Polarized-Neutron-Diffraction Study of Magnetic Moments in Yttrium-Cobalt Alloys

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The magnetic moments in the ordered YCo5, Y2Co7, and YCo3 intermetallic compounds with closely related crystal structures have been investigated on single crystals using the polarized-neutron-diffraction technique. By assuming that only the cobalt atoms have magnetic moments and using Moon's experimental cobalt form factor extrapolated smoothly to unity, a discrepancy was found between the measured and calculated magnetic-structure factors. This can be explained by the existence of either a magnetic moment at the yttrium sites coupled antiparallel to the cobalt moments, or a diffuse negative-spin polarization. In the present study, it is not possible to decide between the two models. The ferromagnetically aligned magnetic moments on the cobalt atoms are influenced by the yttrium neighbors; they are the smallest in YCo3, which is the richest in yttrium, and in all cases are the smallest at the sites having the most yttrium neighbors.

1. INTRODUCTION

SEVERAL intermetallic compounds, each existing only in a very narrow concentration range, occur in the Co-rich side of the rare-earth-cobalt systems. In these alloys a negative coupling was observed between the spins of the rare-earth and Co atoms.¹ It seemed of interest to investigate the magnetic structure of the Y-Co alloys, which have similar crystal-structure types as given, e.g., in the phase diagram of Strnat et al.² A preliminary powder-neutron-diffraction study³ with a poor experimental accuracy showed a ferromagnetic structure for YCo₃. In the present measurements the magnetic structure of the YCo₃, Y₂Co₇, and YCo₅ single crystals has been investigated by polarized neutrons.

2. CRYSTAL STRUCTURES AND MAGNETIC PROPERTIES

The YCo₅, Y₂Co₇, YCo₃, and YCo₂ phase have closely related crystal structures. The basic unit is the hexagonal YCo₅ with the space group P6/mmm,⁴ its unit cell containing two different Co sites and one Y site (Fig. 1). The unit cell of Y₂Co₇ [Fig. 2(a)] can be derived from three superposed cells of YCo5 by substituting a Y atom for one of the Co-I atoms and by submitting this new threefold unit to a rhombohedral translation. The Y atoms in the plane of the substitu-

FIG. 1. Crystal structure of YCo₅. The Y and Co atoms are represented by full and open circles, respectively.



* On leave from the Central Research Institute for Physics,

- ¹ R. Lemaire, Cobalt 32, 132 (1966); 33, 201 (1966).
 ² K. J. Strnat, W. Ostertag, N. J. Adams, and J. C. Olson, Fifth Rare-Earth Research Conference 1965 (unpublished).
- ³ R. Lemaire, R. Pauthenet, J. Schweizer, and I. Silvera, J. Phys. Chem. Solids 28, 2471 (1967).

⁴ J. H. Wernick and S. Geller, Acta Cryst. 12, 662 (1959).

tion are displaced in the direction of the c axis to increase the distance between them. There are five Co and two Y sites, which are determined by five independent position parameters in space group $R\bar{3}m.^{5}$ The structure of YCo₃ [Fig. 2(b)] can be derived similarly from two superposed unit cells of YCo₅, getting again the space group $R\bar{3}m.^{5}$ The three Co and two Y sites



FIG. 2. Crystal structure of (a) Y_2Co_7 and (b) YCo₃. The Y and Co_atoms are represented by full and open circles, respectively. The crystallographic sites which are identical in the two structures are shown by arrows.

⁵ E. F. Bertaut, R. Lemaire, and J. Schweizer, Bull. Soc. Franc. Mineral. Crist. 88, 580 (1965).

TABLE I. Values of the lattice parameters a and c at room temperature, the Curie temperature T_C , and the extrapolated saturation magnetization σ_0 of a unit cell for YCo₅, Y₂Co₇, and YCo₃ intermetallic compounds.

	YCo_5	Y ₂ Co ₇	YCo ₃
a (Å)	4.945	5.002	5.016
c (Å)	3.983	36.21	24.35
T_{c} (°K)	977	639	301
$\sigma_0(\mu_{\rm B})$	7.5	7.4	1.4

are described by two independent position parameters. In this paper, the hexagonal description of these rhombohedral structures will be applied. The unit cell of YCo_2 is obtained by substituting a Y atom for one Co-I atom in every unit cell; the space group is $Fd3m.^6$ In the two-phase fields of the phase diagram these phases can be crystallized together, having common axes a and c, because of the large similarities in the crystal structures.

