THE ISOTOPE EFFECT IN BAND SPECTRA, IV: THE SPECTRUM OF SILICON NITRIDE

By Robert S. Mulliken¹

Abstract

Silicon nitride bands.--(1) A system of bands shaded toward the red, lying between 3800 and 5300A was obtained by Jevons in 1913 by the introduction of SiCl₄ vapor into active nitrogen. His measurements have been repeated and extended to all possible heads. It is important that no oxygen be present. From a sharp intense head each band decreases rapidly in intensity to zero at the null line, then increases to a maximum at about m = 13 in the negative branch, in which the lines get far enough apart to be resolved. With the aid of the quantum theory, Jevons' arrangement was revised, and correct initial (n') and final (n'') vibrational quantum numbers assigned. The null lines of the Si²⁸N bands correspond to the wave-number equation: $v^{\circ} = 24234.2 + 1016.30 n' - 17.77n'^{2}$ $+0.410n'^{4}-0.00487n'-1145.00n''+6.570n''^{2}$. Partial analysis of the band structure indicates that the lines of any band are given by the equation: $\nu = \nu^{\circ}$ $+B'+2B'm+Cm^2$ where B'=0.728-0.097n' and C=-0.0121-0.0097n'+0.0053n''; from this the internuclear distance for the vibrationless SiN molecule is 1.56×10^{-8} cm. Additional weak heads are present whose positions agree very closely with those calculated for the isotopes Si²⁹N and Si³⁰N, isotope 29 being slightly the stronger. This agreement definitely excludes SiO or any other compound than SiN as the emitter of the bands, confirming the chemical evidence. The agreement is also definite, but not conclusive, evidence against the existence of half-quantum numbers for SiN, a result opposite to that for BO. Plate I shows most of the Si²⁸N bands together with some isotope heads. The intensity distribution in each band corresponds to thermal equilibrium at about 80°C. In respect to the initial vibrational quantum number, the distribution is non-thermal and corresponds to a high effective temperature as in other cases such as BO and CN. The intensity distribution with respect to Δn is similar to that of the violet CN bands. The sequence $\Delta n = 0$ is by far the strongest, other sequences of diminishing intensity being observed as far as -3 and +3 or +4. (2) New system of bands, extensive but weak, probably also due to SiN, is described. They all have double heads ($\Delta \nu = 27$), are shaded toward the red and extend from the ultraviolet through the green. An equation for the heads is given. The intensity distribution is characterized by numerically large values of Δn and by the absence of the band $(0 \rightarrow 0)$ and some neighboring bands.

INTRODUCTION

I N 1913 Jevons described² an interesting band spectrum obtained by the introduction of silicon tetrachloride vapor into active nitrogen, and consisting in a system of bands, shaded toward the red, lying in

¹ National Research Fellow.

² W. Jevons, Roy. Soc. Proc. 89A, 187 (1913-14).

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the region between $\lambda 3800$ and about $\lambda 5300$. Jevons ascribed the bands to a nitride of silicon, this being supported by the fact that they were not obtained by the discharge through pure SiCl₄ and by the further fact that a nitrogen-containing product was deposited on the walls of the nitrogen afterglow tube during the emission of the bands. As Jevons pointed out, the action of active nitrogen on SiCl₄ is similar to its action on carbon compounds, the cyanogen bands being emitted in the latter case. Many of the bands, according to Jevons, show a minimum of intensity about 4A from the head, a similar phenomenon being observed in the cyanogen bands when produced in active nitrogen. Jevons arranged all the bands in rows and columns such that the successive intervals of frequency taken vertically and horizontally form arithmetical progressions (the intervals being substantially constant in a given row or column of frequency-intervals), and from these he determined the constants of a Deslandres equation.

In addition to the data on the heads of the silicon nitride bands, Jevons gives a list of silicon lines which are emitted at the same time. In the present work, one additional Si line was found, that at λ 4103.1, and possible indications of one or two others.

In the light of the quantum theory of band spectra, it is now evident that the intensity minimum observed by Jevons in many of the bands must represent the region of the null-line, or missing line, which is of much more importance from a theoretical standpoint than the usually much more obvious head. The unusual prominence of the null-line here must be ascribed to the low temperature of active nitrogen; this subject has been discussed by Birge in the analogous case of the cyanogen bands.³ The null-lines are plainly visible in two of the bands in Jevons' reproductions, and are particularly well brought out in photographs taken by the present writer (cf Plate I). The structure of the bands is of a simple type (probably like that of the violet cyanogen bands) which in the light of the quantum theory, shows that they are due to a diatomic emitter. That they are due to the compound SiN is probable from the chemical evidence (including that above cited and new evidence given below), and is definitely proved by the isotope effect (see below).

A re-examination of the silicon nitride spectrum was undertaken by the writer in 1923 with the object of studying the expected isotope effect. At this time Si was known from Aston's positive ray work⁴

⁸ R. T. Birge, Astrophys. J. 55, 273 (1922).

⁴ F. W. Aston, Isotopes, 2nd ed. p. 77 (1924).

to contain a small amount of an isotope 29 in addition to the dominant isotope 28; there was also doubtful evidence of an isotope 30 in small amounts, the doubt being occasioned by the possible presence of H compounds of the same mass-number. Jevons' data on the SiN bands evidently refer to Si²⁸N heads, and include no measurements which can be attributed to Si²⁹N or Si³⁰N heads. New photographs by the writer showed clearly, however, that each favorably located Si²⁸N head of sufficient intensity is accompanied by two approximately equally spaced weak satellites at the theoretically expected positions for Si²⁹N and Si³⁰N, isotope 29 appearing to be slightly more abundant than isotope 30. This was reported in a letter to Nature.⁵ The existence of isotope 30 was later confirmed by Aston by the positive ray method,⁶ it being found slightly less abundant than 29, in agreement with the results on the SiN bands.

