## Exchange-Degenerate $\Lambda$ -Trajectory Interpretation of $K^+ p$ Backward Elastic Scattering Data\*

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A baryon Regge exchange model for  $K^+p$  backward elastic scattering is constructed in accordance with the requirements of duality and the absence of Y = +2 baryons. The dominant exchange-degenerate amplitude is associated with the  $\Lambda_{\alpha}$  (1115,  $\frac{1}{2}^+$ ) and  $\Lambda_{\gamma}$  (1520,  $\frac{3}{2}^-$ ) particles. Recent data on  $d\sigma/du$  (K<sup>+</sup>p) from 2 to 7 GeV/c are successfully reproduced.

N EW data on  $K^+p$  elastic scattering over the 2–7-GeV/c momentum range exhibit a backward peak with a rapid energy dependence.<sup>1-6</sup> Since the  $K^+ p$ elastic amplitude has no prominent direct-channel resonances, we expect Reggeized baryon exchange to account for the backward peak down to rather low momenta.<sup>7</sup> To describe the present data on  $d\sigma/du$  $(K^+p)$ , we propose a simple model based on the following assumptions: (i)  $\Sigma$ -exchange contributions can be neglected relative to A-exchange contributions; (ii) only exchanges of the leading A trajectories are important; (iii) the Regge amplitudes are exchangedegenerate, in accord with the duality principle<sup>8</sup> and the absence of prominent  $K^+ p$  direct channel resonances. By the above arguments the dominant amplitudes will be associated with the  $\Lambda_{\alpha}(1115, \frac{1}{2}^+)$  and  $\Lambda_{\gamma}(1520, \frac{3}{2}^-)$ particles, which lie on a degenerate trajectory and have the same residue function. Quantitative fits are presented which reproduce the  $K^+ p$  data with few parameters. Further tests of the model are proposed.

Hyperon exchange models for the  $K^+p$  amplitude are complicated by the numerous possibilities for  $\Lambda$ and  $\Sigma$  exchanges. However, the following considerations suggest that the A-exchange contributions will dominate in  $K^+p$  backward scattering.

(i) Coupling constants from dispersion relations give9

 $g_{p\Lambda K}^2 \gg g_{p\Sigma^0 K}^2$ .

(ii) Direct-channel resonance contributions to  $K^-p$ elastic scattering from I=0 resonances are appreciably larger than from I=1 resonances.

(iii) From the known residues of  $N_{\alpha}$  and  $\Delta_{\delta}$  Regge exchanges in  $\pi^{\pm}p$  backward scattering,<sup>10</sup> SU(3) estimates for the residues of  $\Lambda_{\alpha}$ ,  $\Sigma_{\alpha}$ , and  $\Sigma_{\delta}$  exchanges in  $K^+p$  backward scattering give  $\Lambda_{\alpha}$  amplitude  $\gg \Sigma_{\alpha}$  or  $\Sigma_{\delta}$ amplitudes.

(iv) The strong backward peak observed in data<sup>11</sup> on the reaction  $K^- p \rightarrow \pi^0 \Lambda_{\gamma}(1520, \frac{3}{2})$  leads us to expect a significant contribution from  $\Lambda_{\gamma}$  exchange in  $K^+ \not \to K^+ \not p$ .

Since the trajectory for  $\Lambda_{\beta}(1405, \frac{1}{2})$  is expected to lie about a unit below the  $\Lambda_\alpha$  or  $\Lambda_\gamma$  trajectories,  $^{12}$  the  $\Lambda_{\beta}$ -exchange contribution to  $K^+p$  scattering should die out extremely rapidly with energy. We therefore shall retain only  $\Lambda_{\alpha}$ - and  $\Lambda_{\gamma}$ -exchange contributions in subsequent calculations. These trajectories are illustrated in Fig. 1.