The magnetization-versus-temperature curves obtained with polycrystalline specimens¹ exhibit ferromagnetic behavior for YCo₅ and Y₂Co₇ and ferrimagnetic behavior for YCo₃, while YCo₂ is paramagnetic. The values of the Curie temperature T_c and the saturation magnetization σ_0 extrapolated to 0°K are given in Table I. A strong uniaxial magnetocrystalline anisotropy was observed, the *c* axis being the direction of the easy magnetization in all cases.

3. EXPERIMENTAL

The alloys were prepared by melting Y of 99.9%and Co of 99.99% purity in an alumina crucible under a purified helium atmosphere. The single crystals were grown in an alumina crucible cooled at its lower pointed end and placed inside a graphite cylinder around which a heating coil was lifted with a velocity of 15 mm/h. Although the products obtained were not entirely single crystals for Y₂Co₇ and YCo₃, single-crystal pieces of appropriate dimension could be selected after crushing.

According to the x-ray investigations by the rotating crystal method, the YCo₅ crystal contains a single phase, the YCo_3 crystal has small amount of the YCo_2 phase, while the Y₂Co₇ crystal is contaminated by the YCo₃ phase. These impurity phases have common a and c axes with the parent phases. The values of the lattice parameters a and c determined by the Debye-Scherrer method are given in Table I. The atomic position parameters for YCo3 and Y2Co7 were assumed to be the same as in HoCo₃ and Gd₂Co₇, respectively.⁵ The composition of the YCo3 and Y2Co7 crystals is certainly stoichiometric due to the extremely narrow stability range of these phases. The composition of the YCo5 crystal was checked by x-ray fluorescence analysis and by a study of the lattice parameters, and it was found to be also stoichiometric.

The magnetic moments were measured by the polarized-neutron-diffraction technique, which is a relative method comparing the scattered intensities obtained with positive and negative neutron polarization. Consequently, the measurements can be performed even in the presence of an impurity phase, provided that the investigated reflections belong to one phase only. The present study was thus limited to the characteristic super-reflections of each phase, which occur in addition to the common basic reflections. The single-crystal specimen was mounted in a liquid-helium cryostat with its c axis parallel to the external magnetic field of 14 kOe, determining the direction of the polarization vector of the neutron beam. In the usual experimental arrangement with a counter moving in the horizontal plane, only the reflections of the zone (hk0) can be measured, since any other setting of the crystal results in a large depolarization of the beam due to the incomplete saturation of the sample having strong uniaxial anisotropy. To collect reflections in other zones, the measurements were performed by an apparatus

TABLE II. Observed and calculated values of the magnetic-structure factor F_M at 4.2°K in Y₂Co₇. The calculated values were obtained by least-squares refinements: (A) assuming $\mu_{Y-I} = \mu_{Y-II} = 0$ and using all reflections, (B) assuming $\mu_{Y-I} = \mu_{Y-II} = 0$, but using only the six last reflections, (C) assuming $\mu_{Y-I} \neq 0$, $\mu_{Y-II} \neq 0$, and (D) assuming $\mu_{Y-I} = \mu_{Y-II} = 0$ and using a scaled-up free-atom 3d form factor for Co.

