# L-vacancy production in near-symmetric heavy-ion collisions ( $Z \gtrsim 35$ )

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The authors have measured the projectile and target L x-ray spectra and cross sections for 41-MeV Ta projectiles bombarding thin targets between Ag and Th and for 17-60-MeV collisions of Ho on Ho, Au on Au, Pb on Pb, and U on Th. These cross sections, as well as those measured elsewhere, are examined in terms of a simple vacancy-sharing model involving the  $4f\sigma$  and  $3d\sigma$  molecular orbitals (MO). From the  $L\beta_1/L\alpha$  x-ray intensity ratios it is found that in symmetric collisions the  $4f\sigma$  MO correlates to the  $2p_{3/2}$  level of the collision partners (correlation rule of Barat and Lichten). As the asymmetry of the collision system increases, there is an increasing tendency for the  $4f\sigma$  MO to correlate to the 2s level of the lower-Z collision partner (correlation rule of Eichler and collaborators). The physical basis for the shift of the  $4f\sigma$  MO correlation is discussed.

## I. INTRODUCTION

A search of the literature reveals that to date only a few systematic measurements have been made of the *L* x-ray line structure and production cross sections in near-symmetric collisions with  $Z \ge 35.^1$  Notable is the work of Datz *et al.*<sup>2</sup> and of Hagmann *et al.*,<sup>3</sup> who bombarded a range of targets between  ${}_{6}C$  and  ${}_{92}U$  with 6–60–MeV  ${}_{53}I$  projectiles. Datz *et al.*<sup>2</sup> found strong variations in the  $L\beta_1/L\alpha$  x-ray intensity ratio as a function of target *Z*, which point to quasimolecular effects involving level matching. Hagmann *et al.*<sup>3</sup> have attempted a quantitative explanation of the variation in terms of avoided molecular-orbital (MO) level crossings.

In order to extend the available data and to investigate the role of quasimolecular effects in near-symmetric high-Z collisions more fully, we made various measurements of projectile and target L x-ray spectra and cross sections. Using 41-MeV <sub>73</sub>Ta projectiles, a variety of targets between  $_{47}$ Ag and  $_{90}$ Th were bombarded. Also some collision systems were studied as a function of projectile energy between 17 and 60 MeV:  $_{67}$ Ho-Ho,  $_{79}$ Au-Au,  $_{82}$ Pb-Pb,  $_{92}$ U-Th.<sup>4</sup>

The thrust of our work in the framework of the present understanding of L-shell vacancy production is as follows. If a series of targets  $(Z_t)$  is bombarded with a given projectile  $(Z_p)$  at a fixed bombarding energy  $(E_p)$ , regular variations of the cross-section magnitude with  $Z_t$  are found in the target and projectile cross sections, whenever the inner-shell binding energies of the two collision partners happen to match.<sup>5-7</sup> Such levelmatching effects in L x-ray production have been investigated by Kavanagh *et al.*<sup>8</sup> Using the work of Barat and Lichten<sup>9</sup> on electron promotion, Fortner<sup>10</sup> has shown also that in near-symmetric collisions, vacancies are brought into the L levels of the collision partners via the 4*fo* MO. This orbital correlates to the L levels of the lower-Zcollision partner (see Fig. 1, adapted from Ref.



FIG. 1. Diabatic correlation diagram for an asymmetric collision ( $_{36}$ Kr+ $_{54}$ Xe) according to Eichler *et al.* (Ref. 11). The vertical dashed line indicates the vacancy-sharing process examined in this paper. The vacancy-sharing probability  $w_L$  is discussed in Sec. III A.

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11). From the L-vacancy production in the higher-Z partner, Fortner<sup>10</sup> could show that  $3d\sigma$ -vacancy production is at least an order of magnitude smaller than the  $4f\sigma$ -vacancy production in the systems investigated by him ( $E_p = 15-200$  keV,  $Z_p = 15-19$ ,  $Z_t = 6, 18$ ). Since these systems are relatively light, fluorescence effects inhibited accurate determinations of vacancy cross sections.

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As the L levels of the higher-Z and lower-Z partners approach, one expects vacancy sharing to take place on the outgoing part of the collision due to the long-range radial coupling between the MO's correlating to the L levels of the two partners, similar to that found for the K levels.<sup>12-14</sup> (L-vacancy sharing on the ingoing part of a collision has already been established by the work of Lennard and Mitchell.<sup>15</sup>) Since six L levels come into play in the vacancy-sharing process, the situation is even more complex than in K-Lvacancy sharing which involves four levels.<sup>16</sup> For this reason we have applied a simple model to the L-L vacancy sharing process, which despite its schematic nature leads to a reasonable understanding of L-vacancy production in near-symmetric collisions. The model assumes that the relevant inner-shell vacancies are formed in the  $4f\sigma$  MO by ionization<sup>17</sup> or electron promotion<sup>9,10</sup> at small internuclear distances in single- or multiple-collision processes and that on the outgoing part of the collision long-range radial coupling of the Demkov form<sup>12,18</sup> distributes the vacancies between the various MO's leading to the separated atom (SA) L levels. (In the K-L level matching case<sup>16</sup> a more flexible model<sup>19</sup> had to be used, but such a model would introduce too many arbitrary parameters here. See also Ref. 20.)

Our model indicates that in symmetric collisions the 4f $\sigma$  MO correlates to the  $2p_{3/2}$  SA level, as originally proposed by Barat and Lichten,<sup>9</sup> and not to the 2s SA level as suggested by Eichler *et al.*<sup>11</sup> for high-Z systems. On the other hand, if the collision system is asymmetric, the correlation of the 4f $\sigma$  MO seems to shift toward the 2s SA level of the lower-Z collision partner, in accord with the suggestion of Eichler *et al.*<sup>11</sup>

We do not have a model to represent the primary  $4f\sigma$ -vacancy production, but show that the cross-section scales in a manner similar to that found for  $2p\sigma$ - and  $3d\sigma$ -vacancy production.<sup>17,21</sup> Hence, similar mechanisms might operate in all these cases. As in  $3d\sigma$ -vacancy production, there is no clear evidence for multiple-collision effects.<sup>16,17</sup>

In Sec. II, experimental details are given. Experimental results are related to our vacancysharing model in Sec. III. A scaling law for the  $4f\sigma$  cross section is given in Sec. IV. A physical basis for the findings of Sec. III is discussed in Sec. V.

