of Eq. (15) becomes a differential equation for  $\nu_1$ :

$$(1-u^2)\frac{d^2\nu_1}{du^2} - 5u\frac{d\nu_1}{du} + 3(\lambda-1)\nu_1 = 0.$$
(21)

To ensure that Eq. (5) is satisfied, we must impose upon Eq. (21) the boundary condition that  $\nu_{2j+1}$ , the 2*j*th derivative of  $\nu_1$  [see Eq. (20)], is zero. The required solution is then a polynomial in u:

$$\nu_{1} = \sum_{r} b_{2r-1} u^{2r-1},$$

$$2r(2r+1)b_{2r+1} = [(2r-1)(2r+3) - (2j-1)(2j+3)]b_{2r-1},$$
(22)

where the sum over r runs over  $\frac{1}{2}, \frac{3}{2}, \ldots, j$  when j is a half-integer, and over 1, 2,  $\ldots$  j, when j is an integer. We can now use Eq. (22) in conjunction with Eqs. (18) and (19) to determine those functions f and g that yield a linear realization (j,j) constructed from the pion field alone. For example, in the special cases  $j=\frac{1}{2}$  and 1 we find that

$$j = \frac{1}{2}: f^2 + \pi^2 = \alpha, \qquad g = 0, j = 1: f^2 - 2\alpha f + \pi^2 = 0, \qquad g = -1/f,$$
(23)

where  $\alpha$  is an arbitrary constant.

It is easy to show from the commutation rules in Eq. (2) that  $h_n(\pi_+)^n$  [see Eq. (16)] is an eigenstate of isospin with  $T = T_3 = n$   $(n=0, 1, \dots, 2j)$ . Thus, by operating on these states with the isospin-lowering operator  $T_- = T_1 - iT_2$ , we can generate the complete set of isospin states contained in the representation (j, j), and hence the complete representation itself.

Now suppose that we have a new isovector field  $\tilde{\pi}_a$  for which

$$K_a \tilde{\pi}_b = -i (\delta_{ab} F + \tilde{\pi}_a \tilde{\pi}_b G), \qquad (24)$$

where F and G are functions of  $\tilde{\pi}^2$ . In order to convert this to a linear realization, we need to transform  $\tilde{\pi}_a$ 

into  $\pi_a$  and F and G into the functions f and g of the preceding discussion. Following Weinberg,<sup>5</sup> we seek a redefinition of the form

$$\pi_{\alpha} = \tilde{\pi}_{\alpha} \Phi(\tilde{\pi}^2), \quad f = F \Phi, \\ g = \left[ G \Phi + 2(F + \tilde{\pi}^2 G) \Phi' \right] / \Phi^2.$$
(25)

If such a redefinition is to exist for any F and G, then we must be able to express  $\Phi$  in terms of  $\tilde{\pi}^2$  and F.

This expression is not difficult to find. If we define quantities  $\tilde{\sigma}$  and  $\tilde{u}$  analogous to  $\sigma$  and u in Eq. (19), then we find that

$$\sigma = \tilde{\sigma}\Phi, \quad u = \tilde{u}. \tag{26}$$

The condition  $h_1(\pi^2) = -\lambda$  of Eq. (18) then leads to

$$\Phi = -(1/\lambda \tilde{\sigma}) \nu_1(\tilde{u}). \tag{27}$$

Thus  $\Phi$  in Eq. (27) is the redefinition required to transform the nonlinear realization of Eq. (24) into a linear one of the type (j,j). We also note that

$$(\pi_+)^n h_n(\pi^2) \equiv (\tilde{\pi}_+)^n h_n(\tilde{\pi}^2),$$
 (28)

and hence we obtain all the states of this representation. Since j has been left arbitrary in this discussion, it follows that our procedure can be used to convert a given nonlinear realization into any one of the allowed linear realizations.

As a final point, we observe that the quantities in Eq. (28) satisfy the integrability condition<sup>6</sup> required by Weinberg for the existence of the matrix  $\Lambda(\pi)$ . It follows that the components of the matrix are determined by these quantities.

<sup>5</sup> S. Weinberg, Ref. 1, Eqs. (2.12)-(2.15). <sup>6</sup> S. Weinberg, Ref. 1, Eq. (5.6).

## Errata

Inelastic  $\pi^+n$  Interactions in the Center-of-Mass Energy Range 1.40–1.65 GeV, P. J. LITCHFIELD [Phys. Rev. 183, 1152 (1969)]. The Hulthén form for the distribution of the spectator proton momentum was misquoted. It should read

$$P_{p} \propto \left(\frac{1}{\alpha^{2} + p^{2}} - \frac{1}{\beta^{2} + p^{2}}\right)^{2} p^{2}.$$

The correct form was used in the analysis.

The Gravitational Field of a Disk, THOMAS MORGAN AND LESLEY MORGAN [Phys. Rev. 183, 1097 (1969)]. Equation (26) should read

$$\phi = \frac{1}{2} \ln\{(\omega/2b) [1 + (1 + 4b^2 \rho^2)^{1/2}]\}.$$

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