## **Finite-range effects in the two-dimensional repulsive Fermi polaron**

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We study the repulsive Fermi polaron in a two-component, two-dimensional system of fermionic atoms inspired by the results of a recent experiment with 173Yb atoms [N. Darkwah Oppong *et al.*, Phys. Rev. Lett. **122**[, 193604 \(2019\)\]. We use the diffusion Monte Carlo method to report properties such as the polaron energy](https://doi.org/10.1103/PhysRevLett.122.193604) and the quasiparticle residue that have been measured in that experiment. To provide insight into the quasiparticle character of the problem, we also report results for the effective mass. We show that the effective range, together with the scattering length, is needed in order to reproduce the experimental results. Using different model potentials for the interaction between the Fermi sea and the impurity, we show that it is possible to establish a regime of universality, in terms of these two parameters, that includes the whole experimental regime. This illustrates the relevance of quantum fluctuations and beyond mean-field effects to correctly describe the Fermi polaron problem.

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The problem of a single impurity surrounded by a medium has been studied in several quantum many-body systems since its initial formulation [\[1,2\]](#page-4-0). For decades the impurity problem has been studied in many fields: from condensed matter (cf. [\[3–5\]](#page-4-0), for example, for studies in helium), to neutron matter [\[6\]](#page-4-0), and, more recently, in atomically thin semiconductors [\[7\]](#page-4-0). In some particular systems, the presence of impurities is crucial to explain some of its physical properties, e.g., the Kondo effect, originated by the presence of magnetic impurities [\[8\]](#page-4-0), and of Anderson's orthogonality catastrophe [\[9\]](#page-4-0), in fermionic systems. Under some physical conditions, the impurity coupled to the medium behaves as a quasiparticle (polaron), whose properties differ drastically from those of the impurity. For example, in the case in which the medium is fermionic, it is called a Fermi polaron [\[10,11\]](#page-4-0)

Ultracold atoms, due to their high tunability, constitute an excellent platform for the investigation of the Fermi polaron. Precisely for this reason, they have led to intense experimental and theoretical work in different geometries that include one-dimensional (1D) [\[12–15\]](#page-4-0), 2D [\[16–18\]](#page-4-0), and 3D [\[18,19\]](#page-4-0) configurations. Incidentally, efforts have not been restricted to studying the ground state, and recently studies have been extended to finite temperature. In particular, a crossover from the quantum Fermi polaron regime at low temperature to the classical Boltzmann regime as temperature increases has been

reported by means of radiofrequency spectroscopy [\[20\]](#page-4-0) (cf. [\[21,22\]](#page-4-0) for theoretical works).

Interestingly, the interaction between the impurity and the bath can be controlled by means of a Feshbach resonance. This has allowed us to experimentally access the polaron physics in different regimes employing two-component mixtures of ultracold gases with a very small concentration of one of the components. This includes mixtures of two different hyper-fine levels of the same atomic specie [\[23\]](#page-4-0) and of different atoms [\[24–28\]](#page-4-0). While initially only alkali-metal atoms were employed [\[19,29–33\]](#page-4-0), the recent discovery of orbital Feshbach resonance (OFR) in 173Yb [\[34–36\]](#page-4-0) has made it possible to study new physical phenomena in the quantum degenerate regime, for example as spin exchange and SU(N)-symmetric collisions [\[37–39\]](#page-4-0). This has motivated a spectroscopic probe of the energies of the repulsive and attractive branches of the polaron, and measurement of the quasiparticle residue by driving Rabi oscillations (both in 2D [\[17\]](#page-4-0) and 3D systems [\[19,40\]](#page-4-0)).

Previous diffusion Monte Carlo (DMC) calculations reveal the existence of a universal regime in terms of the gas parameter  $na_s^2$  for the 2D repulsive Fermi polaron, which stands for values  $na_s^2 \leq 10^{-3}$  [\[16\]](#page-4-0), with *n* the particle density and  $a_s$  the 2D *s*-wave scattering length. These results contrast with those reported for an unpolarized 2D, two-component Fermi system in which the universal regime stands for  $na_s^2 \lesssim 10^{-2}$  [\[41\]](#page-4-0). This reflects the enhanced relevance of quantum fluctuations in a 2D Fermi polaron problem [\[42\]](#page-4-0), which is a good testbed to study the effect of impurity-bath correlations [\[43\]](#page-4-0).