In order to determine the theoretical positions of the isotope heads, vibrational quantum numbers were assigned to the bands measured by Jevons, making use of the latter's arrangement of the bands in rows and columns, and merely changing his empirical numbers m = 22, 21, ..., 12 and p = 55, 54, ..., 50, to n' = 0, 1, ..., 10 and n'' = 0, 1, ..., 5, n' being the vibrational quantum number of the initial electronic state of the molecule, n'' that of the final state. Measurements were also made on the null-lines, using Jevons' measurements on the heads as reference standards, and an equation for the null-lines in terms of n' and n'' was obtained.⁷ On this basis, the isotope effect showed good agreement with theory for the final state of the molecule but was abnormally large for the initial state, especially for large values of n'; this anomaly was associated with various other peculiarities for the initial state, in particular with an extraordinary low vibration frequency as compared with that of the final state.^{5,7} Complete new measurements of the heads and null-lines of the SiN bands were recently made, in order to be more certain as to the reality of the abnormal isotope effect, and in order if possible to find a means of avoiding it. With the new data, which differ considerably from those of Jevons in a few cases, the above arrangement of the bands in rows and columns now gives rather small, but definite and systematic, deviations from the constancy required by the combination principle for the frequency-intervals between neighboring rows, or neighboring

⁵ R. S. Mulliken, Nature, March 22, 1924.

^e F. W. Aston, Nature, Aug. 23, 1924.

⁷ Paper presented before Am. Phys. Soc.; abstract in Phys. Rev. 23, 554 (1924).

columns. By an arrangement of the bands differing radically from the old, it is found possible to satisfy completely the requirements of the combination principle and thus be sure that the new assignment of vibrational quantum numbers is correct. With this assignment, all the previous peculiarities and anomalies disappear and the isotope effect, in particular, is found to be in complete agreement with the theory. The former plausible but incorrect assignment is now seen to have been due to an unusual combination of misleading circumstances and relations. For the *heads*, it may be noted, the constancy of the frequency intervals is better with the old assignment; but this is of course of no theoretical importance.

EXPERIMENTAL PROCEDURE IN PRODUCTION AND MEASUREMENT OF BANDS

Production of bands; evidence on nature of emitter. The bands were obtained by the same general method as that of Jevons, using active nitrogen. In the latter part of the work, the same apparatus was used as in the work on the copper halide bands,⁸ except that the bulb containing the silicon chloride, instead of being heated as in the case of the copper salts, was separated from the afterglow tube by a stopcock to control the flow of SiCl₄ vapor, SiCl₄ being a very volatile liquid. The SiCl₄ used was some material, free from CCl₄ in particular, which had been especially purified in connection with atomic weight work and which was kindly made available by Professor G. P. Baxter.

As noted in a previous paper,⁹ the purple glow of the SiN bands is obtained in good intensity only when the nitrogen used is very free from oxygen, this behavior being in marked contrast to that of the BO bands and constituting strong evidence for the nitride origin of the present bands. Photographs were taken of an arc between silicon electrodes in an atmosphere of nitrogen in the hope of finding the SiN bands and getting additional evidence as to their nitride origin; but they were not present, perhaps because of a trace of oxygen impurity. The silicon arc in air gives oxide bands.¹⁰ Apparently at high tem-

⁸ R. S. Mulliken, Phys. Rev. 26, p. 1 (July, 1925); cf. Fig. 1 and p. 7-8.

⁹ R. S. Mulliken, Phys. Rev. 25, 259-94 (1925). See p. 277.

¹⁰ A. del Campo, An. Soc. Esp. de Fis. Quim. **13**, 98 (1913); A. del Campo and J. Estalella, ibid **20**, 586 (1922); C. Porlezza, Atti. accad. Lincei **31** (ii) 513 (1922), and Gazz. Chim. Ital. **53**, 215 (1923); W. Jevons, Roy. Soc. Proc. **106A**, 174 (1924). The bands, which are those of a diatomic emitter, are in all probability due to SiO, since the presence of oxygen is required (del Campo, Jevons). The heads can be represented by the equation (cf R. Mecke, Phys. Zeit. **26**, 239, 1925) $\nu = 42,643 + 844.5 \ n' - 5.8 \ n'^2 - 1236.0 \ n'' + 6.04 \ n''^2$.

peratures the affinity of silicon for oxygen exceeds that for nitrogen, while the fact that the carbon arc in air gives the CN bands indicates that the reverse is true for carbon.

New photographs and measurements. The photographs were obtained with the Hilger glass prism spectrograph used in previous work on BO and CuI, and all precautions were taken to secure the best possible definition. Greatly enlarged reproductions from one of the photographs are shown in Plate I. For the measurements, three photographs were used with a copper arc and three others with an iron arc comparison spectrum. Detailed measurements were made on one of these, and enough measurements on the others to make sure that they all gave consistent results, showing the absence of appreciable displacements in the comparison spectra. As in the case of the BO bands,¹¹ the results differed appreciably from those of Jevons, being consistently lower by 2-3 wave-number units in the region from $\lambda 3950$ to $\lambda 4360$, but differing irregularly in the region of longer wave-lengths, being for the most part a few or even several units higher. For the weaker bands, these differences may be ascribed to inaccuracy in Jevons' measurements, in accordance with his statement that the accuracy is low for these bands. The consistently lower present results in the short-wave-length region of stronger bands are more difficult to explain. In the case of BO, it was suggested that such a difference might arise if in Jevons' measurements the setting was made on the extreme high-frequency edge of the head, while in those of the writer it was made at the point of maximum blackening, the heads being treated like lines. A comparison of the two methods of setting for a number of the SiN bands gave an average difference for the two methods of about 0.010 mm, the difference being surprisingly constant for bands of greatly varying intensity and structure. Since this difference corresponds to an average of only about 1.1 wave-units with the dispersion used, the suggested explanation is evidently inadequate to account for the discrepancy between the present results and those of Jevons. No further attempts have been made to determine the cause of the discrepancy, since a possible small constant error is obviously of minor importance in the theoretical interpretation of the data. The data on heads given in the following tables were all obtained by the method of setting on the point of maximum blackening for each head.

Measurements were made on the heads of all possible Si²⁸N bands. The ultraviolet was photographed with a quartz spectrograph, in order

¹¹ Mulliken, loc. cit⁹, p. 267-8.