The Regge plot of the  $\Lambda_{\alpha}$  and  $\Lambda_{\gamma}$  particles<sup>13</sup> in Fig. 1 displays approximate exchange degeneracy for the trajectories. This degeneracy has been speculatively correlated with the nonexistence of  $K^+p$  direct-channel resonances through the duality principle.<sup>14-16</sup> In order that counterclockwise loops are not present in the Argand diagrams of the partial-wave decomposition

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FIG. 1. Exchange degenerate  $(\Lambda_{\alpha}, \Lambda_{\gamma})$  Regge trajectory. The *u* positions of amplitude zeros at wrong-signature nonsense points are indicated by vertical arrows.

of the Regge exchange amplitude, the  $\Lambda_{\alpha}$  and  $\Lambda_{\gamma}$  contributions must be exchange degenerate (by duality, counterclockwise loops would be associated with the existence of  $K^+p$  direct-channel resonances<sup>14</sup>). With this exchange-degenerate requirement, the *u*-channel amplitude for  $K^+p$  backward scattering has the form<sup>17,18</sup>

$$\tilde{t}_{2}(\sqrt{u},s) = \frac{1}{\Gamma(\alpha + \frac{1}{2})} \gamma \left( \frac{1 + e^{-i\pi(\alpha - 1/2)}}{\cos\pi\alpha} + \frac{1 - e^{-i\pi(\alpha - 1/2)}}{\cos\pi\alpha} \right) s^{\alpha - 1/2},$$

where  $\alpha(\sqrt{u})$  and  $\gamma(\sqrt{u})$  denote the trajectory and residue, respectively. The first term above represents the  $\Lambda_{\alpha}$  exchange, the second  $\Lambda_{\gamma}$ . The  $\Lambda_{\alpha}$  amplitude vanishes at  $\alpha = -\frac{1}{2}$  ( $u \simeq +0.2$ ) and the  $\Lambda_{\gamma}$  amplitude vanishes at  $\alpha = -\frac{3}{2}$  ( $u \simeq -0.8$ ), as noted in Fig. 1. However, the sum of the two contributions is a smoothly varying function of u.

For data fitting we assume an approximately linear trajectory, as suggested by the Regge plot in Fig. 1. The residue is parametrized with a simple form consistent with the absence of  $J^P = \frac{1}{2}^-$  and  $J^P = \frac{3}{2}^-$  MacDowell reflected particles,<sup>19</sup>

$$\gamma(\sqrt{u}) = \left(1 + \frac{\sqrt{u}}{M_{\Lambda}}\right) \left(1 + \frac{\sqrt{u}}{M_{Y_0}}\right) \beta(u),$$

<sup>17</sup> The cross-section formulas for fermion Regge exchange are given in Ref. 12. The amplitude  $f_2$  of Ref. 12 is related to  $\tilde{f}_2$  by  $f_2(\sqrt{u},s) = \tilde{f}_2(\sqrt{u},s) (E_u+M)/\sqrt{u}$ . The units of s, t, and u are  $(\text{GeV}/c)^2$ .

<sup>18</sup> Since we retain only the leading power in the Regge expansion, some question exists as to whether  $s^{\alpha}$  or  $(s-t)^{\alpha}$  represents the better approximation at low energies. We have tried both forms, with similar results for  $K^+p$ . Fits to the 3-7-GeV/c  $K^+p$  data were somewhat better with the  $(s-t)^{\alpha}$  form, but fits to the more accurate 2-3-GeV/c data were better with the  $s^{\alpha}$  form. Baryonexchange calculations of  $pp \to K^-K^+$  at low energy are extremely sensitive to the choice of an energy-dependent factor.