Remarkably, the energy of the 2D polaron and the quasiparticle residue have been measured recently outside of the universal regime by exploiting the OFR in  $173\text{Yb}$  [\[17\]](#page-4-0). As

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a consequence, mean-field theory and its first perturbative correction [the Lee-Huang-Yang (LHY) term], which are functions of only the scattering length, are not sufficient to accurately describe this problem. Thus, to provide a quantitative description of the experimental results of Ref. [\[17\]](#page-4-0), effective range effects, which go beyond the LHY correction, must be taken into account. Here we study the repulsive 2D Fermi polaron in terms of the Fermi momentum times the scattering length  $k_{\mathrm{F}}a_s$ , which has a direct relationship with the gas parameter  $k_{\text{F}}a_s = \sqrt{4\pi n a_s^2}$ , well outside the unitary limit. (For a DMC study of the 2D Bose polaron, cf. Ref. [\[44\]](#page-4-0).) We restrict ourselves to a two-dimensional system to mimic the conditions of the experiment in Ref. [\[17\]](#page-4-0).

With the aim of extending the regime of universality, in this Letter we study the 2D Fermi polaron problem with a model in which the two-body potential is constructed taking into account both the *s*-wave scattering length and the effective range. We fix both quantities to values compatible with the experiment of Ref. [\[17\]](#page-4-0). We perform our calculations with two different model potentials, detailed below, in order to check if the scattering length and the effective range are sufficient to quantitatively describe the system in the regime of *k*F*as* considered. A similar approach has been carried out in other systems, where good agreement with experimental results has been found; see, for example, Refs. [\[45–47\]](#page-4-0) for results regarding quantum droplets in Bose-Bose mixtures. Our results show that the explicit consideration of the finite range of the interaction allows for an excellent agreement with experimental data. Interestingly, we observe a regime of universality in terms of the two scattering parameters that covers the experimental regime of Ref. [\[17\]](#page-4-0) for the 2D Fermi polaron.

Our microscopic approach is based on the DMC method. DMC allows us to accurately describe the ground state of quantum systems both in the dilute and in the strongly correlated regimes. Starting from a variational ansatz, the initial wave function  $\Psi_T(\mathbf{R})$  is propagated in imaginary time keeping its nodal surface constant. In this way, one keeps the Fermi sign problem under control, leading to a statistical representation of the best possible wave function within a nodal surface constraint [the fixed-node approximation (FN) [\[48\]](#page-4-0)]. As a consequence, FN-DMC produces variational results whose quality is related to the accuracy of the model nodal surface. The trial wave function is taken as the usual Jastrow-Slater ansatz, consisting of a product of a Jastrow factor  $\Psi_J(\mathbf{R})$ , which is symmetric to the exchange of particles, times an antisymmetric part  $\Psi_A(\mathbf{R})$ , which is taken to be a Slater determinant of plane waves, which is accurate enough for the low densities considered in this work [\[41\]](#page-4-0). Here,  $\mathbf{R} = {\mathbf{r}_1, \dots, \mathbf{r}_{N_t}, \mathbf{r}_{\downarrow}}$  is the set of all  $N_{\uparrow} + 1$  particle coordinates, and  $\mathbf{R}_{\uparrow}$  accounts only for the coordinates of the *N*<sup>↑</sup> particles of the bath. The Jastrow term is chosen as a product of two-body correlation functions, which are taken as the ground-state wave function of the two-body problem at short distances matched with a phononlike long-range term [\[16\]](#page-4-0). The propagator that we employ is accurate up to second order in the imaginary time step. Off-diagonal estimators have an additional bias related to the choice of  $\Psi_T(\mathbf{R})$ . To correct this, up to first order in the trial wave function, we use the extrapolated estimator technique [\[16\]](#page-4-0). The error bars of our

TABLE I. Parameters of the interaction potentials (SWSC, SC) that reproduce the experimental values of  $a_{3D}$  and  $r_{3D}^{\text{eff}}$ .

	$R_0(a_{3D})$	$R_1(a_{3D})$	$U_0[\hbar^2/(ma_{3D}^2)]$	$U_1[\hbar^2/(ma_{3D}^2)]$
SC.	$\mathbf{\Omega}$	2.40593	$^{(1)}$	0.425291
<b>SWSC</b>	0.91627	2.29069	0.62099	0.576351

results account for this source of error, statistical Monte Carlo uncertainty, the bias originated from the finite imaginary time step, and finite-system size effects. A more detailed description of the method and the trial wave function can be found in the Supplemental Material [\[49\]](#page-4-0).