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DESCRIPTION OF PLATE I.

Beginning with the top row, the reproductions show the entire SiN spectrum between $\lambda 3986$ and $\lambda 4800$. They were made in four sections from a single negative; each junction point is indicated by a dot *above*; in each successive section a somewhat more heavily exposed print was used than for its neighbor to the left in order to show both strong and weak heads to best advantage. Except for this (and an undue weakening of the bands at the high-frequency end due to prism absorption, and of the 7,9 band at the other end by decreasing plate sensitivity) the reproduction gives an essentially correct idea of the intensity distribution.

The *head* of each A band of Si²⁸N is marked with a line, and the vibrational quantum numbers (n', n'') are given. In the case of the more intense bands, the fall of intensity from the head to the null-line, and the rise to a maximum in the negative branch before the final fading out, are well shown. The weak Si²⁹N and Si³⁰N heads, which are at the left of the corresponding Si²⁸N heads, are marked when visible. The pairs of dots under the lowest section of the plate indicate the positions of the heads of some of the *new* bands; beginning at the left, the (1,5), (0,5), (1,6), and (2,7) head-pairs are marked; of these (1,5) is the most clearly visible. Unmarked conspicuous heads or lines (aside from structure lines of the bands) are of unknown origin (cf Table VI).



PLATE 1. The entire band spectrum of SiN from $\lambda 3986~(top)$ to $\lambda 4800~(bottom).$

to measure a few heads which were not transmitted by the glass prism. Some new bands of a different type were also found; other new bands were also found in the green (see later section).

The null-lines of as many SiN bands as possible were measured on the plates, the setting being made at the point of minimum intensity. In some bands where the head is at a considerable distance from the null-line, the latter appears as a distinct narrow gap in the shading; in others where it is nearer, as a mere lightening; these effects can be seen in the reproductions (Plate I). Settings on the null-lines are subject to rather greater uncertainty than in the case of heads, but it is thought that the data are nearly as accurate as for the latter. One cause of error is the asymmetry in the rate of increase of blackening on the two sides of the null-line. This should tend to displace the settings away from the heads, but study of the question indicates that the error so introduced is unimportant. In the case of bands where the null-lines were not directly measurable, their positions were calculated from those of the corresponding heads, the necessary correction being obtained from a study of the manner in which the distance from head to null-line varies with the vibrational quantum numbers in the directly measurable cases (see next section).

Measurements on the Si²⁹N and Si³⁰N heads, made wherever possible, are given in Table II. Measurements on null-lines were here impossible, since these are concealed by the shading of the much more intense Si²⁸N bands.

Results of Measurements on SiN Bands

Analysis of band structure. The bands consist of two branches, one starting in each direction from the null-line, the positive branch (starting toward higher frequencies) forming a head. The bands are not resolved near the null-line, nor anywhere in the positive branch; but in the negative branch, they become resolved at a moderate distance from the null-line, and can be followed for some distance (cf Plate I). It is reasonable to assume, in accord with their general appearance, that the bands are of the same type as the violet cyanogen bands, with a single missing line (the null-line) in the otherwise continuous series of lines expressible by the equation¹²

$$\boldsymbol{\nu} = \boldsymbol{\nu}^{\mathbf{o}} + B' \pm 2B'm + Cm^2. \tag{1}$$

In Eq. (1) the positive and negative signs refer to the positive and negative branches, respectively; m, denoting the rotational quantum

¹² Cf A. Sommerfeld, Atombau und Spektrallinien, 4th ed., pp. 718-34.

number of the final state, is assumed to have half-integral values; for the null-line, m = -1/2; ν° corresponds to the change of electronic plus vibrational energy.

Measurements were made on the resolved negative branch lines of the (3,2), (4,3), (5,4), and (4,4) bands, which are at the violet end of the spectrum, where resolution is most complete. By plotting first differences of successive lines, the coefficient C was determined for each of these bands; these values of C are given in Table I. Substitution of m = -1/2 in Eq. (1) gives for the null-line $\nu = \nu^{\circ} + \frac{1}{4}C$, which is equal within experimental error to ν° , the wave-number of the band-origin,¹³ since $\frac{1}{4}C$ is here negligible. For the head,¹² $\nu = \nu^{\circ} + B' - B'^2/C$. Letting H represent the distance from null-line to head, we then have,

$$H = B' - B'^2 / C. (2)$$

The *H* values are obtainable from the data of Table II, and it is now possible to obtain B' for each of the four bands; the results are given in Table I.¹⁴

TABLE I

Experimental values of B' and C.

[Note: The data in bold-face type were determined from measurements on structure lines; the remaining data were calculated from the H data of Table II (H=distance from null-line to head) assuming B' values calculated from Eq. (3). The data are all in wave-number units.]

n' n''	Β'	- C	n'	n''	B'	- C	n'	n''	- C
3 2 4 3 5 4 0 0 1 1 2 2	0.686 0.685 0.680	0.0303 0.0365 0.0403 0.0117 0.0161 0.0199	3 4 5 6 7 2 3	3 4 5 6 7 3 4	0. 704	$\begin{array}{c} 0.0245\\ \textbf{0.0305}\\ 0.0336\\ 0.0384\\ 0.0441\\ 0.0161\\ 0.0210\\ \end{array}$	4 5 6 3 4 5 6	5 6 7 5 6 7 8	$\begin{array}{c} 0.0255\\ 0.0288\\ 0.0323\\ 0.0152\\ 0.0198\\ 0.0244\\ 0.0264\end{array}$

Now B' should be expressible in the form $B' = (h/8\pi^2 J') - a'n' = B_0' - a'n'$, and C (=B'-B'') in the form $C = C_0 - a'n' + a''n''$. From the data on C for the four measured heads, preliminary values of a', a'', and C_0 can be obtained. From a' and the B' data for the four bands, a preliminary value of B_0' is then obtained, and from it and a' can be calculated the B' value for each value of n'. From these and the H

¹³ Cf R. S. Mulliken, Phys. Rev. 25, 119-138 (1925). For definition of "origin," see p. 123.

