THE

Physical Review

A journal of experimental and theoretical physics established by E. L. Nichols in 1893

Second Series, Vol. 81, No. 5

MARCH 1, 1951

A Cloud-Chamber Study of Nuclear Interactions in Lead and Aluminum. Part I^{*}

B. P. GREGORY AND J. H. TINLOT[†]

Department of Physics and Laboratory for Nuclear Science and Engineering, Massachusetts Institute of Technology, Cambridge, Massachusetts

(Received October 9, 1950)

The nuclear interactions of cosmic-ray particles in lead and aluminum have been studied in two cloudchamber experiments. The results of the first experiment, which yields an unbiased sample of interactions of protons, are used to discuss the relative and absolute cross sections in the two materials and the absolute intensity and energy spectrum of the incident protons. The second experiment was designed to select interactions of neutrons in which at least one penetrating ionizing particle was produced.

The types of interactions observed are in this case intimately related to the probability of triggering the cloud chamber. This problem is discussed in some detail, preparatory to more detailed analysis of this experiment in Part II of this paper.

I. INTRODUCTION

MANY experimenters¹⁻⁶ have used counter controlled cloud chambers to study the nuclear interactions of cosmic-ray particles. The greatest difficulty in the interpretion of data so obtained has arisen from the complicated and usually unknown effects of the method used for selecting events of interest. The present investigation was intended to minimize this difficulty by use of simple counter selection systems. The two systems used required (a) the detection of a single incident ionizing primary particle and (b) the detection of a single secondary ionizing penetrating particle.

Alternate thin lead and aluminum plates were mounted in the chamber. This particular arrangement was found useful for two reasons: (1) to compare the characteristics of nuclear interactions in two materials of widely different atomic number, and (2) to simplify the identification of particles and the definition of nuclear interactions.

The cloud chamber was operated under a wooden

¹ Now at The University of Rochester, Rochester, New York. ¹ W. B. Fretter, Phys. Rev. **73**, 41 (1948). (Reference on previous work may be found in this article.)

³ H. S. Bridge and W. E. Hazen, Phys. Rev. 74, 579 (1948).
³ C. Y. Chao, Phys. Rev. 75, 581 (1948).
⁴ W. B. Fretter, Phys. Rev. 76, 511 (1949).
⁵ Lovati, Mura, Salvini, and Tagliaferri, Phys. Rev. 77, 284 (1950). (1950).

⁶W. W. Brown and A. S. McKay, Phys. Rev. 77, 342 (1950).

roof of thickness 3 g/cm² at Echo Lake, Colorado, elevation 10,600 ft (700 g/cm²). The discussion of results has been divided into two papers, which we shall denote as Part I and Part II. In Secs. II and III of Part I, we are concerned with the characteristics of the primary particles. A sample of nuclear interactions of cosmic-ray protons (Sec. II) yields information as to the relative and absolute cross sections for particular interactions and as to the flux and energy distribution of these protons. We shall consider in Sec. III the nuclear interactions of neutrons in the two materials resulting in the production of penetrating particles, and discuss some consequences of our choice of triggering arrangement.

II. EXPERIMENTS A AND A'

(1) Experimental Arrangement

The cloud chamber contained seven lead plates $\frac{1}{4}$ inch thick and six aluminum plates $\frac{5}{16}$ inch thick, alternately arranged as shown in Fig. 1. The depth of the illuminated region was six inches. Stereoscopic photographs were taken with cameras whose axes were separated by 12 inches, at a distance of 55 inches from the front of the cloud chamber.

In Experiment A, the cloud chamber was expanded by a signal from a counter telescope placed above the chamber and shielded by a one-inch lead brick, as shown in Fig. 1. The volume defined by the intersection of the cone of acceptance of the telescope and the top

^{*} This work was supported in part by the joint program of the ONR and AEC.



FIG. 1. Plate assembly and triggering arrangement of Experiment A.

and bottom plates in the chamber was included in the illuminated region within two percent. The primary purpose of the experiment was to obtain an unbiased sample of interactions of these particles with the material in the chamber.

In Experiment A', a tray of eighteen counters was placed below the chamber, and the chamber was expanded whenever the telescope recorded a signal in anticoincidence with this tray, or in coincidence with the discharge of more than one counter in this tray. The resulting pictures were found to be useful only in improving the statistics on the relative numbers of protons and mesons stopping in the chamber.

