SPECTRAL RELATIONS BETWEEN CERTAIN ISO-ELECTRONIC SYSTEMS AND SEQUENCES, PART III; Ti I, V II, Cr III, Mn IV, AND Fe V

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ABSTRACT

Spectral relations between the iso-electronic systems, Ti I, V II, Cr III, Mn IV, and Fe V.—The removal of, one valence electron from neutral vanadium, two valence electrons from neutral chromium, three valence electrons from neutral manganese, and four valence electrons from neutral iron forms with neutral titanium the five isoelectronic systems Ti I, V II, Cr III, Mn IV, and Fe V.

The irregular doublet law.—The irregular doublet law, wherever applicable, proves to be a powerful method of attack in attempting to analyze the spectra arising from ionized atoms. In this report for the electron transition $3d^34p$ to $3d^34s$ about forty lines, and for the electron transition $3d^{3}4d$ to $3d^{3}4p$ about twelve lines, have been traced through the first three elements Ti I, V II and Cr III. In the first electron transition the multiplet ${}^5F' - {}^5G'$ has been traced as far as Fe V.

Term separations, The Lande interval rule, and Hund's rule.—The systematic increase in term separations is given for the ${}^5F'$ and ${}^5G'$ terms arising from the electron configurations $3d^3$ 4s and $3d^3$ 4p respectively. For these same terms the Landé interval rule is found to be in general agreement with observed separations. Hund's rule for relative term positions is followed for the terms thus far identified.

Energy levels and the Moseley law.—^A new type of energy level Moseley diagram for Ti I to Fe V is compared with a similar diagram for the three sequences starting respectively with Sc I, Ca I, and K I. These four diagrams together with a similar diagram for V I, V II, V III, V IV, and V V are found to be almost identical. The constancy in the values of $\Delta\lambda$ between the diagonal lines of certain multiplets is traced through the first five elements of each of the four iso-electronic sequences starting with Ti I, Ca I, Sc I and K I.

'HE neutral atoms of titanium, vanadium, chromium, manganese, and THE neutral atoms or triangular, valid in the contain four valence electrons, $3d^{3}4s^{2}$, five valence electrons, $3d^{3}4s^{2}$, $\frac{3}{4}d^{3} + \frac{3}{4}d^{3}$ and eight valence six valence electrons, $3d⁵4s$, seven valence electrons, $3d⁵4s²$, and eight valence electrons, $3d^{6}4s^{2}$, respectively. The removal of one of these electrons from vanadium, two from chromium, three from manganese, and four from iron, forms with neutral titanium the five iso-electronic systems Ti I, V II, C'r III, Mn IV, and Fe V.

Neutral titanium, Ti I. Identifications of singlet, triplet, and quintet terms and multiplets in the spectra of neutral titanium have been made by several investigators.¹ The most complete analysis, however, has been given by Russell' in which he has classified some 1400 lines involving about 364 energy levels.

Singly ionized vanadium, $V II$. The identification of a number of terms and multiplets in the first spark spectrum of vanadium, V II, has been

¹ Kiess and Kiess, Proc. of Wash. Acad. Sci. 13, 270 (1923); Jour. Opt. Soc. Amer. 8, 607 (1924). Gieseler and Grotrian, Zeits. f. Physik 25, 342 (1924).

² Russell, Astrophys. J. 66, 347-438 (1927).

made by Meggers.³ Most of these terms arise from the three lowest electron configurations in the singly ionized atom, $3d^4$, $3d^34s$, and $3d^34p$.