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¹⁴ B' could also be obtained by extrapolating the first difference curve (a straight line) in a suitable way to the null-line, but this method is incapable of accuracy. The values of B' and C given in Table I were, however, obtained by adjusting the curve in such a way as to give a correct extrapolation to the null-line and at the same time to agree with the measured values of H.

values obtainable from the data of Table II, a large number of C values (see Table I), corresponding to a variety of combinations of n' and n'', can be calculated; and from these, more accurate values of a', a'', and C_0 than before can be obtained. By repeating the calculation of B_0' with the new value of a', and so on, by successive approximations (one or two suffice), the following results are obtained:

 $B' = 0.728 - 0.0097 \ n'; C = -0.0121 - 0.0097 \ n' + 0.0053n''.$ (3) From Eq. (3) the values of B' and C, and so of H, can be calculated for any values of n' and n''. Values of H so obtained were used to reduce the data of Table II, in the cases where heads alone could be measured, to the corresponding values for null-lines. It should be noted that calculated values of H for this purpose could have been obtained in a purely empirical way from the measured values by studying the way in which the latter vary with n' and n''. The results would have been only slightly different, so that the subsequent analysis of the nullline data is practically independent of any possible doubts as to that of the band structure. The procedure actually used amounts to employing the theory as a means of determining the functional relation of H to n' and n'', and then using the measured values of H to determine the necessary constants so as to calculate unmeasured H values.

Dimensions of SiN molecule. From the above-determined values of B_0' and C_0 , can be calculated the moment of inertia and interatomic distance of the vibrationless SiN molecule in its initial and final electronic states. From B_0' one gets $J_0' = 3.78 \times 10^{-39}$ gm cm², and $r_0' = 1.567 \times 10^{-8}$ cm. From $B_0''(=B_0'-C_0)$ one gets $J_0'' = 3.72 \times 10^{-39}$ gm cm², and $r_0'' = 1.554 \times 10^{-8}$ cm. The values of r_0 are considerably greater, as would be expected, than for the CN molecule, where r_0 is 1.17×10^{-8} cm for what is probably the normal state.

Although the writer believes that the foregoing analysis is correct, it would obviously be desirable to study the bands under sufficient dispersion to give complete resolution in the region of the null-lines at least. Also, it may well be that the band lines, which appeared single with the dispersion used, actually consist of narrow doublets as in the violet CN bands.

Analysis of null-line data. In order to obtain an equation for the null-lines of the SiN bands, it is convenient to arrange the null-line data of Table II in a rectangular array like Table III, merely substituting them for the intensities of Table III. By an analysis of data

TABLE IIWave-number data on S1N bands1

Vil	br.	Si ²⁸ N	bands		Isotopic displacements ⁶
nu	m.				Si ²⁹ N heads Si ³⁰ N heads
n' :	n''	Head J-M ²	Null-line ³ O-	-C4	Rotl. ⁶ Calc. ⁶ Obs. ⁷ Rotl. ⁶ Calc. ⁶ Obs. ⁷
6 7 8 9	3 4 5 6	26402 26135 25863 25577	26393 26127 25856 25571	$-5 \\ -4 \\ 0^{-} \\ -4$	
2 3 4 5 6 7 8 9	0 1 2 3 4 5 6 7	26213 — 1 26007 25787 25554 3 25309.7 3 25054.7 3 24790.8 3 24518	26196 25993 25775 25543 25299.9 25045.9 24782.9 24511	$ \begin{array}{r} -3 \\ -2 \\ -1 \\ -1 \\ 0 \\ -1 \\ -5 \end{array} $	Si ²⁹ N and Si ³⁰ N heads concealed in this
1 2 3 4 5 6 7 8 9 10	0 1 2 3 4 5 6 7 8 9	25259.1 2 25080.3 2 24886.5 3 24678.4 3 24457.0 2 24223.9 3 23981.8 3 23731.4 4 23473 -7 23212 -7	25234.8 25060.5 24870.3 24664.8 24444.8 24213.0 23972.1 23722.7 23465 23205	$2 \\ 0 \\ 0 \\ -1 \\ -1 \\ -1 \\ -3 \\ -4$	region by shading of Steaty heads.
0 1 2 3 4 5 6 7 8	0 1 2 3 4 5 6 7 8	24280.6 3 24127.8 2 23960.4 2 23778.3 2 23581.7 2 23372.9 2 23152.9 2 22924.1 3 Masked by o head	24234 .5 24095 .0 23934 .5 23757 .7 23564 .6 23358 .5 23140 .6 22913 .6 r fused with	$ \begin{array}{c} 0 \\ -1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 3,4 \end{array} $	$ \begin{vmatrix} -0.5 & -0.5 & \dots & -1.0 & -1.0 & \dots \\ -0.4 & +0.5 & \dots & -0.7 & +1.0 & \dots \\ -0.2 & 1.7 & \dots & -0.5 & 3.2 & \dots \\ -0.2 & 3.0 & 3.1 & -0.4 & 5.7 & 5.5 \\ -0.2 & 4.4 & 4.5 & -0.3 & 8.4 & 8.8 \\ -0.1 & 6.0 & 5.4 & -0.2 & 11.2 & 11.2 \\ -0.1 & 7.6 & 6.9 & -0.1 & 14.3 & 15.1? \\ -0.1 & 9.2 & 10.0 & -0.1 & 17.3 & 18.7 \end{vmatrix} $

¹ For intensity data, see Table III. For the isotope heads, the intensities are all very low (0to 000(, as can be seen from Plate I.

 2 J-M = excess of Jevons' measured wave-number over the writer's. Blanks in this column represent bands not measured by Jevons.

³ The values in bold-face type were measured directly. The other values were calculated from the data on the heads with the help of Eqs. (2) and (3): see discussion in paragraph following Eq. (3).

 4 O-C = Observed minus calculated. The calculated values are from Eq. (4).

⁵ Isotopic displacement = wave-number of Si²⁹N or Si³⁰N head minus that of corresponding Si²⁸N head.

