

protons on F^{19} in channel spin 1 are most suitable and are discussed below. Since it was not possible to measure the inelastically scattered protons leading to the 114-keV state at these resonances, we discuss only the angular distribution of protons leading to the 200-keV state and of the two γ rays.

The protons to the $5/2^+$ state are distributed as $1 + A_p \cos^2\theta = 1 + B_p P_2(\cos\theta)$, where, because of the two channel spins 2 and 3 in the outgoing state, $-7/9 \leq A_p \leq 1/3$ or $-0.7 \leq B_p \leq 0.2$. The observations (tabulated below) lie within this range. A $3/2^+$ state would also be consistent with the proton distributions.

With an assignment of $1/2^-$ for the 114-keV state, the corresponding γ ray is spherical, in agreement with observation. For the 200-keV γ ray, we expect an angular distribution $f(\theta) = 1 + A_\gamma \cos^2\theta = 1 + B_\gamma P_2(\cos\theta)$. If the state were $3/2^+$, decaying by magnetic dipole, A_γ would be less than or equal to zero; the fact that A_γ is positive eliminates this possibility. For a $5/2^+$ state decaying by electric quadrupole radiation, we get $0.23 \leq A_\gamma \leq 0.75$ or $0.143 \leq B_\gamma \leq 0.4$. Before comparing with experiment, we will discuss some novel features of this problem.

The treatment of the proton spin needs some explanation. In calculating the angular distribution of the inelastically scattered protons, the proton spin is combined with that of the excited F^{19} nucleus to form two channel spins: from each of these, an angular distribution is calculated and the results are the two extreme distributions, the general result being an arbitrary linear combination of the two. In calculating the distributions of the subsequent γ rays, however, the amplitudes from the two channel spins are coherent and the general result contains a term corresponding to the interference of the two channel spins. The extreme distributions can of course be found by diagonalizing the quadratic form. It is interesting to inquire, however, if a different way of combining angular momenta will lead directly to the two extreme distributions which can be combined incoherently. It is readily seen that the appropriate combination for this purpose is the $l + s = j$ of the outgoing proton. The γ -ray distributions for different j values (here $1/2$ and $3/2$) of the outgoing proton are incoherent and, in fact, for $j = 3/2$ we get $A_\gamma = 0.23$, whereas for $j = 1/2$ we get $A_\gamma = 0.75$.

This result leads immediately to the formulation of a general statement as to when we may combine two angular momenta, at a certain stage of a reaction, to form a resultant which may be treated incoherently: Whenever an experiment gives equal weight to all projections of two angular momenta j_1 and j_2 which are to be combined, then we may form $\mathbf{j}_1 + \mathbf{j}_2 = \mathbf{J}$ and the various J values can be treated incoherently for that particular experiment. For example, in observing the proton angular distribution, equal weight is given to the projections of the spins of proton and of excited F^{19} , whereas in observing the γ -ray distribution, equal weight is given to all directions of the proton (projections of \mathbf{l}) and to all projections of the proton spin. We see also when, in the excitation curve of the γ rays from a residual nucleus, two overlapping resonances or states of the compound nucleus can show interference (a term which, as a function of excitation energy, is asymmetric about the resonance center and leads to a rapidly changing angular distribution in the neighborhood of the resonance center). Only those resonances which can lead to the residual state in question by particles of the same j and l can show such interference in the radiations from the residual state.

There is, of course, a correspondence between the angular distributions of inelastically scattered protons and of subsequent γ rays at a given resonance. This is shown by the solid curve in Fig. 1, where B_p , the coefficient of $P_2(\cos\theta)$, is plotted against B_γ . Because of the coherence of the usual channel spins, this correspondence is in the form of an ellipse, instead of a straight line, which is bounded in the B_p and B_γ values by the numbers already computed. Taking the channel spin amplitudes as real numbers, the corresponding experimental points for B_p and B_γ should lie on the perimeter of the ellipse.

In this problem, the situation is further complicated by the long lifetime² of the $5/2^+$ state (10^{-7} sec) which permits some precession of the nuclear spin before γ emission. This will result in a B_γ reduced by multiplying with some factor $\alpha < 1$. In this case it does not seem possible to calculate α since the environment of the radiating F^{19} nucleus is quite uncertain after the p - F^{19} collision which will leave the atom perhaps excited and in a strange lattice position. It should be possible, by correlating sufficiently precise measurements of B_p and B_γ at different resonances, to test the conclusions given here and to find the reduction factor α . The dotted ellipse is drawn for $\alpha = 0.6$. The observations listed below are shown as rectangles in the figure and are not inconsistent with $\alpha \approx 0.6$. In addition, the angular distribution of the 200-keV γ ray as excited by Coulomb excitation under alpha-particle bombardment³ is consistent with α in the range 0.6 to 0.8.

Resonance	A_p	B_p	A_γ	B_γ
873 keV	0 \pm 0.1	0 \pm 0.07	0.17 \pm 0.02	0.11 \pm 0.015
1355 keV	0 \pm 0.1	0 \pm 0.07	0.40 \pm 0.03	0.235 \pm 0.015
1381 keV	-0.45 \pm 0.1	-0.35 \pm 0.1	0.44 \pm 0.03	0.255 \pm 0.015

* Assisted by the U. S. Office of Naval Research and the U. S. Atomic Energy Commission.

¹ Peterson, Barnes, Fowler, and Lauritsen, this issue [Phys. Rev. 94, 1075 (1954)].

² Thirion, Barnes, and Lauritsen, this issue [Phys. Rev. 94, 1076 (1954)].

³ Sherr, Li, and Christy, preceding Letter [Phys. Rev. 94, 1076 (1954)].

Short-Lived Isomeric States of Ag^{110} and In^{116}

F. I. BOLEY

Scott Laboratory, Wesleyan University, Middletown, Connecticut

(Received March 1, 1954)

BETA and gamma radiations from the short-lived isomeric states of Ag^{110} and In^{116} have been investigated using a scintillation spectrometer. The detector arrangements were conventional, using RCA 5819 photomultipliers in conjunction with sodium iodide (thallium activated) or anthracene crystals for the detection of gamma or beta rays, respectively. Data were recorded photographically as dots on 35-mm film. This recording technique provides information concerning both the energy spectrum and decay rate of the sample. Details concerning the photographic dot recording method have been described elsewhere.¹

Ag^{110} was obtained by irradiating 0.001-inch silver foil in the

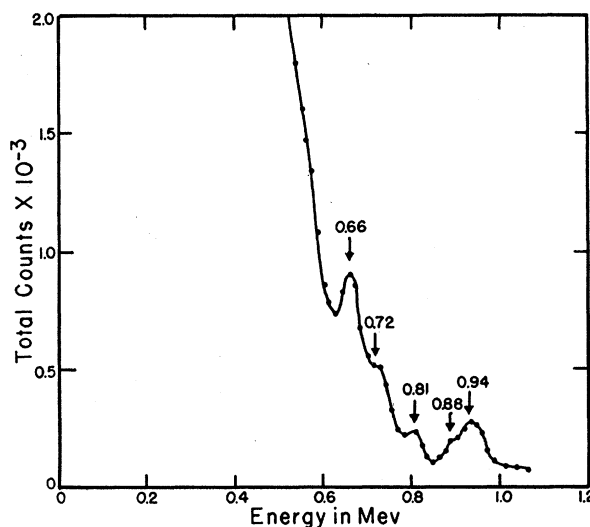


FIG. 1. Gamma spectrum of 24-second Ag^{110} . Energies are in Mev.

