## Strange-Particle Production in $\pi^- p$ Interactions from 1.5 to 4.2 BeV/c. **II.** Two-Body Final States<sup>\*</sup>

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The reactions  $\pi^- \rho \to \Lambda K^0$ ,  $\Sigma^0 K^0$ , and  $\Sigma^- K^+$  in the 1.5- to 4.2-BeV/c momentum range were studied in the Lawrence Radiation Laboratory's 72-in. hydrogen bubble chamber. The total cross sections for the three reactions decrease as  $E_{\rm c.m.}^{-3.6}$ ,  $E_{\rm c.m.}^{-3.3}$ , and  $E_{\rm c.m.}^{-9.3}$ , respectively. The differential cross sections are presented at 11 beam momenta. A peripheral peak is the dominant feature of the reactions  $\pi^- p \to \Lambda K^0$  and  $\Sigma^{0}K^{0}$ , for which K\* exchange is allowed, but no such peaking is seen in  $\pi^{-}p \to \Sigma^{-}K^{+}$ . An exponential fit to the momentum-transfer distributions in the peripheral region yields slope parameters in the 6- to  $10 - (\text{BeV}/c)^{-2}$ range. The differential cross sections for  $\pi^- p \to \Lambda K^0$  and  $\Sigma^- K^+$  show peaking for forward production of hyperons in the c.m. system, to which baryon exchange is expected to contribute. The angular distribution of the  $\Lambda$  polarization in  $\pi^- p \to \Lambda K^0$  is presented.

#### I. INTRODUCTION

UMEROUS authors have reported results on the associated production reactions

> $\pi^- p \longrightarrow \Lambda K^0$ (1)

$$\Sigma^0 K^0 \tag{2}$$

 $\Sigma^-K^+$ (3)

at energies from threshold to  $1.5 \text{ BeV}/c.^1$  This work is

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an extension of these studies into the energy range 1.5 to 4.2 BeV/c. Recently experiments have also been performed in this momentum range<sup>2-7</sup> and at higher energies.8-11

This experiment was performed at the Bevatron with the 72-in. bubble chamber. The experimental procedure, and results on three- and more-body final states are reported in the preceding paper.<sup>12</sup> We refer the reader to that paper for details on the analysis of the data. Here we discuss only those features relevant to the two-body final states  $\Lambda K^0$ ,  $\Sigma^0 K^0$ , and  $\Sigma^- K^+$ .

Our sample, based on 890 000 pictures, consists of 4300  $\Lambda K^0$  events, 1200  $\Sigma^0 K^0$  events, and 2600  $\Sigma^- K^+$ events. This sample satisfies the following selection criteria: For the  $\Lambda K^0$  final state we use events for which either  $\Lambda \to p\pi^-$  or  $K^0 \to \pi^+\pi^-$  or both decays are observed within the fiducial volume. For the  $\Sigma^0 K^0$  final state we require that  $K^0 \rightarrow \pi^+\pi^-$  be observed. For the

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<sup>\*</sup> This work was done under the auspices of the U. S. Atomic Energy Commission. Part of this paper is from a thesis submitted by J. A. Schwartz to the Graduate Division of the University of California, Berkeley, California in partial fulfillment of the requirements for the degree of Doctor of Philosophy. † Present address: TRW Systems, Inc., 1 Space Park, Redondo

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in the second second	$p_{\text{beam}}^{\text{beam}}$ (BeV/c)	<i>Е</i> с.т. (BeV)	$\begin{array}{c} \pi^- p \longrightarrow \\ \sigma \ (\mu b) \end{array}$	ΛK <sup>0</sup> Events	$\begin{array}{c} \pi^{-}p \longrightarrow 2\\ \sigma \ (\mu b) \end{array}$	Σ <sup>0</sup> K <sup>0</sup> Events	$\pi^- p  o \Sigma^- p$ $\sigma(\mu b)$	Κ <sup>+</sup> Events	Reference	Symbol on Fig. 1	
-	1.50	1.930	334 + 19	308	$167 \pm 22$	59	242 + 14	293	14	$\nabla$	*******
	1.508	1.934	$214 \pm 23$	476	$\sim 177$	134			2	ò	
	1.59	1.974	$214 \pm 21$	106 <sup>b</sup>	$178 \pm 22$	65	$262 \pm 16$	285	3	Å	
	1.615	1.985	$208 \pm 25$	286	$111 \pm 20$	70	$180 \pm 20$	319	Present expt.	ō	
	1.69	2.020	$199 \pm 12$	263	$110 \pm 14$	58	$153 \pm 9$	266	14	$\nabla$	
	1.85	2.093	$181 \pm 12$	215	$140 \pm 17$	66	$99 \pm 8$	153	14	$\dot{\nabla}$	
	1.94	2.133	$185 \pm 15$	436	$126 \pm 15$	127	$98 \pm 10$	281	Present expt.	ò	
	1.95	2.137	$182 \pm 11$	255	$94 \pm 13$	53	99 ± 7	182	14	$\nabla$	
	1.98	2.150	$184\pm20$	299	$116 \pm 15$	87	90 ±10	191	Present expt.	ò	
	2.05	2.181	$182 \pm 17$	119	$123\pm21$	33	$70 \pm 9$	60	14	$\nabla$	
	2.05	2.181	$179 \pm 15$	515	$113 \pm 10$	153	$87 \pm 8$	327	Present expt.	Ò	
	2.14	2.219	$162 \pm 20$	78	$100 \pm 20$	23	<b>39</b> ±10	25	Present expt.	0	
	2.15	2.223	$192 \pm 11$	334	$114 \pm 13$	82	$65 \pm 5$	148	14	$\nabla$	
	2.25	2.265	$172 \pm 10$	319	$105 \pm 12$	80	57 $\pm$ 5	138	14	$\nabla$	
	2.35	2.310	$174 \pm 14$	157	$113 \pm 18$	41	$53 \pm 7$	63	14	$\nabla$	
	2.605	2.407	$106 \pm 12$	182	$81 \pm 12$	66	$30 \pm 5$	67	Present expt.	0	
	2.70	2.444	$120 \pm 11$		$85 \pm 12$		$31 \pm 5$		4		
	2.75	2.463	$90 \pm 25$	18	$95 \pm 25$	19	$32 \pm 10$	15	5	•	
	2.86	2.505	$109 \pm 15$	59	$93 \pm 25$	26	$22 \pm 7$	18	Present expt.	0	
	3.00	2.556	$31 \pm 14$	5	$86 \pm 25$	14	$15 \pm 5$	12	6	•	
	3.01	2.560	$84 \pm 12$	111	$74 \pm 12$	52	$22 \pm 4$	43	Present expt.	$\bigcirc$	
	3.125	2.602	$94 \pm 12$	170	$41 \pm 10$	39	$15.5 \pm 3.0$	41	Present expt.	0	
	3.21	2.632	$87\pm10$	301	$50\pm 6$	91	$15.5 \pm 2.0$	76	Present expt.	0	
	3.885	2.862	$67\pm12$	86	$37\pm8$	22	$8.5 \pm 2.5$	16	Present expt.	0	
	4.00	2.900	с		с		$5.0 \pm 3.0$	2	7	$\Delta$	
	4.16	2.948	$49\pm8$	75	$42\pm 8$	30	$4.5 \pm 1.5$	10	Present expt.	0	
	4.65	3.103	d		d			0	8 -		

TABLE I. Cross section for associated production.

<sup>a</sup> The momentum bite is typically between  $\pm 0.03$  and  $\pm 0.05$  BeV/c. <sup>b</sup> This value does not include events where only a  $\Lambda \rightarrow p\pi^-$  decay is seen. <sup>o</sup>  $\sigma(\pi^-p \rightarrow \Lambda K^0) + \sigma(\pi^-p \rightarrow 2^0 K^0) = 93 \pm 14 \ \mu b$  based on 39 events is given in Ref. 7. <sup>d</sup>  $\sigma(\pi^-p \rightarrow \Lambda K^0) + \sigma(\pi^-p \rightarrow 2^0 K^0) = 40 \ \mu b$  based on 8 events is reported in Ref. 8.

 $\Sigma^-K^+$  final state we require the  $\Sigma^- \rightarrow n\pi^-$  decay be

bility that the above requirements are met.