(2) Triggering Events. Experiment A

One could usually identify, from the appearance of the counter age tracks in the pictures, the method by which the counter telescope had been triggered. One observed in a number of pictures only an electronic component, and considered that in this case the telescope had been triggered by an air shower. In most cases, however, a single particle entered the chamber after traversing the counter telescope. By studying the behavior of these particles, we obtain statistical information on the relative abundance of the ionizing components of cosmic radiation. For this purpose, the analysis was restricted to pictures which belonged to a series of pictures of uniformly good quality. The events observed in this set of pictures (a total number of 3827) are listed in Table I, and are discussed in detail in the following paragraphs.

(a) Single Penetrating Particles

Single particles (minimum range 104 g/cm² of lead) were observed to traverse the chamber without interaction in 2397 pictures of the set. The corresponding number of particles defined as belonging to the hard component (particles of range greater than 167 g/cm² of lead) is five percent less, or 2262. Since the flux of the hard component at the altitude in question is a well-known quantity, this number is one to which the number of all other events may be compared.

(b) Particles Stopped

The particles which stopped in the chamber were a mixture of μ -mesons, protons at the end of their range, and protons stopped by nuclear collision. The protons, whether or not at the end of their ranges, show much smaller Coulomb scattering than did the mesons, as is illustrated in Table II. One can make use of this fact to estimate the proportion of mesons and protons stopping in the chamber. One computes, from measurements on all the particles stopped, the root mean square scattering angles at the second lead plate above the plate in which the particles stopped. This value is then compared to the expected root mean square projected angle of scattering for mesons ($\alpha_{\mu} = 12.5^{\circ}$) and protons (α_p) . The upper and lower limits on the number of mesons are obtained by assuming that all protons stop by nuclear collision $(\alpha_p \simeq 0)$ or stop at the end of their range ($\alpha_p = 4.8^\circ$). From the combined pictures of Experiments A and A', one finds in this way that, of 81 particles stopped in the fourth through twelfth plates, between 32 and 39 were mesons. The behavior of the protons is seen to have a small effect on the computation.

Of the 46 stopped particles observed in Experiment A, only 30 stopped in the fourth through twelfth plates. From the above, it is estimated that 13 of these were mesons, and 17 were protons. The correlation of the number of stopped mesons with the flux of slow mesons incident on the telescope is difficult because of the great loss through scattering in the lead block in the telescope. One computes, for example, a loss of 75 percent of all mesons of ranges such as to stop in the middle plate of the chamber. The corresponding loss of protons, however, is only 9 percent, so that the results

TABLE I. Frequency of occurrence of various types of events based on 3827 frames of the A-experiment.

Single par	ticle emergir	ng from te	Elcetron			
Through	Stopping	Inter- acting	Nuclear scat- tering	High energy electron	Air shower	Blank pictures
2397	46	35	9	5	273	1062

concerning stopped protons are significant (see Sec. II-5 and Table III).

(c) Nuclear Interactions

In 44 cases, an ionizing particle emerging from the counter telescope produced a nuclear interaction in the illuminated region of the chamber. It is assumed that all such particles were protons. We shall discuss these interactions in detail in Sec. II-3. In particular, it will be shown that the corrected number of interactions occurring in the second through twelfth plates is 42.

(d) Electronic Component

We consider first the evidence for identification of single incident electrons. An electron of 1-Bev energy passing through the counter telescope would undergo multiplication in the one-inch lead block, and would appear in the chamber as a shower with about ten particles at the maximum.⁷ Only five such showers were observed. This number corresponds to a directional intensity of high energy electrons of about 3×10^{-5} sec⁻¹ ster⁻¹ cm⁻². Hazen⁸ has computed a directional intensity seven times as large for both electron- and photoninitiated showers in the same energy range and at the same altitude. We may explain the difference in the two figures by noting that most of the showers may well be photon-initiated, and that we detect only electron-initiated showers.

It is seen from Table I that over a quarter of the set of pictures of Experiment A showed either a purely electronic component, or were blank. The first type were easily identified as caused by ordinary extensive air showers. The blank pictures are attributable neither to accidental telescope coincidences nor to instrumental failures. It is most likely that, in these cases, the counter telescope responded to air showers of very low density, which were not visible in the cloud chamber.