⁶ The calculated isotopic displacement for any head consists of two parts, a small (negative) *rotational* contribution (for method of calculation see second paragraph under "Confirmation of the isotope effect") and a larger *vibrational* contribution (see third paragraph under "Confirmation of isotope effect"). The "calc." (calculated) displacement is the sum of these two contributions, of which only the former is given explicitly in the table.

⁷ The deficiency of observed data in the low-frequency part of the spectrum is in all cases attributable to insufficient intensity of the isotope heads, or, when so stated in the table, to masking by structure lines from a preceding head.

TABLE I	I—c	on	tinu	ed
Wave-number	data	on	SiN	bands ¹

Vibr. num.	Si ²⁸ N bands	Isotopic displacements ⁴ Si ²⁹ N bands Si ³⁰ N heads
n' n''	Head $J - M^2 Null-line^3 O - C^4$	Rotl. ⁶ Calc. ⁶ Obs. ⁴ Rotl. ⁶ Calc. ⁶ Obs. ⁷
$\begin{array}{ccc} 0 & 1 \\ 1 & 2 \end{array}$	Not found Not found (although reported by Jevons)	
$\begin{array}{ccc} 2 & 3 \\ 3 & 4 \end{array}$	22856.6 22824.6 2 22684.5 -4 22660.6 2	Masked by structure lines, etc., but also apparently abnormally weak.
4 5 5 6 6 7 7 8 8 9	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
0 2 1 3 2 4 3 5 4 6 5 7 6 8 7 9 8 10 9 11	Not found Not found 21772.3 21723.3 -121605.6 -10 21572.8 021431.6 -2 21407.0 121246.3 -2 21226.8 021052.0 -5 21035.3 020848.8 -9 20834.7 120637.5 20625.4 120415 20404 -4	-0.2 16.0 15.2 -0.4 30.9 31.6 Present but masked by structure lines. -0.1 18.6 19.1? -0.2 35.7 37.2?
4 7 5 8 6 9 7 10 8 11 9 12	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
6 10	19006 18980 -1	

TABLE III

Intensity distribution in Si²⁸N bands. The intensities are estimated photographic intensities for a green-sensitive plate, and apply to each band as a whole, not to its head; for data on the heads, reference may be made to Jevons' paper.² The $\Delta n=0$ sequence is indicated by the use of bold-faced type.

->	0	1	2	3	4	5	6	7	8	9	10	11	12
)	5												
	Ō	4											•••
2	000	1	6	1	2								
3		0 –	2	10	3	3							• •
4			0	2	8	2	2	00					
5				0 +	2 +	5	3	1+	00				
6				000	0 +	2	2	2	0+	0	0+		
7					0 –	0	1	1	1	0	0+		
8						0-	0 –	1	3	0	0	0	
9							00	00	0	•		00	- 00
0										0			

on the intervals between adjacent rows and columns, the following equation is then obtained, capable of representing all the null-lines

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to within the amounts given in the "Obs.-Calc." column of Table II: $\nu = 24234.17 + 1016.30 \ n' - 17.773 \ n'^2 + 0.410 \ n'^3$ $-0.00487n'^4 - 1145.00n'' + 6.570n''^2.$ (4)

The comparatively large coefficients of the cubic and biquadratic terms in n' are unusual, but such terms are definitely needed to repsent the data. The relationship between the coefficients of the initial and final states is of a normal type. Since null-lines and origins¹³ are probably practically coincident for the SiN bands (cf. discussion preceding Eq. (2)), Eq. (4) should hold equally for both.

CONFIRMATION OF THE ISOTOPE EFFECT

For each observed Si²⁹N and Si³⁰N head, comparison is made in Table II of the observed isotopic displacement¹³ with that theoretically calculable. For a given band-head, the displacement should be the sum of a small rotational part corresponding to the distance from bandorigin to band-head, and a larger vibrational part corresponding to the distance from system-origin to band-origin.¹³ The rotational displacement must in every case be negative, since the distance H (head minus origin, cf Eq. (2)) is positive in the SiN bands, and is less for the two heavier isotopes than for the lightest isotope Si²⁸N with which the other two are compared. The vibrational displacement should also be negative on the high frequency side of the system-origin, with the result that in each band the Si²⁹N and Si³⁰N heads are superposed on the shading from the Si²⁸N head and so escape detection. On the low-frequency side of the system-origin, however, the vibrational displacement is positive, so that, as soon as the effect of the small negative rotational displacement is overcome, the isotope heads stand out clearly on the high-frequency side of the Si²⁸N head, where there is usually nothing to obscure them seriously. This can be seen in the reproductions (Plate I), where most of the heads of Table I are visible.

The rotational isotopic displacement for a given band can be determined by calculating H of Eq. (2) for Si²⁸N and subtracting the result from the corresponding value for Si²⁹N or Si³⁰N. For Si²⁸N, the values of B' and C used in calculating H are obtained from Eq. (3); for the other isotopes, the following equations (3') and (3'') must be used:

 $Si^{29}N : B' = 0.7196 - 0.00953 n';$

$$C = -0.01196 - 0.00953 \ n' + 0.00521 \ n'' \tag{3'}$$

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 $Si^{30}N : B' = 0.7118 - 0.00938 n';$

$$C = -0.01183 - 0.00938 \ n' + 0.00512 \ n'' \tag{3''}$$

The constant terms of (3') and (3'') are obtained¹³ by multiplying the corresponding terms of Eq. (3) by ρ^2 , and the coefficients of the n' and n'' terms by multiplying the coefficients of Eq. (3) by ρ^3 . In general $\rho^2 = (1/M_2 + 1/M')/(1/M_1 + 1/M')$. In the present case M' = 14 (the atomic weight of N), $M_1 = 28$, and M_2 is either 29 or 30. For Si²⁹N, the values of ρ , ρ^2 , ρ^3 , and ρ^4 are as follows: 0.994236, 0.988505, 0.982808, and 0.977142; for Si³⁰N, they are 0.988826, 0.977777, 0.966852, and 0.956026.