#### **II. EXPERIMENT**

The 6-MV tandem Van de Graaff accelerator of the Swiss Federal Institute of Technology was used to produce beams of 17-60-MeV 67Ho, 73Ta,  $_{79}$ Au,  $_{82}$ Pb, and  $_{92}$ U. Targets of 20-50  $\mu$ g/cm<sup>2</sup> thick 50Sn, 62Sm, Ho, Ta, Au, Pb and 90ThF, deposited on  $20-\mu g/cm^2$  C foils and self-supporting targets of 90- $\mu$ g/cm<sup>2</sup> <sub>47</sub>Ag and 150- $\mu$ g/cm<sup>2</sup> Au were mounted in a 25-cm-diam target chamber at 45° to the beam direction. The x rays passed through 50-300- $\mu$ m Al absorbers and a 37- $\mu$ m Be window before entering a  $80-mm^2 \times 5-mm$  Si (Li) detector placed at 90° to the beam. The particle current was determined by Rutherford scattering of the beam by the target foils into a surface-barrier detector at  $30^{\circ}$  to the beam. Counts due to recoiling C atoms from the target backing were eliminated by pulse-height analysis.

X-ray cross sections could be obtained directly from the x-ray and particle counts, by comparison with the screened Rutherford cross section integrated over the face of the detector. Corrections were made for deadtime, absorption, detection efficiency and for a continuum background under the characteristic x-ray lines. For the Ho and Au beams, separate measurements were made of the projectile x-ray production by the C backing foil: this was always less than 2% of the x-ray yield due to the heavy-atom targets. Typical errors for the total L x-ray cross sections were between 2% and 10%. A computer program was used to separate the L x-ray spectra into  $Ll, L\alpha, L\beta(1)$ ,  $L\beta(2)$  and  $L\gamma$  line groups.<sup>2,3,16</sup> The relevant groups are defined in Sec. III B. Because of possible systematic errors introduced in the separation procedure, we assign a maximum uncertainty of  $\pm 30\%$  to the absolute line-group cross sections. Further experimental details are described in Ref. 4.

For comparison with a theoretical model it is necessary to relate the experimental line-group cross sections to the cross sections for primary vacancy production in  $L_1$ ,  $L_2$ , and  $L_3$  subshells of each collision partner. Details of this procedure are discussed in Sec. III B below and in Appendix A of Ref. 16. Here we mention only that uncertainties in the fluorescence yields and in the Coster-Kronig transition probabilities caused by solid-target effects may cause overestimates in vacancy-production cross sections by as much as a factor of 2 (see Ref. 16 and Sec. II of Ref. 17). Since we use mainly cross-section ratios in comparisons with our model, the error should be considerably smaller. In view of the fact that our model is schematic, it did not seem worthwhile to use more refined methods of crosssection analysis, such as those employed by Hagmann *et al.*<sup>3</sup>

Figure 2 gives an overview of our total Lvacancy cross sections for the 41-MeV  $_{73}$ Ta beam<sup>4</sup> as a function of target Z and compares these with 43-MeV 35Br and 47-MeV 53I cross sections.<sup>16</sup> In the L-L level matching region, i.e., near symmetry, the cross section trends in all three cases are similar. A quantitative discussion is given in Sec. IIIA. Results for L-subshell crosssection ratios are presented and examined in Secs. III B and III C.

#### III. L-L VACANCY-SHARING MODEL

## A. Total L cross sections

As mentioned in Sec. II, we assume that vacancies created in the 4fo MO at small internuclear distances are shared on the outgoing part of the collision between the MO's leading to the SA L levels. If one does not differentiate the SA L subshells, one can define an overall vacancysharing probability  $w_L$  indicated in Fig. 1. The total L-vacancy cross sections of the two collision partners can then be evaluated in terms of the MO-vacancy cross sections, analogous to the K-K vacancy sharing case [Eqs. (2) and (3) of Ref. 22]:

$$\sigma_L(h) = (1 - w_L)\sigma(3d\sigma) + w_L\sigma(4f\sigma) , \qquad (1)$$

$$\sigma_L(l) = w_L \sigma(3d\sigma) + (1 - w_L)\sigma(4f\sigma) + \sigma_{L-M}, \qquad (2)$$

(c) 41-MeV Ta (a) 43-MeV Br (b) 47-MeV Lp

where  $\sigma_L(h)$  and  $\sigma_L(l)$  are the *L*-vacancy-production cross sections of the higher-Z and lower-Z collision partners, respectively. In Eqs. (1)and (2) we have included the possibility that vacancies created in the  $3d\sigma$  MO can also end up in the SA L levels<sup>9,10</sup> (see Fig. 1). In analogy with the K-K vacancy-sharing case<sup>22</sup> we have assumed that the vacancy-sharing probabilities for the  $4f\sigma$  and 3do MO's are identical. We have also envisaged the possibility that for sufficiently asymmetric collision the lower-Z collision partner can obtain vacancies from the 5go MO (see Fig. 1), producing an additional cross section  $\sigma_{L-M}$ . This cross section is expected to dominate  $\sigma_L(l)$ , if the L(l)and M(h) levels overlap,<sup>8,9</sup> leading to a situation analogous to K-L level matching.<sup>16,20</sup>

For near-symmetric collisions one finds experimentally<sup>10,16</sup>

$$\sigma(3d\sigma) \ll \sigma(4f\sigma) , \quad \sigma_{L-M} \ll \sigma(4f\sigma) , \quad (3)$$

so that Eqs. (1) and (2) then yield

$$\sigma_L(h) + \sigma_L(l) \cong \sigma(4f\sigma) , \qquad (4)$$

$$\sigma_L(h)/\sigma_L(l) \simeq w_L/(1-w_L) . \tag{5}$$

These equations allow one to test experimentally model calculations of  $\sigma(4f\sigma)$  and of  $w_L$ . The 4f $\sigma$ cross section is discussed in Sec. IV. Here we concentrate on  $w_L$ .

It is tempting to apply the model calculation of the K-K vacancy-sharing probability<sup>12</sup> to L-L vacancy sharing, since in both cases one deals with near-symmetric collisions. Such a step would be particularly justified, if L-vacancy sharing takes place mainly between identical subshells of the collision partners:  $L_1(l) \rightarrow L_1(h)$ , etc. (It turns out that this is not the case.) Then

> FIG. 2. Vacancy cross sections plotted as a function of target atomic number for (a) 43-MeV <sub>35</sub>Br (Ref. 16), (b) 47-MeV 53I (Ref. 16), and (c) 41-MeV 73Ta (Ref. 4). Capital letters refer to the shells (subshells are not distinguished) and the subscripts to projectile (p) and target (t). Dashed vertical lines indicate symmetric collisions.



one finds from Ref. 12,

$$w_L/(1 - w_L) = \exp(-2x_L)$$
, (6)

where

$$2x_{L} = \pi (I_{h}^{1/2} - I_{l}^{1/2}) / (\frac{1}{2}mv_{p}^{2})^{1/2}.$$
<sup>(7)</sup>

Here  $I_h$  and  $I_l$  are the *L*-ionization energies of the higher-*Z* and lower-*Z* collision partners, *m* is the electron mass and  $v_p$  the projectile velocity.