(3) Description of Nuclear Interactions

Since, in this section and in Sec. II-4, we shall be concerned only with relative numbers of nuclear interactions, we shall consider a more extensive set of pictures, thus improving our statistical results. We consider in addition to the interactions of Table I others that were not of counter age, or that were

			Proton		Meson (214 <i>m</i> .)			
Inter- val	Plate	Energy (Mev)	rms scatt. $(\overline{\alpha})$	$I/I_{\rm min}$	Energy (Mev)	rms scatt. $(\overline{\alpha})$	I/Imin	
1	Pb Al	0-60		-4.8	0–24	4	-2.2	
2 3	Pb Al	42–76 78–103		6.6-4.0 4.0-3.3	16–30 31–42		2.8–1.9 1.6	
4 5	Pb	95–115 117–135	4.3	3.5–3.1 2.9	36-48 48-60	11	1.5 1.4	
6 7	Al Pb	128–145 148–153	1.0 3.5	2.8 2.5	52–62 62–72	2.6 9	1.3	
8 9	Al Pb	157–172 175–189	2.9	2.4 2.3	65–75 73–83	2.2 7.7		
10 11	Al Pb	183–197 199–213	2.5	2.2 2.2	78-86 87-95	1.8 6.8		
12 13	Al Pb	207–220 222–235	2.3	2.1	92–100 97–105	1.6 5.9		
Rang g/cm 10 17 24 31 41	ge in 1 ² Pb 10 70 40 10	300 400 500 600 720	1.7 1.3 1.1 0.9	1.8 1.5 	140 220 300 385 500	4.6 3.2 2.5 2.0 1.5		

observed in groups of pictures whose quality was not considered good enough for inclusion in the set of Table I. All of these interactions were produced by ionizing primaries.

(a) Identification of Nuclear Interactions

The various types of nuclear interactions are best illustrated by the pictures of Fig. 2. Interactions of types (1) and (2) are called "nuclear scattering." In these cases, one required that a particle of minimum ionization traverse two lead plates with no appreciable scattering (less than 1°) and then be deflected through an angle of more than 10°. When the deflection occurred

TABLE III. Absolute numbers of protons of various energies incident on the telescope. These numbers are normalized to 2262 particles of the "hard component."

	Protons stopping 4th-12th	Protons interacting (2nd-12th plates)					
		Types 1-2	Types 3-4	Types 5-6	Ty	pe 7	
Corrected number of events Number of protons incident on telescope Approximate energy of the protons (Bev) Intensities relative to the hard component	$ \begin{array}{r} 17 \\ 23 \\ 0.2 \text{ to } 0.3 \\ 10^{-2} \end{array} $	$ 13 \\ 56 \\ 2.5 \times 10^{-2} $	$ \begin{array}{r} 11 \\ 47 \\ 0.3 \text{ to } 1 \\ 2.1 \times 10^{-2} \end{array} $	$13 \\ 56 \\ 2.5 \times 10^{-2}$	$2 \\ 8 \\ 1 \text{ to } 2 \\ 0.3 \times 10^{-2}$	3 12 >2 0.5×10 ⁻²	

⁷ I. G. Tamm and S. Belenky, J. Phys. U.S.S.R. 1, No. 2 (1939).
 ⁸ W. E. Hazen, Phys. Rev. 65, 67 (1944).

TABLE II. Energy, scattering, and ionization of particles stopping in a lead plate. In this computation only losses by ionization are taken into account.



FIG. 2. A sample of nuclear interactions (Experiment A).

after traversal of more lead plates, scattering angles of 2° were accepted. All angles were measured in projection. The expected number of μ -mesons abnormally scattered through Coulomb interaction (and thus mistaken as protons suffering nuclear scattering) can then be calculated. We consider only the effect of multiple

scattering. (For $\frac{1}{4}$ -inch lead plates, the effect of single Coulomb scattering is negligible, if one assumes that the maximum angle of single scattering is equal to \hbar/Rp , in which R is the radius of the nucleus, and p is the momentum of the meson.) The probability of observing scatterings in the specified sequence



FIG. 3. Mean free path in lead and aluminum under the theory of transparency. These mean free paths are plotted as functions of the cross sections $(\bar{\sigma})$ for the interaction of the individual nucleons with the incident particle for $R=1.37A^{\frac{1}{2}10^{-13}}$ cm. The value of r is the expected ratio of the numbers of nuclear inter-actions occurring in 7 lead plates (49.7 g/cm²) and 6 aluminum plates (12.8 g/cm²).

