and we get a positive  $S_0$  in both cases, the two values differing by about 20 percent, but both essentially in agreement with the value given by AOW. It would appear, therefore, that, unless their measurements are greatly in error, their conclusion that liquid He' must show a transition below  $1^{\circ}K$  is correct.

<sup>1</sup> T. C. Chen and F. London, Phys. Rev. **89**, 1038 (1953) (referred to as CL); see also Weinstock, Abraham, and Osborne, Phys. Rev. **89**, 787 (1953).<br><sup>2</sup> Abraham, Osborne, and Weinstock, Phys. Rev. **80**, 366 (1950) (refe

## Kinetic Energies of  $V_1^0$  Particles\*

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N the period November 1 to December 11, 1952, 77  $V^0$  events N the period investment in a cloud chamber<sup>1</sup> operated at the Inter-University High Altitude Laboratory at Echo Lake, Colorado (elevation 10 600 feet).

The purpose of this note is to comment on the remarkably large fraction of the observed  $V^0$  particles having low kinetic energies and to give particulars of two  $V^0$  events which do not fit recently proposed decay schemes.

The cloud chamber operated in an average magnetic field of 5400 gauss and was triggered by a combination of Geiger counters and proportional counters as shown in Fig. 1. A presentation of the production data for the first 49 of these  $V^{\mathbf{0}}$ 's is given in Table I.

TABLE I. Summary of cloud-chamber pictures obtained at Echo Lake, Colorado, November 1-December 2, 1952.&

	No. of pic-	Events with pene- trating tures showers Air	No. of penetrating Central Top Cu	showers from: Сu	Pb	Mag- net	Single pene- trating par- ticles	Ran- dom par- ticles or	Elec- tron blanks events	
í.	5122	1149	117	416	395	365	198	1193	1632	1084
No. V <sup>0</sup>	49	47		18	19	8		0		0

<sup>3</sup> 1  $V^0$  per 110 pictures, 1  $V^0$  per 25 penetrating shower pictures, 1  $V^0$  per 35 penetrating showers.

'

Total running time 427 hours. Time lost in recycling chamber 171 hours.

Approximately three  $V^0$  particles were observed per 24 hours of running time, a rate appreciably higher than reported for previous cloud-chamber investigations performed at similar altitudes. $2-5$ 

Wherever possible the following measurements were made on the decay products of the  $V^0$  events: (a) momentum, (b) visual estimate of the ionization, (c) total space angle between decay products, (d) angle between each particle and the line of motion of the  $V^0$ . As a result, the 77  $V^0$  particles were classified into three categories:

- 
- (1) Those consistent with a decay  $V_1^0 \rightarrow p+\pi+39$  Mev.<br>(2) Those inconsistent with the  $V_1^0$  scheme (called  $V_2^0$ ) (2) Those inconsistent with the  $V_1^0$  scheme (called  $V_2^0$ ).<br>(3) Those for which there is insufficient information for
- Those for which there is insufficient information for classification in one of the above groups.

Since we consider that any ionization of less than twice minimum is indistinguishable from minimum, the *identified*  $V_1^0$  particles had momenta below about 0.8 Bev/c. Nevertheless, these lowenergy  $V_1^0$  particles represent an appreciable fraction of all our observed  $V^0$  particles. Table II presents the kinetic-energy data.

TABLE II. Kinetic energy of  $V1^0$  particles.<sup>a</sup>

	Number	Kinetic energy (Mev)	$P$ (Mev/c)
Known $V_1^0$	6	70 $30-$ $70 - 150$ $150 - 260$ $260 - 380$	$250 - 400$ $400 - 600$ $600 - 800$ 800-1000
Assumed $V_1^0$	20 18 4	$200 - 830$ 200-4000 $\cdots$	700-1600 700-5000 Undetermined

<sup>4</sup> Total number of  $V^0$  –77, number identified  $V_1^0$  –20, number  $V^0$  not  $V_1^0$  –15, unclassified  $V_1$  –42.