Once the consistency of the kinematic fits with bubble density is verified on the scan table, reaction (3) is well enough constrained that the sample is essentially uncontaminated. The same holds true for reactions (1) and (2) if both the  $\Lambda$  and  $K^0$  decays are observed. If only one decay is observed, assignment of events is based on missing-mass selection criteria.<sup>13</sup> By reprocessing the well-constrained two-decay events as if only one decay were observed, we found that the cross contamination between the  $\Lambda$  and  $\Sigma^0$  channels for the whole sample is less than 10% at all beam momenta.

# **II. TOTAL CROSS SECTIONS**

For cross-section measurements only, the experiment was divided into two parts. Results on the first part  $(\pi 72)$  have been given by Schwartz,<sup>14</sup> and are merely quoted here. In this case, the total number of interactions was estimated from a scan of every fifth frame

in a randomly chosen sample of film; frames with more than 22 tracks (TMT's) were treated separately. A sample of 270 TMT's was scanned, yielding a mean of 28.3 tracks/TMT; the total number of interactions at each beam momentum was prorated accordingly. Corrections of  $+2\pm2\%$  for scanning efficiency, and -2.5%for events falling outside the fiducial volume were applied; the path length corresponding to the total number of interactions at each momentum was calculated using the cross-section values reported by Diddens et al.15

In the second part ( $\pi 63$ ) a selected sample of film was scanned completely for all interactions in each momentum interval. The number of observed two-prong events was corrected by  $+10\pm3\%$  to account for unnoticed small-angle scatterings. Using the information from this special scan, and with the data of Diddens et al.<sup>15</sup> and Citron et al.,<sup>16</sup> we determined the cross section per event found in the general scan. Final cross sections were determined by comparing the corrected number of fitted events of a given type with the corresponding number of events found in the general scan. This procedure is described in detail in the preceding paper.12

Since cross-section determinations were not identical,

<sup>&</sup>lt;sup>13</sup> If only a  $K^0 \rightarrow \pi^+\pi^-$  decay is seen, the event is admitted to the sample if the square of the missing mass is 1.15 (BeV)<sup>2</sup> < MM<sup>2</sup> <1.56 (BeV)<sup>2</sup>. If only a  $\Lambda \rightarrow p\pi^-$  decay is seen, the limits are 0.2 (BeV)<sup>2</sup><MM<sup>2</sup><0.3 (BeV)<sup>2</sup>. Cross-section values are corrected for the loss of events due to these cuts. <sup>14</sup> Joseph A. Schwartz, Lawrence Radiation Laboratory Report

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there may be small systematic differences in the two parts of the experiment. Our results, as well as those of other experiments<sup>2-8</sup> are presented in Table I. In Fig. 1 the same data are plotted on a log-log scale as a function of total c.m. energy,  $E_{\rm c.m.}$ . In each case the cross section decreases monotonically with increasing energy. Since the data in Fig. 1 lie essentially on three straight lines, they have been fitted with

$$\sigma_T = A E_{\text{c.m.}}^{B}. \tag{4}$$

This expression provides adequate fits to reactions (2) and (3). For the  $\Sigma^0 K^0$  final state, the least-squares fit gives  $B = -3.30 \pm 0.30$ , with  $\chi^2 = 24.6$  for 24 data points. For the  $\Sigma^-K^+$  final state, we have  $B = -9.30 \pm 0.25$  with  $\chi^2 = 34.5$  for 25 data points. For the  $\Lambda K^0$  final state, we have  $B = -3.57 \pm 0.20$  with  $\chi^2 = 60.1$  for 25 data points; consequently, in this case the fit is poor.

We have considered the possibility that the poor fit in the  $\Lambda K^0$  channel reflects a significant contribution to the cross section from *s*-channel resonances. It is not difficult to see that a better fit to  $\sigma_T(\Lambda K^0)$  in Fig. 1 may be obtained with a linear "background" and a peak superimposed near  $E_{\rm c.m.} \simeq 2200$  MeV. It appears reasonable to identify this with  $N_{1/2}^*(2190)$ ; however, most data with  $E_{\rm c.m.} < 2350$  MeV represent ( $\pi$ 72),



FIG. 1. Total cross sections as a function of the total c.m. energy for the reactions  $\pi^- p \to \Lambda K^0$ ,  $\pi^- p \to \Sigma^0 K^0$ , and  $\pi^- p \to \Sigma^- K^+$ . Log-log scale is used. The lines represent least-squares fits of the data to the expression  $\sigma_T = A E_{\text{c.m.}}^B$ . The symbols are explained in Table I.



FIG. 2. Differential cross sections for the reaction  $\pi^- p \to \Lambda K^0$ . The angle  $\theta$  is defined by  $\cos \theta = \hat{P}_{K^0} \cdot \hat{P}_{\text{beam}}$  in the reaction c.m. system. The curves correspond to least-squares fits of Legendre polynomials to the data. The data are also given in Table II, and the values for the parameters of the fits in Table III.

while most data with  $E_{\rm c.m.} > 2350$  MeV were obtained in ( $\pi 63$ ). Consequently, possible systematic differences in normalization are crucial. Should the peak represent a contribution from decay of  $N_{1/2}$ \*(2190), characteristic structure will appear in angular distributions and polarizations, these considerations are discussed further in Secs. III and IV.

Recently, Morrison pointed out the existence of strong regularities in the energy dependences of cross sections for a large number of reactions.<sup>17</sup> By fitting measured cross sections to the expression

$$\sigma_T = C(p_{\rm in}/p_0)^{-n}, \qquad (5)$$

where  $p_{in}$  is the beam momentum in the laboratory system and  $p_0$  is a constant, he found that values of the exponent *n* fall into at least three distinct groups. When the reaction can be interpreted as exchange of a nonstrange meson,  $n\simeq 1.5$ ; when the reaction involves exchange of a strange meson,  $n\simeq 2.0$ ; when the reaction occurs through baryon exchange,  $n\simeq 4.0$ .

For comparison, the data in the present experiment have been fitted to expression (5). We find that n=1.45 $\pm 0.08$  for  $\pi^- p \rightarrow \Lambda K^0$ ;  $n=1.36\pm 0.13$  for  $\pi^- p \rightarrow \Sigma^0 K^0$ ; and  $n=3.78\pm 0.10$  for  $\pi^- p \rightarrow \Sigma^- K^+$ . Since the isotopic spin is  $\frac{1}{2}$  for all presently known strange mesons, it is likely that only the  $\Lambda K^0$  and  $\Sigma^0 K^0$  final states can be

<sup>&</sup>lt;sup>17</sup> D. R. O. Morrison, review paper delivered at the Conference on Two-Body Reactions, Stony Brook, April 1966 (to be published).



FIG. 3. Differential cross sections for the reaction  $\pi^- p \to \Sigma^0 K^0$ . The angle  $\theta$  is defined by  $\cos \theta = \hat{P}_{K^0} \cdot \hat{P}_{\text{beam}}$  in the reaction c.m. system. The curves correspond to least-squares fits of Legendre polynomials to the data. The data are also given in Table II, and the values for the parameters of the fits in Table III.

produced through single-meson exchange. For the  $\Sigma^-K^+$  final state, the simplest production mechanism involves baryon exchange. Consequently the observed



FIG. 4. Differential cross sections for the reaction  $\pi^- p \to \Sigma^- K^+$ . The angle  $\theta$  is defined by  $\cos \theta = \hat{P}_R^+ \cdot \hat{P}_{\text{beam}}$  in the reaction c.m. system. The curves correspond to least-squares fits of Legendre polynomials to the data. The data are also given in Table II, and the values for the parameters of the fits in Table III.

n values are roughly consistent with the pattern suggested by Morrison; however, over the energy range studied they do not support the distinction between reactions involving exchange of strange and nonstrange mesons.