In Fig. 3, we compare Eq. (6) with  $our^4$  and other<sup>16,23</sup> data for  $_{47}Ag$ ,  $_{53}I$ ,  $_{73}Ta$ , and  $_{92}U$  projectiles bombarding various targets near symmetry. We have made two different assumptions for  $I_h$  and  $I_l$ . In Fig. 3(a),  $I_h$  and  $I_l$  were chosen to be the  $L_2$ -subshell binding energies of each partner  $(L_1 \text{ or } L_3 \text{ could have been used equally})$ well), corresponding to the assumption that vacancy sharing takes place mainly between identical subshells. In Fig. 3(b),  $I_h$  and  $I_l$  were chosen to be equal to the  $L_3$  binding energy of the higher-Z partner and the  $L_1$  binding energy of the lower-Z partner, respectively, corresponding to the assumption that vacancy sharing depends primarily on the energy separation of the MO's leading to the SA levels and less on their electronic configurations. One sees from Fig. 3(b), that the latter choice for  $I_h$  and  $I_l$  gives a much better agreement with Eq. (6), than the former. This leads to two conclusions. First, energy separation between MO's appears to be the most important quantity determining vacancy sharing. Second, in near-symmetric collisions the Demkov model<sup>12,18</sup> may be used to estimate vacancy-sharing ratios. This model takes into account, albeit schematically, the energy separation between levels which couple.

### B. L-subshell cross sections

## 1. Symmetric collisions

We were able to obtain experimentally cross sections for Ll,  $L\alpha$ ,  $L\beta(1)$ ,  $L\beta(2)$ , and  $L\gamma$  line groups for various symmetric collision systems. As discussed in Appendix A of Ref. 16, the Ll,  $L\alpha$ , and  $L\beta(2)$  cross sections all reflect transition probabilities to the  $L_3$  subshell, so that only one of these cross sections, e.g.,  $L\alpha$  is sufficient to examine  $L_3$ -vacancy production. The  $L\beta(1)$  and  $L\gamma$  x-ray cross sections reflect combinations of transitions to the  $L_1$  and  $L_2$  subshells, unfortunately with similar relative transition probabilities. Therefore, one cannot extract the individual  $L_{\rm 1}\text{-}$  and  $L_{\rm 2}\text{-vacancy production cross}$ section from these groups.<sup>24</sup> But it is sufficient to examine one of these line groups, e.g.,  $L\beta(1)$ , in order to obtain information on the combination of  $L_1$ - and  $L_2$ -vacancy production cross sections.



FIG. 3. Target-to-projectile *L*-vacancy cross-section ratio for near-symmetric collisions vs scaling parameter  $2x_L$  defined in Eq. (7). See text (Sec. III A) for difference between (a) and (b). Line is model prediction of Eq. (6). Symbols have the following meaning:  $\bigcirc 23-58-$ MeV  $_{92}U+_{82}$ Pb (Ref. 4);  $\blacklozenge, \blacktriangle, \bigtriangledown, \blacksquare, 41-$ MeV  $_{73}$ Ta+ $_{67}$ Ho,  $_{79}$ Au,  $_{82}$ Pb,  $_{90}$ Th (Ref. 4),  $\bigcirc 47-$ MeV  $_{53}$ I projectiles on various targets (Ref. 16),  $\square$  15-MeV  $_{47}$ Ag projectiles on various targets (Ref. 23).

Calling  $\sigma_1$ ,  $\sigma_2$ , and  $\sigma_3$  the primary  $L_1$ -,  $L_2$ -, and  $L_3$ -subshell vacancy-production cross sections, and  $\sigma'_2$  and  $\sigma'_3$  the Coster-Kronig altered cross sections, one finds for the  $L\alpha$  and  $L\beta(1)$  line group x-ray cross sections.<sup>3,16,25</sup>

$$\sigma_{\alpha} = \sigma_3' \omega_3 (\Gamma_{3,M4} + \Gamma_{3,M5}) / \Gamma_3, \qquad (8)$$

$$\sigma_{\beta(1)} = \frac{\sigma_2' \omega_2 \Gamma_{2,M4}}{\Gamma_2} + \frac{\sigma_1 \omega_1 (\Gamma_{1,M2} + \Gamma_{1,M3})}{\Gamma_1}, \qquad (9)$$

$$\equiv \sigma_2'' \,\omega_2 \Gamma_{2,M4} / \Gamma_2 \,. \tag{10}$$

Here

$$\sigma'_{3} = \sigma_{3} + f_{23}\sigma_{2} + (f_{12}f_{23} + f_{13})\sigma_{1}, \qquad (11)$$

$$\sigma_2'' = \sigma_2' + r\sigma_1 = \sigma_2 + (f_{12} + r)\sigma_1, \qquad (12)$$

$$r = \frac{\omega_1(\Gamma_{1,M2} + \Gamma_{1,M3})/\Gamma_1}{\omega_2 \Gamma_{2,M4}/\Gamma_2} . \tag{13}$$

In Eqs. (8)-(13),  $\omega_i$  and  $\Gamma_i$  are the fluorescence yield<sup>25</sup> and total radiative width<sup>26</sup> of the subshell  $L_i$ ,  $\Gamma_{ik}$  is the partial radiative width<sup>26</sup> for the transition from a higher subshell k to the subshell  $L_i$ , and  $f_{ij}$  is the Coster-Kronig transition prob-

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ability<sup>25</sup> from subshell  $L_i$  to subshell  $L_j$ . The  $\beta(1)/\alpha$  x-ray intensity ration, which turns out to be useful for our purposes, is given by

$$\beta(1)/\alpha \equiv \sigma_{\beta(1)}/\sigma_{\alpha} \tag{14}$$

$$=\Omega \frac{\sigma_2 + (f_{12} + r)\sigma_1}{\sigma_3 + f_{23}\sigma_2 + (f_{12}f_{23} + f_{13})\sigma_1}, \qquad (15)$$

where

$$\Omega = \frac{\omega_2 \Gamma_{2,M4} / \Gamma_2}{\omega_3 (\Gamma_{3,M4} + \Gamma_{3,M5}) / \Gamma_3} .$$
 (16)

The consequences of substituting tabulated singlevacancy fluorescence yields,<sup>25</sup> Coster-Kronig transition probabilities<sup>25</sup> and radiative widths<sup>26</sup> in Eqs. (8)-(16) has been discussed extensively in Appendix A of Ref. 16 and in Ref. 17 and comparisons with experiment are presented in Refs. 16 and 24. One may expect up to a "factor of three" systematic errors in computed cross sections, but considerably smaller errors in computed cross ratios, such as Eq. (14). We consider such systematic errors acceptable, since we shall be interested often in trends with atomic number or bombarding energy rather than in absolute values. Hence, in view of the great convenience of using the tabulations,<sup>25,26</sup> singlevacancy values for  $\omega$ , f and  $\Gamma$  are used throughout this paper. With these values one finds that in the Z region of interest here  $(47 \le Z \le 92)$ , r  $\cong 0.45$  [Eq. (13)] and  $\Omega \cong 1.0$  [Eq. (16)].