					$F_{M \text{ cale }}$ (10 ⁻¹² cm)	
h k l	$\sin \! heta / \lambda$	γ	$F_{M, \text{ obs}} (10^{-12} \text{ cm})$	Α	B	Ć	D
1 0 1	0.116	-1.97	-2.11 ± 0.09	-1.87	-1.80	-2.10	-2.02
0 1 2	0.119	-2.90	-0.78 ± 0.12	-0.71	-0.70	-0.83	-0.78
$1 \ 0 \ 4$	0.128	-0.64	0.40 ± 0.06	0.38	0.35	0.41	0.41
0 1 8	0.160	-0.36	0.29 ± 0.06	0.27	0.25	0.27	0.25
1 0 10	0.180	-0.06	0.18 ± 0.03	0.23	0.21	0.18	0.21
0 1 11	0.191	0.08	-0.20 ± 0.05	-0.15	-0.14	-0.17	-0.16
0 2 1	0.231	0.30	1.08 ± 0.04	1.11	1.09	1.09	1.10
2 0 2	0.233	0.55	0.89 ± 0.04	0.92	0.88	0.89	0.90
0 2 4	0.238	0.19	-0.29 ± 0.02	-0.29	-0.29	-0.29	-0.29
$2 \ 0 \ 5$	0.241	0.55	-0.62 ± 0.10	-0.63	-0.59	-0.62	-0.61
0 2 7	0.250	0.84	1.23 ± 0.08	1.21	1.19	1.15	1.18
2 0 8	0.256	1.35	2.32 ± 0.25	2.63	2.54	2.52	2.54

⁶ J. H. Wernick and S. Geller, Trans. AIME 218, 867 (1960).

for Co.

TABLE III. Observed and calculated values of the magneticstructure factor F_M at 4.2°K in YCo₃. The calculated values were obtained by least-squares refinements: (A) assuming $\mu_{Y-I} = 2\mu_{Y-II} \neq 0$, and (B) assuming $\mu_{Y} = 0$ and using the scaled-up 3*d* form factor for Co.

h	k	ı	$\sin \! \theta / \lambda$	γ	$F_{M, obs}$ (10 ⁻¹² cm)	$\begin{array}{c}F_{M,}\\(10^{-1}\\\mathrm{A}\end{array}$	^{calc} ² cm) B
$ \begin{array}{c} 1 \\ 1 \\ 0 \\ 0 \\ 2 \\ 2 \end{array} $	0 0 1 2 0	1 7 8 1 2 5	$\begin{array}{c} 0.117 \\ 0.184 \\ 0.200 \\ 0.231 \\ 0.234 \\ 0.252 \end{array}$	$\begin{array}{c} -0.697 \pm 0.019 \\ -0.054 \pm 0.009 \\ 0.020 \pm 0.006 \\ 0.058 \pm 0.001 \\ 0.170 \pm 0.007 \\ 0.437 \pm 0.012 \end{array}$	$\begin{array}{r} -0.59 \pm 0.02 \\ -0.12 \pm 0.02 \\ 0.04 \pm 0.01 \\ 0.15 \pm 0.01 \\ 0.22 \pm 0.01 \\ -0.63 \pm 0.02 \end{array}$	-0.58 -0.14 0.06 0.15 0.20 -0.64	-0.58 -0.15 0.05 0.15 0.20 -0.64

allowing the counter to lift from the horizontal plane in an angular interval of 28° . The accuracy of this method was calculated earlier.⁷

Single-crystal specimens of irregular shape were used with the approximate size of $4 \times 2 \times 3$ mm for YCo₃, $6 \times 1 \times 5$ mm for Y₂Co₇, and $4 \times 1 \times 4.5$ mm for YCo₅, the last numerals giving the dimension in the direction of the c axis. The reflections were measured in the three symmetrical positions around the threefold c axis, and the equivalence of these reflections gave evidence that the crystals were free from extinction effects. The presence of multiple scattering was tested by rotating the crystals around the scattering vector. Since no change in any of the measured polarization ratios could be detected, the possible contribution to the scattered intensity from multiple scattering was considered to be not significant. The possible depolarization of the beam in the sample was checked by measuring the (111) reflection of a Heusler-alloy (Cu₂MnAl) single crystal stuck successively in front of and behind the sample. A slight depolarization was found in Y₂Co₇ and YCo₅.

