly the observed decreasing  $\Delta E$  with increasing  $J$ , superimposed by an oscillatory term which increases with  $F$  (and  $J$ ). Note that the oscillations in the <sup>3</sup>Π<sub>1</sub> and <sup>3</sup>Π<sub>0</sub> states are predicted to be out of phase, again in agreement with the observation (Fig. 3, middle and bottom).

From a least-squares fit to all data, the following set of hfs constants was derived for N<sub>2</sub> ( $B, v = 10$ ):

$$\begin{aligned} G_{11} &= 82 \text{ MHz}; \quad D_{11} = 0 \text{ MHz}; \\ K_{11} &= 69 \text{ MHz}; \quad D_{1-1} = -171 \text{ MHz} . \end{aligned} \quad (15)$$

Using these constants and Eqs. (12)–(14), the dashed lines shown in Fig. 3 were calculated. The overall fit with the experimental data is very satisfactory; the remaining discrepancies are ascribed partly to the first-order perturbation theory and partly to our neglect of the quadrupole interaction. The first-order treatment alone is not responsible: Excluding from the fit the  $J = 9$ – $12$  data points, where this approximation begins to fail, the agreement was only slightly improved. The above constants are therefore only tentative, and a more rigorous analysis is in progress.

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