## **III. DIFFERENTIAL CROSS SECTIONS**

For the analysis of differential cross sections the data were divided into 11 momentum bins centered at  $p_{in} = 1.50, 1.60, 1.70, 1.86, 1.95, 2.05, 2.20, 2.35, 2.60, 3.15$ ,



FIG. 5. Momentum-transfer distribution in the region of peripheral peaking (a)-(c) for  $\pi^- p \to \Lambda K^0$  and (d)-(f) for  $\pi^- p \to \Sigma^0 K^0$ . The lines represent maximum-likelihood fits to the expression  $d\sigma/dt = C \exp[-D(t_0-t)]$  in the region  $0 < t_0 - t < 0.4$  (BeV/c)<sup>2</sup>. The beam momenta and the fitted slope parameters are as follows. For  $\pi^- p \to \Lambda K^0$ :

	(a)	1.9–2.1 BeV/c,	D =	$6.4 \pm 0.5$	$({\rm BeV}/c)^{-2};$
	(b)	2.9–3.3 BeV/c,	D =	$7.7{\pm}0.6$	$({\rm BeV}/c)^{-2};$
	(c)	3.8–4.2 BeV/c,	D =	$9.9{\pm}1.1$	$(\mathrm{BeV}/c)^{-2}$ .
For $\pi^- p$	$\rightarrow \Sigma$	<sup>0</sup> K <sup>0</sup> :			
	(4)	$10_{-2}1 \text{ BeV}/c$	<i>n</i>	7510	$(\mathbf{D}_{a}\mathbf{V}/a)=2$

(d) 1.9-2.1 BeV/c,  $D = 7.5 \pm 1.0 (\text{BeV}/c)^{-2}$ ; (e) 2.9-3.3 BeV/c,  $D = 10.7 \pm 1.2 (\text{BeV}/c)^{-2}$ ; (f) 3.8-4.2 BeV/c,  $D = 6.3 \pm 2.0 (\text{BeV}/c)^{-2}$ .

and 4.0 BeV/c. For the first nine bins,  $\Delta p_{\rm in}$  is  $\pm 50$  MeV/c; for the bins centered at  $p_{\rm in}=3.15$  and 4.0 BeV/c, events were accepted with  $2.9 \le p_{\rm in} \le 3.3$  BeV/c and  $3.8 \le p_{\rm in} \le 4.2$  BeV/c, respectively.

The results are summarized in Table II, and are plotted in Figs. 2 to 4. The dashed curves represent least-squares fits to

$$\frac{d\sigma}{d\Omega} = \sum_{n} A_{n} P_{n}(\cos\theta), \qquad (6)$$

where  $P_n$  are Legendre polynomials, and  $\theta$  is the c.m.

		1.0	17.6	13.6	14.8	9.1	10.6	26.6	14.5 7.8 12.3		10									1.0	10~0			~		+~~~
		.95	76.6±	H8199	86.5±	$118.4\pm$	122.9+	168.5土	$106.4\pm$ 119.0\pm 123.0\pm			$52.8 \pm 23.9$	$14.2 \pm 14.7$ $10.1 \pm 14.3$	77.1±20.8	$53.1\pm 9.9$	$13.0\pm 9.5$	$34.2 \pm 18.4$ $32.0 \pm 9.3$	0.5±13.7		~	$7.0\pm2.3$ $1.4\pm0.6$ $2.0\pm1.0$	$1.7 \pm 1.0$	$0.9\pm0.9$	0.8+0.4	1.8±1.2	0.0±0.4 0.6±0.3 0.2±0.3
ction angle.		0 6.	$110.2\pm20.8$	$65.5\pm 13.4$	$73.7\pm 13.5$	$68.2\pm 6.8$	$70.3\pm7.9$	$84.6\pm 18.5$	$50.5\pm 9.7$ $49.7\pm 4.9$ $22.7\pm 5.2$		0 05	0.9+18.1 5	8.1±13.5 4	2.9±20.1 7	4.0± 7.8	$1.0\pm 8.0$ 4 $3.7\pm 16.8$	7.6±10.4 3.2± 3.6	<b>9.0± 6.7</b> 7		0.8	$0.8\pm0.8$ $0.4\pm0.4$ $1.5\pm0.9$	$2.1\pm1.0$	$1.2\pm0.4$	$0.2\pm0.2$	$0.8 \pm 0.8$	$0.4\pm0.4$ $0.0\pm0.1$ $0.2\pm0.2$
		0.8 (	0 76.0±12.2	$ \begin{array}{c} 2 \\ 0 \\ 30.4\pm 6.3 \end{array} $	6 34.8± 6.5	$7 37.5 \pm 3.5$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3 37.4± 8.6	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		8 0.9	9.1±6.5 3	$36.4\pm9.5$	$9.7\pm4.0$	16.0±3.8	$14.0\pm4.0$ $18.7\pm9.4$	$11.4\pm4.7$ $7.4\pm1.9$	$7.7 \pm 3.2$ 1		0.6	$\frac{4.8\pm2.0}{3.1\pm1.2}$ 2.9 $\pm1.2$	$3.7 \pm 1.4$	$4.0\pm0.8$ $2.7\pm0.7$	$1.0 \pm 0.4$	$1.7 \pm 1.2$	$0.0\pm0.4$ $0.1\pm0.1$ $0.0\pm0.2$
l the produ		0.6	) 37.7±6.	24.7±4.	21.3±3.	18.6±1.	19.0±2.	18.6±4.	$11.2\pm2.$ 8.1±1.0 $3.6\pm1.$		0.0	9.0±4.5	$3.3\pm 1.9$	1.2±2.9 5.5+1.5	5.5±1.5	$1.0\pm2.0$	$4.7\pm 2.1$ 5.4 $\pm 1.2$	4.2土1.6		0.4	+2.1 +1.4 +2.0	±2.1	0.0 10.0	±0.8	±1.4	±0.1 ±0.1 ±0.2
nentum and		.4	$37.9\pm6.0$	$16.5 \pm 3.2$	13.8±2.8	$11.8 \pm 1.4$	$14.0\pm1.7$	8.6±2.9	$8.1\pm 2.0$ $5.0\pm 0.8$ $0.0\pm 0.3$		0.6	$2\pm 5.5$	$2\pm3.0$	$4\pm 4.4$	$.7 \pm 1.8$	$.3\pm 2.2$ $.4\pm 5.0$ 1	$.4\pm 3.0$ $.6\pm 1.2$	·0±0.0		0.2	5.5 8.4 8.7	8.9	0 m	3.5	2.4=	0.0
beam mon		2 0	$28.8\pm 5.2$ 14 2+2 7	$9.5\pm 2.5$	$6.3 \pm 1.9$	$9.4\pm 1.2$	$10.4\pm1.5$ 6 1+1 2	7.7±2.7	$4.4\pm1.4$ 2.1 $\pm0.5$ 0.4 $\pm0.4$		0.4	(土3.2 12 1+3.3 12	十二, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,	5 11.9 14 14 14	5±2.5 7	主 <i>1.7</i> 1 1 4.5 8	)±2.2 2±0.9 5	0.0±0			$12.4\pm3.1$ 6.3 $\pm1.6$ 9.9 $\pm2.1$	$9.2\pm 2.1$	$4.7 \pm 0.9$	$2.3\pm0.6$	$0.8\pm0.8$	$0.5\pm0.0$ $0.5\pm0.2$ $0.2\pm0.2$
as a function of the	$\pi^- p \to \Lambda K^0$	0 0	$20.6\pm4.4$ 9.9+2.2	$8.2\pm 2.3$	$6.9\pm 2.0$	5.8±0.8	$5.2\pm1.0$ 1.7+0.6	$3.2 \pm 1.9$	$0.0\pm0.3$ $0.9\pm0.3$ $0.0\pm0.3$	$K^0$	0.2	±3.3 4.5	++2.5 -+	$\pm 2.2$ 12.8 $\pm 2.2$ 9.3	±1.9 13.0	±2.4 14.1 ±3.2 9.0	±2.7 5.0	±0.0 U.(	4	0.0	9 <u></u> +3.6 4+2.4 2+2.7	$7\pm 1.9$	0±0.9 9+1.1	$0\pm 0.7$	$6\pm 1.2$	$3\pm0.2$ $0\pm0.2$
		0	$5.5\pm 2.3$ 11.3+2.4	$5.8 \pm 1.9$	$4.7 \pm 1.7$	2.1±0.0	$2.5\pm0.7$ $2.1\pm0.7$	$2.9 \pm 1.7$	$0.9\pm0.0$ $1.3\pm0.4$ $0.0\pm0.3$	$\pi^-p \to \Sigma^0$	0.0	4.0 3.3 2.4 5.0	2.3	1.7 11.5	1.6 8.3	1.0 10.1 7.4 4.6	1.4 7.7 0.4 2.0	0.0	$\pi p \rightarrow L$ -0.2	-0.2	16. 13.	r- v				:00
its of $\mu \mathrm{b/s}$		-0.2	$6\pm 2.1$ $0\pm 1.6$	$5{\pm}1.3$	$1\pm 1.5$	(#0.0 2 0 2 2	$1\pm 0.7$ $3\pm 0.5$	$0\pm 1.0$	9±0.7 8±0.3 0±0.3		-0.2	6.9 4 8+	3.9+	1.2井	5.8± 62-	19.01	2.0 0.7 1 1	₩0.0		4	$16.0\pm3.5$ 17.0±2.7 15.6±2.6	$6.2\pm1.7$	$8.9\pm1.2$	$4.4 \pm 0.8$	$4.0\pm 1.8$	$1.0\pm0.3$ $0.0\pm0.2$
ection in un		-0.4	7±2.1 4. 1±0.8 5.	<u>6</u> ±0.9 2.	3±1.0 4.		1. 1. 1. 1. 1.	)±1.7 1.	日 二 二 二 二 二 二 二 二 二 二 二 二 二		0.4	$4.8\pm3.4$ $6.2\pm2.8$	4.6±2.3	$6.7\pm1.6$	$7.0\pm 1.8$	$0.0\pm 1.0$	$0.0\pm1.0$ $0.3\pm0.3$	0.U±U.0		-0-	$1\pm 4.5$ $1\pm 3.2$ $7\pm 2.9$	7 ± 2.6 7 ± 1 2	$7 \pm 1.2$	9±1.1	$1\pm 1.6$ $8\pm 1.9$	8±0.4 6±0.3
tial cross s		-0.6	E2.9 4.7 E1.8 1.1	E2.0 1.3	E2.3 1.8		E1.2 1.5 E1.1 2.5	E1.8 2.9	E0.3 0.0		ł	$1\pm 11.5$ 0+ 4.2	.1± 3.9	.5王 3.1 .5王 1.6	·2± 1.4	·7王 0.9 ·4土 2.4	.0± 1.0 .0± 0.3	0.0 <u>∓</u> 0.	-0.6	-0.6	6 27. 2 24. 18.	ی 14	4	1 7.	0 v v, v	5 4 2 0
I. Differen		-0.8	.2 8.6 <u>-</u> .1 6.5 <u>-</u>	.2 6.5 <del>-</del>	.6 8.9 <u>-</u> 2 8.9-		5.2	.4 3.1=			-0.6	7.1 42	4.0	1.1 6	1.2	2.4 2	0.3 0.3 0.5	0.0		80	$40.5\pm 5$ $36.0\pm 3$ $23.4\pm 3$	143+1	12.2±1.	7.2±1.	8.5±2. 63+1	3.4±0. 1.0±0.
TABLE I		0.9	$25.8\pm7$ 23.0±5	$28.4\pm 6$	$17.1\pm 4$	2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$14.4\pm 2$ 11.3 $\pm 2$	5.9±3	$1.2\pm0$ 1.2 $\pm0$		-0.8	$15.5\pm 9.2\pm$	11.1	3.2	$3.3\pm$	110.0	1.0 0.3 ⊥ 1.0 1.0	Ξ0.0		0	)±6.8 5±3.9 1±3.2	5±2.0 8+1.4	5十1.4	<u> </u> ±1.6	+13.0 +180	10.7
		1	41.6±9.6 38.5±6.6	$41.9 \pm 7.8$	$19.2\pm 5.0$	22 1 ± 2 3	$23.1 \pm 3.2$ 12.8 \pm 2.5	$12.4\pm 5.1$	$3.5\pm0.9$ $3.1\pm1.4$		- 0	$9.1\pm 5.2$ $1.5\pm 1.5$	$0.0\pm1.1$	5.5±1.7	$2.3\pm 1.1$ $2.0\pm 1.2$	$0.0\pm 2.4$	$0.0\pm1.0$ $0.3\pm0.3$	0.0±0.0		0-1.0	62.0 36.5	15.5	12.3	16.4	17.0	5.6
	-	$(BeV/c) \cos\theta - 1.($	1.50 1.60	1.70	1.80	1.70	2.20	2.35	3.15 4.00	/	$\frac{p_{\text{beam}}}{(\text{BeV}/c) \setminus \cos\theta} - 1.$	1.50 1.60	1.70 1.86	1.95	2.05 2.05	2.35	3.15 3.15	00.4	Pheam	(BeV/c)\cost	1.50 1.60 1.70	1.95	2.05	2.20	2.55	3.15

