

The ratio $\sigma_{\text{He}}/\sigma_{\text{H}}$ has been normalized in Fig. 1 to 8.6 at its maximum value; this is the previously observed^{1,2} ratio of the absolute cross sections at that point. At the time of this experiment it was not possible to obtain neutrons of higher energy from carbon because of generator voltage limitations, but it is hoped that these measurements may be extended in the near future. Below 0.6 Mev neutron energy, the yield is quite small, so that ionization currents in the electroscope were of the order of the natural background. Furthermore, small effects from $d-d$ neutrons, arising from deuteron contamination of the target, would become correspondingly quite large at these low energies, and hence points below 0.6 Mev were not thought to be reliable. However, Carroll and Dunning⁴ have shown that $\sigma_{\text{He}}/\sigma_{\text{H}}$ for thermal neutrons is only 0.05.

The curve rises smoothly to a maximum at about 1.1 Mev; if it is continued symmetrically beyond this maximum, the resonance shows a half-width of nearly 0.6 Mev. This is in agreement with cloud-chamber work which has been done here.²

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¹ H. Staub and W. E. Stephens, Phys. Rev. **55**, 131 (1939).

² E. Hudspeth and H. Dunlap, Phys. Rev. **57**, 971 (1940).

³ W. E. Bennett and T. W. Bonner, Phys. Rev. **57**, 1086A (1940).

⁴ H. Carroll and J. R. Dunning, Phys. Rev. **54**, 541 (1938).

Dispersion of Supersonic Waves in Cylindrical Rods

In a recent issue of this journal a paper¹ appeared on the dispersion of supersonic waves in cylindrical rods. A number of experimental results were reported and compared with the theory of Giebe and Blechschmidt.² It was shown that agreement was good out to the region where the theoretical "dead zone" begins, but at higher frequencies the theory quoted was quite inadequate.

As certain work, which was reported by the writer some years ago, seems to have escaped attention, it seems worth while to recall here some of the results obtained at that time which are relevant to the recent paper by Shear and Focke and which amplify certain of the conclusions reached by these authors.

When a sound wave is propagated down a cylindrical tube filled with liquid, it has been shown³⁻⁵ that dispersion of the wave occurs at frequencies corresponding to those of the resonant radial vibrations of the column. In the neighborhood of these resonant frequencies the longitudinal wave is propagated only with difficulty and what might be called a "dead zone" exists.

That this "dead zone" also exists for tubes was shown later by Giebe and Blechschmidt,² who obtained satisfactory agreement between their experimental results and data calculated from the simple theory of coupled oscillations.

It was thought at one time⁶ that this same type of anomalous dispersion occurred for solid cylindrical rods. The curves upon which these views were based, however, were apparently inaccurate at the higher frequencies and

it seems probable that certain resonances were attributed to longitudinal vibrations which actually belonged to other modes, e.g., torsional or flexural. Later experimental work by Röhrich⁷ and now confirmed by Shear and Focke¹ has shown that the "dead zone" does not exist for solid rods, and, in fact, it is not predicted by the theory which should correctly be applied to this particular case. This theory is that due originally to Pochhammer,⁸ summarized by Love,⁹ and discussed in detail a few years ago in several papers.^{10, 6}

In a concluding paper published in 1934¹¹ the writer considered longitudinal vibrations for the three cases mentioned above and offered a suggestion for the absence in the last case of the "dead zone" which was so striking a phenomenon in the first two cases. This suggestion was that for the solid rod shear forces were of very great importance and would prevent anomalous dispersion and hence the dead zone from occurring. A theoretical discussion showed this to be the case.

Thus it appears that the limitations of the theory discussed by Shear and Focke exist because this particular theory is applicable only to the special and limited case of a tube. If in each case the appropriate theory be considered, it has been shown that the experimental confirmation is quite gratifying.

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¹ Sidney K. Shear and Alfred B. Focke, Phys. Rev. **57**, 532 (1940).

² E. Giebe and E. Blechschmidt, Ann. d. Physik [5] **18**, 417 (1933).

³ G. S. Field, Can. J. Research **5**, 131 (1931).

⁴ R. W. Boyle, D. K. Froman and G. S. Field, Can. J. Research **6**, 102 (1932).

⁵ G. S. Field and R. W. Boyle, Can. J. Research **6**, 192 (1932).

⁶ G. S. Field, Can. J. Research **5**, 619 (1931).

⁷ K. Röhrich, Zeits. f. Physik **73**, 813 (1932).

⁸ L. Pochhammer, J. Math. (Crelle) **81** (1876).

⁹ A. E. H. Love, *Mathematical Theory of Elasticity* (Cambridge University Press, 1927).