For comparison with the model calculations, discussed below, we introduce the experimentally determined vacancy fractions

$$v_3 = \sigma'_3 / \sigma_L , \qquad (17)$$

$$v_2 = \sigma_2'' / \sigma_L . \tag{18}$$

Here  $\sigma'_3$  is obtained from  $\sigma_{\alpha}, \sigma''_2$  is obtained from  $\sigma_{\beta(1)}$  and  $\sigma_L$  is the total *L*-vacancy production cross section

$$\sigma_L = \sigma_1 + \sigma_2 + \sigma_3 \tag{19}$$

$$= (\sigma_{I} + \sigma_{\alpha} + \sigma_{\beta(1)} + \sigma_{\beta(2)} + \sigma_{\gamma}) / \tilde{\omega}_{L} .$$
 (20)

One finds<sup>16</sup> that  $\omega_L \cong \omega_3$ .

Using a model similar to that applied in Ref. 16, we now assume that in a symmetric collision, vacancies produced in the  $4f\sigma$  MO at small internuclear distances are shared between the L subshells of the collision partners in ratios predicted by the two-state Demkov vacancy-sharing model of Ref. 12. The application of a two-state model to a many-level situation is justifiable only, if the ignored couplings, e.g., in the Barat-Lichten scheme [Fig. 4(a)] between the MO's correlating to the  $L_1$  and  $L_2$  levels, are indeed small. This is difficult to know *a priori*. It may also be



FIG. 4. Schematic  $4f\sigma$ correlation proposals considered in the model calculations for symmetric collisions. Vertical arrows indicate vacancy-sharing transitions considered in the model. Subsequent Coster-Kronig transitions are not shown, but are taken into account. (a) Proposal of Barat and Lichten (Ref. 9). (b) Proposal of Eichler *et al.* (Ref. 11).

questioned whether the Demkov model is applicable at all to couplings between MO's which lead to subshells of the same collision partner, although a similar model was applied successfully in this manner in Ref. 16. One reason for the success may be that, as Nikitin has shown,<sup>19</sup> many different forms of radial coupling lead to a vacancysharing ratio close in form to that of Demkov's model. In each case a characteristic energy gap between the MO's enters into an exponential factor. As a result, the MO energy separation turns out to be the most critical quantity for the vacancy-sharing ratio, in accord with the findings of Sec. III A.

We distinguish two possible correlations of the  $4f\sigma$  MO to the L subshells, as sketched in Fig. 4: the Barat-Lichten (BL) proposal,<sup>9</sup> that the  $4f\sigma$  MO correlates to the  $L_3$  subshell [Fig. 4(a)], and the Eichler-Wille-Fastrup-Taulbjerg (EWFT) proposal,<sup>11</sup> that the  $4f\sigma$  MO correlates to the  $L_1$  subshell [Fig. 4(b)]. For the BL correlation, the model then gives

$$\sigma_1 / \sigma_L = [\exp(-2x_{31})] / \Sigma_B,$$
 (21)

$$\sigma_2/\sigma_L = [\exp(-2x_{32})]/\Sigma_B, \qquad (22)$$

$$\sigma_3/\sigma_L = 1/\Sigma_B , \qquad (23)$$

where

$$\Sigma_B = 1 + \exp(-2x_{31}) + \exp(-2x_{32}) . \tag{24}$$

Similarly, for the EWFT proposal,

$$\sigma_1 / \sigma_L = 1 / \Sigma_E , \qquad (25)$$

$$\sigma_2/\sigma_L = [\exp(-2x_{21})]/\Sigma_E, \qquad (26)$$

$$\sigma_3 / \sigma_L = \left[ \exp(-2x_{31}) \right] / \Sigma_E , \qquad (27)$$

where

$$\Sigma_E = 1 + \exp(-2x_{21}) + \exp(-2x_{31}) . \tag{28}$$

In these equations,

$$2x_{ij} = \pi / |I_i^{1/2} - I_j^{1/2}| / (\frac{1}{2}mv_p^2)^{1/2}, \qquad (29)$$

(30)

where  $I_i$  and  $I_j$  are the  $L_i$  and  $L_j$  subshell ionization energies, respectively.

To compare the model with experiment, Eqs. (21)-(24) or (25)-(28) must be substituted into Eqs. (15) or (17) and (18). One then finds for the BL proposal

$$\frac{\beta(1)}{\alpha} = \Omega \frac{\exp(-2x_{32}) + (f_{12} + r)\exp(-2x_{31})}{1 + f_{23}\exp(-2x_{32}) + (f_{12}f_{23} + f_{13})\exp(-2x_{31})},$$

and for the EWFT proposal

L ß(1)

Lα

2.0

1.5

1.0

0.5

0

40

50

NTENSITY RATIO

+ EWFT

× BL

$$\frac{\beta(1)}{\alpha} = \Omega \frac{\exp(-2x_{21}) + f_{12} + r}{\exp(-2x_{31}) + f_{23}\exp(-2x_{21}) + f_{12}f_{23} + f_{13}} .$$
(31)

In Fig. 5 expressions (30) and (31) are compared with experimental values of  $\beta(1)/\alpha$  from our<sup>4</sup> and other<sup>2</sup> work, as a function of Z, for a projectile energy of 41 MeV. In Fig. 6 a comparison is made as a function of projectile energy, for Z = 47, 67 and 82 (Refs. 4, 23 and 27). Despite the uncertainties caused by the use of single-vacancy values of  $\omega$ , f and  $\Gamma$  in Eqs. (30)

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FIG. 5.  $\beta(1)/\alpha$  x-ray intensity ratio for symmetric collisions as a function of the atomic number of the collision partners, for 41-MeV projectiles. Experimental points:  $\blacksquare$  interpolated from Ref. 2,  $\odot$  from Ref. 4. The large fluctuations in the EWFT model points are due to the use of single-vacancy Coster-Kronig transition probabilities.

60

ATOMIC NUMBER

70

80

90

Z

and (31), it is clear from Figs. 5 and 6 that our model is consistent only with the BL correlation scheme. To check whether the good agreement between the model calculation for the BL and experiment is fortuitous, we have varied the values of f and  $\omega$  in accordance with the suggestions of Hagmann *et al.*<sup>3</sup> Although the EW-model values are quite sensitive to f and  $\omega$ , the BL model values are very insensitive. This can also be seen in Fig. 5. Hence we can conclude that in symmetric collisions with  $Z \gtrsim 47$  the  $4f\sigma$  MO correlates to the  $L_3$  subshell [Fig. 4(a)].