production angle<sup>18</sup>; the fitted coefficients  $A_n$  are given in Table III.

The dominant characteristics of the angular distributions are: (a) sharp peaking near  $\cos\theta = +1$  for both the  $\Lambda K^0$  and  $\Sigma^0 K^0$  channels which may be mediated by single-meson exchange; (b) peaking near  $\cos\theta = -1$  for the  $\Sigma^- K^+$  channel which can occur only through baryon exchange; and (c) the smaller peak near  $\cos\theta = -1$  for the  $\Lambda K^0$  channel. We discuss each of these features in turn.

Rather than use  $\cos\theta$ , it is convenient to introduce the square of the four-momentum transfer

$$t = (E_Y - E_p)^2 - (\mathbf{p}_Y - \mathbf{p}_p)^2, \qquad (7)$$

which is Lorentz invariant. The subscripts V and p denote the hyperon and proton, respectively. In the c.m.



FIG. 6. Coefficients of the Legendre-polynomial fit to the  $\pi^- p \to \Lambda K^0$  angular distribution as a function of the beam momentum. The curves represent the expansion of the function  $d\sigma/dt = C \exp[-7(t_0-t)]$  in terms of Legendre polynomials.



FIG. 7. Momentum-transfer distribution in the *u* channel for  $\pi^- p \to \Sigma^- K^+$ . The lines represent maximum-likelihood fits to the expression  $d\sigma/du = C \exp[-D(u_0-u)]$  in the region  $0 < u_0 - u < 1$  (BeV/c)<sup>2</sup>. The beam momenta and the fitted slope parameters are (a) 1.9–2.1 BeV/c,  $D=0.79\pm0.12$  (BeV/c)<sup>-2</sup>; (b) 2.9–3.3 BeV/c,  $D=1.30\pm0.30$  (BeV/c)<sup>-2</sup>; (c) 3.8–4.2 BeV/c,  $D=1.45\pm0.8$  (BeV/c)<sup>-2</sup>.

system  $dt = 2p_{F}p_{p}d(\cos\theta)$ . The maximum value  $t_{0}$  occurs at  $\cos\theta = +1$ . The distributions in  $t_{0}-t$  are shown in Fig. 5 for the  $\Lambda K^{0}$  and  $\Sigma^{0}K^{0}$  final states. The lines represent maximum-likelihood fits to the expression

$$\frac{d\sigma}{dt} = C \exp\left[-D(t_0 - t)\right] \tag{8}$$

over the region  $0 \le t_0 - t \le 0.4$  (BeV/c)<sup>2</sup>. Over the energy range covered in this experiment, secondary maxima in the differential cross sections are significant. When a wider interval of momentum transfer is included in the fit, the slope *D* changes beyond the range of errors. Consequently, the fit shown in Fig. 5 must be considered qualitative.<sup>19</sup>

To explore further the connection between the Legendre and the exponential fits, expression (8) was expanded in Legendre polynomials.<sup>20</sup> For this calculation we set D equal to 7 (BeV/c)<sup>-2</sup>; to avoid problems of normalization, the ratios  $A_n/A_0$  for each beam momentum were compared with the corresponding fitted quantities from Table III. On Fig. 6 this comparison is shown for the  $\Lambda K^0$  final state. Clearly, for the low-order

<sup>&</sup>lt;sup>18</sup> The following guideline was used for selecting the highestorder polynomial used for fitting the angular distributions: Once the need for a certain order is indicated by a rise of the confidence level in the fit, at least that order is used for all higher beam momenta.

<sup>&</sup>lt;sup>19</sup> The break in the roughly exponential distribution near t = -0.5 (BeV/c)<sup>2</sup> and the secondary peak at larger values of |t| in the  $\Sigma^0 K^0$  channel is a common feature of many two-body reactions. The dip near t = -0.5 (BeV/c)<sup>2</sup> in the reaction  $\pi^- p \to \pi^0 n$  has been interpreted as due to the vanishing of the helicity-flip amplitude at the zero in the  $\rho$  Regge trajectory by Arbab and Chiu [F. Arbab and C. B. Chiu, Phys. Rev. 147, 1045 (1966)]. Their idea has been generalized to other reactions by Frautschi [S. Frautschi, Phys. Rev. Letters 17, 722 (1966)].

<sup>&</sup>lt;sup>20</sup> The expression for the expansion coefficients can be written in a relatively simple form. The calculation is tedious to perform by hand, however. We are grateful to Dr. Gerald Lynch for illuminating conversations on this point, and for the use of a computer program he has written to perform the expansion.

