## PHYSICAL REVIEW A

## VOLUME 21, NUMBER 6

## **Comments and Addenda**

The section Comments and Addenda is for short communications which are not appropriate for regular articles. It includes only the following types of communications: (1) Comments on papers previously published in The Physical Review or Physical Review Letters. (2) Addenda to papers previously published in The Physical Review or Physical Review Letters, in which the additional information can be presented without the need for writing a complete article. Manuscripts intended for this section must be accompanied by a brief abstract for information-retrieval purposes. Accepted manuscripts follow the same publication schedule as articles in this journal, and page proofs are sent to authors.

## Pretransitional viscosity in the isotropic phase of cholesteric liquid crystals

P. P. Crooker and W. G. Laidlaw\*

Department of Physics and Astronomy, University of Hawaii, Honolulu, Hawaii 96822 (Received 18 September 1979; revised manuscript received 11 February 1980)

The measurements of the anomalous effective viscosity  $\eta$  obtained by Keyes and coworkers are analyzed in terms of the two separate viscosity coefficients  $\nu$  and  $\mu$ .

In the past several years a number of papers have appeared in which the pretransitional behavior near the isotropic to cholesteric transition has been probed.<sup>1</sup> Of particular interest have been those cases such as cholesteryl oleyl carbonate (COC) where an intermediate "blue phase" can be detected.<sup>2</sup>

Recently, Keyes and coworkers<sup>3,4</sup> reported light scattering and shear viscosity measurements near the transition temperature which show, to quote Keyes and Yang,<sup>3</sup> "an anomaly in the viscosity coefficient  $\nu$  similar to the anomaly in  $\eta$ ." These authors go on to comment that the anomalous decrease in  $\nu$  goes<sup>3</sup> "hand-in-hand with the increase in  $\eta$ ."

A careful analysis of the pretransitional theory of liquid crystals leads one to the position that the shear viscosity  $\eta$  measured in a capillary-flow experiment is an effective viscosity which depends explicitly on "uncoupled or ordinary shear viscosity  $\eta_0$ ." For example, Stephen and Straley<sup>5</sup> as long ago as 1974 pointed out that the shear viscosity is  $\eta_0 = \eta' + \nu^2/\xi$  which, in terms of the notation employed by DeGennes<sup>6</sup> and subsequently, by Keyes *et al.*, is just

$$\eta = \eta_0 + 2\mu^2 / \nu \,. \tag{1}$$

We argue that the ordinary viscosity does not have anomalous behavior in the region of a liquid-crystal transition so that the anomalous behavior in  $\eta$ can then be attributed to the anomalous behavior in  $\nu$  and/or the anomalous behavior of  $\mu$ .

We now apply these ideas to the interpretation of the viscosity data of Keyes *et al.*<sup>3,4</sup> (see Fig. 1).

In the temperature region of COC where the viscosities show only Arrhenius-type temperature dependence, Harada and Crooker<sup>1(a)</sup> have shown



FIG. 1. Coefficients of the hydrodynamical equations.  $\eta$  (poise) and  $\nu'$  (10<sup>-5</sup> s K) are from Ref. 3.  $\eta_0$  (poise),  $\sqrt{2/k} \ \mu (10^{-5} \text{ s K poise})^{1/2}$  and  $-\sqrt{k} \ \lambda (\text{poise}/10^{-5} \text{ s K})^{1/2}$  are discussed in text.

2174

21

that  $\mu^2/\eta\nu = 0.093$ , a value similar to that found in

nematics.<sup>7</sup> Using Eq. (1) we then get  $\eta_{0A} = 0.81\eta_A$ where the subscript A refers to values in the Arrhenius region. We now postulate that  $\eta_0$  remains Arrhenius-type well into the anomalous region; this is reasonable since  $\eta_0$  is the ordinary or uncoupled viscosity and we associate the anomalous behavior with order-parameter coupling. Hence,

 $\eta = 0.81 \eta_A + 2\mu^2/\nu$ 

and the anomaly in  $\eta$  will be due to the anomalous behavior of  $\mu$  and  $\nu$ .

Given the data reported by Keyes and Yang for  $\eta$  and  $\nu' = \nu/k$  (k is a constant), it is now an easy matter to extract the temperature dependence of  $\mu$  as shown in Fig. 1. We find that  $\mu$  shows a very significant pretransitional increase which, together with the decrease in  $\nu$ , results in the sig-

- \*Permanent address: Department of Chemistry, University of Calgary, Calgary, Alberta, Canada T2N 1N4.
- <sup>1</sup>(a) C. C. Yang, Phys. Rev. Lett. <u>28</u>, 955 (1972); (b)
  T. Harada and P. P. Crooker, *ibid.* <u>34</u>, 1259 (1975);
  (c) D. S. Mahler, P. H. Keyes, and W. B. Daniels, *ibid.* <u>36</u>, 491 (1976); (d) J. Cheng and R. B. Meyer, Phys. Rev. A <u>9</u>, 2744 (1974).
- <sup>2</sup>D. Coates and G. W. Gray, Phys. Lett. <u>51A</u>, 335 (1975);
  D. Demus, H.-G. Hahn, and F. Kuschel, Mol. Cryst. Liq. Cryst. <u>44</u>, 61 (1978); U. Wurz, G. Klar, and S.-K. Chan, J. Phys. (Paris) <u>40</u>, C3-404 (1979).

nificantly increased  $\eta$ . Also, we calculate the temperature dependence of the flow-order-parameter-coupling coefficient  $\lambda$  which, along with  $\eta_0$  and  $1/\nu$ , would appear naturally in the expression for the order-parameter flux  $R_{\alpha\beta}$  in terms of the conjugate forces  $e_{\alpha\beta}$  and  $\phi_{\alpha\beta}$  as in

$$(\partial/\partial t)Q_{\alpha\beta} = R_{\alpha\beta}, \ R_{\alpha\beta} = \lambda e_{\alpha\beta} + (1/\nu)\phi_{\alpha\beta}$$

and in the momentum equation

$$(\partial/\partial t)(\rho v_{\alpha}) = \partial/\partial_{\beta}\sigma_{\alpha\beta}, \quad \frac{1}{2}\sigma_{\alpha\beta} = \frac{1}{2}\eta_{0}e_{\alpha\beta} - \lambda\phi_{\alpha\beta}.$$

Figure 1 shows that  $\lambda$  exhibits an anomalous increase at the phase transition which parallels that of  $1/\nu$ . This is not unexpected since both  $\lambda$  and  $1/\nu$  are coefficients associated with the order-parameter coupling.

Experiments to independently probe the pretransitional behavior of  $\mu$  (which our analysis predicts) would seem to be in order.

- <sup>3</sup>P. H. Keyes and C. C. Yang, J. Phys. (Paris) <u>40</u>, C3-376 (1979).
- <sup>4</sup>P. H. Keyes and D. G. Ajgaonkar, Phys. Lett. <u>64A</u>, 298 (1977).
- <sup>5</sup>M. J. Stephen and J. P. Straley, Rev. Mod. Phys. <u>46</u>, 617 (1974).
- <sup>6</sup>P. G. DeGennes, Mol. Cryst. Liq. Cryst. <u>12</u>, 193 (1971).
- <sup>7</sup>T. W. Stinson, J. D. Litster, and N. A. Clark, J. Phys. (Paris) <u>33</u>, C1-69 (1972); P. Martinoty, F. Kiry, S. Nagai, S. Candau, and F. DeBeauvais, *ibid.* 38, 159

(1977).