#### 2. Asymmetric collisions

In asymmetric collisions, one can obtain the cross sections  $\sigma_{\alpha}$  and  $\sigma_{\beta(1)}$  for each collision





FIG. 6.  $\beta(1)/\alpha$  x-ray intensity ratios for symmetric collisions as a function of the projectile energy. Experimental points:  $_{47}$ Ag + Ag from Ref. 23,  $_{67}$ Ho + Ho from Ref. 4,  $_{82}$ Pb + Pb  $\bullet$  from Ref. 4,  $\blacksquare$  from Ref. 27. Curves marked BL and EW are the model results for the  $4f\sigma$ -correlation proposals of Ref. 9 and 11, respectively.

partner, but with considerable uncertainty, if the L spectra of the collision partners overlap. In Fig. 7 we show the target- $Z(Z_t)$  dependence of the  $\beta(1)/\alpha$  ratios for the projectile (p) and the target (t) for four different projectiles, each at a fixed bombarding energy.<sup>2-4,23,27</sup> Only the near-symmetric range of  $Z_t$  is presented. For convenience the symmetric values of  $Z_t$  have been lined up vertically. This makes it easy to recognize the qualitatively common trends in the  $Z_t$ dependence of the projectile and target ratios. We have also obtained experimental vacancy fractions from Eqs. (17) and (18). These are discussed below.

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The model calculations for vacancy sharing in the asymmetric case are considerably more complicated than in the symmetric case. As Fig. 8



FIG. 7.  $\beta(1)/\alpha$  x-ray intensity ratios for projectile (p) and target (t) atoms for various projectiles, as a function of the target atomic number. The abscissa in each case has been shifted so that the symmetric collisions are lined up with the dashed vertical line. Curves have been drawn to guide the eye. (a) 15-MeV <sub>47</sub>Ag (Ref. 23), (b)  $\blacktriangle$  15-MeV <sub>53</sub>I data from Ref. 2,  $\bigtriangleup$  and  $\blacklozenge$  17-MeV I data from Ref. 3, (c) 41-MeV <sub>73</sub>Ta (Ref. 4), (d) 291-MeV <sub>82</sub>Pb (Ref. 27).

shows, one has to consider six subshells and, in our model, five vacancy-sharing ratios analogous to Eq. (6). Also, for sufficiently asymmetric collisions, vacancy feeding into the higher-Z Lsubshells from the  $3d\sigma$  MO has to be taken into account. Eventually, vacancy feeding into the lower-Z L subshells due to L-M level matching would have to be included [see Eqs. (1) and (2)], but in the present work we avoid consideration of collisions which are so asymmetric that L-Mlevel matching effects become appreciable.

Figure 8(a) sketches our model for the correlations and couplings according to the BL scheme,<sup>9</sup> and Fig. 8(b), according to the EWFT scheme.<sup>11</sup> In principle it is also possible for the 4f $\sigma$  MO to correlate according to the BL scheme, and the 3d $\sigma$  MO to correlate according to the EWFT scheme, and vice versa. With the help of Fig. 8, it is not difficult to write down the cross-section ratios for  $Z_1$  and  $Z_h$  analogous to Eqs. (21)–(23) and (25)–(27). As illustration we write down the cross-section ratio,  $\sigma_2(h)/\sigma_L(\text{sum})$  in the BL scheme, where  $\sigma_L(\text{sum})$  is the summed L-vacancy production cross section of both collision partners:

$$\sigma_L(\operatorname{sum}) = \sigma(4f\sigma) + \sigma(3d\sigma) . \tag{32}$$

Let

$$\epsilon \equiv \sigma(3d\sigma)/\sigma(4f\sigma)$$
.

Then

$$\frac{\sigma_2(h)}{\sigma_L(\text{sum})} = \frac{1}{1+\epsilon} \left( \frac{\exp(-2x_{3(l)2(h)})}{\Sigma_B(4f\sigma)} + \epsilon \frac{\exp(-2x_{3(h)2(h)})}{\Sigma_B(3d\sigma)} \right),$$
(34)

(a) BL correlation (b) EWFT correlation



FIG. 8. Schematic correlation proposals used in the model calculations for asymmetric collisions. Vertical arrows indicate vacancy-sharing transitions considered in the model. Coster-Kronig transitions are not shown, but are taken into account. Symbols l and h refer to the lower-and higher-Z partners, respectively. (a) Proposal of Barat and Lichten (Ref. 9). (b) Proposal of Eichler *et al.* (Ref. 11).

(33)



where  $\Sigma_{B}(3d\sigma) = 1 + \exp(-2x_{3(h)2(h)}) + \exp(-2x_{3(h)1(h)}), \quad (35)$   $\Sigma_{B}(4f\sigma) = 1 + \exp(-2x_{3(l)2(l)}) + \cdots + \exp(-2x_{3(l)1(h)}).$ (36)

Each quantity  $2x_{ij}$  is of the form of Eq. (29). Substitution of the ratios similar to Eq. (34) into equations analogous to Eqs. (15), (17) and (18) allows model estimates of  $\beta(1)/\alpha$  ratios and of the vacancy fractions for each collision partner. From Fig. 2 one can estimate, by comparison with Fig. 10 of Ref. 16, that  $\epsilon \cong 0.03$ , 0.01 and 0.001 for 43-MeV Br, 47-MeV I, and 41-MeV

FIG. 9. Projectile Lshell vacancy fractions, defined by Eqs. (17) and (18), for 41-MeV  $_{73}$ Ta projectiles, plotted as a function of target atomic number. Vertical dashed lines indicate symmetric collisions. The symbols h and *l* denote the regions where the projectile is the higherand lower-Z partner, respectively. (a) Model calculation using the proposal of Barat and Lichten [Fig. 8(a)], (b) experimental points (Ref. 4; typical errors  $\pm 30\%$ ), (c) model calculation using proposal of Eichler et al. [Fig. 8 (b)].

Ta projectile-induced collisions, respectively. In Fig. 9(b) we present the experimentally extracted projectile-vacancy fractions  $v_2$  and  $v_3$ , Eqs. (17) and (18), with  $\sigma_L$  replaced by  $\sigma_L(\text{sum})$ , for 41-MeV Ta projectiles bombarding various targets.<sup>4</sup> In Figs. 9(a) and 9(c) we give the BLand EWFT-model results, assuming  $\epsilon = 0$ . Figure 10 gives the experimental and model results for the target-vacancy fractions. In Figs. 9 and 10, triangles represent  $v_2$  and circles  $v_3$ . The symbols h and l indicate the  $Z_l$  regions, separated by the vertical dashed symmetry line, where the particular atom, projectile or target, is the higheror lower-Z partner. We have not applied the



FIG. 10. Target *L*-shell vacancy fractions, defined by Eqs. (17) and (18) for 41-MeV <sub>73</sub>Ta projectiles. The symbols *h* and *l* denote the region where the target is the higher-lower-*Z* partner respectively. Otherwise, caption is identical to that of Fig. 9. model in the region where the L levels of the two partners overlap. The symmetric points for  $v_2$ and  $v_3$  are simply connected by dashed lines with the sufficiently asymmetric points.

Before discussing Figs. 9 and 10, we note from Eqs. (8)-(12) and (15)-(18) that, for each partner,

$$\beta(1)/\alpha = \Omega v_2/v_3 \,. \tag{37}$$

Hence, the experimental points in Figs. 9(b) and 10(b) are directly related to the data shown in Fig. 7(c).