In a previous report on the sequence of iso-electronic systems Sc I to Mn V⁴ the quartet multiplet ${}^{4}F' - {}^{4}G'$ ($3d^{2}4s - 3d^{2}4p$), following very closely the irregular doublet law, was found to be displaced to higher frequencies by approximately $12,000 \text{ cm}^{-1}$ in going from one element to the next (Fig. ⁷⁴ in the previous report). It was also found that the quartet multiplet $^4G' - ^4H'$ (3d²4p – 3d²4d) was displaced to higher frequencies by approximately $20,000 \text{ cm}^{-1}$ in going from one element to the next. In the sequence of iso-electronic systems starting with Ti I the multiplet ${}^5F' - {}^5G' (3d^34s 3d^{3}4\rho$) in going from Ti I to V II has been displaced to higher frequencies by approximately 12,000 cm⁻¹. By analogy with the preceding sequence it was predicted that the multiplet ${}^5C' - {}^5H'(3d^34p - 3d^34d)$ in going from Ti I to V II would be displaced to higher frequencies by some $20,000$ cm⁻¹. This prediction is verified by the finding of the multiplet ${}^5G' - {}^5H'$ in the spark spectrum of vanadium, V II, approximately $20,000$ cm⁻¹ higher than the corresponding multiplet in Ti I. The wave-lengths, relative intensities, and frequencies of the lines thus identified are given in multiplet form in Table XVI. The term values given in the table have been computed from the lowest term in the spectrum ${}^5D_0(3d^4)$ taken as zero.³

TABLE XVI. Singly ionized vanadium, V II.
 $^{6}G' - ^{5}H'$ (3d³4p-3d³4d)

		$^{5}G_{6}$ ' 290 35483.3	$^{5}G_5{}'$ 247 35192.9	$^{5}G_{4}$ 201 34946.3	${}^5G_3{}'$ 153 34745.5	$^{5}G_2{}'$ 34592.5
$5H_7{}'$	73018.1	100n 2664.19 37534.8				
	182.	20n 2677.20	90n 2656.57			
$5H_6{}'$	72835.6	37352.5	37642.6			
	157.	2?n	20n	80n		
^{5}H s $^{\prime}$	72678.8	2688.39 37197.0	2667.66 37486.0	2650.24 37732.4		
	129.		2?n	20n	70n	
$5H_4{}'$	72549.7		2676.86 37357.2	2659.32 37603.5	2645.21 37804.2	
	102.			P	20n	60n
$5H_3'$	72446.1			37501.5	2652.36 37702.3	2641.74 37853.8

Doubly ionized chromium, Cr III. Applying the irregular doublet law to the spectra of Ti I and V II, Gibbs and White' were able to identify the quintet multiplet ${}^5F' - {}^5G'$ arising from the electron transition $3d^34p$ to

³ Meggers, Zeits. f. Physik 33, 509 (1925); 39, 114 (1926).

⁴ White, Phys. Rev. 33, 681 (1929). '

Gibbs and White, Proc. Nat. Acad. Sci. 13, 525 (1927).

 $3d³4s$ in doubly ionized chromium, Cr III. With the ${}^5G'_{2,3,4,5,6}(3d³4p)$ term separations thus known the ${}^5G' - {}^5H' (3d^34p - 3d^34d)$ multiplet (using again the irregular doublet law) was predicted and identified approximately $20,000$ cm⁻¹ higher than the corresponding multiplet in V II.

The triad of triplet terms ${}^{3}D'$, ${}^{3}F$, ${}^{3}G'(3d^{3}4p)$ are found to combine strongly with b^3F' of $3d^34s$ and with a ${}^3F'$ and ${}^3G'$ of $3d^4$. The latter electron configuration of b^3F' of $3d^34s$. ation gives the lowest terms in the spectrum, the ${}^5D_{0,1,2,3,4}$, terms of which have not yet been definitely identified. The relative term values for Cr III are given in Table XVII. Since the lowest terms, ${}^5D(3d^4)$ and intercom-