		$A_{11}$										6.0土1.9																							
		$A_{10}$										$3.0\pm1.4$ $7.3\pm1.6$											$3.5\pm1.5$ $4.1\pm2.3$												
$P_n(\cos\theta).$		$A_9$										$6.7\pm 1.4$ 13.2 $\pm 2.7$											6.1±1.8 5.6±2.4												
$-/d\Omega = \sum_{nA_n} A_n$		$A_8$						$4.7{\pm}2.8$	$6.3\pm 2.6$	7.8±5.1	7.8±2.4	$12.5\pm1.7$ $14.2\pm2.7$											$10.0\pm 2.1$ 8.6 $\pm 3.1$												
tribution: do		$A_7$					$5.5 \pm 2.1$	$11.0\pm 2.5$	$13.2\pm 2.4$	$9.0{\pm}5.2$	$11.4\pm 2.6$	$17.4\pm1.8$ $17.4\pm3.0$										$5.0 \pm 4.4$	$11.7\pm 2.0$ $9.3\pm 3.0$												
e angular dis		$A_6$					$12.4\pm 2.0$	$17.0 \pm 3.0$	$18.3 \pm 3.1$	20.6±6.3	$18.0 \pm 3.3$	$21.0\pm1.8$ $18.5\pm2.8$		$8.8 \pm 8.6$	$2.8 \pm 4.8$	$2.9\pm 5.2$	$18.4\pm 5.7$	$5.0\pm 2.8$	$8.4{\pm}2.9$	$4.7 \pm 2.8$	$3.4{\pm}7.2$	$8.9{\pm}3.5$	$13.4\pm1.9$ $10.6\pm3.1$												
omials to the	icients	$A_5$	$K^0$ 5.7 $\pm 3.4$ 14.2 $\pm 2.3$	$18.2\pm 2.7$	$22.0\pm 2.7$	$22.5\pm 5.8$	$15.4\pm 3.1$	$20.3\pm1.7$ 19.7±2.8	${}^{0}K^{0}$	$10.2\pm7.0$	$12.7 \pm 4.3$	$14.5 \pm 4.1$	$16.1{\pm}4.6$	$8.0\pm 2.2$	$12.5\pm 2.4$	$9.9\pm 2.6$	$5.5 \pm 6.0$	$15.2 \pm 3.8$	$13.1\pm1.8$ $10.9\pm2.8$	-K+															
gendre polyn	Coeff	$A_4$	$\pi^- p \rightarrow \Lambda$	$9.6\pm4.8$ 21.7+3.0	$16.5 \pm 3.2$	$15.1 \pm 3.1$	$22.8{\pm}2.1$	$23.4{\pm}2.5$	25.9±2.6	$31.0\pm 5.6$	$19.5\pm 2.9$	$23.2 \pm 1.0$ $20.9 \pm 2.5$	$\pi^-p \to \Sigma$	$-3.1\pm7.5$	$7.0 \pm 4.1$	$4.3 \pm 4.1$	$8.5\pm 5.0$	$14.6\pm 2.0$	$14.7\pm 2.1$	$11.5 \pm 2.4$	$6.7 \pm 6.0$	$11.5 \pm 3.1$	$11.5\pm1.7$ $12.1\pm2.6$	$\pi^- b \rightarrow \Sigma^-$	4 :									0.6±0.3	0.0±0.4
lares fit of Le		$A_3$		$-6.1\pm4.7$ $-0.6\pm2.7$	$-2.7\pm 2.8$	$10.0 \pm 3.3$	$13.1 \pm 1.9$	$13.4{\pm}2.2$	$25.2\pm 2.3$	$27.8 \pm 4.9$	18.5±2.0	$21.1\pm 1.4$ $18.8\pm 2.1$		11.9±5.8	$17.4 \pm 3.3$	$17.0 \pm 3.5$	9.6土4.0	$9.7{\pm}1.9$	$10.6 \pm 1.9$	$4.7{\pm}2.0$	$6.3\pm 5.0$	$9.7 \pm 3.1$	$9.5\pm1.5$ 12.3±2.2								0.6±0.6	$-3.0\pm1.5$	$-1.3\pm0.6$	$-1.1\pm0.3$	-0.1 HU.J
i the least-squ		$A_2$		$33.7\pm4.5$ $26.1\pm2.7$	$28.1 \pm 3.1$	$26.9 \pm 2.8$	$33.7{\pm}1.6$	$31.0{\pm}1.8$	$36.0{\pm}1.9$	$35.7 \pm 4.1$	25.4±2.2	21.0±1.1 17.8±1.7		9.5土4.2	$7.9\pm2.7$	8.9±2.8	$10.7 \pm 3.1$	$6.8 \pm 1.7$	$6.7 \pm 1.8$	$4.2{\pm}1.8$	$8.5 \pm 4.2$	9.5±2.5	$9.8\pm 1.2$ 11.4 $\pm 1.8$		$14.1{\pm}2.5$	9.1 + 1.4	$2.6\pm 1.4$	$-0.2\pm1.3$	$1.0 \pm 0.6$	$0.8 \pm 0.6$	$3.2 \pm 0.7$	$5.5 \pm 1.4$	$3.2\pm0.7$	$2.0\pm0.5$	···日7.F
Coefficients of		$A_1$		$25.8\pm 3.4$ $11.4\pm 2.0$	$10.4\pm 2.3$	$15.3\pm 2.1$	$16.2 \pm 1.2$	$17.7 \pm 1.3$	$23.3 \pm 1.4$	$24.7\pm 2.9$	18.1±1.0	11.0±1.1		$0.4 \pm 3.4$	$4.8{\pm}2.0$	$6.5 \pm 2.1$	$9.3 \pm 2.4$	$7.5 \pm 1.2$	$9.1{\pm}1.2$	$10.0 \pm 1.3$	$12.8 \pm 3.1$	$11.0 \pm 1.7$	$9.2 \pm 0.8$ $8.2 \pm 1.2$		$-28.2\pm2.2$	$-22.0\pm1.4$	$-14.3\pm1.3$	$-6.5\pm1.0$	-8.4±0.6	$-7.1\pm0.6$	$-6.8\pm0.5$	$-5.9\pm1.2$	$-4.4\pm0.6$	$-2.0\pm0.3$	7.0HC.0-
TABLE III. (		${\cal A}_0$		$25.4\pm1.6$ $16.4\pm1.0$	$15.4\pm 1.0$	$13.9{\pm}1.0$	$14.5 \pm 0.5$	$14.3 \pm 0.5$	$13.9 \pm 0.6$	$13.6\pm 1.2$	8.3±0.0	7.0±0.3 4.4±0.4		$10.4{\pm}1.7$	$7.9{\pm}1.0$	$7.9{\pm}1.0$	$9.5 \pm 1.1$	$8.9{\pm}0.6$	$8.4{\pm}0.6$	$8.4{\pm}0.7$	$7.3 \pm 1.5$	$5.8 \pm 0.8$	$4.2\pm0.3$ $3.0\pm0.5$		18.3±1.2 -	14.0±0.8 -	11.8±0.7 -	$7.4 \pm 0.6$	$7.5 \pm 0.3$	$6.3 \pm 0.3$	$4.3 \pm 0.3$	$3.8\pm0.5$	$2.3\pm0.3$	1.3±0.1	T'NHON
	h.h.;11:4			10.6 94.8	68.5	37.2	53.0	44.6	44.4	58.3	2.00	24.3 0.8		9.1	22.8	23.3	44.7	6.8	26.1	90.5	23.5	14.5	1.5 50.6		8.5	57.8	37.3	14.3	25.9	97.8	0.1	62.1 22.2	93.9 25.0	57.9	1.10
		x <sup>2</sup>		13.18 2.78	5.66	7.58	4.13	3.71	3.73	2.85	4.04	9.70		9.48	6.90	6.84	4.75	11.73	7.69	2.16	6.81	6.84	12.39 1.36		12.53	5.68	7.56	10.01	8.92	1.61	23.73	4.42	1.17	2.00 00.5	20.4
	-	(BeV/c)		1.50 1.60	1.70	1.86	1.95	2.05	2.20	2.35	2.00	4.00		1.50	1.60	1.70	1.86	1.95	2.05	2.20	2.35	2.60	3.15 4.00		1.50	1.60	1.70	1.80	1.95	2.05	2.20	2.35	7.00	61.6 4 00	>>•F

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coefficients  $(n \le 5)$ , the expansion gives consistently larger values of  $A_n/A_0$  than the fit to the differential cross section. For the high-order coefficients  $(n \le 6)$ , however, the agreement in size and energy dependence is remarkably good. This suggests, that the appearance of higher partial waves is dictated by the peripheral peak alone.

