

parallel to a field of about 100 gauss, provided by a small permanent magnet. A 2  $\mu$ fd condenser, initially charged to 8 kv, was discharged through the coil, with 500 ohms in series, in such a sense that the field in the coil reversed to about -100 gauss, with a time constant of about 0.2  $\mu$ sec and decayed back to the original field with a time constant of 1 msec. The crystal was quickly returned, through the earth's field, to the strong magnet and the  $\text{Li}^7$  resonance sampled. The operation could be done in 2 to 3 sec. A reversed deflection was found and it decayed, through zero, to the equilibrium state with the characteristic 5-min time constant. A typical record is shown in Fig. 1.

The state of spin system just after this treatment is thought to be properly described by a negative spin temperature. The system loses internal energy as it gains entropy, and the reversed deflection corresponds to induced radiation. Statistically, the most probable distribution of systems over a *finite* number of equally spaced energy levels, holding the total energy constant, is the Boltzmann distribution with either positive or negative temperature determined by whether the average energy per system is smaller or larger, respectively, than the mid-energy of the available levels. The sudden reversal of the magnetic field produces the latter situation.

One needs yet to be convinced that a single temperature adequately describes the nuclear spin state. Bearing on this is the fact that the crystal passes through the earth's field after the inverted population is produced, on its way back to the main magnet. The retention of the reversed magnetization requires that the spin-only-state, in the earth's field, have an inverted population and be described by a suitably small ( $\sim -1^\circ\text{K}$ ) negative temperature. Thus a very short time is required for the attainment of thermal equilibrium within the spin system itself (not the ordinary  $T_2$ , however).

A system in a negative temperature state is not cold, but very hot, giving up energy to any system at positive temperature put into contact with it. It decays to a normal state through infinite temperature.

This and related experiments indicate that the spin system is able to follow changes in even a small field adiabatically unless they occur in a time presumed to be less than about 20  $\mu$ sec.

<sup>1</sup> R. V. Pound, Phys. Rev. **81**, 156 (1951).

<sup>2</sup> N. F. Ramsey and R. V. Pound, Phys. Rev. **81**, 278 (1951).

### Erratum: Experiments on the Effect of Atomic Electrons on the Decay Constant of $\text{Be}^7$ . II

[Phys. Rev. **76**, 897 (1949)]

R. F. LEININGER, E. SEGRÈ, AND C. WIEGAND  
Radiation Laboratory, Department of Physics, University of California,  
Berkeley, California

IN Fig. 1 we have erroneously plotted  $2\delta e^{\lambda t}$  instead of  $\delta e^{\lambda t}$  as indicated on the ordinate scale on the left. The final result is in error by a factor 2 and should read:

$$\lambda(\text{BeO}) - \lambda(\text{BeF}_2) = (0.69 \pm 0.03) 10^{-3} \lambda(\text{BeO})$$

$$\lambda(\text{Be}) - \lambda(\text{BeF}_2) = (0.84 \pm 0.10) 10^{-3} \lambda(\text{Be}).$$

### On the Nuclear Magnetic Moment of $\text{Na}^{23}$

R. A. LOGAN AND P. KUSCH  
Columbia University,\* New York, New York  
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A DISCREPANCY occurs between the nuclear  $g$  values of  $^1\text{Ga}$  and  $^2\text{In}$  as determined from measurements on the hfs spectrum of these atoms in the ground state ( $^2P_{1/2}$ ) and as determined by the nuclear resonance method where the nuclei occur in molecules. Foley<sup>3</sup> has discussed the effect of the partial decoupling by the applied magnetic field of the  $L$  and  $S$  vectors in the  $^2P_{1/2}$  state on the nuclear  $g$ -value obtained from observational data under the assumption that decoupling does not occur. He concludes that the diagonal magnetic interaction term  $m_I g_I \mu_0 H$  which was assumed in finding  $g_I$  from the experimental data is to

be modified by a small perturbation term which is, itself, proportional to the applied magnetic field. For the cases of gallium and indium the apparent  $g$ -value determined from the hfs of atoms is thus greater than the  $g$ -value obtained in the nuclear resonance experiments. Foley indicates a satisfactory agreement between the observed and calculated values of the discrepancy, especially in view of uncertainties in the theoretical calculations and a rather large experimental error.