is found to have an average value of 0.2 percent for mesons of range between 15 and 170 g/cm^2 of lead, and to be negligible for mesons of greater range. Since the intensity of "slow" mesons is 10 percent of that of the hard component, one finds that for the set of pictures of Table I, the expected number of mesons thus scattered is $0.002 \times 0.10 \times 2262 \approx 0.4$, as compared with the 9 cases of "nuclear scattering." Moreover, these events occurred about as frequently in lead and aluminum, and the observed deflection was larger than 20° in 9/10 of the cases. These are further indications of the nuclear origin of these interactions.

The minimum requirement for identification of interactions of types (3) to (7) was the observation of one heavily ionizing particle, or of one penetrating particle emitted at an angle of more than 10° (in projection) with the direction of the incident particle. These conditions were found to be sufficient to reject all knock-on showers of mesons.

Nuclear scatterings could not be observed in the first three plates in the chamber because of the criterion used in their selection. Moreover, the identification of all interactions occurring in the top and bottom plates was not considered reliable, and the corresponding pictures were rejected. We shall therefore consider in the following discussions only interactions observed in the second through twelfth plates, and correct the number of nuclear scatterings for the loss in plates 2 and 3. The relative frequencies of occurrence of the interactions of various types (Fig. 2) are obtained from this corrected number of 70 interactions.

(b) Estimate of the Energy of the Primary Protons

The following observations indicate that the energy of the protons producing the great majority of the observed interactions is below 1 Bev. If we consider the group of interactions of types (1), (2), (3), and (4), we find that in no case can a secondary meson or electronic component be detected. Furthermore, the incident protons in one quarter of these cases was visibly scattered. The protons producing interactions of types (5) and (6) were of somewhat higher energy than those of the first group, since none were visibly scattered. However, the estimated energy of the ionizing secondary particles was less than 450 Mev, and in only 4 cases out of 22 did one identify a secondary meson or electronic component.

The example of type (7) is one of the small group (11 percent of the total) of interactions of high energy protons. These were characterized by the production of two or more penetrating particles. In one-half of these cases, the energy of the ionizing secondary particles was estimated to be greater than 1 Bev.

(c) The Possibility of Single Proton-Nucleon Collision

We have investigated the possibility that some of the interactions of types (3) and (4) were due to a single collision between the incident proton and a proton of the nucleus.9 We determined the directions in space of the particles, and set limits to their energies. We could then compare these values with those predicted by the energy-angle relation for collisions between free nucleons, corrected for the motion of the nucleons in the nucleus. In 22 out of 26 cases we could not interpret the event as a simple proton-proton collision, even by assuming the most favorable velocity for the struck proton. One may therefore conclude that in the collision of a proton of average energy 500 Mev with a nucleus of lead or aluminum, the secondary nucleons are a result of multiple collisions within the nucleus.

(d) Proton-Neutron Charge Exchange

On the basis of the results obtained in Berkeley¹⁰ with 350-Mev protons, we expected to observe a considerable proportion of events of the type "charge exchange," in which a proton would turn into a neutron of almost the same energy. A number of interactions of types (1), (3), and (6) were interpreted as possible examples of charge exchange, in which cases an average of 100 Mev was transferred to secondary protons; this corresponded to a probable total energy loss of 200 Mev. Only one case was found in which no visible secondary particle was produced. We shall derive similar conclusions in Sec. III concerning the inverse process of neutron-proton charge exchange.

(4) Numbers of Nuclear Interactions in Lead and Aluminum. Transparency

The choice of lead and aluminum for the plates was made for the purpose of obtaining relative cross

⁹ J. G. Wilson, Proc. Roy. Soc. (London) A174, 72 (1940). (This has been found to be the case in one picture.) ¹⁰ University of California Radiation Laboratory Report UCRL

^{637,} unpublished.

sections for the production of nuclear interactions in a light and heavy element. The results of this section and of Sec. III-4 will be compared with the expected relative number of interactions under the assumption of geometric cross sections (nuclear radius proportional to $A^{\frac{3}{2}}$). This ratio, for the seven lead plates (49.7 g/cm²), and the six aluminum plates (12.8 g/cm²), is found to be

$r_{g} = 2.0.$

Of the 70 nuclear interactions considered in Sec. II-3, 41 occurred in five lead plates, and 29 in six aluminum plates. The ratio of the interactions in lead and in aluminum normalized to the total amount of material of the chamber is, therefore,

$r_A = 2.0 \pm 0.5$.

