

TABLE I. Ratio of the differential cross section for an extended nucleus to that for a point nucleus for 16.5-Mev electrons being scattered by Al and Au nuclei.

Z	$\theta = 30^\circ$			90°			150°		
	R_B	R_C	R_{exp}	R_B	R_C	R_{exp}	R_B	R_C	R_{exp}
Al 13	1.00	0.99	0.97	0.97	0.95	0.75	0.89	0.84	0.94
Au 79	0.99	0.97	0.88	0.45	0.30	0.45	0.29	0.19	0.38

between models (B) and (C). R_{exp} would therefore be expected to lie between R_B and R_C . It is seen that in view of the preliminary nature of the experimental results agreement is quite satisfactory.

A full account of this investigation will be published in the *Proceedings of the Physical Society*.

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¹ J. A. Wheeler, *Rev. Mod. Phys.* **21**, 133 (1949).

² W. A. McKinley, Jr. and H. Feshbach, *Phys. Rev.* **74**, 1759 (1948).

³ J. H. Bartlett and R. E. Watson, *Proc. Am. Acad. Arts Sci.* **74**, 53 (1940).

⁴ Lyman, Hanson, and Scott, *Phys. Rev.* **79**, 228 (1950).

Stopping Power of K-Electrons

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AN expression for the contribution B_K of the K-electrons to the stopping number has been given by Livingston and Bethe¹ in the form

$$B_K(\theta, \eta) = A(\theta) \ln \eta + B(\theta) - C_K(\theta, \eta), \quad (1)$$

$$[\eta = (mv^2/2Z_{eff}^2 Ry) \gg 1].$$

Here θ is the ratio of the observed ionization potential to the "ideal ionization potential" $Z_{eff}^2 Ry$, m is the electronic mass, and v is the velocity of the incident particle; $A(\theta)$, $B(\theta)$, and $C_K(\theta, \eta)$ can be computed directly by using the excitation and ionization probabilities of the K-shell.^{1,2} The coefficient of the $\log \eta$ term is described in reference 1 as "the total oscillator strength of all optical transitions from the K-shell into the continuous spectrum (and to the unoccupied discrete levels)," and the formula has been applied, with this interpretation of $A(\theta)$, to higher atomic shells.³ It is the purpose of this letter to show that this coefficient, $A(\theta)$, is actually $1+f$ where $2f$ is the above-mentioned total oscillator strength.

The Born approximation expression for the stopping number (per K-electron) is

$$B = \sum_n' \int_{q_{min}(n)}^{q_{max}} (dq/q) \varphi_n(q), \quad (2)$$

with $\varphi_n(q) = (E_n - E_1) |e^{i q x} 1_n|^2 / q^2$, E_n being the energy of the n th atomic state and q^2 being the square of the momentum loss of the incident particle divided by $2m$ (both E_n and q^2 measured in units of $Z_{eff}^2 Ry$). Energy-momentum considerations give $q_{max} = (4\eta)^{1/2}$ and $q_{min} = (E_n - E_1)(4\eta)^{-1/2}$; \sum_n' indicates the summation over all unoccupied states. Letting q_1 be a small value of q , independent of n and η , and $q_0 = q_{min}(n = \infty) = (4\eta)^{-1/2}$, we can write

$$B = \sum_{\substack{\text{all} \\ \text{states}}} \int_{q_0}^{q_{max}} \varphi_n(q) dq/q$$

$$- \sum_{\substack{\text{occupied} \\ \text{levels}}} \left[\int_{q_0}^{q_1} \varphi_n(0) dq/q + \int_{q_1}^{\infty} \varphi_n(q) dq/q \right]$$

$$- \sum_n' \int_{q_0}^{q_{min}(n)} \varphi_n(0) dq/q. \quad (3)$$

This expression is correct, except that in the second and last term $\varphi_n(q)$ has been replaced by $\varphi_n(0)$, neglecting higher terms in q^2 because q_0 , q_1 , and $q_{min}(n)$ are all small for large η . In the third

TABLE I. Calculated results for hydrogenic wave functions.