The vibrational isotopic displacement for any band can be obtained in a similar way, using Eq. (4) for the Si²⁸N band, and subtracting the result from that obtained by Eq. (4') or (4'') for Si²⁹N or Si³⁰N. Eqs. (4') and (4'') are obtained from (4) by multiplying each coefficient in the latter by a power of ρ equal to the power of n' or n''with which the coefficient is associated, the constant term being left unchanged since no electronic isotope effect is to be expected.¹³

 $Si^{29}N: \nu^{0} = 24,234.17 + 1010.44 \quad n' - 17.569 \quad n'^{2} + 0.403 \quad n'^{3} \\ -0.00476 \quad n'^{4} - 1138.40 \quad n'' + 6.494n''^{2} \\ Si^{30}N: \nu^{0} = 24,234.17 + 1004.96 \quad n' - 17.394 \quad n'^{2} + 0.396n'^{3} \end{cases}$ (4')

 $-0.00466 \ n^{\prime 4} - 1132.21 \ n^{\prime \prime} + 6.424 n^{\prime \prime 2} \qquad (4^{\prime \prime})$

Practically, of course, equations obtained by subtracting (4) from (4') or (4''), respectively, are convenient in the calculation of vibrational isotopic displacements.

Comparison of observed with calculated isotopic displacements in Table II shows complete agreement, within experimental error, throughout the range of n' and n'' values for which data could be obtained.¹⁵ This thoroughgoing agreement seems the more remarkable when it is noted that each calculated isotopic displacement is the sum of a number of terms involving a variety of powers of ρ .¹⁶ But such a detailed

¹⁶ The calculated values are considerably larger (especially for larger values of n, where the higher power terms in n have their greatest effect) than they would be if calculated according to the approximate relation¹³ (which would be exact if there were no higher power terms) $(\nu_2^n - \nu_1^n) = (\rho - 1)\nu_1^n$, ν_1^n being the vibrational part of the emitted frequency for Si²⁸N (equal to wave-number for given band-origin minus that for system-origin). For example, the correct calculated vibrational displacement for the (7,7) band of Si³⁰N is 17.40, whereas the value obtained by the above approximate relation is (22914 - 24235)(-0.011174) = +14.76.

¹⁵ The apparent slight increase of the observed displacements relative to the calculated, as n' is increased, may be real but is within experimental error; note especially that the largest discrepancies are in the cases of the (7,7), (7,8) and (6,8) heads, which were the three weakest heads that were measurable. Also, the calculated displacements may be slightly in error due to inaccuracy in the coefficients of Eq. (4).

agreement, if any at all, is to be expected, since the theory is of such a nature that its detailed predictions in regard to the various coefficients all stand or fall together.¹⁷

The agreement of the observed with the calculated isotope effect is evidence against the possibility that half-integral quantum numbers $(\frac{1}{2}, 1\frac{1}{2}, 2\frac{1}{2}, \ldots)$ should have been employed instead of the integral numbers (0, 1, 2, ...) actually used in the calculation. If halfintegral numbers were applicable, all the calculated values of Table II should be increased to approximately the mean of the given value and the value for the band having values of n' and n'' both one unit greater; this increase amounts to about 0.8 units for Si²⁹N and 1.4 units for Si³⁰N. As a matter of fact, however, there are distinct indications¹⁵ that there may be an effect of this sort masked by a small constant displacement in the other direction. The mean value of the observed minus calculated isotope effect is -0.1 for Si²⁹N and +0.4 for Si³⁰N (giving half weight to observed data marked doubtful, and omitting the value 31.2 for the 7,8 band). Adding 0.9 to all observed values would bring these averages to 0.8 and 1.3, respectively, which are very near the amounts 0.8 and 1.4 above calculated. Such a relative displacement in the measured, as compared with the true, interval between a Si²⁹N or Si³⁰N head and a corresponding Si²⁸N head is not inconceivable, in view of the enormous difference of intensity. Hence the question of half vibrational quantum numbers for SiN cannot be considered definitely settled in the negative. It should be further noted that the existence of integral quantum numbers here would be in contradiction to the probable close analogy of SiN to BO for which the evidence⁹ is strongly in favor of the half-integral numbers.

The evidence of the isotope effect in favor of SiN as emitter of the present bands is more definite. The only compounds other than SiN whose theoretical isotopic displacements are at all near those observed are SiC and SiO. The former need not be considered; for the latter, the value of $(\rho - 1)$ is -0.00629 for Si²⁹O and -0.01220 for Si³⁰O. These are about 9 percent greater than the corresponding values for SiN; and the same is true for $(\rho^2 - 1)$, $(\rho^3 - 1)$, etc., since, approximately,

¹⁷ Although, of course, the observed agreement does not constitute a quantitative confirmation of theory for the small higher power terms, it does involve a close agreement for the linear and at least approximate agreement for the quadratic terms. An attempt to obtain equations for the Si²⁹N and Si³⁰N heads directly from the experimental data (such a method was used in the case of B¹⁰O and B¹¹O) in order to compare the coefficients with those of Eq. (4) for Si²⁸N, would not have been of much value here, on account of the fewness of the data on the isotope heads.

 $(\rho^2 - 1) = 2(\rho - 1)$, $(\rho^3 - 1) = 3(\rho - 1)$, etc. Hence, every term in (and so the total magnitude of) any calculated isotopic displacement, must be about 9 percent greater for SiO than for SiN. If one adds 9 percent to each of the calculated displacements of Table II, it is apparent that the agreement with the observed displacements becomes much poorer than at present.¹⁸ This evidence in favor of SiN is strongly supported by the chemical evidence previously cited. The fact that the known SiO bands¹⁰ are not obtained with the present bands and have no coefficients in common with those of the latter also supports the case against SiO as a possible emitter of the present bands.