In this analysis the unknown  $V^0$  particles of group (3) were assumed to be  $V_1$ <sup>0</sup>'s. The upper and lower limits of their momenta were calculated from the space angle between the decay products. Table II shows that at least a fraction 20/62, or 32 percent, of the  $V_1^0$  particles observed in our cloud chamber are produced with kinetic energies below 400 Mev and  $\sim$ 10 percent with kinetic energies below 70 Mev. These percentages can be taken as lower limits since it is likely that not all the unidentified  $V^0$  particles are actually  $V_1^{\mathbf{0}}$ 's. However, because of biases these figures cannot be taken as absolute fractions. The probability that a  $V$  particle will decay inside the chamber is proportional to  $1-\exp[-L(P)/$  $P_{C_0}$ , where P is the momentum of the V particle (in units of  $Mc$ ,  $\tau_0$  is the proper lifetime, and  $L(P)$  is a suitably averaged "available" path length in the chamber. The average path length  $L$  is expected to be an increasing function of  $P$ , since higher-energy particles are more nearly collimated in the vertical direction and are less likely to escape from the sides of the chamber. From the known value of  $\tau_0$ , and from a consideration of the geometry of our chamber, we estimate that the relative bias against high-momentum V particles is not serious below  $\sim$ 2–3 Bev/c.

Other investigators<sup>3, 4, 6</sup> also report large fractions of  $V_1^0$  particles produced with low kinetic energies.

Q values were calculated for five selected  $V_1^0$  events for which good measurements of the momenta and ionization of both decay products could be made. These values are in agreement with those given by Bridge et al.<sup>6</sup> and Armenteros et al.<sup>7</sup> However, two events do not seem to fit either the  $V_1^0$  or  $V_4^0$  ( $\pi^+ + \pi^- + 214$  Mev)<sup>8</sup> decay schemes. The relevant data are given in Table XII. There is supporting evidence that the mass and momentum of the positive decay track in event 79—166 are within the stated limits, because the same photograph also contains a positive track of momentum  $375 \text{ Mev/c}$  and ionization of  $3-5$   $I_{\text{min}}$ , which corresponds to a particle with the mass of a proton. This event cannot therefore be a  $V_1^0$ . In order for it to be a  $V_4^0$  the positive momentum would have to be increased from 372 Mev/c to 1000 Mev/c.

In event 80–206 the negative decay product penetrated the  $1\frac{1}{2}$ in. copper plate in the center of the cloud chamber. Allowing for momentum loss in the copper, we found that its momentum in the upper half of the cloud chamber checks within experimental error with its momentum in the lower half, on the assumption

TABLE III. Data on two unusual events.

Event	Decay					Angles				
No.	products	$P$ (Mev/c)	$I/I_{\min}$	Mass	$\theta -$	$\theta_{+}$	$\theta -$	V10	$V_{2}^{0}$	
$79 - 166$	Positive Negative	$372 + 100$ $87 + 15$	$\lesssim^2$	< 1200 < 400	36.5 $\pm 1$	$\cdots$	$\ldots$	$\cdots$	$66 + 24$	
$80 - 206$	Positive Negative	$325 + 100$ $262 \pm 40$	$\leq 2.5$	< 1400 < 800	32.5 $\pm 1$	$7.5 - 11$	$25 - 21.5$	$82 + 24$	$45 + 17$	



SIDE VIEN

FIG. 1. Experimental arrangement.

that the particle is a  $\pi$  meson. The measurement of the positive momentum is subject to larger errors. However, in order for the event to be consistent with the  $V_1^0$  scheme, the positive momentum would have to be increased to 950 Mev/ $c$  and the negative decreased to 220 Mev/c. To fit the  $V_4^0$  scheme the positive momentum must be 1250 Mev/c, and the negative 300 Mev/c.

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<sup>g</sup> Thompson, Buskirk, Etter, Karzmark, and Rediker, Phys. Rev. 90, 329 (1953).