The result is compatible with geometric cross sections. The ratio r can be related to the absolute cross sections in the two materials by application of the theory of transparency of the nucleus.^{11,12} The curves of Fig. 3 illustrate the variation of this ratio and of the collision mean free paths of particles in the two materials as a function of the assumed particle-nucleon cross sections. One sees from these curves that the value r=2.5 (still consistent with the experimental result) corresponds to mean free paths of 200 g/cm² of lead and 140 g/cm² of aluminum.

(5) Spectrum and Absolute Intensity of Protons at 10,600 Feet

In this section we shall estimate the absolute directional intensity of protons and obtain a qualitative description of their energy spectrum. For this purpose, we shall now consider only the set of pictures of Table I.

The first row of Table III gives the number of protons stopped in the fourth through twelfth plates of the chamber [as obtained in Sec. II-2(b)], and the corrected numbers of nuclear interactions observed in the chamber from the second through twelfth plates [from Sec. II-2(c)]. We list in the third row the estimated energies of the incident protons responsible for these various types of interactions.

We obtain the absolute numbers of protons entering the telescope (listed in the second row of Table II) in the following two steps: (1) We compute the numbers of protons entering the chamber by assuming that all protons of the first column stop at the end of their ranges, and that all the other protons interact in the chamber with geometric cross sections; and (2) we increase these numbers for the loss by interaction (also with assumed geometric cross section) in the material above the chamber.

We can now compare these numbers with the corresponding flux (2262 particles) of the hard component. These relative intensities are listed in the last row of Table III. The sum of the numbers yields the relative flux of protons of energy larger than 200 Mev:

$$I_p/I_h = 0.089 \pm 0.018$$

The relative flux of "fast protons" (energy greater than 400 Mev) is

$$I_{fp}/I_h = 0.079 \pm 0.015$$
.

The large statistical errors are due to the relatively small number of observed events.

We deduce further that the energy spectrum described by the last row of Table III is either flat from 0.2 to 1 Bev, or has a peak in this range. Such a spectrum is expected from qualitative considerations.

III. EXPERIMENT B

(1) Experimental Arrangement

In this experiment the cloud chamber was triggered by a signal from a shielded counter telescope placed below the chamber when not accompanied by a signal from a large tray of counters placed above the chamber (Fig. 4).

This arrangement favored the recording of events in which a neutral primary particle produced secondary ionizing particles. The plate assembly was identical with that used in Experiment A. We had intended to study the effect of varying the thickness of the lead shields S_1 , S_2 , and S_3 . Thus, the thickness of S_1 was 0, 1 in., or 7 in., while the thicknesses of S_2 and S_3 were either 1 in. and 1 in., 0 and 4 in., or 1 in. and 9 in., respectively. However, the number of pictures taken in



FIG. 4. Plate assembly and triggering arrangement of Experiment B.

¹¹ Fernbach, Serber, and Taylor, Phys. Rev. 75, 1352 (1949).

¹² R. Serber, Phys. Rev. 72, 1114 (1947).

TABLE IV. Summary of nuclear interactions of Experiment B. The 136 nuclear interactions were due to non-ionizing primaries and occurred in the first through tenth plates. The corrected relative frequency is obtained as described in Section III-3.

	Group I						
Type of picture Number of penetrating particles Number of electronic showers Total number—showers and particles	(1) 1 0	(1)′ 1 ≥1	(2) 2 0	$\begin{array}{c}(2)'\\2\\\geqslant 1\end{array}$	$ \begin{array}{c} (3) & (3)' \\ >2 & >2 \\ 0 & \geqslant 1 \\ \leqslant 6 \end{array} $	$(4) (4)' >2 >2 0 \ge 1 >6$	(5) >2 ≥1 of high energy
Number of interactions Corrected relative frequency	36 0.	5 69	20 0.	22 ⁷	9 ²⁵ 25 0.06	2 12 0.01	20 0.02
normalized to 7 Pb and 6 Al (Fig. 3)	2.3 ± 0.6				$5.0{\pm}1.4$		

each arrangement was not sufficient to allow us to draw more than qualitative conclusions on this effect. For instance, with no lead above the anticoincidence tray, we observed a few purely electronic showers which apparently were due to materialization of incident photons. This was confirmed by the fact that these events were eliminated when the thickness of S_1 was 1 in. or 7 in.