In the presence of an *s*-channel resonance strongly coupled to the  $\Lambda K^0$  system, it may be expected that the coefficients  $A_n/A_0$  will vary rapidly in the neighborhood of the resonance. The behavior of all coefficients shown on Fig. 6 is smooth; consequently the data show no evidence for any *s*-channel resonance. In particular we find no evidence for the process  $\pi^- p \rightarrow N^*(2190) \rightarrow \Lambda K^0$ .

The  $\Sigma^-K^+$  final state, in contrast to  $\Lambda K^0$  and  $\Sigma^0 K^0$ shows no peripheral peaking. What one observes is rather an "antiperipheral" peak, near  $\cos\theta = -1$ . This behavior follows the pattern of other reactions such as  $K^-p \to \Xi^-K^+$ , where the *t*-channel quantum numbers require the exchange of an  $I = \frac{3}{2}$  strange meson. It is therefore plausible to assume that the dominant contribution to the reaction arises from *baryon exchange* in the *u* channel.<sup>21</sup> Among the known baryons those with I=0 or 1 can contribute in the  $\Sigma^-K^+$  reaction. However, the lack of "antiperipheral" peaking in the  $\Sigma^0 K^0$  case, where only I=1 baryons could be exchanged, suggests the dominance of I=0 exchange.<sup>22</sup>

In analogy with Eq. (7) we define the Lorentzinvariant four-momentum transfer squared in the u



FIG. 8. Coefficients of the Legendre-polynomial fit to the  $\pi^- p \rightarrow \Sigma^- K^+$  angular distribution as a function of the beam momentum.



channel as

$$\boldsymbol{u} = (E_K - E_p)^2 - (\mathbf{p}_K - \mathbf{p}_p)^2. \tag{9}$$

In the c.m. system we have  $du = -2p_K p_p d(\cos\theta)$ . The maximum value  $u_0$  occurs when  $\cos\theta = -1$ . The distribution in  $u_0 - u$  is presented on Fig. 7. The line superimposed on the data represents a maximum-likelihood fit to the expression

$$\frac{d\sigma}{du} = C \exp[-D(u_0 - u)] \tag{10}$$

in the region  $0 \le u_0 - u \le 1$  (BeV/c)<sup>2</sup>.

The  $\Sigma^-K^+$  channel also differs from  $\Lambda K^0$  and  $\Sigma^0 K^0$ in the simplicity of its production angular distribution. The Legendre-polynomial fit is in reasonable agreement with the expansion of expression (10), [with D=1.4 $(\text{BeV}/c)^{-2}$ ] above 2.2 BeV/c. This behavior suggests that the interaction volume is considerably smaller for  $\pi^-p \rightarrow \Sigma^-K^+$  than for  $\pi^-p \rightarrow \Lambda K^0$ ,  $\Sigma^0 K^0$ , or most other reactions. Below 2.2 BeV/c the fit to Legendre polynomials up to second order is adequate. To remove the dependence on the total cross section, we divide by  $A_0$ ,

TABLE IV. Least-squares fit of the energy dependence of the cross sections to the expression  $d\sigma/dt$  (or  $d\sigma/du$ ) =  $FE_{\text{c.m.}}^{m}$ .

Reaction	Momentum-trans- fer interval (BeV/c) <sup>2</sup>	Data points	$\chi^2$	m
$\pi^- p \longrightarrow \Lambda K^0$	$0 < t_0 - t < 0.4$	10ª	15.8	$-2.0{\pm}0.4$
	$0.4 < t_0 - t < 0.8$	10ª	8.5	$-4.7{\pm}0.5$
	$0 < u_0 - u < 1.0$	10ª	18.3	$-10.5 \pm 0.6$
$\pi^-  ho  o \Sigma^0 K^0$	$0 < t_0 - t < 0.4$	11	3.0	$-1.5{\pm}0.6$
	$0.4 < t_0 - t < 0.8$	11	10.1	$-5.1{\pm}0.8$
$\pi^- p \longrightarrow \Sigma^- K^+$	$0 < u_0 - u < 1.0$	11	13.3	$-9.8{\pm}0.4$
	$1.0 < u_0 - u < 2.0$	7ь	3.8	$-11.5 \pm 0.9$

<sup>a</sup> The point at 1.5 BeV/c was eliminated because it fell several standard deviations outside the fit. <sup>b</sup> Only data above 1.9 BeV/c were used, because at lower momentum, kinematics does not allow the momentum transfer  $u_0 - u = 2$  (BeV/c)<sup>2</sup>.

<sup>&</sup>lt;sup>21</sup> For a review of the analysis of other reactions in terms of baryon exchange, see Peter E. Schlein, in *Lectures in Theoretical Physics* (University of Colorado, Boulder, Colorado, 1966), Vol. VIIIB, p. 111; and L. Lyons, Nuovo Cimento 43, A888 (1966).

<sup>&</sup>lt;sup>22</sup> The contribution of I=1 baryon exchange to  $\Sigma^0 K^0$  would have to be twice as large as to  $\Sigma^- K^+$ .



FIG. 10. Distribution of the quantity  $\alpha_{\Lambda} \mathcal{O}(d\sigma/d\Omega)$  for the reaction  $\pi^- p \to \Lambda K^0$ . The angle  $\theta$  is defined by  $\cos\theta = \hat{p}_{K^0}, \hat{p}_{\text{beam}}$  in the production c.m. system. The curves represent least-squares fits to the series  $\sin\theta \sum_n B_n [dP_{n1+}(\cos\theta)]/d(\cos\theta)$ . The data are also given in Table V, and the parameters of the fit in Table VI.

and present the ratios  $A_1/A_0$  and  $A_2/A_0$  on Fig. 8. It is interesting to note that the fitted coefficients  $A_1$  and  $A_2$  go through marked variations near 1.9 BeV/c. We have no explanation for the observed behavior.

The "antiperipheral" peak in the  $\Lambda K^0$  final state can also be considered in terms of a baryon-exchange model. Here, as in the  $\Sigma^0 K^0$  case, only hyperons with I=1 can contribute in the *u* channel.<sup>23</sup> In Fig. 9 we present the  $d\sigma/du$  distribution in the 2-BeV/*c* region only. At higher energies the number of events near

 $\begin{array}{lll} A_{\Sigma^{\bullet}K^{+}} = & C_{1}\Sigma + C_{2}Y_{1}^{*}(1385) + C_{3}\Lambda, \\ A_{\Sigma^{0}K^{0}} = & -\sqrt{2}C_{1}\Sigma - \sqrt{2}C_{2}Y_{1}^{*}(1385), \\ A_{\Delta K^{0}} = & C_{4}\Sigma - (\sqrt{6})C_{2}Y_{1}^{*}(1385), \end{array}$ 

where the particle symbols on the right represent the contribution from the exchange of that object. If the ratio of d- and f-type coupling is d/>1.0, we find that (a)  $C_3/C_1 \ge 3$ , and (b) the relative sign of the coefficients for  $\Sigma$  and  $V_1^*(1385)$  is different for  $\pi^-p \to \Lambda K^0$  and for  $\pi^-p \to \Sigma K$ . For d/f=1.5, for example, we have  $C_1=4/25$ ,  $C_2=1/6$ ,  $C_4=18/25$ , and  $C_4=(2\sqrt{6})/25$ . The lack of a baryon exchange peak in the  $\pi^-p \to \Sigma^0 K^0$  differential cross section can then be interpreted as destructive interference between the Xand the  $V_1^*(1385)$ . The same holds for  $\pi^-p \to \Sigma^- K^+$ , and  $\Lambda$ exchange is expected to give a large cross section. For the reaction  $\pi^-p \to \Lambda K^0$  the interference between  $\Sigma$  and  $V_4^*(1385)$  becomes constructive, and a sizeable baryon exchange peak can be expected, as is found in the experiment. We thank Professor David Jackson for bringing this argument to our attention.