INTENSITY DISTRIBUTION IN THE SiN BANDS

Rotational distribution. The reproductions show strikingly, especially for the bands belonging to the sequence for which $\Delta n = 0$, the rise in intensity in each branch from the null-line. In the negative branch, the intensity can be seen to rise rather rapidly to a maximum and then to fall slowly; in fact, irradiation at the end of the image of the slit on the plate has traced for each band a sort of flattened intensity distribution curve resembling that for a Maxwellian distribution. A similar rise to a maximum in the positive branch, followed by a fall before the head is reached, can be seen in the (0,0) and less clearly in the (1,1)band. Of course the apparent intensity distribution is greatly affected, especially in the positive branch, where also there is the overlap of lines returning from the head, by the changing spacing of the lines. A very rough estimate of the position of the most intense line in each branch, after attempting to discount the above effects, gives $m_{max} = 13$. For thermal equilibrium, this would correspond by the equation $T = (1.431)(2B)m^2_{max}$ to a temperature of 80°C, a reasonable figure for the actual temperature, and similar to the result obtained by Birge in the case of the CN bands generated in active nitrogen.³

Vibrational distribution. As in the cases of BO and CN, the low effective temperature indicated by the rotational quantum number distribution is belied by the vibrational energy distribution. Instead of the very rapid fall of intensity from intense bands with n'=0 to very weak bands with n'=1 and undetectable intensity for higher n' values, the summed emission intensity actually rises from n'=0 until n'=3, and then falls gradually (cf Fig. 1). This type of phenomenon

¹⁸ It should be noted that the effect of substituting half-quantum numbers, and that of substituting SiO for SiN, *both* would produce an *increase* of the calculated isotopic displacements, so that there is no possibility of a mutual cancellation of the two effects.

has been discussed in previous papers^{19,20} on BO and on CuI, to which reference should be made.

The intensity distribution with respect to observed values of Δn appears to be very similar to that in the violet CN bands,²¹ and of a type indicating, according to Lenz's theory, that the motion of the excited electron is unusually little affected by the vibration of the molecule. The sequence $\Delta n = 0$ is by far the most intense, ± 1 are fairly strong, while +2, -2, +3, -3, and +4 (the last represented only by one weak head, which may be spurious) follow in diminishing order of intensity. In spite of the restricted range of Δn values as compared with cases such as BO and CuI, two relations found to hold for the latter^{19,20} are also clearly present in the SiN bands. These are a preference for positive over negative Δn values, and a tendency, also noted in several additional cases by Birge,²⁰ for the numerically larger Δn values to be associated with the larger values of n'. The general preponderance of intensity in Table III on the positive side of the diagonal drawn through the members of the sequence $\Delta n = 0$, shows the existence of the first relation. The second is shown by the increasing length of the rows of figures in Table III as n' increases; particular attention may be called to the low intensity of the bands (1,0), (2,0), and (0,1), (1,2), (0,2), (1,3), the last four not having been found at all.²² An explanation of these effects in terms of Lenz's theory has been given in the paper on CuI.²⁰

NEW SYSTEM OF BANDS IN THE SILICON NITRIDE SPECTRUM

In addition to the intense system of SiN bands discussed above, which for convenience will in the following be called the A bands of SiN, a number of additional, but very much weaker bands, are

¹⁹ See ref. 9, p. 292-3, (BO).

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²⁰ See ref. 8, pp. 20-24, (CuI); also abstract of paper by R. T. Birge, Phys. Rev. 25, 240 (1925), in regard to n' and Δn distribution.

²¹ The resemblance is well brought out when the CN bands are obtained by the action of active nitrogen on carbon compounds. In the violet CN bands, the dominance of the sequence $\Delta n = 0$ and the tendency toward the restriction of Δn to small values are much as in the SiN bands, but perhaps somewhat less marked. Although the violet CN bands are shaded toward the violet, not toward the red like the SiN bands, this difference is a superficial one from the theoretical standpoint, being due to the fact that the coefficient C has small positive values in the first case and small negative values in the second case.

²² This is partly due to the weakness of the *heads* of these bands, due to their large (calculated) distance from the null-lines in this region. But if the bands had been at all intense, the region of maximum intensity on either side of the null-line would certainly have been seen.

TABLE IV

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Wave-number data on heads of new bands. Heads marked "masked" are concealed usually by bands of the more intense SiN system. Heads marked * appear only as emphasized structure lines of a SiN or NO band; in the case of those marked \dagger , two heads fall together; those marked ? are of doubtful identity as members of the system. Wave-numbers for n'=7, n''=0 should be added to the Table. They are 31372 and 31348.

1	n'-	→ 0	1	2	3	4	5	6
<i>n</i> ″ 0 ↓)		••••	28050*678 28017*682 1019 1012	28728 673 28699 674 1018 1017	29401 664 29373 665 1021 1019	30065 657 30038 659 1022 1020	30722 650 30697 651 1020 1027
1		••••	26348† <i>683</i> 26318 <i>687</i> <i>1005</i>	27031 679 27005 677 1008 1004	27710 670 27682 672 1009 1010	28380 663 28354 664 1009 1010	29043 659 29018 652 1008 1014	29702* 29670*
2	2		25343 680 Masked 1001	26023 678 26001*671 997	26701 670 26672 672	27371 664 27344 660 998 996	28035* 28004*	
3	5		24342 <i>684</i> 24318	25026 Absent	Absent Absent	26373 26348* 979 978	•••••	
4		Masked 22649	••••		Absent? Absent	25394 25370		
5	;	21708 <i>691</i> 21679 <i>691</i>	22397 689 22370 688 958 957	23086 23058 <i>681</i>	Masked 23739?			
6	5	· • • • • •	21439 21412 943 943	Absent or Masked	22802 668 Masked 937	23470* 23438* <i>943</i>	••••	
7	7	19804 <i>692</i> 19784 <i>685</i> <i>931</i> <i>935</i>	20496 685 20469 685 934 930	21181 684 21154 679 933 936	21865?662 21833? 938 938	22527 Masked	Absent or Masked	
8	3	18873† <i>689</i> 18849† <i>690</i>	19562 686 19539 679 923 931	20248 679 20218 677 921 915	20927 20895 <i>913</i>	Absent or Masked	••••	
9)		18639?688 18608*?695	19327 19303 679 911 912	19982 674 910	20678 20656 <i>910</i>	••••	••••
10)		••••	18416 <i>681</i> 18931* <i>681</i>	19097 671 19072 894 895	19768 <i>895</i>		
11		 	••••		18203 670 18177 672	18873† 18849† 877 880	•••••	
12	2		••••	•••••	••••	17996 17969 [866] [864]	••••	
13	;	· • • • • •	••••	••••		[663 [663]17793]17768	••••

present. Their presence is obvious only in the near ultraviolet and in the green, but on careful examination it was found that they extend through the intervening region and belong to a single system. They are all shaded toward the red, and in the ultraviolet, where conditions are most favorable, are seen to become resolved, at a moderate distance from the head, into a series of structure lines. The heads are in pairs of about equal intensity, with a separation averaging 26.8 wave-number units and apparently constant or nearly so.