From a total of about 5000 pictures obtained in this experiment, we selected for study 322 pictures of nuclear interactions. Of these interactions 237 occurred in the illuminated region, and were clearly responsible for the triggering of the counter telescope.

(2) Effect of the Triggering Requirement

In this section we shall examine in some detail the effect of the triggering arrangement of the choice of the particular events photographed. In order to be photographed, a nuclear interaction originating within the illuminated region must produce at least one particle which penetrates the shielded counter telescope. The probability that a particular interaction will accomplish this depends primarily on the multiplicity of the penetrating particles produced, and on the location of the point of origin.

One can compute, for any point of origin, the solid angle Ω_{\bullet} within which a penetrating particle must be emitted in order to traverse the telescope. The value of this angle (averaged over the surface of each plate) varies from 0.007 to 0.014 steradian from the first to the tenth plate. We shall use also the solid angle Ω_D subtended by tray D at various points within the illumination (varying from 0.03 to 0.05 steradian) and the solid angle Ω_B subtended by tray B (varying from 0.03 to 0.14 steradian). The values of these average solid angles for the middle plate of the chamber are:

$\Omega_s = 0.01, \quad \Omega_D = 0.04, \quad \Omega_B = 0.05.$

Note that a particle aimed at tray D from almost any point in the illuminated region traverses tray C, and therefore that the effect of tray C can be neglected.

From the above numbers, one could, in principle, compute the absolute probability of triggering for any event of given multiplicity of penetrating particles and electronic showers, originating anywhere in the chamber. It seems useless to attempt this calculation rigorously, because of the necessity of making detailed assumptions as to the energy and angular distributions of the secondary particles and showers. We shall make instead the approximation that the penetrating particles are emitted uniformly within a cone of solid angle Ω . For the present we neglect the absorption or scattering of these particles in the lead shielding

of the telescope, and take a value of Ω (0.55 steradian) which corresponds to an average angle of emission of 16° (Sec. II, Part II).

We can now calculate the probability that any interaction producing N penetrating particles triggers the telescope singly (one particle traversing trays A, B, and C):

$$P_s = 1 - (1 - \Omega_s / \Omega)^N \simeq N \Omega_s / \Omega$$

This probability is not very sensitive to the particular plate in which the interaction occurs, and is nearly proportional to N even for high multiplicities, because of the small values of Ω_{*}/Ω . P_{*} is of the order of 2 percent for an interaction producing one penetrating particle.

The probability P_m of multiple triggering (by separate particles traversing tray *B* and trays *C* and *D*) is easily shown to be much smaller than P_s for low multiplicity interactions occurring in the top plates and to increase sharply with the plate number and the multiplicity *N*. One may use the formula:

$$P_m = \Omega_B \Omega_D N (N-1) / \Omega^2$$

for interactions occurring in the upper plates of the cloud chamber and having a multiplicity less than five. The total probability of triggering is the sum of P_{\bullet} and P_{m} . An important result is that multiple triggering is the dominant process for interactions occurring in the bottom half of the chamber and having multiplicity larger than three. For example, P_{m} is equal to P_{\bullet} for N=4 in the seventh plate, and for N=3 in the ninth plate.

The probability of triggering tray B approaches one when a number of electronic showers are produced, particularly if the interaction occurs in the lower plates. In this case, the triggering process is complete if one penetrating particle is emitted in the solid angle Ω_D so as to discharge tray D. The probability of this modified single triggering is, therefore,

$$P_s' \simeq \Omega_D N / \Omega \simeq 4 P_s.$$

It is evident that the triggering probability varies over a wide range, depending upon the characteristics of the nuclear interaction. For example, the value P_s' for N=5 is 20 times the value of P_s for N=1.

The considerations of the preceding paragraphs are involved in the interpretation of practically all of the data obtained in Experiment B. They will be found particularly useful in discussing the following:

(i) The true frequencies of occurrence of various interactions.

(ii) The relative cross sections for nuclear interactions in different materials (since the character of the interactions, and consequently the triggering probabilities, may depend upon the material).

(iii) The relative numbers of penetrating particles and electronic showers (Part II).

(iv) The nuclear interactions of secondary penetrating particles (Part II).

