was experimentally observed by Albers-Schönberg et  $al.^2$  by using a metallic indium single crystal. Qualitatively, the observed phase shift can be explained from the present theory as due to the thermal vibrations of the lattice points. The effect of these thermal vibrations is to produce, at the site of the radioactive nucleus, an asymmetric fluctuating electric field gradient which is responsible for the phase shift in the rotational pattern of anisotropy.

### **IV. CONCLUSION**

In this formalism one has a systematic treatment which contains a description of the effects of the changes of the state of the environment. For a solid-state environment the present theory predicts a temperature dependence of the anisotropy.

The rotational dependence of the angular correlation has been developed for the cases of asymmetric crystalline fields. This will greatly increase the interpretability of experiments and the possibility of investigating nuclear quadrupole moments in excited states. For the case of an axially symmetric crystalline field, Eq. (5.5) predicts the phase shift in the rotational pattern of anisotropy as a function of crystal temperature.

The accuracy of the calculation of the nuclear electric quadrupole moment depends highly on the computations of the electrostatic field gradient at the nuclear site. The calculation of this crystalline field is very difficult and a model for the charge distribution in the lattice system is needed. Here we use the point-charge model and introduce an adjustable parameter  $\xi_i$ , to take the shielding, antishielding, and covalent effects into account. For the determination of this parameter one has to rely entirely on other measurements.<sup>20</sup>

Since a sufficient knowledge of the wave function of the electronic shell is available,23 the present theory [i.e., Eqs. (2.12) and (2.13)] will be suitable to investigate the effect of the nuclear spin relaxation due to coupling with atomic electrons on the angular correlation.<sup>24</sup>

<sup>23</sup> K. D. Bowers and J. Owen, Rept. Progr. Phys. 18, 304 (1955).
 <sup>24</sup> H. J. Leisi and R. T. Deck, Phys. Rev. 129, 2117 (1962).

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# **A-Binding Energies in Heavy Hyperfragments** $(35 \leq A \leq 80)$

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Analysis of 16 short-range ( $\leq 10\mu$ ) hyperfragments, produced from 1.5-GeV/c K<sup>-</sup> interactions in L<sub>4</sub> hypersensitized emulsions and decaying  $\pi^-$ -mesonically, is presented. Of these, 9 are classified as due to the residual spallation products of silver and bromine nuclei, 5 as beloning to lighter species ( $A \leq 20$ ), and 2 as ambiguous. The masses of the 9 spallation hyperfragments are determined using the "spallation model." It is concluded that for hyperfragments of masses  $A \simeq 35$  to 80, the upper limits of  $B_{\Lambda}$  could vary from 21.9 to 24.5 MeV.

### I. INTRODUCTION

**POLLOWING** Jones *et al.*,<sup>1</sup> it is now generally believed that the majority of hyperfragments (HF's) of ranges  $\leq 10 \,\mu$  produced by high-energy K<sup>-</sup> interactions at momenta 0.8,1-3 1.3 and 1.5,4 2.2,5 and 3.06 GeV/c and of ranges  $\leq 3 \mu$  produced by K<sup>-</sup>-at-rest<sup>7</sup> interactions are the residual spallation products of silver and bromine nuclei, and possess mass numbers in the range  $A \simeq 20$  to 100, the limits on A depending on the  $K^-$  momentum used. The determination of the  $\Lambda$  binding energies  $(B_{\Lambda})$  and masses of these heavy<sup>8</sup> HF's is of great interest since these can be effectively utilized for estimating the potential well-depth  $D_{\Lambda}$  seen by a  $\Lambda$  particle in nuclear matter.

In their first investigation, Davis et al.<sup>9</sup> used  $K^$ interactions at momenta 0, 0.8, and 1.5 GeV/c and reported 5 examples of  $\pi^-$ -mesonic decays of short-range HF's attributed to mass numbers  $A \simeq 60$  to 100. Although the calculated values of the upper limits of

<sup>&</sup>lt;sup>1</sup>B. D. Jones, B. Sanjeevaiah, J. Zakrzewski, M. Csejthey-Barth, J. P. Lagnaux, J. Sacton, M. J. Beniston, E. H. S. Burhop, and D. H. Davis, Phys. Rev. 127, 236 (1962).

<sup>&</sup>lt;sup>2</sup> N. A. Nickols, S. B. Curtis, and D. J. Prowse, Phys. Letters 1, 327 (1962).

