A Possible Mechanism for 1/f Noise Generation in Semiconductor Filaments*

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I N describing the mechanism to be proposed here for 1/f noise generation in semiconductor file. generation in semiconductor filaments, it is first of all assumed that the low-frequency noise is caused by random fluctuations in the number of mobile charges (i.e., holes and electrons). This explains the fact that noise power seems to vary as the square of the current through the semiconductor. The fluctuations of mobile charges are, in turn, assumed to be due to the random creation and annihilation of trapping centers.1 For reasons that will appear later, it will be assumed that these trapping centers are all on the surface of the material. The physical model which describes this random creation and annihilation process will be as follows. A lattice atom or impurity atom at the surface of the material is knocked out of its equilibrium position (by a source which will not be specified) and starts to diffuse throughout the surface. The motion will then be a sort of Brownian movement about the equilibrium position O. It is assumed that the diffusion must be confined to the surface (i.e., it takes place only over two dimensions). From the theory of Brownian motion the diffusion atom at any time t after its release will on the average be within a circle whose center is at O and whose radius \bar{r} is determined by

$$\tilde{r}^2 = 4D(t+t_0)$$
. (1)

D is the diffusion constant. The vacancy O is assumed to act as a trapping center for a hole or electron until its diffusing atom or another diffusing atom gets captured in it. At the instant of atom capture the trapped hole or electron is released to become a mobile charge again. Thus, during the time O was unoccupied there was one less mobile charge. With a constant current through the sample, this would have produced a square pulse at the output voltage, whose length is the time O was unoccupied.

It is assumed that the trapping centers are being created randomly at a more or less constant average rate. Their rate of annihilation is dependent upon the intensity of diffusing atoms (and, therefore, the number of trapping centers present); thus, after a while there will be an equilibrium condition where the average density of diffusing atoms and trapping centers will be constant. This is the condition with which we will be concerned

The output voltage will then be a sum of randomly occurring square pulses of varying lengths. If the probability of any one pulse width being between s and s+ds is g(s)ds, then it can be shown that the correlation function R(t) of the output voltage will be

$$R(t) = K \int_{t}^{\infty} (s - t)g(s)ds$$
$$= K \int_{t}^{\infty} \rho(s)ds, \tag{2}$$

where

$$\rho(s) \equiv \int_{s}^{\infty} g(u) du,$$

and K is the average number of pulses per unit length of time. The power spectrum $G(\omega)$ for output will then be

$$G(\omega) = K \int_0^\infty \left[\int_t^\infty \rho(s) ds \right] \cos \omega t dt$$

= $(K/\omega) \int_0^\infty \rho(t) \sin \omega t dt$. (3)

Now $\rho(t)$ can also be shown to be the probability that an unoccupied trapping center is still unoccupied after a time t, after having been created at t=0. $\rho(t)$ is to be determined from the following relation:

$$- (d\rho/dt) = \left[(\vec{N}\sigma_c \vec{v}) + ((\sigma_c \vec{v})/(\pi \delta \hat{r}^2)) \right] \rho, \tag{4}$$

where σ_c is the capture cross section, \bar{v} is the average velocity of the

diffusing atom, δ is the thickness of the surface layer, and \bar{N} is the average density of the diffusing atoms from other vacancies at the position of a given vacancy. Equation (4) expresses the fact that a trapping center can be annihilated in two ways. The first way (given by the second term on the r.h.s. of the equation) is by having its own diffusing atom come back and be recaptured. The second way (denoted by the first term) is by capturing a diffusing atom from another trapping center.

If (1) is substituted in (4) and the boundary condition $\rho(0) = 1$ is used, $\rho(t)$ can be obtained specifically and has the form,

$$\rho(t) = [t_0/(t+t_0)]^n \exp(-t/T), \tag{5}$$

where

$$T \equiv (\bar{N}\sigma_c \bar{v})^{-1},\tag{6a}$$

$$n \equiv (\sigma_c \bar{v})/(4\pi \delta D)$$
. (6b)

 $G(\omega)$ can be obtained by substituting (5) into (3), with the result

$$G(\omega) = \frac{K\pi t_0^n F(n, \theta)}{\left[\omega^2 + (1/T)^2\right]^{(2-n)/2}} \quad \text{when} \quad \omega < 1/t_0,$$

$$= 1/\left[\omega^2 + (n/t_0)^2\right] \quad \text{when} \quad \omega > 1/t_0,$$
(7a)

where $\theta \equiv \tan^{-1}(\omega T)$ and

$$F(n,\theta) = \frac{\sin(1-n)\theta}{\Gamma(n)[\sin n\pi][\sin \theta]}.$$
 (7b)

When $1/T < \omega < 1/t_0$, (7a) shows that $G(\omega)$ varies as $1/\omega^m$, where m=2-n. Thus $G(\omega)$ has the observed $1/\omega$ dependence if n=1. Experimental data indicate that m may vary from 0.8 to 1.5, so ncan vary from 0.5 to 1.2.

A crude estimate of n will now be made in terms of the physical parameters which are involved. From the theory of diffusion, it can be shown that D and \bar{v} can have the following forms: 2,3

$$D = \frac{1}{4} \tilde{f} a^2, \tag{8a}$$

$$\bar{v} = \bar{f}a.$$
 (8b)

In the above equation \tilde{f} is the average jump frequency and a is the separation between adjacent potential wells. It should also be noted at this point that $\sigma_c = \delta \lambda_c$, where λ_c is a mean capture length. Thus with the aid of (8a) and (8b), n from (6b) can be brought into the following simple form:

$$n = \lambda_c / (\pi a). \tag{9}$$

If n is to be of the order of unity, λ_c must be of the order of πa (=10⁻⁷ cm), a value which is not too unreasonable physically.

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¹The general picture up to this point is similar to noise models of other investigators. See, for example, G. G. Macfarlane, Proc. Phys. Soc. (London) B63, 807 (1950); J. M. Richardson, Bell System Tech. J. 29, 117 (1950).

²See, for example, A. H. Cottrell, Theoretical Structural Metallurgy (Longmans Green, New York, 1948), pp. 190–5.

³ Equation (8a) was derived on the assumption that the jumps can take place in any direction.

Infrared Absorption Induced by Static Electric Fields

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ONDON¹ showed theoretically in 1932 that vibrational modes normally infrared inactive could be rendered active by a static electric field. He estimated the magnitude of the effect and concluded that, although the absorption would be small, it should be observable under suitable experimental conditions.

The rotation-vibration spectrum of hydrogen induced by a static electric field has been observed and initial results are reported in this letter.

The absorption cell was that used in the investigation of pressure-induced absorption.² The light guide also served as a parallel