Aluminum-doped silicon  $(3 \times 10^{17} \text{ atoms/cc})$  was similarly unproductive.

We are indebted to W. H. Brattain for stimulating discussion, to N. B. Hannay and E. D. Kolb for the special silicon crystals, and to P. Breidt and W. F. Flood for preparing the silicon samples.

<sup>1</sup> C. J. Gallagher, Phys. Rev. **88**, 721 (1952).<br><sup>2</sup> Holden, Kittel, Merritt, and Yager, Phys. Rev. **77**, 147 (1950).

## Energy of the High-Lying Acceptor Level in Copper-Doped Germanium

I. F. BATTEY AND R. M. BAUM

Electronics Division, Sylvania Electric Products, Ipswich, Massachusetts (Received April 5, 1954)

'N addition to the much investigated' level at about 0.037 ev **L** above the valence band, it has been reported that copper introduces another higher-lying acceptor level<sup>2</sup> in the forbidden energy gap of germanium. If this is the case, the level should make itself very evident in Hall and resistivity data at room temperature and below if it can be arranged that the lower-lying level is substantially completely populated and the higher level is partially populated at these temperatures. This requires the Fermi level to be within a few  $kT$  of the upper level and will lead to an exponential variation of carrier density in the temperature region where the carrier concentration of a sample doped only with Group III and Group V atoms is approximately constant.

This situation may be achieved by diffusing copper into an originally *n*-type sample of Group V impurity concentration  $N_d$ . If a density of copper atoms,  $N_a$ , between  $\frac{1}{2}N_d$  and  $N_d$  is introduced, the lower copper level will be entirely filled and the upper level partially filled with the Group V donor electrons. The solid solubility of copper in germanium as a function of temperature may be estimated from the work of Fuller and Struthers,<sup>3</sup> and Finn,<sup>3</sup> and the time necessary to achieve a reasonable approximation of solid solubility may be estimated from a knowledge of the diffusion coefficient as a function of temperature.<sup>3</sup>

The sample for which data are shown in Fig. 1 was  $1.5 \times 0.58$  $\times 0.27$  cubic centimeters and had about  $1.2\times 10^{15}$  Group V donor per cc. It was copper plated, held at 630'C for about ten days in an argon atmosphere, then quenched rapidly to room temperature



Fig. 1. Temperature dependence of Hall coefficient R and resistivity  $\rho$  for a germanium sample doped with 1.2  $\times 10^{14}$  copper atoms per cc.<br>approximately 8  $\times 10^{14}$  copper atoms per cc.

to try to introduce about  $8 \times 10^{14}$  copper atoms/cc. Room-temperature measurement following this treatment showed the sample to be high-resistivity  $\phi$  type.

The condition for electrical neutrality in this semiconductor at room temperature and below requires that  $p+p_a=2N_a-N_d$ , where p is the hole density in the valence band and  $p_a$  is the density of empty upper copper levels. This may be written as

$$
N_v \exp[-(F - E_v)/kT] + N_a / (1 + \exp[(F - E_a)/kT]) = 2N_a - N_d,
$$

where  $N<sub>v</sub>$  is the effective density of states in the valence band, F is the Fermi energy level,  $E_v$  is the energy of the top of the valence band, and  $E_a$  is the upper copper energy level. For the sample measured  $N_a \approx 8 \times 10^{14}$ /cc,  $2N_a - N_d \approx 4 \times 10^{14}$ /cc, and at room temperature  $p \approx 9 \times 10^{13}/c$ . Thus for values of p smaller than the room-temperature value, the Fermi level should coincide with the upper copper level to within an energy of the order of  $kT$ , and  $p=N_v \exp[-(E_a - E_v)/kT]$ .

Hall and resistivity data are shown in Fig. 1. The curves exhibit a temperature dependence below the intrinsic range which is consistent with the premise of a partially populated level at about 0.3 ev above the valence band. Both Hall coefficient and resistivity curves show a very steep activation energy below room temperature where  $F$  and  $E_a$  coincide. Both curves go into the usual intrinsic line above room temperature, and the Hall curve exhibits a reversal of sign at about 355'K. The activation energy for the upper copper level is 0.304 ev from the Hall curve and 0.308 ev from the resistivity curve if other temperature dependences in these expressions are neglected. If it is assumed that  $N_v$  goes as  $T^{1.5}$ ,  $\mu_H/\mu$  as  $T^{0.5, 4}$  and  $\mu$  as  $T^{-2.3, 5}$  where  $\mu$  is the drift pendences in these expressions are neglected. If it is assumed tha  $N_v$  goes as  $T^{1.5}$ ,  $\mu_H/\mu$  as  $T^{0.5,4}$  and  $\mu$  as  $T^{-2.3,5}$  where  $\mu$  is the drif mobility, and  $\mu_H$  the Hall mobility, a plot of  $\rho T^{-0.8}$  or  $1/T$  should be proportional to  $\exp\left[(E_a - E_v)/kT\right]$ . Using this procedure the Hall data give  $E_a - E_v = 0.285$  ev and the resistivity data  $E_a - E_v = 0.315$  ev.

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<sup>1</sup> See for instance F. J. Morin and J. P. Maita, Phys. Rev. 90, 337 (1953); W. C. Dunlap, Bull. Am. Phys. Soc. 29, No. 3, 21 (1954). J. A. Burton *et al.*, J. Phys. Chem. 57, 853 (1953); W. C. Dunlap, Bull. Am. Phys. Soc

## Doppler Line-Width Reduction\*

M. W. P. STRANDBERG AND H. DREICER Research Laboratory of Electronics and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts (Received April 13, 1954)

combination of microwave spectroscopic and molecular bean  $\mathbf{W}^{\text{E}}$  have succeeded in observing a large reduction in the Doppler width of a molecular absorption line by using a techniques.<sup>1</sup> This procedure, utilizing the effect of the matter on the electromagnetic radiation, solves the onerous detection problem encountered in the usual molecular beam experiments where the effect of the radiation on the matter is observed. The high resolution of molecular beam experiments afforded by the interaction of the radiation field and the transverse molecular beam is thus made available for microwave spectroscopic use.

In the exploratory study reported here the ammonia inversion absorption transition for the rotational state  $J=3$ ,  $K=3$  was observed with the microwave radiation propagated transverse to a beam of ammonia molecules. The radiation was detected and displayed by conventional techniques.<sup>2</sup> However, because of the resulting narrow line width the microwave oscillator was swept in saw-tooth fashion only over a region 80 kc/sec wide, centered at about 23 870 Mc/sec. Figure 1 shows the absorption signal of the