Config. Term (Limit)		Triplet Terms Value	Combi- nations	$(\nu)^{1/2}$	Config. (Limit)	Term	Quintet Terms Value	Combi- nations	$(\nu)^{1/2}$
3d ⁴ (3d ³) $(^{4}F')$	$a^3F_2{}'$ $a^3F_3{}'$ $a^3F_4{}'$ 3G_3 3G_4	19000 56 19056 75 19131 21250 148 21398 146	${}^3D', F$ ${}^{3}G'$ ${}^{3}F, {}^{3}G'$	472	$3d^34s$ $(3d^3)$ $(^{4}F')$	$5F_1'$ $5F_2'$ $5F_3'$ $5F_4'$ $5F_5'$	50000 136 50136 200 50336 263 50559 319 50918	${}^5G'$, 5F	438
3d ³ 4s $(3d^3)$ 4F' $3d^34p$ (3d ³) $(^{4}F')$	${}^{3}G_{5}$ $b^3F_2{}'$ $b^3F_3{}'$ $b^3F_4{}'$ D_1' $^{3}D_{2}$ $^{3}D_{3}$ ${}^3G_3{}'$ ${}^3G_4{}'$ ${}^{3}G_{5}{}'$	21544 57194 342 57536 430 57966 97621 228 97849 378 98227 100384 259 100643 323 100966	$^{3}D^{\prime}$, ^{3}F ${}^{3}G'$ a^3F' , b^3F' a^3F' , 3G b^3F'	469 429 379 375	$3d^34p$ $(3d^3)$ $(^{4}F')$	$5G_2'$ $5G_3'$ $5G_4'$ $5G_5'$ $5G_6'$ $5F_1$ $5F_{2}$ $5F_3$ $5F_4$ 5F ₅	94273 264 94537 347 94884 425 95309 504 95813 97281 147 97428 200 97628 239 97867 259 98126	5F' 5F'	383 380
	3F_2 ${}^{3}F_{3}$ 3F_4	101988 302 102290 354 102644	a^3F' , 3G b^3F'	373	$3d$ ³ $4d$ $(3d^3)$ $(^{4}F')$	$5H_3'$ $^{5}H_{4}$ $5H_5'$ ^{5}H 6' ^{5}H ₇ $^{\prime}$	152694 184 152878 229 153107 280 153387 323 153710	5G'	298

TABLE XVII. Term values of doubly ionized chromium, Cr III

binations between triplet and quintet terms have not been identified with certainty, absolute term values have not been given in the table. For convenience only the $a^3F'_2(3d^4)$ term has been taken to be 19,000 cm⁻¹, and the ${}^5F_1'$ (3d³4s) taken to be 50,000 cm⁻₁, above the ${}^5D_0(3d^4)$ term. The values of $(\nu)^{1/2}$ given in the fifth and tenth columns of this table are taken with respect to ${}^{4}F_{5}'(3d^{3})$ of the once more ionized atom, and were obtained from an extrapolation of a Moseley diagram. The wave-lengths, relative intensities, frequencies and designations of the lines thus far identified in this report on Cr III are given in Table XVIII.

Triply ionized manganese, Mn IV. Extrapolating by means of the irregular doublet law the quintet multiplet ${}^{5}F' - {}^{5}G' (3d^{3}4s - 3d^{3}4p)$ was pre-