¹⁰ R. Ruedy, Can. J. Research **5**, 149 (1931).

¹¹ G. S. Field, Can. J. Research **11**, 254 (1934).

On the Dynamics of Complex Fission

In a letter of the same title¹ we pointed out that our coefficients of the higher order terms in the potential energy of distortion of a liquid drop, the radius of which is described by the expression $r=R(1+a_0P_0+a_2P_2+a_4P_4)$, do not check those given by Bohr and Wheeler.² Dr. Wheeler has explained that the discrepancy arises from the fact that the coefficients α_2 and α_4 as used in their Eq. (22) are not as defined in their paper and that (22) is obtained by using another definition based on spheroidal harmonics.³ Our definition gives a_4 positive at the a_2-a_4 saddle point for the range of x from zero to one. The interpretation of this fact as given in Section two of our letter is partially incorrect. The equatorial bulge which a positive a_4 would introduce is so small that it does not compensate for the equatorial constriction automatically brought in by the second harmonic, as was pointed out to us by Dr. Wheeler. For values of x sufficiently far from unity the drop in its critical shape develops a concavity about the equatorial belt. We cannot conclude that the positive value for a_4 is

in itself an indication of ternary or asymmetric binary fission. The possibility of ternary fission has not been sufficiently investigated.

We should state again that the coupling terms between odd and even harmonics provide an explanation of the marked asymmetry of fission. In the calculations so far there has been found evidence for two modes of fission. One is by way of a saddle point for which the drop when in the critical shape has a symmetrical form ($a_3=0$). The other is by way of a twofold saddle point for which the critical shape is not symmetrical ($a_3 \neq 0$). Which mode requires the less activation energy cannot be decided at the present stage of the calculations. The odd-even coupling terms will have an effect in determining the final products of either mode. It must be emphasized that higher order terms, which are being introduced, may materially affect the entire situation.

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¹ R. D. Present and J. K. Knipp, Phys. Rev. **57**, 751 (1940).

² N. Bohr and J. A. Wheeler, Phys. Rev. **56**, 426 (1939).

³ Except for a misprint in (22) which when corrected removes the inconsistency with (23).

Neutron-Induced Radioactivity of Tungsten

On bombarding tungsten with slow neutrons, Fermi and his co-workers¹ found an activity decaying with a period of about 1 day, and McLennan and others² and Jaeckel³ obtained, as its half-life, 23 hours and 24.5 ± 1 hours, respectively. They ascribed this activity to the reaction $W^n(n, \gamma)W^{n+1}$, but the isotope concerned was not determined.

To see if there are some other periods, pure metallic tungsten powder (99.97 percent purity) was irradiated for about 100 hours (intermittently) with neutrons produced in the Tokyo cyclotron according to the following conditions:

Target	Sample
fast neutrons: Li+D, enclosed in Cd+B box, immediately behind a Li-target.	
slow neutrons: Li+D, enclosed in a paraffin block, about 30 cm apart from the target.	
Be+D, enclosed in a paraffin block.	

A Lauritsen type electroscope was used to observe the activity. In all of these samples, besides the well-known 24-hour tungsten period (in our case 24.0 ± 0.1 hours), a long-lived activity of half-life 77 ± 3 days was found.

Chemical separation showed that the carrier of this long-lived activity is also tungsten and is neither Ta nor Hf. With a thin-walled G-M counter and magnetic field, it was found that both carriers emit negative electrons.

From the relative intensities of both periods in the above three cases, it was found that the shorter period is produced practically only with slow neutrons and the longer one both with fast and slow neutrons. The above results lead to the conclusion that 24-hour activity is due to W^{187} and 77-day activity to W^{185} .

By using the Al absorption method and the range-energy relation,⁴ the upper limits of energy of the β -rays were measured and were found to be 1.1 ± 0.1 Mev (24 hours), and about 0.4–0.5 Mev (77 days), respectively. Both periods were accompanied by a considerable amount of γ -rays. A more detailed report will be published shortly in the *Scientific Papers of the Institute of Physical and Chemical Research*.

In conclusion the writer wishes to express his best thanks to Professor H. Nagaoka for his interest and kind encouragement throughout this work, and to Dr. Y. Nishina for his kind suggestions and discussions, and to Mr. T. Shirai for assistance in chemical separations of the samples.

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¹ E. Fermi *et al.*, Proc. Roy. Soc. **149**, 522 (1935).

² J. C. McLennan, L. G. Grimmett and J. Read, Nature **135**, 147 (1935).

³ R. Jaeckel, Zeits. f. Physik **104**, 762 (1937).

⁴ N. Feather, Proc. Camb. Phil. Soc. **34**, 599 (1938).