	1.0	$70.4\pm 25.6$	$7.0\pm 16.0$	$3.5 \pm 15.6$	$11.1 \pm 18.8$	$17.3 \pm 10.8$	$37.5\pm 12.5$	$14.7 \pm 14.3$	$24.4 \pm 32.4$	$1.0 \pm 18.3$	$10.8 \pm 8.7$	$-6.3\pm 12.3$
	0.0	64.2±18.2	$8.4{\pm}13.1$	$4.3 \pm 10.1$	$23.8 \pm 11.7$	$21.2\pm 6.4$	$24.0\pm 7.0$	$26.3 \pm 7.8$	$14.2 \pm 16.0$	$14.3 \pm 9.9$	$7.2 \pm 3.6$	-9.0± 5.7
	0.8	$16.9 \pm 10.8$	$12.9\pm 5.7$	$12.0\pm 7.0$	$10.9 \pm 6.6$	$-0.6\pm 3.2$	$4.0\pm3.4$	$-3.8\pm3.5$	-11.9± 9.1	$-3.7 \pm 3.8$	$-4.8\pm 1.7$	$-1.9\pm 2.0$
ı angle.	0.6	23.6±11.7	$9.5\pm 4.9$	$11.1\pm 5.7$	$7.1\pm 5.3$	$-2.1\pm 2.6$	-2.6± 3.3	$-10.4\pm 2.9$	-9.3±5.9 -	$-5.4\pm 3.0$	$-3.2\pm 1.5$	-0.0± 0.2
and production	0.4	$-7.0\pm10.2$	$1.6\pm 6.2$	-7.2± 4.2	$-5.3\pm 3.3$	-4.4土 2.3	$0.2\pm 2.3$	-2.5±1.9 -	-3.2± 5.8	$-4.8\pm 2.7$	$0.0 \pm 0.7$	1.2± 1.2
m momentum	) 0.2	-6.2±9.2	$-5.1\pm3.9$	$-7.1\pm5.0$	-3.5±4.4 -	$-2.1\pm1.6$	$-1.9{\pm}1.8$	-1.2±0.9 -	3.9±4.4 -	0.0±0.4	$-0.3\pm0.7$	$-0.0\pm0.2$
inction of bear	.2 0.0	$-3.6\pm 2.7$	$-6.1\pm 5.1$	$-1.5\pm4.2$	$-3.0\pm 2.1$	$0.0 \pm 0.7$	$0.3 \pm 1.1$	$-0.2\pm1.1$	$1.2 \pm 3.6$	$0.5 \pm 0.5$	$-1.2\pm0.7$	-0.0±0.2
of μb/sr as a fi	4 -0	$-9.4\pm4.9$	$1.3 \pm 2.1$	$-4.1\pm 2.9$	$-6.6\pm3.5$	$-1.2\pm0.9$	$-1.9{\pm}1.4$	$-1.7\pm1.1$	$-3.5\pm3.5$	$0.4{\pm}0.4$	$1.0 \pm 0.8$	$-0.0\pm0.2$
given in units	9.	$-3.1\pm3.5$	$-0.1\pm1.2$	$2.7 \pm 1.9$	$1.8{\pm}1.6$	$1.0 \pm 1.5$	$0.1{\pm}1.3$	$-1.3\pm1.5$	$-5.3\pm3.8$	$-0.0\pm0.4$	$-0.1\pm0.1$	$-0.0\pm0.2$
	8.	$0.7{\pm}1.9$	$0.4 \pm 3.5$	$1.3 \pm 4.7$	$-5.7\pm4.1$	$-1.5\pm 2.1$	$-0.2\pm2.2$	$0.5 \pm 1.7$	$-5.9\pm5.3$	$1.7 \pm 1.3$	$-0.0\pm0.1$	0.3±0.3
	0-	$10.0 \pm 10.4$	$3.6\pm 6.9$	$7.0\pm 8.2$	5.3土 6.9	$0.2\pm 3.6$	4.4土 3.7	$5.3 \pm 3.4$	$-1.2\pm5.7$	$3.6\pm 2.0$	$1.6\pm 0.8$	-1.1± 2.0
	$\frac{p_{\text{beam}}}{(\text{BeV}/c) \cos\theta} - 1.0$	1.50	1.60	1.70	1.86	1.95	2.05	2.20	2.35	2.60	3.15	4.00

TABLE V. Distribution of the polarization times the differential cross section for the reaction  $\pi^- p \rightarrow \Lambda K^0$ . The values of  $\alpha \rho (d\sigma/d\Omega)$  are

<sup>&</sup>lt;sup>23</sup> The relative size of the baryon exchange peaks in the three reactions considered can be understood in the framework of  $SU_3$  invariance. If we assume that the I=0 contribution comes from  $\Lambda$ , and that the I=1 contribution comes from  $\Sigma$  and  $Y_1^*(1385)$  exchange, the amplitudes for the three reactions become

TABLE VI. Coefficients of the least-squares fit of the angular distribution of A polarization in the reaction $\pi^- \rho \rightarrow \Lambda K^0$ to the series
$\alpha  \theta  d\sigma / d\Omega = \sin \theta  \sum_n B_n \left[ dP_{n+1}(\cos \theta) / d(\cos \theta) \right].$

¢ <sub>beam</sub> (BeV/c)	$\chi^2$	Probabilit (%)	У В о	$B_1$	$B_2$	$B_3$	$B_4$	$B_5$	<i>B</i> <sub>6</sub>
$\begin{array}{c} 1.50\\ 1.60\\ 1.70\\ 1.86\\ 1.95\\ 2.05\\ 2.20\\ 2.35\\ 2.60\\ 3.15\\ 4.00\\ \end{array}$	$\begin{array}{c} 6.66\\ 3.72\\ 5.78\\ 7.45\\ 5.49\\ 4.74\\ 5.53\\ 0.35\\ 1.91\\ 6.19\\ 1.25 \end{array}$	35.4 71.5 44.8 28.1 35.9 44.8 35.5 98.6 75.3 28.8 87.0	$\begin{array}{c} +5.0{\pm}2.8\\ +2.4{\pm}1.7\\ +5.0{\pm}1.8\\ +1.1{\pm}1.6\\ -0.2{\pm}0.8\\ +1.6{\pm}0.9\\ -1.1{\pm}0.8\\ -2.8{\pm}2.1\\ -0.4{\pm}0.8\\ -0.5{\pm}0.4\\ -0.7{\pm}0.4\end{array}$	$\begin{array}{c} +9.1\pm2.5\\ +3.7\pm1.5\\ +1.7\pm1.6\\ +3.6\pm1.6\\ +1.3\pm0.9\\ +2.3\pm0.9\\ +0.1\pm0.9\\ +0.8\pm2.2\\ -0.9\pm1.0\\ -0.3\pm0.4\\ -1.0\pm0.5\end{array}$	$\begin{array}{r} +10.8\pm2.2\\ +3.1\pm1.5\\ +3.9\pm1.6\\ +4.2\pm1.5\\ +2.3\pm0.8\\ +3.7\pm0.9\\ +2.8\pm0.9\\ -0.2\pm2.0\\ +1.4\pm1.0\\ +0.7\pm0.4\\ -1.1\pm0.6\end{array}$	$\begin{array}{c} +4.2\pm2.0\\ +1.2\pm1.2\\ +0.8\pm1.2\\ +2.5\pm1.2\\ +2.6\pm0.8\\ +2.6\pm0.8\\ +2.3\pm0.9\\ +2.1\pm1.9\\ +1.3\pm1.0\\ +0.7\pm0.4\\ -0.9\pm0.5\end{array}$	$\begin{array}{c} +3.6 \pm 1.7 \\ -0.3 \pm 1.1 \\ -0.9 \pm 1.1 \\ +0.2 \pm 1.0 \\ +1.9 \pm 0.7 \\ +3.0 \pm 0.8 \\ +3.4 \pm 0.8 \\ +3.9 \pm 1.8 \\ +2.0 \pm 0.9 \\ +1.4 \pm 0.4 \\ -0.7 \pm 0.4 \end{array}$	$+0.9\pm0.5$ $+1.3\pm0.6$ $+1.4\pm0.6$ $+2.1\pm1.5$ $+0.7\pm0.5$ $+0.9\pm0.3$ $-0.3\pm0.2$	$+0.3\pm0.5$ $+0.9\pm0.5$ $+0.8\pm0.5$ $+0.8\pm1.3$ $+0.3\pm0.4$ $+0.6\pm0.2$ $-0.2\pm0.2$

 $\cos\theta = -1$  is too small to give a meaningful spectrum.

We fitted the energy dependence of the differential cross section at constant momentum transfer to the expression

$$\frac{d\sigma}{dt} = FE_{\text{c.m.}}^{m} \tag{11}$$

in the region of the peripheral peaks. For the antiperipheral peaks we fitted  $d\sigma/du$  to an expression of the same form. Results of the fit are presented in Table IV. We note that

(a) the values of the exponent *m* found for the  $\Lambda K^0$ and  $\Sigma^0 K^0$  data are similar for the peripheral peak;

(b) the values of *m* found for the  $\Lambda K^0$  and  $\Sigma^- K^+$  data are similar for the antiperipheral peak;

(c) the cross sections fall faster at larger momentum transfer. This "shrinking" of the peaks may indicate some Regge-type behavior.