4. RESULTS

The polarization ration $R=I_+/I_-$, where I_+ and $I_$ are the intensities with positive and negative polarization, was measured at 4.2°K for 6, 12, and 8 reflections in YCo₃, Y₂Co₇, and YCo₅, respectively. The measurements on YCo₃ were repeated at 90 and 215°K, as well. The observed values of R were corrected for the

 $F_{M, \, calc} \ (10^{-12} \, cm)$ $F_{M, \text{ obs}}$ (10⁻¹² cm) h k l В $\sin\theta/\lambda$ γ 1 0 0 0.117 3.124 -0.91 ± 0.04 0.91 0.95 0.382 0.38 0.39 1 0 0.200 0.40 ± 0.02 2 1 2 2 0 0 0.235 0.552 0.71 ± 0.03 0.680.681 1 0.240 0.646 0.99 ± 0.05 1.001.000 1 0.288 5.107 -1.07 ± 0.10 1.211.21 1 0 0 0.311 -1.871 -0.54 ± 0.12 -0.52-0.523 2 0 0.352 0.208 0.22 ± 0.01 0.22 0.222 0 0.406 0.413 $0.84 {\pm} 0.02$ 0.840.83

TABLE IV. Observed and calculated values of the magnetic-

structure factor F_M at 4.2°K in YCo₅. The calculated values

were obtained by least-squares refinements: (A) assuming $\mu_{\rm Y} \neq 0$,

and (B) assuming $\mu_{\rm Y} = 0$ and using the scaled-up 3d form factor

incomplete polarization of the incident beam (0.980) and for the incomplete polarization reversal (0.995) to obtain the ratio $\gamma = F_M/F_N$, where F_M and F_N are the magnetic- and nuclear-structure factors, respectively. Calculating F_N from the nuclear scattering amplitudes $b_{\rm X} = 0.79$ and $b_{\rm Co} = 0.25$, the values of F_M were obtained. The results are given in Tables II–V.

The magnetic moments associated with the different sites in the unit cell were computed from the observed values of F_M by least-squares refinements. The calculations were performed first for Y₂Co₇, which has the largest unit cell and thus the most reflections measurable at the low-angle region.

In Y₂Co₇, the Co-II atoms have identical environments. Consequently, their magnetic moments were taken to be identical. In the first refinement, the magnetic moments for the Co sites were calculated by assuming that the Y atoms have no magnetic moment and by using the experimental form factor of Co measured by Moon⁸ extrapolated smoothly towards unity at $(\sin\theta)/\lambda=0$. The calculated values of F_M and the magnetic moments are given in column A of Tables II and VI, respectively. As can be seen, the agreement between the measured and calculated values of F_M is very poor for the reflections at low angles. This can be explained by supposing the existence of magnetic moments on the Y atoms. Assuming that similar to the other 4d elements, Y has a form factor falling more rapidly with the reflection angle than that of Co, its

TABLE V. Observed and calculated values of the magnetic-structure factor F_M at 90 and 215°K in YCo₃. The calculated values were obtained by least-squares refinements using the form factor of Y derived for Y_2 Co₇.

90°K				215°K			
h k	i l	γ	$F_{M, obs}$	$F_{M, calc}$	γ	$F_{M, { m obs}}$	$F_{M, { m calc}}$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} 1 \\ 0 \\ 7 \\ 1 \\ 8 \\ 2 \\ 1 \\ 0 \\ 2 \\ 0 \\ 5 \end{array}$	$\begin{array}{c} -0.639 {\pm} 0.023 \\ -0.044 {\pm} 0.008 \\ 0.014 {\pm} 0.010 \\ 0.058 {\pm} 0.001 \\ 0.152 {\pm} 0.004 \\ 0.409 {\pm} 0.016 \end{array}$	$\begin{array}{c} -0.54{\pm}0.02\\ -0.10{\pm}0.01\\ 0.03{\pm}0.02\\ 0.15{\pm}0.01\\ 0.20{\pm}0.01\\ -0.59{\pm}0.02\end{array}$	$-0.54 \\ -0.12 \\ 0.05 \\ 0.15 \\ 0.18 \\ -0.60$	$\begin{array}{c} -0.264 {\pm} 0.003 \\ -0.014 {\pm} 0.006 \\ 0.002 {\pm} 0.006 \\ 0.029 {\pm} 0.001 \\ 0.073 {\pm} 0.005 \\ 0.187 {\pm} 0.006 \end{array}$	$\begin{array}{c} -0.22 {\pm} 0.01 \\ -0.03 {\pm} 0.01 \\ 0.00 {\pm} 0.01 \\ 0.08 {\pm} 0.01 \\ 0.09 {\pm} 0.01 \\ -0.27 {\pm} 0.01 \end{array}$	$-0.22 \\ -0.05 \\ 0.01 \\ 0.08 \\ 0.08 \\ -0.27$

⁷ A. Delapalme, R. Georges, and J. Schweizer, Nucl. Instr. Methods 63, 283 (1968).