(3) Description of Interactions and Results

Results relating to 136 selected nuclear interactions are given in Table IV. These interactions were caused by a non-ionizing primary, and occurred in the illuminated region of the first ten plates in the chamber. We divided them into two groups (low and high multiplicity) and subdivided them according to the multiplicity of penetrating particles and numbers of electronic showers. The distinction of penetrating particles is often difficult in the cases of interactions of type (5), because of the production of high energy electronic showers (energy greater than 1 Bev).

The remainder of the total number (237) of interactions occurring in the illuminated region, although not included in Table IV, are considered in later discussions. These include a small number caused by ionizing primaries incident at a large inclination and a large group (76) of interactions occurring in the three lowest plates. Analysis of this last group is difficult, since one cannot identify penetrating particles or, in most cases, recognize electronic showers. These pictures will be useful only for statistical considerations for which the type of event is not of great importance. The relation frequency of occurrence of different events has been corrected for the effect of the triggering requirement according to the estimates made in the next paragraphs.

(a) Corrected Frequencies of Occurrence of Various Interactions

By applying the results of the discussion on the probability of triggering, one can estimate the true relative rates of occurrence of the events of the various types. In the four types of interactions of group I the electronic showers were nearly always of low energy, and did not contribute appreciably to the triggering process. Since a single particle was in nearly all cases responsible for the discharge of the counter telescope, the probabilities of triggering are given by the equation for P_s . These interactions were, as expected, fairly evenly distributed among the plates. The events of higher multiplicity (group II) occur most frequently in the lower plates, e.g., 13 in the first four plates, compared with 48 in plates 7 through 10. This is expected if the triggering process was predominantly of the multiple type. For the interactions of type (3), we estimate the triggering probability by taking an intermediate figure between the values of P_{s} and P_{s}' for a multiplicity N=4. When tray B was discharged with a probability of almost one (types (4) and (5)), the triggering probability was assumed to be given by P. for N=5. From the observed numbers of events of each type and with the knowledge of the appropriate triggering probabilities, one readily obtains the corrected relative frequencies of occurrence as listed in the fourth line of Table IV.

(b) Estimate of the Energy of the Primary Neutrons

From the amount of penetration required of the triggering particles one can estimate the minimum energy (about 400 Mev) of the neutrons producing them. The average energy of the neutrons is believed

to be in the range where meson production is fairly common (i.e., about 1 Bev). For example, one observed in one-quarter of the cases of types (1) and (2) either electronic component or scattering of the penetrating particles greater than that expected for a proton.

Interactions of types (3), (4), and (5) produced ionizing secondary particles and electronic showers whose combined energy appeared to be 4 Bev, on the average. This is a crude lower limit, since one neglects the production of secondary neutrons, and arbitrarily assigns a minimum energy to each relativistic unscattered particle.

(c) Neutron-Proton Charge Exchange

The interactions of type (1) can be interpreted as examples of neutron-proton charge exchange. One assumes then that a neutron of energy greater than 400 Mev turned into a proton, and that a part of the original energy was dissipated in exciting a nucleus. The average energy delivered to slow protons was found to be on the average, about 200 Mev. Although this type of interaction is quite frequent (see Table IV), we are unable to compare its probability of occurrence with the probability of interactions which produce only low energy nucleons, since the latter event would not be recorded.

On the other hand, we may obtain the relative probability of charge exchange at the higher energies (above 4 Bev). If a neutron of this energy turns into a proton of nearly equal energy, one should observe in the chamber interactions of type (1) followed by an interaction of the resulting proton types (3), (4), or (5). This succession of events was never observed. From this fact, one computes a lower limit on the mean free path for neutron-proton charge exchange at high energies by the following arguments:

Let us consider all the interactions of high multiplicity occurring in the lower half of the chamber. The number of these due to neutrons incident at a large inclination can be assumed equal to the number produced by ionizing primaries which missed the anticoincidence tray. The neutrons producing the remaining interactions are assumed to have traversed the upper half of the chamber. The total amount of material thus traversed was 1900 g/cm² of lead and 600 g/cm² of aluminum.

One therefore concludes that the simple process of charge exchange is an extremely rare one at very high energies. If the process occurs at lower energies, the resultant excitation of the nucleus is of the order of 400 Mev (deduced from the observed energy of slow secondary protons).

