To treat the more general case where we impose no restriction on the nature of the nuclear wave functions, we can define an "effective neutron wave function" by

$$
\zeta_{I'I}^{M'M}(\mathbf{r}) = \int \Omega_{I'}^{M'}(\mathbf{x}, \mathbf{r}) \,^*\Omega_I^M(\mathbf{x}) d\mathbf{x},\tag{9}
$$

where Ω 's are the initial and final nuclear wave functions and $x \equiv$ coordinates of all initial nuclear particles. This can be expanded into a series containing all the i values compatible with the nuclear spins and parities, and the m summation can be easily performed. The only important point (as is clear from references 1 and 2} is that there is no interference between different l 's.

+ Work performed under the auspices of the AEC. I S. T. Butler. Proc. Roy. Soc. (London) 208, 559 (1951). ² Bhatia, Huang, Huby, and Newns, Phil. Mag. 43, 485 (1952).

Half-Lives of Eu¹⁵², Eu¹⁵⁴, and Sm¹⁵¹

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HE half-lives of Eu¹⁵², Eu¹⁵⁴, and Sm¹⁵¹ have been measured directly by mass spectrometric methods. In each case, the half-life was determined by the change with time of the isotopic constitution of samples containing an appreciable percentage of the nuclide under investigation. For Eu¹⁵² and Eu¹⁵⁴ the sample used for the determination of the half-lives was a normal europium sample irradiated in a pile. Data on this sample have been used previously for an indirect determination of the half-lives of Eu^{152} and $\mathrm{Eu}^{154,1}$

The half-life of $Sm¹⁵¹$ was determined by the change in isotopic abundance of Sm'5' in a sample of purified. fission-produced samarium, used for a previous indirect determination of the halflife by Inghram, Hayden, and Hess.²

In every case, isotopic analysis was made on a 12-inch radius of curvature 60°-deflection mass spectrometer.³ The europium sample was purified from its daughters by elution with pH 3.06 ammonium citrate from an ion exchange column filled with Dowex 50 resin. No further purification was made on the samarium. The data pertinent to the calculations and the results are given in Table I.

The errors quoted for the half-lives consider only the mean deviation of the isotopic determinations.

The value for the half-life of $Sm¹⁵¹$ is in fair agreement with the 122-year value determined indirectly by Inghram, Hayden, and Hess, but disagrees markedly with the 10³-year half-life obtained by Marinsky. ⁴

The serious discrepancy between the half-lives determined for Eu¹⁵² and Eu¹⁵⁴ and the half-lives obtained by Hayden, Reynolds, and Inghram may be caused by an experimental error in the determination of the absolute amount of the gadolinium present after bombardment. The presence of a short-lived isomer of $Eu¹⁵⁴$ would otherwise be necessary to explain the error in half-life of Eu¹⁵⁴. No such isomer is known.

The values for the branching ratios of the 9.2-hour Eu¹⁵², the 13-year Eu¹⁵², and the proportion of Eu¹⁵¹ capture that goes to each of the two Eu¹⁵² isomers, all measured indirectly by Hayden,

TABLE I. Decay data.

	$\%$ decay	Decay period (yr)	Half-life (yr)
E_{11} 152	16.7 ± 2.4	3.4	$13 + 2$
E ₁₁ 154	13.9 ± 3.3	3.4	$16 + 4$
Sm151	$3.6 + 0.9$	3.8	$73 + 25$

Reynolds, and Inghram, are almost certainly in error since they involve the above determined half-lives. No statement about the mvorve the above determined han-nves. To statement about the experiment.

¹ Hayden, Reynolds, and Inghram, Phys. Rev<mark>. 75</mark>, 1500 (1949).
² Inghram, Hayden, and Hess, Phys. Rev. **79**, 271 (1950).
³ Inghram, Hess, and Hayden (to be published).
⁴ Way, Fano, Scott, and Thew, *Nuclear Data*, ards, Circular 499 (1950).

Fast Coincidences with Čerenkov Counters

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~HE duration of the light Rash from a Cerenkov radiator is expected to be much shorter than that from a scintillation crystal. This letter reports an experiment performed at the National Bureau of Standards to study the resolving time limitations of Čerenkov counters¹ in preparation for coincidence experiments with high energy particles. The light was produced in Lucite radiators of two different types (A and B of Fig. 1), by secondary

FIG. 1. Cerenkov radiator designs. Heavy arrow indicates direction of high energy electron. Thin lines show paths of optical radiation.

electrons in the x-ray beam of the 50-Mev betatron. The light was brought to an approximate focus by refraction at the spherical end surfaces of the radiators. At the focal point the duration of the light flash from radiator type B is expected to be about 1.5×10^{-10} second due to unequal light collection times. That from type A is expected to be much shorter as the optical path differences are just compensated by the transit time of the electron through the Lucite. However, imperfect focusing can produce path differences of about 3 millimeters and a pulse duration of about 10^{-11} second. The light beam is divided by the mirrors M_1 and M_2 so as to stimulate two 1P21 photomultipliers P_1 and P_2 in coincidence. One can expect to liberate about 6 photoelectrons from each photo-cathode per centimeter penetration of the electron.² The phototubes were operated at 1400 volts dc potential. The current pulses from the individual tubes were amplified by 200 megacycle band width distributed amplifiers (Hewlett Packard Model 460A) and brought out of the betatron room through 40 meters of RG 59/ U cable. The coincidences vanish if a piece of black cloth is placed between the Lucite and the mirrors. Thus they are caused by optical radiation coming from the Lucite. The small solid angles $(10^{-3}$ of 4π) subtended by the photo-cathodes inhibit detection of any weak isotropic radiation from the Lucite.