⁸ R. M. Moon, Phys. Rev. **136**, A195 (1964).

TABLE VI. Magnetic moments at 4.2°K in Y_2C_{07} obtained by the least-squares refinements explained in Table II. μ_{total} is the magnetic moment of a unit cell. All values are given in μ_B .

	А	в	С	D
μ _{Y-I}			-1.02 ± 0.24	
$\mu_{\rm Y-II}$		• • •	-0.45 ± 0.22	•••
µCo-I	1.36 ± 0.10	1.26 ± 0.06	1.31 ± 0.06	1.28 ± 0.06
$\mu_{Co-II} - \mu_{Co-III}$	1.52 ± 0.08	1.47 ± 0.06	1.44 ± 0.06	1.45 ± 0.05
μ _{Co-IV}	1.41 ± 0.05	1.37 ± 0.02	1.34 ± 0.03	1.37 ± 0.03
μ_{Co-V}	1.14 ± 0.03	1.10 ± 0.02	1.10 ± 0.02	1.11 ± 0.02
μ_{total}	9.25 ± 0.20	8.92 ± 0.14	7.32 ± 0.35	8.92 ± 0.13

TABLE VIII. Magnetic moments at 4.2°K in YCo₅ obtained by the least-squares refinements explained in Table IV. μ_{tot} is the magnetic moment of a unit cell. All values are given in $\mu_{\rm B}$.

	Α	в
μy	-0.40 ± 0.30	•••
HCo-T	1.68 ± 0.04	1.66 ± 0.04
HCo-II	1.67 ± 0.04	1.66 ± 0.04
Htotal	7.97 ± 0.34	8.30 ± 0.15

contribution to the scattered intensities at higher angles thus being negligible, a new refinement of the magnetic moments of Co was carried out, this time using only the six reflections at higher angles [from (021) to (208)]. The obtained moments and the calculated values of F_M for all the 12 reflections are given in column B of Tables II and VI. The difference ΔF_M between the calculated and observed values of F_M for the first six reflections can be now attributed to the contribution of yttrium. Extrapolating to $(\sin\theta)/\lambda=0$, the values of the form factor can be deduced. The results of a new refinement using the form factor thus determined are given in column C of Tables II and VI. The agreement between the calculated and measured values of F_M is quite good.

As suggested by Moon,⁹ the discrepancy between the measured and calculated values of F_M can be also explained by another model in which the Y atoms have no magnetic moment, but the Co moments are separated into a 3*d*-like part and a negative constant, similar to the metallic Co. The magnetic moments for the Co sites are calculated with a scaled-up (by a factor of 1.18) free-atom 3d form factor as determined in metallic Co.⁸ The results for this model are given in column D of Tables II and VI. A good agreement between the measured and calculated values of F_M can be seen for the first reflections; the values for the Co moments are very similar to those in the previous model, but they now imply both a local 3*d* moment and a diffuse negative moment.

The results of the least-squares refinements, assuming that the Y atoms have magnetic moments and using the

TABLE VII. Magnetic moments at 4.2, 90, and 215°K in YCo₃ obtained by the least-squares refinements explained in Tables III and V. μ_{tot} is the magnetic moment of a unit cell. All values are given in μ_B .

	4.29	°К		
	A	В	90°K	215°K
$\mu_{Y-I} = 2\mu_{Y-II}$	-0.35 ± 0.19	•••	-0.30 ± 0.22	-0.07 ± 0.10
μC_{o-I}	0.55 ± 0.04	$0.55 {\pm} 0.03$	0.49 ± 0.04	0.18 ± 0.03
μC_{o-II}	0.83 ± 0.05	0.79 ± 0.04	0.78 ± 0.06	0.34 ± 0.03
μCo-111	0.40 ± 0.02	0.40 ± 0.01	0.37 ± 0.02	0.17 ± 0.01
<i>µ</i> total	1.30 ± 0.27	1.51 ± 0.04	$1.22\!\pm\!0.33$	0.59 ± 0.16