Measurements, of no great accuracy, were made on the heads of the new bands in the hope of finding possible relations between them and the A bands. The wave-number data are given in Table IV, and the intensities in Table V. The former are so arranged as to show the

Intensity distribution in new bands (estimated photographic intensities). Vacant spaces represent bands not found; a few of these may be weakly present but masked													
by heads of	the r	nore ir	itens	e SiN	syste	m.							
$m'' \rightarrow 0$	1	2	3	4	5	6	7	8	0	10	11	12	13

TABLE V

$n^{\prime\prime} \rightarrow$	0	1 2	2 3	5 4	5		6	7	8	9 1	10 1	1 1	2 13	3
n' 0					00	0	 0±	0-	0+	0				
$\begin{array}{c} 1 \\ 2 \\ 2 \end{array}$	 00	1-	1-	(2)	•••	0	0+	0^{+}	1	2^{+1}	0		•••	•••
3 4	1-	2 -		 0-	0	0r 	0+ 1-	0		1	1^{+}_{00}	0+	i	· · · ·
5 6	0-0-	0 000	00	 	· · ·	· · ·	 	· · · ·	 	 	 	 	•••	0
7	00													• • •

constant differences between adjacent rows and columns which is the basis of the assignment of vibrational quantum numbers made. On account of the peculiar intensity distribution, the absolute numbering is somewhat uncertain in respect to n', but is quite definite in regard to n'', since there is no indication of additional bands in the ultraviolet beyond the relatively intense series for which n'' = 0. The positions of the heads of the new bands can be represented approximately (a systematic analysis to determine the best values of the coefficients has not been made) by the equation:

$$\nu = \begin{cases} 26676\\ 26649 \end{cases} + 694n' - 3.3n'^2 - 1025.9n'' + 6.4n''^2. \tag{5}$$

From a comparison of Eqs. (4) and (5) it is evident that the new bands have no term in common with the A bands. Although the new bands are presumably due to SiN, there is no definite proof of this from the isotope effect; but this could not have been expected, on account of the low intensity of the bands even in the most intense exposures.

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Observations on the new bands showed them to be quenched in the same manner as the A bands by small amounts of oxygen. This indicates that they are due to the same emitter. Also, the numerical values of the coefficients and the spacing of the structure lines are of the same order of magnitude as for the A bands. It is possible, of course, that the new bands are not due to SiN, but to some other diatomic emitter such as Si₂ or SiP. SiCl must be ruled out, since the relative abundance of the isotopes of chlorine is such that both SiCl³⁵ and SiCl³⁷ heads should have been visible even with the low intensities used.²³

Wave-No.	Туре	Int.	Wave-No.	Туре	Int.	Wave-No.	Туре	Int.
24267 149 23989 960 871	1? 1?	$ \begin{array}{c} 1\\ 0\\ 3\\ 0\\ 0 \end{array} $	$ \begin{array}{r} 22777 \\ 745 \\ 446 \\ 423 \\ 016 \\ \end{array} $	v v v? v?	3 - 3 - 0 + 1 + 0	21088 071 20816 773 736	1? r	1d 1d 0 0-d
836 712 232 176 22997 985	1 1? 1? 1?	0+1+0 1+1 3-3-	21970 963 925 914 822 818	v 1? 1? v? v? v?		146 142 19993	r v? v? r	00 00 00
983 970 949 894 870	v? v? v v	3 - 2 + 1 = 3 = 3	818 800 797 715 291	v? 1? v?	1 0 1-			

TABLE VI Unidentified heads or lines in SiN spectrum.

Notes: l = line; v = shaded toward violet; r = shaded toward red; d = diffuse; * means superposed on structure line.

The intensity distribution (cf Table V) in the new bands is of an interesting type characterized by a preference for numerically large Δn values, and by the non-occurrence of the band $(0\rightarrow 0)$ and neighboring bands. This distribution approaches that typified by the visible iodine bands.²⁴ It indicates that the motion of the emitting electron is very markedly affected by the vibration of the molecule.—It should be stated that Tables IV and V include all bands of appreciable intensity, except possibly at the extreme red end.

From the analogy of SiN to CN one might expect in the red or near infrared a system of SiN bands analogous to the red CN bands. No such bands were found, presumably because they lie too far in the infrared. Possibly the new SiN system has for its final electronic state a doublet state identical with the initial state of the hypothetical red SiN bands. In

²⁴ Cf refs. 12 and Birge, ref. 20; and especially R. Mecke, Phys. Zeits. 26, 234 (1925).

²³ Also, these bands have not been reported by Jevons (Proc. Roy. Soc. 106A, 174, 1924) in his investigation of the discharge through pure SiCl₄ vapor.

addition to the new bands and the A bands, there are a number of unidentified lines or heads; the data are given in Table VI. Some of these are rather intense, and many are shaded toward the violet; it is possible that these last will prove of importance in the spectrum of SiN.

The writer wishes to express his gratitude to Prof. G. P. Baxter of the Chemistry Department for the pure $SiCl_4$ used in the above work.

JEFFERSON PHYSICAL LABORATORY, HARVARD UNIVERSITY, June 5, 1925



PLATE 1. The entire band spectrum of SiN from $\lambda 3986$ (top) to $\lambda 4800$ (bottom).