λ (vac.)	Int.	$\boldsymbol{\nu}$	Desig- nation	Mult. No.	λ (vac.)	Int.	$\boldsymbol{\nu}$	Desig- nation	Mult. No.
2483.79	25	40261.0	$b^3F'_{4}-3D'_{3}$	$\mathbf{1}$	2104.05	20	47527.5	${}^5F'_{4} - {}^5F_{5}$	5
2480.53	22	40313.9	$b^3F_3' - ^3D_2'$	$\mathbf{1}$	2103.90	20	47530.8	$\frac{5F_3}{-5F_4}$	5
2473.56	20	40427.5	$b^3F_2' - ^3D_1'$	1	1735.89	25	57574.2	${}^{5}G_6' - {}^{5}H_6'$	6
2459.69	6	40655.5	$b^3F_2^{\prime}-{}^3D_2^{\prime}$	1	1730.16	20	57798.1	$^{5}G_{5}^{\prime}-^{5}H_{5}^{\prime}$	6
2457.54	7	40691.1	$b^3F_3' - ^3D_3'$	1	1727.19	100	57897.5 董	$^{5}G_{6}^{\prime}$ - $^{5}H_{7}^{\prime}$	6
2343.18	6	42677.1	$b^3F_4' - 3G_4'$	$\boldsymbol{2}$	1724.31	15	57994.2	$^{5}G_{4}^{\prime}-^{5}H_{4}^{\prime}$	6
2333.80	4	42848.5	$b^3F_3' - {}^3G_3'$	2	1721.82	90	58078.1	$^{5}G_{5}^{\prime}-^{5}H_{6}^{\prime}$	6
2325.60	80	42999.6	$b^3F_4' - {}^3G_5'$	$\sqrt{2}$	1719.51	15	58156.1	$^{5}G_3' - ^{5}H_3'$	6
2319.78	70	43107.5	$b^3F_3' - {}^3G_4'$	\overline{c}	1717.54	80	58222.8 $\bar{\alpha}$	$^{5}G_{4}^{\prime}-^{5}H_{5}^{\prime}$	6
2315.35	60	43190.0	$b^3F_2^{\prime}-{}^3G_3^{\prime}$	$\overline{\mathbf{c}}$	1714.08	70	58340.3	$^{5}G_3' - ^{5}H_4'$	6
2275.99	$\boldsymbol{2}$	43936.8	${}^5F_3' - {}^5G_2'$		1711.74	60	58420.1	$^{5}G_{2}' - ^{5}H_{3}'$	6
2275.93	2	43938.1	$5F_4' - 5G_3'$	$\frac{3}{3}$	1271.90	15	78622.5	$a^3F_2' - ^3D_1'$	7
2274.47	2	43966.3	$5F_5' - 5G_4'$	3	1269.19	20	78790.4	$a^3F_3' - 3D_2'$	7
2265.65	15	44137.4	${}^5F_2{}' - {}^5G_2{}'$	3	1268.23	tr	78850.0	$a^3F_2' - ^3D_2'$	7
2262.40	15	44200.8	$5F_4' - 5G_3'$	3	1266.06	tr	78985.1	${}^3G_4-{}^3G_4{}'$	8
2258.70	50	44273.2	${}^5F_1' - {}^5G_2'$	3	1264.27	25	79097.1	$a^3F_4' - ^3D_3'$	7
2258.11	15	44284.8	$5F_4' - 5G_4'$	3	1264.27		79097.1	${}^3G_5-{}^3G_4{}'$	8
2256.17	6	44322.9	$b^3F_4' - ^3F_3$	4	1263.65	20	79135.8	${}^{3}G_{3} - {}^{3}G_{3}$	8
2252.70	15	44391.2	$5F_5' - 5G_5'$	3	1263.11	5	79169.6	$a^3F_3' - ^3D_3'$	7
2252.18	60	44401.4	${}^5F_2' - {}^5G_3'$	3	1261.91	30	79244.9	${}^3G_4-{}^3G_4{}'$	8
2249.62	8	44451.9	$b^3F_3' - ^3F_2$	4	1259.52	8	79395.3	${}^3G_3-{}^3G_4{}'$	8
2244.83	70	44546.8	${}^5F_3' - {}^5G_4'$	3	1259.10	40	79421.8	${}^{3}G_{5}-{}^{3}G_{5}{}'$	8
2238.25	60	44677.6	$b^3F_4' - ^3F_4$	$\overline{4}$	1256.85	2	79564.0	${}^3G_4-{}^3G_5{}'$	$\bar{8}$
2236.62	80	44710.4	${}^5F_4' - {}^5G_5'$	3	1238.60	40	80736.3	${}^3G_3-{}^3F_2$	9
2234.45	50	44754.8	$b^3F_3' - ^3F_3$	$\boldsymbol{4}$	1236.23	50	80891.1	${}^3G_4-{}^3F_3$	9
2232.46	40	44793.6	$b^3F_2' - ^3F_2$	$\overline{\mathbf{4}}$	1233.99	tr	81037.9	${}^3G_3-{}^3F_3$	9
2227.40	100	44895.4	$5F_5' - 5G_6'$	3	1233.04	60	81100.3	${}^3G_5-{}^3F_4$	9
2217.53	2	45095.3	$b^3 F_2' - ^3F_2$	$\overline{4}$	1230.84	tr	81245.3	${}^3G_4-{}^3F_4$	9
2216.92	2	45107.6	$b^3F_3' - ^3F_4$	$\overline{4}$	1229.52	10	81332.5	$a^3F_3' - ^3G_3'$	10
2129.95	$\overline{2}$	46949.4	${}^5F_5' - {}^5F_4$	5	1228.67	15?	81388.8	$a^3F_2' - ^3G_3'$	10
2126.37	5	47028.6	${}^5F_4' - {}^5F_3$	$\overline{\mathbf{5}}$	1226.81	8	81512.2	$a^3F_4' - {}^3G_4'$	10
2123.50	5	47092.1	${}^5F_3' - {}^5F_2$	$\overline{5}$	1225.69	20	81586.7	$a^3F_3' - ^3G_4$	10
2121.09	10	47145.6	$5F_2' - 5F_1$	5	1221.97	20	81835.1	$a^3F_4' - ^3G_5'$	10
2118.27	60	47208.3	${}^5F_5' - {}^5F_5$	5	1205.79	$\overline{2}$	82933.2	$a^3F_3' - ^3F_2$	11
2115.60	50	47267.8	${}^5F_4' - {}^5F_4$	5	1204.97	30	82989.6	$a^3F_2' - ^3F_2$	11
2115.00	20	47281.3	${}^5F_1' - {}^5F_1$	5	1202.49	8	83160.7	$a^3F_4' - ^3F_3$	11
2114.50	60	47292.5	$5F_3' - 5F_3$	$\overline{5}$	1201.41	40	83235.5	$a^3F_3' - ^3F_3$	11
2114.50		47292.5	${}^5F_2' - {}^5F_2$	5	1200.61	2	83291.0	$a^3F_2' - ^3F_3$	11
2108.43	10	47428.7	${}^5F_1' - {}^5F_2$	5	1197.42	50	83512.8	$a^3F_4' - ^3F_4$	11
2105.61	15	47492.2	$5F_2' - 5F_3$	5	1196.33	2	83589.0	$a^3F_3' - ^3F_4$	11

