

FIG. 1. Energy levels as a function of (r_1/r_0) .

to give the closest fit to the square-well function, and as these can be matched quite closely, r_1 can be determined.

The $(d_{5/2})^3$ configuration is expected between $A = 19$ and $A = 25$. The calculation gives: at $A = 19$, 5/2 lower for $r_0 < 3.5 \times 10^{-13}$ cm; at $A = 25$, 4/1 lower for $r_0 < 3.8 \times 10^{-13}$ cm. The $(f_{7/2})^3$ configuration is expected between $A = 43$ and $A = 55$. The limits are: At $A = 43$, 7/2 lowest for $r_0 < 3.75 \times 10^{-13}$ cm, 5/2 lowest in the interval 3.75×10^{-13} cm $< r_0 < 4.0 \times 10^{-13}$ cm, 3/2 lowest for $r_0 > 4.0 \times 10^{-13}$ cm. At $A = 55$, 7/2 lowest for $r_0 < 4.1 \times 10^{-13}$ cm, 5/2 lowest in the interval 4.1×10^{-13} cm $< r_0 < 4.35 \times 10^{-13}$ cm, 3/2 lowest for $r_0 > 4.35 \times 10^{-13}$ cm. The usually accepted value for r_0 is about 2.8×10^{-13} cm, so the estimated cross-over points lie close to the region of physical interest, especially for the light elements.

Experimentally one finds a spin of $\frac{3}{2}$ for Na^{23} , and the β -decay scheme for Ne^{23} can be understood with an excited state of 5/2 for Na^{23} . In the β -decay of O^{19} one would like to assume a spin of $\frac{3}{2}$ for its ground state.⁴ Also the β -decay of Na^{25} to Mg^{25} (experimental spin of 5/2) shows a smaller ft value for decay to the excited state than to the ground state. These three cases all involve $(d_{5/2})^3$ configurations, which could give a spin of $\frac{3}{2}$ if the cross-over actually lies somewhat lower, and thus account for the experimental results.

In the $(f_{7/2})^3$ case, the experimental spin of V^{51} is 7/2, thus indicating that elements in this part of the periodic table are on the other side of the cross-over region. For heavier nuclei in higher shells, the δ -function approximation is approached, and it seems reasonably certain to conclude that the (jj) model will give the spin of the ground state as that of the odd nucleon. The only remaining exception to the (jj) rule for the spin of odd nuclei is Mn^{55} , which has an experimental spin of 5/2. Since this has a proton configuration of three holes in the $f_{7/2}$ shell, it might be explained by saying that in the $f_{7/2}$ shell elements are still quite close to the cross-over region, and the close-lying 5/2 and 7/2 levels can be inverted by some small perturbation.

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Os¹⁸² and Os¹⁸³, New Radioactive Osmium Isotopes*

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TWO new neutron-deficient radioactive isotopes of osmium metal in the Berkeley 184-in. cyclotron and the proton linear accelerator. The half-lives are 12.0 ± 0.5 hr. and 24.0 ± 1 hr. which have been assigned to Os¹⁸³ and Os¹⁸², respectively.

To obtain a pure osmium fraction, the bombarded rhenium metal was placed in a small distilling flask, osmium carrier added, then dissolved with nitric acid. Osmium tetraoxide was distilled in a stream of air and collected in 6*N* NaOH as sodium osmate. Both osmium and rhenium were precipitated as the sulfides by bubbling hydrogen sulfide through warm acidified solutions of each to which hydroxylamine hydrochloride had been previously added to reduce the nitric acid. Similar chemistry was employed to determine the osmium-rhenium parent-daughter relationships.

Bombardment of rhenium (Re¹⁸⁵, 37.07 percent; Re¹⁸⁷, 62.93 percent) with 25-Mev protons in the linear accelerator produced the known¹ 97-day Os¹⁸⁵ and a 12.0-hr. osmium activity which was shown to be the parent of the² 120-day Re¹⁸³. Magnetic counter and absorption data show that the 12.0-hr. Os¹⁸³ decays by electron capture, and emits conversion electrons of energies 0.15 Mev and 0.42 Mev, and gamma-rays of energies 0.34 Mev and 1.6 Mev. The relative abundances of these radiations, calculated from absorption data, are as follows: 0.15 Mev e^- : 0.42 Mev e^- : L x-rays: K x-rays: 0.34 Mev γ : 1.6 Mev γ = 0.18: 0.009: 0.53: 1: 0.18: 0.10.

With 40-Mev protons in the 184-in. cyclotron, an additional activity of 24-hr. half-life was formed which decayed to the² 12.7-hr. Re¹⁸². The 24-hr. Os¹⁸² decays by electron capture, no positrons having been detected. Analysis of the radiations was limited by the growth of Re¹⁸² and the decay of Os¹⁸³ in the Os¹⁸² samples.

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Sheath Formation in Ion-Neutralized Electron Beams

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BY "ion-neutralized electron beam" is meant an electron beam in which positive ions exist with a density equal to the beam electron density. Such beams may be formed when positive ions are produced, and trapped in the potential depression of a beam until the potential depression disappears by virtue of neutralization of electron space charge. The resulting medium is similar to a plasma except that the electrons are beam electrons and do not exist as an electron gas. The ions, however, do exist as a gas. This type of beam, and associated effects, are discussed in detail in a forthcoming paper by Linder and Hernqvist.¹

A necessary condition for the existence of such beams is that the surrounding walls be unipotential, or nearly so. Thus, when neutralization is complete, the space is field-free, and the beam potential equals the wall potential. However, if the collector electrode (anode) is varied from beam potential V_0 to potential V , a sheath forms. Within the sheath, ions are swept out, and the beam is unneutralized; outside the sheath, ion-neutralization persists.

A theory of such sheath formation yields for the sheath thickness x ,

$$x = \frac{1.5(10^{-8})V_0^{\frac{1}{2}}}{j^{\frac{1}{2}}} \left[\left(\frac{V}{V_0} \right)^{\frac{1}{2}} + 2 \right] \left[\left(\frac{V}{V_0} \right)^{\frac{1}{2}} - 1 \right]^{\frac{1}{2}},$$