It is worthwhile to remark that a similar attempt has been made recently with the aim of extending the current stateof-the-art theory. In Ref. [\[18\]](#page-4-0), the authors present a model that, by effectively including finite-range effects, is able to reproduce the Rabi oscillations both from the 3D [\[19\]](#page-4-0) and 2D [\[17\]](#page-4-0) Fermi polaron experiments. On the other hand, although the quasiparticle residue that they report improves previous theoretical results, it is not able to match the experimental ones. In addition, some controlled numerical results (without considering effective range effects) have been presented in the literature for the Fermi polaron (cf., for example, Ref. [\[50\]](#page-4-0) for the resonant Fermi polaron and Refs. [\[51–54\]](#page-4-0) for diagrammatic Monte Carlo studies of the Fermi polaron).

To describe the 2D Fermi polaron, we study a system of  $N = N_{\uparrow} + 1$  particles composed by a Fermi sea of  $N_{\uparrow}$  noninteracting fermions and a spin  $\downarrow$  impurity, all with the same mass *m*. The Hamiltonian of the *N*-particle system reads

$$
\hat{H} = -\frac{\hbar^2}{2m}\nabla_{\downarrow}^2 - \frac{\hbar^2}{2m}\sum_{i=1}^{N_{\uparrow}}\nabla_i^2 + \sum_{j=1}^{N_{\uparrow}}V^{\text{int}}(r_{\downarrow j}),\tag{1}
$$

where  $r_{\downarrow j} \equiv |\mathbf{r}_{\downarrow} - \mathbf{r}_{j}|$  is the distance between a bath particle at  $\mathbf{r}_i$  and the impurity position  $\mathbf{r}_\downarrow$ . The two-body potential  $V<sup>int</sup>(r)$  models the interaction of the polaron with the bath. We use two different models: The first one is a square-wellsoft-core (SWSC) potential, which reads

$$
V^{\text{int}}(r) = \begin{cases} -U_0, & 0 < r < R_0, \\ U_1, & R_0 < r < R_1, \\ 0, & R_1 < r < \infty, \end{cases}
$$
 (2)

with all the parameters  $(R_0, R_1, U_0, \text{ and } U_1)$  being positive. The second model is a soft-core (SC) potential, which can be considered a limiting case of the previous one by setting  $R_0$  and  $U_0$  to zero, and thus it is uniquely described by  $U_1$ and  $R_1$ . The values of the parameters of Eq.  $(2)$  are reported in Table I. These values are chosen so that the potential reproduces the experimental results from Ref. [\[35\]](#page-4-0), which corresponds to setting  $a_{3D} = 1878a_0$  and  $r_{3D}^{\text{eff}} = 216a_0$ , with  $a_0$  the Bohr radius [\[35,55\]](#page-4-0). In Ref. [\[35\]](#page-4-0), a second value is reported for the effective range, which is smaller ( $r_{3D}^{\text{eff}} = 126a_0$ ), but we checked with DMC that experimental data are only reproduced by choosing the larger value,  $r_{3D}^{\text{eff}} = 216a_0$ . See the Supplemental Material [\[49\]](#page-4-0) for further details concerning the interaction models employed.

One of the most relevant quantities in the study of the polaron is the polaron energy, which is in fact the chemical

<span id="page-2-0"></span>

FIG. 1. Polaron energy in units of the bath Fermi energy  $E_F =$  $2\hbar^2 \pi n/m$ . The red dashed line corresponds to the mean-field prediction of Eq. (4), and the orange solid line corresponds to the experimental results reported in Ref. [\[17\]](#page-4-0). Symbols are DMC results: circles correspond to the HD model reported in Ref. [\[16\]](#page-4-0), and squares and triangles correspond to results obtained using the SWSC and SC potentials, respectively. Dashed lines joining the symbols are guides to the eye.

potential of the impurity. Within the DMC framework, it can be evaluated by means of the energy difference,

$$
\varepsilon_p = [E(N_\uparrow, 1) - E(N_\uparrow, 0)]_V,\tag{3}
$$

where  $E(N_1, 0)$  is the energy of the *N*-particle pure system, and  $E(N_1, 1)$  is the energy obtained when the impurity is added, keeping the volume constant. Within the mean-field approximation, the polaron energy is given by

$$
\varepsilon_{\rm MF} = \frac{4\pi\,\hbar^2 n}{m\ln\left(c_0 n a_s^2\right)},\tag{4}
$$

with  $c_0$  a free parameter  $[56]$  that is related to the energy scale of the system. Following previous works [\[16,41,57\]](#page-4-0), we fix it so that the choice for the energy scale corresponds to that of the free Fermi system  $(E_F = \frac{\hbar^2 k_F^2}{2m} = 2\hbar^2 \pi n/m)$ , which results in  $c_0 = e^{2\gamma} \pi/2 \simeq 4.98$ , where  $\gamma \simeq 0.577$  is Euler's gamma constant.