From Figs. 9 and 10 one can see that the model predictions are qualitatively different for the BL and the EWFT proposals. In the BL scheme,  $v_2/v_3$  is always less than unity, or  $\beta(1)/\alpha < 1$  (since  $\Omega \cong 1.0$ ), both for  $Z_h$  and  $Z_1$ . In the EWFT scheme,  $v_2/v_3$  is less than unity for  $Z_h$ , but greater than unity for  $Z_1$ . The experimental fractions cannot distinguish between two schemes on the  $Z_h$  side, but on the  $Z_1$  side there is a clear trend from  $v_2/v_3 < 1$  to  $v_2/v_3 \ge 1$ , as the asymmetry of the collision increases. Figure 7 shows that this trend occurs not only for 41-MeV Ta, but is quite general (in this figure the projectile is the lower-Z partner for  $Z_t > Z_p$  and the target for  $Z_t < Z_p$ ).

Keeping in mind the limitations of our model, it appears then that with increasing asymmetry of the collision, the diabatic correlation of the  $4/\sigma$ MO moves from the  $L_3$  level in the symmetric situation (Sec. IIIA) toward the lower- $Z L_1$  level, i.e., toward the EWFT proposal (Fig. 1). In Sec. V we attempt to explain this shift in the correlation in terms of physical features of avoided crossings of the adiabatic MO's correlating to the lower- $Z L_3$  and  $L_1$  levels. This is similar to the treatment of Hagmann *et al.*,<sup>3</sup> but they did not take into account any long-range radial coupling between the MO's represented here by "vacancy sharing."

If avoided crossings enter the picture, one would expect the crossing probability to be velocity dependent and to increase with increasing projectile velocity. Figure 11 shows the projectile energy dependence of the lower- $Z \beta(1)/\alpha$  ratio for  ${}_{47}Ag + {}_{57}La$  (Ref. 23) and for  ${}_{53}I + {}_{64}Gd$ ,  ${}_{70}Y$  (Refs. 2 and 3). It appears that at least at higher projectile velocities, the correlation approaches the EWFT scheme.

We return to Figs. 9 and 10 and consider the higher-Z partner. The model calculations with  $\epsilon = 0$  [Eq. (33)] predict that  $v_2$  and  $v_3$  should decrease rapidly with increasing asymmetry of the collision. Experimentally one finds that for 41-MeV Ta,  $v_2$  and  $v_3$  do not decrease below ~10<sup>-3</sup>



FIG. 11.  $\beta(1)/\alpha$  x-ray intensity ratio for the lower-Z partner as a function of the atomic number. (a)  $_{47}$ Ag  $+_{57}$ La (Ref. 23), (b)  $_{53}$ I  $+_{64}$ Gd,  $_{70}$ Y ( $\bullet$  from Ref. 2,  $\blacksquare$  from Ref. 3). The curves marked BL and EW are the model results for the correlation proposals of Refs. 9 and 11, respectively.

[Fig. 9(b)]. Furthermore, the model predicts that  $(v_2/v_3)_b \cong [\beta(1)/\alpha]_b \le 0.3$ , whereas experimentally  $[\beta(1)/\alpha]$ , reaches values close to unity, as the asymmetry increases (Fig. 7). These facts can be explained only, if one assumes  $\epsilon$  $\neq 0$ , i.e., vacancy feeding from the 3do MO into the higher-Z L levels<sup>10</sup> (Figs. 1 and 8). One can then apply the model calculations in order to check whether the 3do MO correlates according to the BL proposal<sup>9</sup> [Fig. 8(a)] or according to the EWFT proposal<sup>11</sup> [Fig. 8(b)]. The available data<sup>2-4,27</sup> are shown in Fig. 12. There is no consistent trend in the data, but one notes that the energy dependence of the  $\beta(1)/\alpha$  ratio appears to follow that of the computed EW curves [Figs. 12(b) and 12(d)]. Contrary to the BL curves, the absolute magnitudes of the EW curves are quite sensitive to the f and  $\omega$  values used in Eq. (15). As shown by Hagmann et al.<sup>3</sup> there can be major deviations of these values from the tabulated ones,<sup>25</sup> because of excitation or stripping in the L and M shells of the projectile and target atoms. Hence we can only tentatively conclude from Fig. 12 that the  $3d\sigma$  MO may correlate according to

the EWFT scheme.<sup>11</sup> More experimental evidence is needed to establish the correlation.

#### IV. 4fo-VACANCY-PRODUCTION CROSS SECTION

According to our model, the 4fo-vacancy-production cross section near symmetry is given by the summed L-vacancy-production cross section of both collision partners [Eq. (4)]. We show in Fig. 13 that the experimental cross sections<sup>4, 16, 28, 29</sup> appear to obey the same kind of united-atom (UA) scaling law which was found by Behnke et al.<sup>21</sup> for the  $2p\sigma$ -vacancy cross section and subsequently by Meyerhof<sup>17</sup> for the  $3d\sigma$ -vacancy cross section: at a given projectile velocity the cross section is a nearly unique function of the UA  $Z(=Z_{p}+Z_{t})$ , independent of  $Z_p$ . (Each different symbol in Fig. 13 represents a different value of  $Z_{b}$ .) In Ref. 17 it was shown that a UA ionization model proposed by Briggs<sup>30</sup> can produce such a scaling law, but it could not be demonstrated that ionization alone is responsible for  $3d\sigma$ -vacancy production. The semiclassical approximation ionization amplitudes needed to apply the Briggs model to the 4fo case are presently not available, but are being computed.<sup>31</sup> In systems considerably lighter than those considered here, i.e.,  $Z \lesssim 20$ , the 4*fo*-vacancy production cross section has been successfully explained solely on the basis of electron promotion.<sup>32</sup> Electron promotion is also invoked by Lutz et al.,<sup>33</sup> who examine the threshold behavior of  $\sigma_L(l)$  in Xe+Ag collisions, but Fortner *et al.*<sup>34</sup> suggest that 4*f* o ionization is needed to explain the threshold behavior in Kr + Kr and Kr + Xecollisions.