## The Spectrum and Half-Life of the  $\kappa$  Meson\*†

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'HE experimental evidence gathered to date indicates' that the  $\kappa$  meson has the following mode of decay

> $\kappa^{\pm} \rightarrow \mu^{\pm} + 2\nu$ .  $(1)$



FIG. 1. The variation of half-life of the  $\kappa$  meson is plotted against its mass in units of the electron mass. The solid curve is for decay into a meson and two neutrinos while the dashed curve is for decay into an elec

Michel<sup>2</sup> has discussed the general problem of the interaction between four Dirac particles and applied this to the decay of the  $\mu$  meson. Before one can apply these considerations directly to the  $\kappa$ -meson decay some decision as to the nature and size of the interaction constant must be made. In a recent paper Peaslee' has concluded from studies of beta decay that the correct interaction is  $(S \pm T + P)$ , where the  $\pm$  refers to  $\beta^{\pm}$  emission. If the same linear combination is assumed for  $\mu$ -meson decay, the coupling constant for this process is identical with that obtained from beta decay,

$$
|f_1| = 1.44 \pm 0.04 \times 10^{-49} \text{ erg cm}^3. \tag{2}
$$

Applying the transformation (67) of reference three to the spectrum formula (45) of reference two, one obtains

$$
P(E)dE = \frac{8(E^2 - \mu^2)^{\frac{1}{2}}}{3\hbar(2\pi\hbar^2 c^2)^3} (3E(W - E)f^2 + (E^3 - \mu^2)(f_3^2 + f_4^2 + 2f_5^2) + 3\mu(W - E)(f_3^2 - f_4^2 + f_1f_2) \, dE, \quad (3)
$$

where  $\kappa$  and  $\mu$  are the rest energies of the  $\kappa$  and  $\mu$  mesons, respectively,  $f^2$  is the sum of the squares of the coupling constants, and the range of E is  $\mu \leq E \leq W = (\kappa^2 + \mu^2)/2\kappa$ .

If one now assumes that the linear combination for  $\kappa$ -meson decay is the same as that for  $\mu$ -meson and beta decay, then the only  $f_i$  not zero is  $f_1$  and the half-life and decay spectra are immediately determined. Further, since the experimental evidence does not rule out the mode of decay,

$$
\kappa^{\pm} \rightarrow e^{\pm} + 2\nu,\tag{4}
$$

the above remarks can be applied to this also.

The variation of half-life with rest mass is plotted in Fig. 1 for both mocles of decay. It is seen that for the present best estimate of the rest mass<sup>1</sup> ( $\kappa = 940m_e$ ) the decay into an electron and two neutrinos is some 40 percent more rapid than the decay into  $a \mu$  meson and two neutrinos. One would thus expect roughly



FIG. 2. The spectrum of the charged decay particle for the  $\kappa$ -meson decay<br>The  $\kappa$ -meson rest mass was taken to be 940  $m_e$ . The solid curve is for decay<br>into a  $\mu$  meson and two neutrinos, while the dashed curve is

equal numbers of  $\kappa \rightarrow e+2\nu$  and  $\kappa \rightarrow \mu+2\nu$  decays from half-life considerations. The half-life of the  $\kappa \rightarrow \mu + 2\nu$  mode associated with a rest mass of 940  $m_e$  is  $1.63\times10^{-9}$  second, which is in agreement with recent work by Alford and Leighton. <sup>4</sup>

In Fig, 2 the spectrum of the decay particle is plotted for both modes of decay using 940  $m_e$  for the  $\kappa$  rest mass. The end point for the  $\kappa \rightarrow \mu + 2\nu$  decay is 145 Mev while that for the  $\kappa \rightarrow e+2\nu$ mode is 240 Mev.

From these considerations it would seem fruitful to investigate further the energy distribution of the decay products of the meson. From Fig. 2 one would expect two distributions (if both modes of decay exist), the electron distribution being the more asymmetric with the bulk of the decay electrons having high energies. Since almost twice as much energy is available to the electron, this mode of decay, if it exists, should be readily apparent. Probably the best method of identifying the  $\kappa-\mu$  decay