TABLE XVIII. Doubly ionized chromium, Cr III

dicted and identified approximately $12,000$ cm⁻¹ higher than the corresponding multiplet in Cr III. The wave-lengths, relative intensities, and frequencies of the lines thus identified are given in multiplet form in Table XIX. The quintet multiplet ${}^5G' - {}^5H' (3d^34p - 3d^34d)$ for Mn IV, although the frequencies of the radiated lines are quite accurately predictable in the region

of 1200 A.U., has not been definitely identified owing to its low intensity even with long exposures.

Quadruply ionized iron, Fe V. Just as for Cr III and Mn IV the quintet multiplet ${}^{5}F' - {}^{5}G'(3d^{3}4s - 3d^{3}4p)$ was predicted and identified approximately 12,000 cm⁻¹ higher than in the preceding element. The wave-lengths, re-

lative intensities, and frequencies of the lines thus identified are given in multiplet form in Table XX.

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The irregular doublet law. The irregular doublet law, wherever applicable, proves to be the most powerful method of attack in attempting to analyze the spectra arising from ionized atoms. The irregular doublet law is applicable to those radiated lines arising from electron transitions involving no

Fig. 8. Irregular doublet law.

change in total quantum number. For sequences of iso-electronic systems involving only one valence electron (i.e. K I, Ca II, Sc III, etc.) an electron transition gives rise to only two or three radiated lines. In the sequence starting with Ti I, however, where four valence electrons are involved and electron transition may give rise to over a hundred radiated lines. In this

Atom	$3d^{3}4s - 3d^{3}4p$ $5F_5 - 5G_6 \Delta p$	$3d^34s - 3d^34p$ $3F_4 - 3G_5$ $\Delta \nu$	$3d^34p - 3d^34d$ ${}^5G_6 - {}^5G_7$ $\Delta \nu$	
Ti I	20068)	15973)	17224)	
V II	$\frac{12253}{2}$	544542	20311	
	32321	30515	37535.	
Cr III	$\frac{12574}{5}$	12484	$\frac{20362}{ }$	
	44895	42999	57897	
Mn IV	12504	-12688	$\frac{20403}{ }$	
	57399	*55687	*78300	
Fe V	12506 69905	(68567) (12880)	(98734) ²⁰⁴³⁴)	

TABLE XXI. Irregular doublet law.