(4) Ratio of Numbers of Interactions in Lead and Aluminum

As has been indicated, it is not possible in the case of Experiment B to obtain relative cross sections for interactions in the two materials simply by comparing the number of interactions observed in lead and aluminum. One can, however, obtain other information from a study of these numbers. As is shown in Table IV, the ratio of numbers of interactions having multiplicity ≥ 2 is 2.3±0.6, which is well in agreement with the ratio 2 expected for geometric cross sections. In the case of higher multiplicity interactions, however, the ratio¹³ is 4.9 ± 1.1 . (Note that, from Fig. 3, a ratio 4)

¹³ This number differs from the one in Table IV because it includes the interactions of high multiplicity occurring in the lowest three plates.

corresponds to vanishingly small cross sections, assuming the ratio to be unbiased by the selection of events.)

One concludes that the measured ratio 4.9 reflects the effect of different detection probabilities for interactions of different multiplicities. The change in ratio with multiplicity is, in consequence, proof that nuclear interactions of high energy neutrons produce, on the average, a higher multiplicity of penetrating particles in lead than in aluminum. The same result has been obtained by Lovati and his co-workers.⁵

PHYSICAL REVIEW

VOLUME 81, NUMBER 5

MARCH 1, 1951

A Cloud-Chamber Study of Nuclear Interactions in Lead and Aluminum. Part II*

B. P. GREGORY AND J. H. TINLOT[†] Department of Physics and Laboratory for Nuclear Science and Engineering, Massachusetts Institute of Technology, Cambridge, Massachusetts (Received October 9, 1950)

The results of the cloud-chamber Experiment B described in Part I are used to discuss some properties of the particles produced in nuclear interactions. Evidence is presented showing that the electronic showers produced in nuclear interactions are all photon-initiated. Upper limits on the proportion of directly produced electrons are found to be 20 percent in interactions in aluminum and 41 percent in lead. The possibility that the photons are decay products of neutral π -mesons is strongly indicated, although no definite proof can be given. It is shown that the mean free paths for nuclear interaction of secondary penetrating particles are 172 ± 30 g/cm² in lead and 164 ± 50 g/cm² in aluminum. Assuming that the penetrating particles consist of equal numbers of π -mesons and protons, one obtains an upper limit of 250 g/cm² for the mean free path for interaction of π -mesons in lead.

I. INTRODUCTION

E shall be concerned in this paper (Part II) with the study of the secondary particles produced in interactions observed in Experiment B (see Part I). In Sec. II, we shall discuss the production of the electronic component, stressing the likelihood that all of the electronic showers originate as photons. In view of recent evidence^{1,2} on the existence of the neutral π meson, it will be of interest to investigate this hypothesis in relation to the evidence obtained in this experiment.

In Sec. III, we shall show that the secondary penepenetrating particles produce nuclear interactions in lead and aluminum with cross sections near the geometric values. It will be seen that the bias introduced by the counter selection system is important even in the case of the simple selection system used in this experiment, and therefore that the difficulty of computing corrections for this effect may account for the fact that our results are at variance with those obtained in similar cloud-chamber experiments.³⁻⁵

We present in Figs. 1-4 some examples of nuclear interactions which are thought to be of unusual interest.

II. SOME GENERAL PROPERTIES OF SECONDARY PARTICLES

Let us first note some general properties of the secondary particles produced in the nuclear interactions of Experiment B. We are concerned here only with the penetrating particles (particles of minimum ionization traversing two lead plates without multiplication) and the electronic showers (of two or more electrons). The discussion in this paragraph and in Sec. III will be limited to a group of 82 nuclear interactions resulting in the production of more than two penetrating particles. The numbers of penetrating particles and showers observed in these cases are given in Table I. The average multiplicity of the penetrating particles is seen to be 4.5. The angle of emission of a penetrating particle is defined as the angle of its track with the average direction of the group. The average value of these angles was found to be 16°. The electronic showers are grouped

TABLE I. Production of penetrating particles and electronic showers in nuclear interactions of types 3, 3', 4, 4', and 5.

Number of inter- actions	Pene-	Average	Electron	of electrons)		
	trating particles	angle of production	>10	5 to 10	3 to 5	no penetra- tion <3
82	355	16°	22	58	43	25

^{*} This work was supported in part by the joint program of the ONR and AEC.

NK and ALC.
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FIG. 2. A sample of nuclear interactions (Experiment A).