It is of interest to determine whether or not a similar discrepancy appears for the case of a nucleus which occurs in an atom in the  $^2S_{1/2}$  state, where the effect considered by Foley cannot appear. A previous measurement<sup>4</sup> has indicated that the apparent nuclear  $g$ -value of Cs is, indeed, the same within a rather large experimental uncertainty when measured in a molecule and when measured in an atom in the  $^2S_{1/2}$  state. A precision measurement of the  $g$ -value of sodium is reported here.

Essentially use is made of the fact that certain lines ( $F, m$ )  $\leftrightarrow$  ( $F, m-1$ ) consist of doublets, one component of which arises in the state  $F=I+\frac{1}{2}$  and the other one of which arises in the state  $F=I-\frac{1}{2}$ . The frequency separation of the doublet is  $2g_I \mu_0 H/h$  and the mean frequency of the doublet permits determination of the quantity  $x = (g_J - g_I) \mu_0 H/h \Delta\nu$ , if  $\Delta\nu$  is itself known, and hence of  $g_I/g_J$ . The  $\Delta\nu$  of  $\text{Na}^{23}$  was found to be  $1771.631 \pm 0.002 \times 10^6 \text{ sec}^{-1}$  by a method previously described<sup>4</sup> which depends on the existence of a maximum in the frequencies of certain lines in the hfs spectrum. The doublet ( $F, 1$ )  $\leftrightarrow$  ( $F, 0$ ) was observed at a field of about 6800 gauss where the mean frequency of the doublet is still sufficiently field dependent to permit an accurate determination of  $x$  and the doublet separation becomes large enough ( $\sim 16 \times 10^6 \text{ sec}^{-1}$ ) to permit accurate measurement in the face of a large over-all frequency ( $\sim 430 \times 10^6 \text{ sec}^{-1}$ ). We find then that

$$g_I(\text{Na}, ^2S_{1/2})/g_I(\text{Na}, ^2S_{1/2}) = -2488.39 \pm 0.15.$$

Since<sup>5</sup>  $g_I(H)/g_I(\text{Na}, ^2S_{1/2}) = -15.1927 \times 10^{-4} \pm 0.005$  percent, we find  $g_I(\text{Na}, ^2S_{1/2})/g_I(H) = 0.26451 \pm 0.008$  percent. This is to be compared with Bitter's<sup>6</sup> result  $g_I(\text{Na, mole})/g_I(H) = 0.26450 \pm 0.01$  percent. The excellent agreement indicates that the apparent nuclear  $g$ -value measured in an atom in the  $^2S_{1/2}$  state is, in fact, equal to the true nuclear  $g$ -value within the diamagnetic correction. Since no effect is here observed, it appears that the effect discussed by Foley accounts for the entire discrepancy observed for atoms in the  $^2P_{1/2}$  state.

Determinations of the spin  $g$ -value of the electron reported heretofore depend on a measurement of the ratio of the electronic  $g_J$  of atoms in different electronic configurations. A combination of our present result with that of Bitter and with the result of Gardner and Purcell<sup>7</sup> for  $2g_L/g_I(H)$  yields  $g_s/g_L = 2(1.00107 \pm 0.00012)$  under the assumption that  $g_J(\text{Na}, ^2S_{1/2}) = g_s$  and that no differential diamagnetic correction is to be applied to the nuclear moment of sodium in an atom and in a molecular configuration. It is of interest that this result does not depend on any assumption as to the  $g_J$ -values of  $P$ -states. The result agrees with other data on the spin moment of the electron. While it could be improved, a very accurate determination is precluded by the nature of the assumptions.

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<sup>1</sup> P. Kusch, Phys. Rev. **78**, 615 (1950).

<sup>2</sup> Private communication from W. G. Proctor.

<sup>3</sup> H. M. Foley, Phys. Rev. **80**, 288 (1950).

<sup>4</sup> P. Kusch and H. Taub, Phys. Rev. **75**, 1477 (1949).

<sup>5</sup> H. Taub and P. Kusch, Phys. Rev. **75**, 1481 (1949).

<sup>6</sup> F. Bitter, Phys. Rev. **75**, 1326 (1949).

<sup>7</sup> J. H. Gardner and E. M. Purcell, Phys. Rev. **76**, 1262 (1949).

### Numerical Evaluation of the Fermi Beta-Distribution Function

D. G. E. MARTIN  
George Holt Physics Laboratories, University of Liverpool, Liverpool, England  
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ATTENTION has recently been drawn by Feister<sup>1</sup> to methods of calculating the Fermi  $\beta$ -distribution function,

$$f(z, \eta) = \eta^{z+2s} e^{\pi y} |\Gamma(1+s+iy)|^2.$$