## V. DISCUSSION

We have shown that a simple molecular model can explain the basic trends of L x-ray cross sections produced in near-symmetric heavy-ion collision with  $Z \ge 35$ . The model is based on the proposal<sup>16</sup> that inner-shell vacancies are formed predominantly in highly promoted MO's ( $2p\sigma$ ,  $3d\sigma$ ,  $4f\sigma$ ,  $5g\sigma \cdot \cdot \cdot$ ) at small internuclear distances and that, on the outgoing part of the collision, the vacancies are shared between the various SA subshells. For L x-ray production near symmetry the most relevant MO is the  $4f\sigma$ MO.<sup>9,10</sup>

The projectile velocity region examined by us, corresponds, for 41-MeV Ta, to  $v_p/v_L \cong 0.1$ , where  $v_L$  is the Bohr *L*-electron velocity. Therefore, the use of a quasimolecular model of the collision process appears to be appropriate. One then expects that the long-range coupling between the 4for MO and the other MO's on the outgoing



FIG. 12.  $\beta(1)/\alpha$  x-ray intensity ratio for the higher-Z partner as a function of projectile energy. (a)  $_{47}Ag + _{32}Ge$  (Ref. 23), (b)  $_{53}I + _{40}Zr$  (Ref. 2), (c)  $_{73}Ta + _{47}Ag$ (Ref. 4), (d)  $_{82}Pb + _{52}Te$ ,  $_{53}I$  ( $\blacksquare$  from Ref. 27,  $\bullet$  from inverse collision, Ref. 3; equivalent Pb projectile energies are shown). The curves marked BL and EW are the model results for the correlation proposals of Refs. 9 and 11, respectively.

part of the collision should be influenced strongly by the level separation and, to a lesser degree, by the detailed structure of the MO's. This may justify use of a vacancy-sharing model such as that of Refs. 12 and 16.



FIG. 13. Cross sections for  $4f\sigma$ -vacancy production at 0.49-MeV/a.m.u. projectile energy, plotted as a function of the united-atom atomic number. Experimental points:  $\bullet_{35}$ Br projectiles on various targets (Ref. 16),  $\bigvee_{47}$ Ag + Ag (Ref. 28),  $\blacksquare_{53}$ I projectiles on various targets (Ref. 16),  $\wedge_{53}$ I+ $_{52}$ Te (Ref. 29),  $\bullet_{67}$ Ho+Ho,  $\bullet_{79}$ Au+Au,  $\bullet_{82}$ Pb + Pb (extrapolated from Ref. 4).

Perhaps the most interesting result of the present work is the possibility of distinguishing experimentally between two correlation schemes proposed, respectively by Barat and Lichten<sup>9</sup> and by Eichler *et al.*<sup>11</sup> In terms of adiabatic level schemes, the correlations of interest in L x-ray production are determined by the nature of the avoided crossings marked 1 and 2 on Figs. 14(a) and 14(b). These figures, taken from Ref. 11, can serve as prototypes of a symmetric and an asymmetric collision system. Appropriate relativistic diagrams are presented in Refs. 35 and 36.

Our finding that at symmetry the 4fo MO correlates to the  $2p_{3/2}$  level, but that with increasing asymmetry the correlation moves to the lower-Z 2s level, will now be discussed from two points of view. First, we show that in region 1 in the symmetric case the crossing probability from the  $3\sigma_u(4f\sigma)$  MO [in the relativistic case<sup>35,36</sup> called  $4(\frac{1}{2})_u$ ] to the  $2\sigma_u(3p\sigma)[3(\frac{1}{2})_u]$  MO is small, so that



FIG. 14. Adiabatic correlation diagrams according to the nonrelativistic calculations of Eichler et al. (Ref. 11). (a) 54Xe +Xe. The boxed region 1contains the  $4f\sigma - 3p\sigma$ avoided crossing  $(3\sigma_u - 2\sigma_u)$ , shown by dashed lines). The boxed region 2 contains the  $3d\sigma$ -2s $\sigma$  avoided crossing  $(3\sigma_g - 2\sigma_g, \text{ shown})$ by solid lines). (b) (on next page)  $_{36}$ Kr +  $_{54}$ Xe. The boxed region 1 contains the  $4f\sigma$ - $3p\sigma$ avoided crossing  $(6\sigma - 5\sigma)$ and 2 the  $3d\sigma$ -2s $\sigma$  avoided crossing  $(4\sigma - 3\sigma)$ .



Fig. 14. (Continued)

the 4fo MO is expected to follow the adabatic correlation to the SA  $2p_{3/2}$  level.<sup>9</sup> But for a sufficiently asymmetric system the crossing probability from the  $6\sigma(4f\sigma)$  to the  $5\sigma(3p\sigma)$  MO increases so that the 4fo MO tends to correlate to the lower-Z 2s level. [In the relativistic case,<sup>35,36</sup> two crossings are involved here:  $8(\frac{1}{2})$  $+7(\frac{1}{2})$  and  $7(\frac{1}{2}) + 6(\frac{1}{2})$ , but the latter energy gap is so narrow that only the former needs to be considered. Hagmann  $et \ al.^3$  have considered the crossings in the relativistic case in greater detail.] Second, we show that the nature of the avoided  $4f\sigma$ - $3p\sigma$  crossing 1 changes drastically with symmetry as the result of a rapidly changing Stark effect.<sup>9,11</sup> The situation for the avoided  $3d\sigma - 2s\sigma$  crossing 2, which determines the  $3d\sigma$ correlation, seems to be quite different.

A quantitative estimate of the crossing probability between two adiabatic MO's can be obtained from the Landau-Zener formula.<sup>37</sup> Following Eichler *et al.*,<sup>11</sup> we write the Landau-Zener crossing probability at a projectle velocity  $v_p$  as

$$P = (\frac{1}{2})^{v_{c}/v_{p}}, \tag{38}$$

where

$$\nu_{c} = \frac{2\pi}{\ln 2} \frac{|H_{12}|^2}{\Delta(\partial \epsilon/\partial R)} . \tag{39}$$

Here  $H_{12}$  is equal to one-half of the minimumenergy splitting between the adiabatic energy curves  $E_1(R)$  and  $E_2(R)$  and  $\Delta(\partial \epsilon / \partial R)$  is the difference in slopes between the diabatic curves  $\epsilon_1(R)$  and  $\epsilon_2(R)$  at the crossing point. If  $v_c$  is larger than  $v_p$  one expects a small transition probability, i.e., a correlation according to the BL proposal<sup>9</sup> in the case considered here. If  $v_c$ is considerably smaller than  $v_p$ , one expects a large transition probability, i.e., a correlation according to the EWFT proposal.

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Avoided crossing <sup>a</sup>	System	$\frac{Z_1}{Z_h}$	<i>v<sub>c</sub></i> (VSM) (a.u.)	Reference <sup>b</sup>	v <sub>c</sub> (HFD) <sup>c</sup> (a.u.)	$\frac{\Delta W}{\Delta E}$	
4fσ <b>-</b> 3pσ	Xe-Xe	1	0.15, 1.3	11, 35	•••	0.50	
(region 1)	Kr-Kr	1	0.8	11	•••	0.45	
	Ag-Xe	0.87	• • •	• • •	0.9	0.29	
	I–Au	0.67	0.2	35	4.1	0.14	
	Kr-Xe	0.67	0.1	11	•••	0.13	
$3d\sigma$ - $2s\sigma$	Xe-Xe	1	0.01, 0.06	11, 35	•••	0.09	
(region 2)	Kr-Kr	1	0.02	11	•••	0.08	
	Ag-Xe	0.87	•••	• • •	1.1	0.12	
	I–Au	0.67	1.5	35	2.0	0.31	÷.,
	Kr-Xe	0.67	0.04	11	• • •	0.20	

TABLE I. Landau-Zener critical velocity and subshell to Stark splitting ratio.