<sup>19</sup> V. Barger and D. Cline, Phys. Letters **26B**, 83 (1967). The observed  $\Lambda_{\beta}(1830, \frac{5}{2}^{-})$  particle is presumably the MacDowell reflected state associated with  $\Lambda_{\alpha}(1815, \frac{5}{2}^{+})$ .

$$\tilde{f}_2(\sqrt{u},s) = \frac{2\beta(u)}{\Gamma(\alpha + \frac{1}{2})\cos\pi\alpha} \left(1 + \frac{\sqrt{u}}{M_\Lambda}\right) \left(1 + \frac{\sqrt{u}}{M_{Y_0}}\right) s^{\alpha - 1/2}.$$

The fits to the 2–7-GeV/c data<sup>1-6</sup> are shown in Figs. 2 and 3. The  $(\Lambda_{\alpha}, \Lambda_{\gamma})$  trajectory was determined to be

$$\alpha = -0.72 + 1.01u$$

as compared with

$$\alpha = -0.7 + 0.96u$$

from the Regge spin-mass plot of particles in Fig. 1. The curves in Figs. 2 and 3 correspond to the residue parametrization (in  $\text{GeV}^{-1}$ )<sup>20</sup>

$$\beta = 9.1e^{2 \cdot 1u} + 3.1e^{-1 \cdot 5u}$$

The second term in  $\beta$  was needed to account for the tendency of the  $d\sigma/du$  data to flatten at larger |u|. The model seems to provide a reasonable over-all description of the present  $K^+p$  data.

The measurement of  $K^+n \to K^0\rho$ ,  $K_2\rho \to K_1\rho$ , or  $K^+n \to K^+n$  backward scattering will provide a straightforward experimental test of the  $\Lambda$ -exchange dominance assumption of this model. We expect the



FIG. 2. Fitted curves for  $d\sigma/du$   $(K^+p)$  based on  $(\Lambda_{\alpha}, \Lambda_{\gamma})$  exchange-degenerate Regge model. Data from Ref. 3.

<sup>20</sup> For an  $(s-t)^{\alpha}$  energy dependence (see Ref. 18), the fitted residue was  $\beta = 7.8e^{1.9u} + 1.2e^{-1.7u}$ . The parametric form for the residue is not well suited for extrapolation outside the *u* range considered in the data analysis.

following relations to hold:

$$\frac{d\sigma}{du}(K^+n \to K^0p) \approx \frac{d\sigma}{du}(K^+p \to K^+p),$$
$$\frac{d\sigma}{du}(K_2p \to K_1p) \ll \frac{d\sigma}{du}(K^+p \to K^+p),$$
$$\frac{d\sigma}{du}(K^+n \to K^+n) \ll \frac{d\sigma}{du}(K^+p \to K^+p).$$

The assumption of exchange degeneracy is somewhat more difficult to evaluate experimentally. The polarization is predicted to be zero in the exchange-degenerate limit, but polarization phenomena are typically sensitive to small background contributions. Finite-energy sum rules (FESR) for the *u* channel provide an alternative test of the exchange degeneracy, since the  $\Lambda_{\alpha}$ and  $\Lambda_{\gamma}$  amplitudes can be separated through their opposite signature.<sup>21</sup> However, lack of information on the  $\bar{p}p \rightarrow \bar{K}K$  channel will cause uncertainties in such FESR evaluations.

The absence of prominent resonances in the  $K^+p$  elastic channel makes it a particularly interesting reaction for phenomenological study. Our analysis indicates that  $\Lambda$  exchanges can account for the backward peak at intermediate energies. It will be of interest to see to what extent this model can account for  $K^+p$  backward scattering data below 2 GeV/c. At the same time, experiments above 7 GeV/c are highly desirable to determine if the measured energy dependence for

<sup>21</sup> D. Beder and J. Finkelstein, Phys. Rev. **160**, 1363 (1967); C. Chiu and M. Der Sarkissian, Nuovo Cimento **55A**, 396 (1968).



FIG. 3. Fitted curves for  $d\sigma/du$   $(K^+\rho)$  based on  $(\Lambda_{\alpha}, \Lambda_{\gamma})$  exchange-degenerate Regge model. Data from Refs. 1 (3.53 GeV/c), 2 (3.55 GeV/c), 4 (5.2 and 7.0 GeV/c), and 5 (2.76 GeV/c).

 $d\sigma/du$  (K+p) remains compatible with the predictions from  $(\Lambda_{\alpha}, \Lambda_{\gamma})$  exchanges.

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