* Not definitely identified.

report on the latter sequence of iso-electronic systems only a few of the strongest lines have been traced through five elements. For the electron transition $3d^34p$ to $3d^34s$ about forty lines, and for the electron transition $3d^{3}4d$ to $3d^{3}4p$ about twelve lines, have been traced through the first three elements, Ti I, V II, and Cr III. Examples of the almost linear progression in frequency of these radiated lines may be seen in Table XXI where the lines ${}^5F_5' - {}^5G_6'$ and ${}^3F_4' - {}^3G_6'$ are chosen to represent the electron transition $3d^{3}4p$ to $3d^{3}4s$ and the line ${}^{5}G_{6}'-{}^{5}H_{7}'$ chosen to represent the electron transition $3d^34d$ to $3d^34p$. This almost linear progression is best brought out graphically as in Fig. 8. Each frequency scale, although the same for each element and corresponding multiplet, has been displaced to the left of the one just preceding it by $12,000 \text{ cm}^{-1}$ and $20,000 \text{ cm}^{-1}$ for the two electron transitions respectively.

Term separations, the Lande interval rule, and IIund's rule. The systematic increase in term separations in going from one element to the next for one set of terms from each of the two electron configurations $3d³4s$ and $3d^34p$ is shown in Table XXII. In the lower half of the table it is seen that the Landé interval rule for quintet terms is in general in agreement with the observed separations.

Atom	$5F_1'$	$5F_2'$	$3d^34s$ $5F_3'$	$5F_A'$ $5F_S'$	$5G_2'$	$5G_3'$	$3d^34p$ $^{5}G_{4}'$	${}^5G_6{}'$ $5G_5'$
Ti I	42	62	82	100	70	93	116	148
V II	82	122	159	$194 -$	153	201	246	290
Cr III	136	200	263	319	264	347	425	504
Mn IV	204	302	394	475	410	535	661	786
Fe V	284	427	573	669	585	775	971	1152
Theor.	2.0	3.0	4.0	5.0	3.0	4.0	5.0	6.0
Ti I	2.1	3.1	4.1	5.0	2.8	3.8	4.7	6.0
V II	2.1	3.1	4.1	5.0	3.2	4.2	5.1	6.0
Cr III	2.1	3.1	4.1	5.0	3.1	4.1	5.1	6.0
Mn IV	2.1	3.2	4.2	5.0	3.1	4.1	5.0	6.0
Fe V	2.1	3.2	4.3	5.0	3.0	4.0	5.0	6.0

TABLE XXII. Quintet term separations.

Hund's rule for relative term positions gives a satisfactory account of the terms thus far identified. A11 of the terms given in this report are built upon, and therefore have as a limit, the ${}^{4}F'(3d^3)$ terms of the once more ionized atoms.

Energy levels and the Moseley law. Combining the data now available for Ti I, and V II, and the data here given for Cr III, Mn IV, and Fe V, the same type of energy level Moseley diagram may be drawn for the triplet and quintet terms of these spectra as was drawn for the doublet and quartet terms of the sequence Sc I to Mn V, Fig. $5⁶$ for the singlet and triplet terms of the sequence Ca I to Cr V, Fig. 4' and for the doublet terms of the sequence K I to V V, Fig. 17. This type of diagram is shown in Fig. 9 for all four of the above mentioned sequences.

For each electron configuration shown in the diagram, including the limits, a point has been plotted for the term involving the largest R , L ,

⁶ White, Phys. Rev. 33, 672 (1929)

[~] White, Phys. Rev. 33, 538 (1929}.

and J value. Points for all the terms in each configuration would lie within the range covered by the circles. It has been convenient to draw a single line to represent each set of energy levels and a single arrow to represent all of the observed radiated frequencies resulting from jumps between two sets of energy levels. The electron configuration corresponding to each setof four heavy diagonal lines is given below each sequence in the order in which they appear for the last elements. It is apparent from the figure that there is a striking similarity between the separate diagrams for each sequence of iso-electronic systems. The parallelism existing between three of the four heavy diagonal lines for each diagram involve those energy levels between which the transition frequencies have been shown to follow very closely the irregular doublet law. The increased binding of the electron configuration

Fig. 9. Regularities between energy levels.