<sup>a</sup> See Figs. 14 and 15.

<sup>b</sup> Energy curves of Ref. 11 have been computed nonrelativistically; others, relativistically. <sup>c</sup> Reference 36.

authors of Refs. 11, 35, and 36, we have obtained  $v_c$  for the crossing region 1 in Fig. 14. Table I gives the results. Unfortunately, the variable screening model (VSM) used in Refs. 11 and 35 are the Hartree-Fock-Dirac model (HFD) used in Ref. 36 give widely divergent results, so that a quantitative application of Eq. (38) is not meaningful. Nevertheless, one sees that the VSM is in qualitative accord with our findings, in that  $v_{a}$ tends to decrease with increasing asymmetry: this signals a shift toward the EWFT correlation scheme. Our projectile velocities correspond to  $v_{b} \cong 2-3$  a.u. Hence our findings for the shift in the  $4f\sigma$  correlation (Sec. III) would require  $v_c$  $\gtrsim$  3 a.u. for symmetric collisions and  $v_c \lesssim$  2 a.u. for sufficiently asymmetric collisions. We note that Nikulin and Guschina<sup>38</sup> find no evidence for any  $4f\sigma$ - $3p\sigma$  avoided crossing in the Kr + Kr system. In the language of Eq. (38) this would correspond to a very large value for  $v_c$ .

According to the VSM,<sup>11</sup> the  $3d\sigma$ -2s $\sigma$  crossings in region 2 are all characterized by very small values of  $v_c$ , listed in Table I. The HFD model<sup>36</sup> gives much larger values. A similar effect was found in a comparison of the VSM and HF results for the same crossing in Ne+Ne.<sup>39</sup> Nevertheless the generally smaller values of  $v_c$  in region 2 as compared to region 1, suggest a tendency toward the EWFT scheme. Unfortunately the experimental evidence (Fig. 12) is not conclusive.

Returning to  $4f\sigma$ - $3p\sigma$  avoided crossing regions 1 in Figs. 14(a) and 14(b) one may now inquire which physical features of the collision system determine the trend of the  $4f\sigma$  correlation, as the asymmetry of the system changes. Following suggestions of Barat and Lichten,<sup>9</sup> Eichler *et al.*<sup>11</sup> have explored the competing roles of the Coulombic one-electron Stark splitting  $\Delta E$  and of the 2p-2ssubshell splitting  $\Delta W$ , in determining whether a given correlation follows the BL or EWFT schemes. Figure 15, adapted from Ref. 11, illustrates the argument: as  $\Delta E$  increases from small values (with respect to  $\Delta W$ ) to large values, the avoided crossing should become increasingly dia-



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FIG. 15. Schematic diagram for the adiabatic correlations to the L levels of the lower-Z (l) and higher-Z (h) collision partners in a slightly asymmetric system (adapted from Ref. 11). The Coulombic Stark splitting is denoted by  $\Delta E$  and the 2p-2s subshell splitting by  $\Delta W$ . Dashed curves show the energy levels for a one-electron system. Solid curves illustrate the situation for a screened system.



FIG. 16. Coulombic Stark splitting  $\Delta E$  for a one-electron, two-center system as a function of the asymmetry ratio  $Z_l/Z_h$ . Points are computed from Ref. 40. Curve 1 applies to the  $4f\sigma$ - $3p\sigma$  splitting, curve 2 to the  $3d\sigma$ - $2s\sigma$  splitting (see Fig. 15).

batic, i.e., the correlation should shift increasingly from the BL to the EWFT scheme.

To put this criterion on a quantitative basis we have calculated the ratio  $\Delta W / \Delta E$  as a function of the asymmetry of the system, for the MO's correlating to the lower-Z and higher-Z L levels. To obtain the Coulombic one-electron  $4f\sigma$ - $3p\sigma$ and  $3d\sigma - 2s\sigma$  Stark splittings  $\Delta E$ , we have used the calculations of Hartmann and Helfrich.<sup>40</sup> Figure 16 gives their values of  $\Delta E/Z_1^2$  as a function of  $Z_l/Z_h$ , which allow approximate interpolation for any collision pair  $Z_1, Z_h$ . The 2p-2ssubshell splittings  $\Delta W$  were computed from tabulations.<sup>41</sup> Figure 17 shows the resultant values of  $\Delta W / \Delta E$  for Ta projectiles. For other projectiles similar results are obtained. One sees that for the  $4f\sigma$ - $3p\sigma$  case (curve 1), the value of  $\Delta W/$  $\Delta E$  peaks at symmetry and drops rapidly with increasing asymmetry. This is in qualitative accord with our findings: at symmetry, the large value of  $\Delta W / \Delta E$  leads to the expectation of BL correlation  $(4f\sigma - L_3)$ ; the decreasing values of  $\Delta W/\Delta E$  with increasing asymmetry lead to the expectation of increasing EWFT correlation  $[4f\sigma - L_1(l)]$ . The trend appears to be in accord with the overall trend of  $v_c$  for region 1 given in Table I, where we list also the values of  $\Delta W / \Delta E$ for each collision pair.

For the  $3d\sigma$ -2s $\sigma$  case, curve 2 in Fig. 17, the ratio  $\Delta W / \Delta E$  is small throughout the region near symmetry. This leads to the expectation of



FIG. 17. Subshell to Stark splitting ratio for  $_{73}$ Ta projectiles bombarding various targets, plotted as a function of the target atomic number. Vertical dashed line indicates symmetry. Curve 1 applies to the  $4f\sigma$ - $3p\sigma$  MO's, curve 2 to the  $3d\sigma$ - $2p\sigma$  MO's (see Fig. 15). According to Ref. 11, as  $\Delta W/\Delta E$  decreases, the MO correlations are expected to change from adiabatic to diabatic.

EWFT correlation  $[3d\sigma - L_1(h)]$  in the entire region. As discussed above, experimentally this is not definitely ascertained (Fig. 12).

By comparing the numerical values of  $\Delta W / \Delta E$ and  $v_c$  one can, for a given model, establish an approximate one-to-one relationship (Table I). This simply indicates quantitatively that a weak Stark splitting leads to a broad avoided crossing with a large gap (BL correlation), whereas a strong Stark splitting leads to an avoided crossing with a small gap (EWFT correlation). From Fig. 16 one can see that our findings for the  $4f\sigma$ correlation find a natural explanation in terms of the rapid increase of the Stark splitting as the asymmetry of the system increases. The experimental features of the  $3d\sigma$  correlation must be investigated further. From a theoretical point of view there is a need to establish the validity of various MO calculations and then to compute the actual couplings between the 4fo MO and the MO's leading to the lower-Z subshells. Similarly the couplings between the 3do MO and the higher-Z subshells must be calculated, as has been done in Refs. 42 and 43 for the Ne-Ne system.

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