To benchmark the present results, we compare our DMC energies for the SWSC and SC models to those obtained with a hard-disk (HD) potential (from Ref.  $[16]$ ) and to the mean-field prediction (4). While the hard-disk potential shares the same scattering length with the SWSC and SC potentials, its effective range is different and cannot be imposed in the construction of the model, as the HD potential has only one free parameter: the diameter of the disk.

We report in Fig. 1 our DMC results for the polaron energy corresponding to the SWSC and SC potentials. In the same figure, we include the mean-field prediction, the HD model results [\[16\]](#page-4-0), and the experimental results of Ref. [\[17\]](#page-4-0). As can be seen in the plot, both mean-field theory and the HD model fail to reproduce the experimental data. As mentioned previously, mean-field theory cannot accurately reproduce the experimental results because the system resides at gas parameters outside the universal regime. The HD model is also



FIG. 2. Quasiparticle residue *Z* as  $k_F a_s$ . Orange circles correspond to the experimental results reported in Ref. [\[17\]](#page-4-0). Green circles, squares, and triangles are results for the hard-disk of Ref. [\[16\]](#page-4-0) and for the SWSC and SC models described in the text, respectively. The red point corresponds to a calculation with the soft disk potential with a small effective range. Dashed lines are guides to the eye.

unable to provide the experimental energy because it only reproduces the experimental 3D scattering length, not the effective range. On the other hand, our two present models, in which both scattering length and effective range are fixed at the same time, show good agreement between them and with the experimental measurements [\[17\]](#page-4-0). Therefore, the dimensionless parameter  $k_{F}a_{s}$  is not the only relevant quantity to quantitatively describe the system, and, to this end, finite range effects need to be included. Moreover, the independence of the specific shape of the potential, when both scattering length and effective range are reproduced, hints at a universal behavior in these two quantities for the range of  $k_F a_s$  values shown in the figure.

To better characterize the Fermi polaron, we evaluate properties that are related to its quasiparticle character. First, we study the quasiparticle residue *Z*, which is defined as the overlap between the wave function of the system, featuring an interacting impurity, and the wave function of a pure system with a noninteracting impurity with zero momentum,  $k = 0$ [\[52\]](#page-4-0). Formally, it reads

$$
Z = |\langle \Phi^{\rm NI} | \phi \rangle|^2. \tag{5}
$$

For the calculations presented here,  $\Phi^{\text{NI}} = |FS + 1\rangle$ , which stands for a Fermi sea (FS) with an added noninteracting impurity with zero momentum. Following previous works [\[16](#page-4-0)[,58,59\]](#page-5-0), we evaluate the quasiparticle residue from the long-range asymptotic behavior of the one-body density matrix when the interacting polaron moves in the Fermi bath. In our DMC implementation, this is obtained from the following estimator:

$$
Z = \lim_{|\mathbf{r}'_{\downarrow} - \mathbf{r}_{\downarrow}| \to L/2} \left\langle \frac{\Psi_T(\mathbf{R}_{\uparrow}, \mathbf{r}'_{\downarrow})}{\Psi_T(\mathbf{R}_{\uparrow}, \mathbf{r}_{\downarrow})} \right\rangle.
$$
 (6)

In Fig. 2, we show DMC results for *Z* using the SWSC, SC models. Again, we benchmark our results in the weakly interacting regime with a HD model. In the same figure, we include the experimental results of Ref. [\[17\]](#page-4-0) for this quantity.