	λ	f	$\theta^2 f$
Hydrogen	1.1018	1	—
$\theta = 0.7$	0.9542	0.813	0.398
0.75	0.9392	0.722	0.406
0.8	0.9295	0.646	0.413
0.9	0.9207	0.525	0.425

term, the upper limit q_{max} has been replaced by ∞ because, for occupied states, $\varphi_n(q)$ decreases as q^{-14} with increasing q .

To evaluate the first term, we change the order of summation and integration and use the well-known rule² that $\sum \varphi_n(q) = 1$; then we obtain simply $\ln(q_{max}/q_0) = \ln 4\eta$. Since q_0 and q_1 are both independent of n , we obtain for the second term

$$-(1-f) \ln(q_1/q_0) = -\frac{1}{2}(1-f) \ln 4\eta - (1-f) \ln q_1$$

where $f = \sum' \varphi_n(0)$ is the total oscillator strength per electron for transitions going to unoccupied states. Since q_1 is independent of η and since the third integral converges at $q = \infty$, it yields a result independent of η . The last term gives

$$-\sum' \varphi_n(0) \ln(q_{min}/q_0) = -\sum' \varphi_n(0) \ln(E_n/E_1)$$

which is also independent of η . The η -dependent part of B arises therefore from the first and second terms alone and is:

$$\ln \eta - \frac{1}{2}(1-f) \ln \eta = \frac{1}{2}(1+f) \ln \eta. \quad (4)$$

It is not possible to calculate $B(\theta)$ by this general method, but if we write Eq. (1) in the form

$$B_K(\theta, \eta) = (1+f) \ln(2mv^2/\lambda Z_{eff}^2 Ry) - C_K(\theta, \eta), \quad (5)$$

a Born approximation calculation² using hydrogenic wave functions gives the results displayed in Table I. The first line of Table I refers to the complete hydrogen atom, the other lines to the K-shells of heavier atoms, θ increasing with Z . It is remarkable that λ is so very nearly constant; note that this makes the "effective ionization potential" close to $Z_{eff}^2 Ry$, not to the observed ionization potential. It may also be useful to note that f is very nearly inversely proportional to θ^2 (last column of Table I).

¹ M. S. Livingston and H. A. Bethe, *Rev. Mod. Phys.* **9**, 264 (1937).

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Decay of Au¹⁹⁹

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AN estimate¹ given for the capture cross section of Au¹⁹⁸ for slow neutrons was based on the intensity of a 159-keV transition from Au¹⁹⁹. A decay scheme for Au¹⁹⁹ devised by Beach, Peacock, and Wilkinson² was used and a value of 3.5×10^4 barns was obtained for the cross section.

The radiations from a Au¹⁹⁹ source³ separated from Pt¹⁹⁹ have since been studied and the complete identity of the spectra from Au¹⁹⁹ produced by both methods has been shown. Further analysis of the Au¹⁹⁹ electron conversion spectrum is given in Table I. Other lines present in the spectrum are due to the conversion of mercury K x-rays (~ 70 keV) and L x-rays (~ 10 keV). If a 230-keV γ -ray is present, as claimed by Beach *et al.*,² it can be estimated from the absence of its K conversion line that its intensity is less than 15 percent of the 158.5-keV transition.

The N_K/N_L ratio of 0.37 for the 158.5-keV transition suggests a 2³-pole electric transition, for which according to Hebb and Nelson the theoretical value is 0.4. However, the N_{L111}/N_{L1} ratio for electric 2³, according to Goodrich and Drell,⁴ is of the order of 20, whereas the experimental value is 0.55 ± 0.1 . Nor will a combination of 2² magnetic and 2³ electric transitions assist in bringing these values into closer accord with theory. A similar conflict for