

where $\bar{I} = \langle I(t) \rangle_M$ = average electron current, $\omega = 2\pi f$ = angular frequency of observation, $G(\omega)$ = a.c. conduction of gas discharge plasma, N = total number of electrons in the plasma.

The available noise power P_ω from a gas discharge plasma placed in the transverse plane of a rectangular wave guide propagating only in its lowest mode is

$$P_\omega = |I_E|^2 / 4G(\omega). \quad (6)$$

Here I_E = a.c. electron current in the direction of the E vector of the wave guide. Hence in this case,

$$P_\omega = \left\{ kT \epsilon + \frac{P_0}{NZ} \cos^2 \theta \left[2 + \frac{Z^2 - \omega^2}{Z^2 + \omega^2} \right] \right\} df, \quad (7)$$

where θ = angle between E vector and axis of gas tube, and P_0 = d.c. power dissipated in tube. For ordinary gas tubes that are used as microwave noise standards, the contribution of the frequency sensitive term is of the order of a few percent of the total noise power output. This calculation does not account for noise power due to other fluctuations.

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Nuclear Magnetic Resonance of Sb^{121} and Sb^{123} *

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WE have made attempts to find the nuclear resonance of Sb in Sb_2O_3 and $SbCl_3$ without success. On the supposition that this failure was due to a large interaction between the electric quadrupole moment of the Sb nucleus and the non-uniform electric field of the above molecules a search was made in an ion in which the electric field would be symmetrical. This requirement is fulfilled in the $SbCl_6^-$ ion in which the Cl atoms are believed to be arranged in a regular octahedral configuration about the Sb.

A search was made in a solution of $HSbCl_6$ in HCl guided roughly by the spectroscopic values of the magnetic moments as given by Crawford and Bateson¹ using a radiofrequency magnetic resonance spectrometer.² Distinct resonances were observed in the vicinity of 9800 kc and 5300 kc which from the spectroscopic information would presumably be associated with Sb^{121} and Sb^{123} respectively. Repeated series of readings were taken comparing the Sb^{121} resonance to that of Na in solid NaCl, and the Sb^{123} resonance to that of D in D_2O . The frequencies of resonance were measured by means of a U. S. Signal Corps frequency meter type EC 221-Q, calibrated at 100 kc intervals against harmonics generated by a General Radio crystal controlled oscillator operating at 100 kc and in turn standardized against Station WWV. The magnetic field was electronically controlled to a constancy of about one part in 50,000.

The average values of the ratios of the observed frequencies are:

$$[\nu(Sb^{121})/\nu(Na^{23})] = 0.90469 \pm 0.00004$$

and

$$[\nu(Sb^{123})/\nu(D^2)] = 0.8442 \pm 0.0001.$$

If we take Bitter's³ value of the observed ratio of $\nu Na/\nu H = 0.26450 \pm 0.01$ percent, and used a first-order atomic diamagnetic correction for Sb of 1.00517 as calculated from the Hartree-Fock functions⁴ and the value⁵ for H^2 of 1.000027, we get for the ratio $g(Sb^{121})/g(H^1) = 0.24052 \pm 0.00003$. Taking the spectroscopic value of 5/2 for the spin of Sb^{121} and the value for μ_H as measured by Taub and Kusch,⁶ we get

$$\mu(Sb^{121}) = 3.3595 \pm 0.0004.$$

One must note that this value of the magnetic moment may possibly be in error as a result of second-order molecular effects which we are unable to evaluate at this time.

Similarly, taking Bloch's⁷ value of

$$\mu(P)/\mu(D) = 3.257195 \pm 0.00002,$$

we get $[g(Sb^{123})/g(H)] = 0.13025 \pm 0.00002$, and taking the value 7/2 for the spin, we get for the magnetic moment

$$\mu = 2.5470 \pm 0.0003 \text{ nuclear magnetons.}$$

It is of interest to compare the ratio of the g -values of the two Sb isotopes as obtained spectroscopically by Crawford and Bateson,

$$[g(Sb^{121})/g(Sb^{123})] = 1.82 \pm 0.02 \text{ to our } 1.8466.$$

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Effect of Magnetic Fields on Conduction— "Tube Integrals"

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THE effect of a magnetic field H on electrical conduction can be reduced to integrals by using "tubes." Choose parallel to H an axis P_H in the $P = \hbar k$ space of the Brillouin zone. Then the region lying between planes P_H and $P_H + dP_H$ and energy surfaces $E(P) = E$ and $E + dE$ is a "tube." For spherical energy surfaces the tube is a torus with a parallelogram cross section. For more complex surfaces and for energies for which the surfaces reach the boundary of the Brillouin zone the tube may possibly take a helical path and eventually fill most of the space between E and $E + dE$. We shall discuss only simple closed tubes of interest for semiconductors.

For any tube α an angle variable θ and a tube mass m_α are defined by equations

$$m_\alpha \theta = \int_0^{P_i} dP_i / v_i, \quad 2\pi m_\alpha = \oint dP_i / v_i, \quad (1)$$

where P_i is the distance in the P -space along the tube from an arbitrarily selected fixed point and v_α is the scalar magnitude of the component perpendicular to H of the group velocity $\mathbf{v} = \nabla E(P)$. H produces incompressible flow along the tube α with

$$\begin{aligned} d\mathbf{P}/dt &= (-e/c)\mathbf{v} \times \mathbf{H}, & \dot{P}_i &= (-e/c)v_\alpha H \\ \dot{\theta} &= \dot{P}_i / v_\alpha m_\alpha = -eH / m_\alpha c = \omega_\alpha, \end{aligned} \quad (2)$$

so that $\dot{\theta}$ is constant and the period is given by the classical formula with a mass m_i .

If we assume that after one transition, due to thermal vibration for example, an electron will have average velocity zero, then the current produced by a given tube can be reduced to closed form as follows. When an electric field E is applied each element dV_P of volume in P -space becomes a source of electrons of strength

$$(-eV/kTh^3)f(1-f)\mathbf{E} \cdot \mathbf{v} dV_P, \quad (3)$$

where V is the volume of the crystal, f the Fermi-Dirac distribution function and e , k , T , h are as usual. If $v(\varphi) = 1/\tau(\varphi)$ is the probability of being scattered per unit time at tube position φ , the total current density $d\mathbf{I}_\alpha (= (-e/V)\epsilon v(\varphi))$ due to electrons brought into tube α by E is

$$\begin{aligned} d\mathbf{I}_\alpha &= (e^2/kTh^3)f(1-f)dEdP_H(m_\alpha/\omega_\alpha) \\ &\int_0^{2\pi} d\theta \int_0^\infty d\varphi \mathbf{E} \cdot \mathbf{v}(\theta)\mathbf{v}(\varphi) \exp\left[-\int_0^\varphi v(\varphi')d\varphi'/\omega_\alpha\right]. \end{aligned} \quad (4)$$