For values of  $k_F a_s < 0.2$ , we find that the results of the three models coincide, in agreement with the universal regime for this observable, as reported in Ref. [\[16\]](#page-4-0). However, as  $k_F a_s$  is increased, the results of the SWSC and SC models, for which the effective range and scattering length are fixed simultaneously, show good agreement with the experimental data of Ref. [\[17\]](#page-4-0) and a clear discrepancy with the HD short-range model. These results reinforce those for the polaron energy, and they highlight the importance of going beyond the usual mean-field prescription in order to provide an accurate description of the 2D Fermi polaron. For completeness, in the same plot we also include a point in which the quasiparticle residue is evaluated for an SC model with a small effective range. As can be seen from the figure, in this case the shortrange SC model does not reproduce the experimental results and seems to be in good agreement with the HD model. In Ref. [\[16\]](#page-4-0), it was already shown that the HD model is in agreement with the T-matrix results of Ref. [\[60\]](#page-5-0), assuming a short-range model, up to values of the gas parameter  $k_F a_s \sim 1$ .

To provide further insight into the description of the Fermi polaron as a quasiparticle, we evaluate its effective mass. This mass corresponds to that of a quasiparticle, formed by the impurity "dressed" by the medium, which propagates freely. In the DMC algorithm, the effective mass can be obtained by evaluating the long imaginary-time asymptotic behavior of the diffusion coefficient of the impurity throughout the bath [\[5](#page-4-0)[,61\]](#page-5-0),

$$
\frac{m}{m^*} = \lim_{\tau \to \infty} \frac{1}{4\tau} \frac{D_s^{\downarrow}(\tau)}{D_0},\tag{7}
$$

with  $D_0 = \frac{\hbar^2}{2m}$  corresponding to the free-particle diffusion constant, and  $D_s^{\downarrow}(\tau) = \langle [\mathbf{r}_{\downarrow}(\tau) - \mathbf{r}_{\downarrow}(0)]^2 \rangle$  the mean-squared imaginary-time displacement of the impurity in the medium. The effective mass of the polaron can be experimentally accessed through its low-momenta excitation spectrum,

$$
\varepsilon_p(\mathbf{k}) = \varepsilon_p(\mathbf{k} = 0) + \frac{\hbar^2}{2m^*}k^2 + O(k^4),
$$
 (8)

with  $\varepsilon_p(\mathbf{k})$  being the polaron energy corresponding to a state with momentum **k**, and  $\varepsilon_p(\mathbf{k} = 0)$  is the ground-state polaron energy, as defined in Eq. [\(3\)](#page-2-0). Unfortunately, we are not aware of any measurement of *m*<sup>∗</sup> in this range of densities to compare with.

We present in Fig. 3 our DMC results for the effective mass of the polaron. Similarly to previous reported quantities, we show results for the SWSC and the SC models. As can be seen from the figure, both models agree within the statistical error, coming from the MC sampling, for  $k_F a_s \leq 1$ . As expected, the effective mass increases as  $k_F a_s$  approaches 1 and the contribution of polaron-medium correlations is enhanced. However, the observed increase of the effective mass with  $k_F a_s$  is less pronounced than that predicted by T-matrix theory [\[60\]](#page-5-0).

In conclusion, inspired by a recent experiment with  $173$ Yb [\[17\]](#page-4-0), we have addressed the two-dimensional repulsive Fermi polaron problem by means of the DMC technique. The experimental results of Ref. [\[17\]](#page-4-0) are outside of the universal regime in terms of the gas parameter [\[16\]](#page-4-0). With the aim of



FIG. 3. Inverse effective mass of the polaron as a function of the the Fermi momentum  $k_{F}a_{s}$ . Squares and triangles are results for the SWSC and SC potentials, respectively. The dashed line is a guide to the eye.

reproducing them, we include, through the two-body potential, information of the effective range of the impurity-bath interaction. Our results for the polaron energy and the quasiparticle residue show agreement between two different model potentials with the same scattering length and effective range, and they are in good agreement with the experimental results. This hints at the existence of a universal regime in terms of two parameters: the Fermi momentum and the effective range. This assertion seems to be confirmed when the effective mass of the polaron is evaluated.

Therefore, we have shown that the employment of *ab initio* quantum Monte Carlo techniques can offer insight into the polaron problem once the universality limit is surpassed. Similar results have been shown recently in the formation of droplets in Bose-Bose mixtures [\[45\]](#page-4-0) and in the description of dipolar droplets of dysprosium atoms [\[62\]](#page-5-0). In addition to the static properties discussed in this paper, a proper inclusion of the *s*-wave effective range into an underlying density functional might also affect the dynamics [\[47](#page-4-0)[,63,64\]](#page-5-0). We strongly believe that the observation of many-body effects, going beyond the simple mean-field approach, will stimulate further theoretical and experimental work.

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