 $3dⁿ$ over the electron configurations $3dⁿ⁻¹4s$, $3dⁿ⁻¹4p$ and $3dⁿ⁻¹4d$ (where $n=1, 2, 3, 4$ for the first, second, third and fourth sequences respectively) appears to be almost identical for each sequence. In going from one sequence to the next (from left to right) the heavy diagonal line $3d^n$ gradually shifts down with respect to the other three parallel diagonals.

A careful examination of the plotted points for, V II in the fourth sequence of Fig. 9, V III in the third sequence, V IV in the second sequence and V V in the first sequence shows that smooth curves can be drawn through certain sets of energy levels. These points for the various stages of ionization of vanadium have been replotted as shown in Fig. 10. Figures similar to that of Fig. 10 have been drawn for Ti I to Ti IV and for Cr I to Cr VI. A comparison of all these diagrams with those of Fig. 9 shows them to be almost identical.

The multiplet structure of ${}^5F' - {}^5G'(3d^34s - 3d^34p)$. The characteristic wavelength separations and relative intensities of the diagonal lines in the

Fig. 10. A new energy level relation.

Fig. 11. Quintet multiplets.

 ${}^5F' - {}^5G'(3d^34s - 3d^34p)$ multiplet for Ti I to Fe V are almost identical. This multiplet is so easily recognized by sight that for Cr III, Mn IV and

Fe V the diagonal lines were identified on the spectrograms before any wavelength determinations were made. Owing to this striking similarity this multiplet, for each of the five elements Ti I, V II, Cr III, Mn IV, and Fe V, has been enlarged from the original plates to exactly the same scale of wavelengths and reproduced in Fig. 11. It is interesting to note in this figure the different types of spectra present. The first three spectra, the titanium arc spectrum, the vanadium spark spectrum and the chromium vacuum spark spectrum were taken on the same apparatus with the same dispersion and have been enlarged about six times. The last two, spectra of manganese and iron were taken with a vacuum spectrograph and are enlarged about 15 times. The wave-numbers for the strongest line (given at the right and below each multiplet) are the ones given in Column 2, Table XXI, which indicates the almost linear progression of frequency with atomic number, Fig. 8. The constancy of $\Delta\lambda$ between the diagonal lines indicated in Fig. 11 is a characteristic which also appears in the corresponding quartets, triplets, and doublets of the sequences mentioned above starting with Sc I, Ca I, and K I. This constancy in the value of $\Delta\lambda$ for all four sequences is shown in Table XXIII.

Atom		$3d^{3}4s - 3d^{3}4p$	${}^5F' - {}^5G'$		Atom		$3d^24s - 3d^24p$ $4F' - 4G'$			
Ti I VН Cr III Mn IV Fe V	9.3 9.2 9.2 9.5 9.9	8.4 8.4 8.2 8.2 8.3	7.7 7.6 7.4 7.3 7.3	7.0 6.7 6.5 6.4 6.4	Sc I Ti II V III Cr IV Mn V	15.0 11.8 11.4 11.8 12.4	13.3 11.6 11.1 11.2 11.4	11.6 11.0 10.6 10.8 11.3		
Atom			$3d4s - 3d4p$ $3D-3F$		Atom		$4s-4p$ $2S-2P$			
Ca I Sc II Ti III V IV CrV		23.5 16.9 11.8 12.4 12.0	3.12 12.0. 12.0 11.6 11.5		K I Ca II Sc III Ti IV V V		34.1 34.8 35.0 35.6 36.5			

TABLE XXIII. Wave-length separations of diagonal lines. $(\Delta \lambda \text{ in A.U.})$

The analysis of complex spectra as exemplified by Ti I (the lines of which are nearly all accessible with existing high dispersion apparatus) when extended to Cr III, Mn IV, etc. must rely upon spectrograms taken with relatively small vacuum spectrographs. In wor'king with these complex spectra of atoms in the higher states of ionization one cannot help but feel the need for vacuum spectrograms taken with much higher dispersion and resolving power. Since in the vacuum region the frequencies of lines increase so rapidly in going toward shorter wave-lengths, and since analysis of spectra depends upon the frequency separations, apparatus capable of giving higher disper-

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sion and resolving power must be constructed before much progress can be made in identifying high frequency spectral lines.

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Fig. 11. Quintet multiplets.