The data presented allow us to make a few comments concerning the reaction  $\pi^+ p \rightarrow \Sigma^+ K^+$  in the 3- to 4-BeV/c range. We use the relation between the complex amplitudes  $A^+$ ,  $A^0$ , and  $A^-$  for the reactions  $\pi^+ p \rightarrow \Sigma^+ K^+$ ,  $\pi^- p \rightarrow \Sigma^0 K^0$ , and  $\pi^- p \rightarrow \Sigma^- K^+$ , respectively. Charge independence predicts

$$A^{-} + \sqrt{2}A^{0} = A^{+}.$$
 (12)

Near  $\cos\theta = +1$  the cross section for the  $\Sigma^- K^+$  reaction is much smaller than that for  $\Sigma^{0}K^{0}$ , and therefore  $A^{-}$  is small compared to  $A^0$  ( $A^0$  is small compared to  $A^-$  near  $\cos\theta = -1$ ). In a first approximation we neglect the small amplitude, to obtain  $(d\sigma/d\Omega)_{\Sigma^+K^+} \approx 2(d\sigma/d\Omega)_{\Sigma^0K^0}$ near  $\cos\theta = +1$ , and since the total cross section is dominated by the peripheral peak, we have  $(\sigma_T)_{\Sigma^+K^+}$  $\sim 2(\sigma_T)_{\Sigma^0 K^0}$  above 3 BeV/c. In the same way we find that  $(d\sigma/d\Omega)_{\Sigma^+\kappa^+}$  will have a small peak of the same order of magnitude as  $(d\sigma/d\Omega)_{\Sigma^-K^+}$  near  $\cos\theta = -1.^{24}$ 

### IV. POLARIZATION

For the reaction  $\pi^- p \rightarrow \Lambda K^0$  the  $\Lambda \rightarrow p \pi^-$  decay is a good analyzer of the  $\Lambda$  polarization. The angular distribution of the decay proton with respect to the production normal  $\mathbf{n} = \mathbf{p}_{\text{beam}} \times \mathbf{p}_{K^0}$  is of the form  $(1+\alpha_{\Lambda} \Theta \cos \xi)$ , where  $\alpha_{\Lambda}=0.66$  is the asymmetry parameter,  $\mathcal{O}$  is the polarization, and  $\xi$  is the angle between the momentum of the decay proton and  $\mathbf{n}$  in the  $\Lambda$  rest frame. The product of the differential cross section and the polarization at the production angle  $\theta$ is given by

$$\alpha_{\Lambda} \mathcal{P}(\theta) \frac{d\sigma}{d\Omega} = 3c \sum_{i} \cos \xi_{i},$$

where the sum is over the events within an interval of the production angle,<sup>25</sup> and the constant c converts this sum into cross-section units.

The results are presented in Fig. 10 and Table V. The curves on Fig. 10 represent least-squares fits to the form18

$$\alpha_{\Lambda} \mathcal{P}(\theta) \frac{d\sigma}{d\Omega} = \sin\theta \sum_{n} B_{n} \frac{dP_{n+1}(\cos\theta)}{d(\cos\theta)},$$

where  $P_n$  is the *n*th-order Legendre polynomial. The fitted coefficients  $B_n$  are shown in Table VI. In Fig. 11 we present the polarization as a function of the momentum transfer. The size and shape of the distribution are similar for the data near 2 and 3 BeV/c.<sup>26</sup> We find the polarization positive at low momentum transfer, then negative in the region  $t-t_0 \approx -1$  (BeV/c)<sup>2</sup>. The crossover point is near  $t-t_0 = -0.5$  (BeV/c)<sup>2</sup>. The

$$\sum_{i} \frac{\cos \xi_{i}}{\epsilon_{i}} \pm \left[\sum_{i} \left(\frac{\cos \xi_{i}}{\epsilon_{i}}\right)^{2}\right]^{1/2}$$

<sup>&</sup>lt;sup>24</sup> Data on the reaction  $\pi^+ p \to \Sigma^+ K^+$ , and a comparison with the other  $\Sigma K$  channels along the lines outlined here have recently been presented. See R. R. Kofler, R. H. Hartung, and D. D. Reeder, contribution of the XIIIth International Conference on With Description (2006) Red L. C. With Statement of the Statement of t High-Energy Physics, 1966, Berkeley, California (University of California Press, Berkeley, 1967).

<sup>&</sup>lt;sup>25</sup> Actually the term in the sums were weighted by the inverse of the detection probability  $\epsilon_i$ . The complete sum, including the error is then

See F. T. Solmitz, Ann. Rev. Nucl. Sci. 14, 375 (1964), especially

p. 399. <sup>26</sup> Our results are in good agreement with the polarization measurements at 1.5 BeV/c by Yoder *et al.* (Ref. 2), at 1.59 BeV/c by Goussu *et al.* (Ref. 3), and at 1.5 and 1.8 BeV/c by Kim *et al.* (Ref. 1).



FIG. 11. Polarization of the  $\Lambda$  in the reaction  $\pi^- p \rightarrow \Lambda K^0$  as a function of the momentum transfer squared. The data for the 1.9- to 2.1-BeV/c interval are shown as circles; those for the 2.9- to 3.3-BeV/c interval are shown as triangles.

largest negative value of the polarization remains consistent with 100% even at the highest beam momenta.

We note that the simplest one-particle- and one-Regge-pole-exchange models predict no polarization for the final-state hyperon. Using a model based on the exchange of both the  $K^*(890)$  and  $K^*(1410)$  Regge trajectories, Sarma and Reeder<sup>27</sup> successfully fitted both the angular distribution and the  $\Sigma^+$  polarization in the reaction  $\pi^+ \not p \rightarrow \Sigma^+ K^+$  at 3.23 BeV/ $c.^{24}$  Since the qualitative features of the  $\Sigma^+ K^+$  channel are strikingly similar to the data presented here, extension of their analysis to include the  $\Lambda K^0$  final state seems highly desirable.<sup>28</sup>

Due to lack of statistics in  $\Sigma^0$  and to the small value of the asymmetry parameter in  $\Sigma^-$  decay, we have no significant results on  $\Sigma$  polarization.<sup>29</sup>

## V. SUMMARY

In summary, we find that the dominant features of the reactions  $\pi^- p \rightarrow \Lambda K^0$ ,  $\Sigma^0 K^0$ , and  $\Sigma^- K^+$  can be described in terms of meson and baryon exchange in the t and u channels, respectively. All cross sections decrease with increasing beam momentum, more slowly for meson exchange than for baryon exchange. The polarization of the  $\Lambda$  in  $\pi^- p \rightarrow \Lambda K^0$  remains large in the region of moderate momentum transfer  $[|t| \leq 1 (\text{BeV}/c)^2]$ , even at the highest energies available in this experiment.

The energy dependence of the total cross sections and the momentum-transfer distribution is suggestive of Regge-type behavior. In terms of the Regge picture the observed polarization requires that two  $K^*$  trajectories contribute to  $\pi^- p \rightarrow \Lambda K^0$ .

The results presented indicate a break in the peripheral peaks near  $t-t_0 = -0.5$   $(\text{BeV}/c)^2$  and a change of sign of the  $\Lambda$  polarization at about the same value of the momentum transfer. Similar phenomena observed in several other reactions<sup>24,30</sup> have been associated with the passage of the exchanged Regge trajectories through zero.<sup>19,27</sup>

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<sup>&</sup>lt;sup>27</sup> K. V. L. Sarma and D. D. Reeder, University of Wisconsin Report, 1966 (unpublished).

<sup>&</sup>lt;sup>28</sup> A model involving two Regge-pole exchange has also been developed by Arnold [R. C. Arnold, Phys. Rev. **153**, 1506 (1967)]. <sup>29</sup> Polarization of the  $\Sigma^0$  has been measured at 1.5 and 1.8 BeV/*c* by Y. S. Kim, G. R. Burleson, P. I. P. Kalmus, A. Roberts, and T. A. Romanowsky, Phys. Rev. **143**, 1028 (1966).

<sup>&</sup>lt;sup>30</sup> For a list of references on this subject see S. Frautschi, Ref. 19.