⁹ R. M. Moon (private communication).

form factor of Y determined above, are given in column A of Tables III and VII for YCo₃ and in column A of Tables IV and VIII for YCo₅. Since in YCo₃ the values of μ_{Y-I} and μ_{Y-II} cannot be calculated separately because of the form of the structure factor expressions, $\mu_{Y-I} = 2\mu_{Y-II}$ was assumed as in Y₂Co₇. The results of the least-square refinement based on the data at 90 and 215°K for YCo₃ are given in Tables V and VII. The results of the calculations for the Co moments at 4.2°K in YCo₃ and YCo₅, assuming that the Y atoms have no magnetic moments and using the same scaled-up form factor for the Co as above for Y₂Co₇, are given in column B of Tables III, IV, VII, and VIII.

The polarization ratios for the YCo_3 phase occurring in small quantity in the Y_2Co_7 crystal were also measured at 4.2°K and were found to be identical with those measured in the YCo_3 crystal.

5. DISCUSSION

The magnetic moments measured in the three compounds are summarized in Fig. 3. The results obtained on pure Co metal⁸ and on YCo₂ having no magnetic order at all¹⁰ are also included. The moments associated with the sites having identical environments are connected by straight lines in the figure.



FIG. 3. Magnetic moments associated with the different Co sites in pure Co, YCo_5 , Y_2Co_7 , YCo_3 (present study), and YCo_2 (Ref. 9).

¹⁰ R. Lemaire and J. Schweizer, Phys. Letters 21, 366 (1966).

As seen in Fig. 3, the magnetic moment of Co decreases with increasing concentration of Y in a strikingly similar way for the different crystallographic sites. The decrease is probably a consequency of the gradual filling up of the 3d band of the cobalt, and this is further supported by the fact that the highest magnetic moments of Co in a compound are associated with the crystallographic sites having the least Y nearest neighbor (Co-II sites in both Y₂Co₇ and YCo₃), while the lowest values are associated with those having the most Y neighbors (Co-V in Y₂Co₇ and Co-III in YCo₃).

The Co-I and Co-II sites in YCo₅ have the same value of magnetic moment, while those for the corresponding Co-II, or Co-III and Co-IV sites in Y₂Co₇ are different. As seen in Fig. 3, the magnetic moment of Co, which is strongly dependent on the Y concentration between Y₂Co₇ and YCo₃, is rather insensitive to the composition near YCo₅. Thus, the difference in the local electronic concentrations around the Co-I and Co-II sites of YCo₅ does not produce a noticeable change in the Co moments.

The magnetic moment on the Y atoms, if it exists, is probably induced by the ferromagnetic Co environment. The values of the observed Y moment can be compared with the induced moments on other 4d-metal atoms: $1.0 \mu_B$ on Rh and $0.34 \mu_B$ on Pd in FeRh and FePd₃, respectively.^{11,12} It is higher at Y_I sites which have 18 nearest-neighbor Co atoms than at Y_{II} sites which have only 12. The form factor of Y as evaluated from the Y_2Co_7 data changes sign around $(\sin\theta)/\lambda = 0.17$.

The values of the total magnetic moment μ_{total} of a unit cell are given in Tables VI-VIII and are in good agreement with the results of the magnetization measurements, shown in Table I, for the model in which the Y moment exists. For the other model, the agreement is not so good. This may indicate that the ratio between the 3d-like moment and diffuse negative polarization is different from the ratio measured in metallic Co. However, it seems difficult to determine this ratio with the help of the magnetization results obtained with polycrystalline specimens because of the inaccuracy of these measurements due to the very large magnetic anisotropy.

Present measurements do not allow us to decide between the two interpretations of the results. Further measurements are in progress in order to obtain a spindensity map of YCo₅ by Fourier inversion.

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ham, 1964 (The Institute of Physics and The Physical Society, London, 1965), p. 223.

¹¹ E. F. Bertaut, F. de Bergevin, and G. Roult, Compt. Rend.

 <sup>256, 1688 (1963).
 &</sup>lt;sup>12</sup> G. Shirane, R. Nathans, S. J. Pickart, and H. A. Alperin, in Proceedings of the International Conference on Magnetism, Notling-