<sup>&</sup>lt;sup>321</sup> (1962).
<sup>8</sup> I. R. Kenyon, Nuovo Cimento 29, 589 (1963).
<sup>4</sup> E. R. Fletcher, J. Lemonne, P. Renard, J. Sacton, D. O'Sullivan, T. P. Shah, A. Thompson, P. Allen, Sr., M. Heeran, A. Montwill, J. E. Allen, M. J. Beniston, D. A. Garbutt, R. C. Kumar, P. V. March, T. Pniewski, and J. Zakrzewski, Phys. Letters 3, 280 (1963).
<sup>6</sup> R. J. Prem and P. H. Steinberg, University of Maryland report, 1963 (unpublished).
<sup>6</sup> J. Lemonne, I. Sacton, G. Schorochoff, M. A. Sheuhet, W. W.

<sup>&</sup>lt;sup>6</sup> J. Lemonne, J. Sacton, G. Schorochoff, M. A. Shaukat, W. T. Toner, P. Allen, D. H. Davis, E. R. Fletcher, J. E. Allen, V. A. Bull, M. M. Kasim, P. V. March, K. Pniewska, T. Pniewski, M. Suk, M. Votruba, J. Herynek, J. Piekarz, and J. Zakrzewski, Université de Bruseller, Bulleti, M. 19, 164 (doct de lite) Université de Bruxelles-Bulletin No. 18, 1964 (unpublished).

<sup>&</sup>lt;sup>7</sup> J. Lemonne, C. Mayeur, J. Sacton, D. H. Davis, D. A. Garbutt, and J. E. Allen, Nuovo Cimento 34, 529 (1964). <sup>8</sup> Henceforth we shall denote HF's having A > 20 as "heavy,"

<sup>≤ 20</sup> as "light."

<sup>&</sup>lt;sup>9</sup>D. H. Davis, R. Levi Setti, M. Raymund, O. Skjeggestad, G. Tomasini, J. Lemonne, P. Renard, and J. Sacton, Phys. Rev. Letters 9, 464 (1962).

 $B_{\Lambda}$  of these HF's were found to range from 23.1 to 38.5 MeV, the authors considered an upper limit of  $B_{\Lambda}$  at about 25 MeV as valid for the total sample of HF's, keeping in view the fact that the excitation of the decay recoil and neutron emission in the decay pass undetected. Further examples of  $\pi^-$ -mesonic decays of heavy spallation HF's were subsequently reported by other groups.<sup>6-7,10-17</sup> The latest work is that of Lemonne et al.<sup>18</sup> who report 20 spallation HF's, decaying  $\pi^{-1}$ mesonically, produced by the interactions of  $K^-$  mesons at rest (also reported are 2 HF's produced by  $\Sigma^$ captures at rest). The upper limits of  $B_{\Lambda}$  of six  $\pi - p - r$ decays of these HF's are found to vary from 22.8 to 26.6 MeV. These authors, however, consider an upper limit of  $B_{\Lambda}$  at 22.8 MeV as valid for the whole sample of HF's ( $60 \leq A \leq 100$ ).

In the present paper we report the analysis of 16 short-range mesonic HF's produced in 1.5-GeV/c  $K^$ interactions in nuclear emulsions. We find that for HF's having  $A \simeq 35$  to 80 the upper limits of  $B_{\Lambda}$  could vary from 21.9 to 24.5 MeV. The plan of the paper is as follows. In Sec. II details of the experimental procedure followed are given. The selection of heavy spallation HF's among observed short-range HF's and the analyses leading to their  $B_{\Lambda}$  and A determinations are presented in Sec. III. The discussion and final conclusions are given in Sec. IV.

#### **II. EXPERIMENTAL PROCEDURE**

#### A. Exposure and Scanning of the Stack

An emulsion stack consisting of 100  $L_4$  hypersensitized pellicles of dimensions,  $20 \text{ cm} \times 15 \text{ cm} \times 600 \mu$ , was exposed to a 1.5-GeV/c  $K^-$  beam at CERN. The beam composition was  $K:\pi:\mu=2.7:0.4:0.6$ . A total of about  $3 \times 10^5$  K<sup>-</sup> particles entered the stack. The choice of fine-grain  $L_4$  emulsion (grain size  $\sim 0.3 \,\mu$  in developed emulsion) was made in order to attain a higher accuracy in the measurement of the ranges of short recoil tracks

<sup>10</sup> J. Cuevas, J. Diaz, H. Harmsen, W. Just, H. Kramer, H. Spitzer, M. W. Teucher, and E. Lohrmann, Nuovo Cimento 27, 1500 (1963).

<sup>11</sup> A. Perlmutter, Phys. Letters 4, 336 (1963)

<sup>12</sup> G. Baumann (private communication, 1965); see, however, Proceedings of the Sienna Conference on Elementary Particles, edited by G. Bernardini and G. P. Puppi (Società Italiana di Fisica, Bologna, 1963), p. 341.

<sup>13</sup> Bologna, Firenze, Geneva Collaboration (private communication).

<sup>14</sup> A. W. Key, S. Lokanathan, and Y. Prakash, Nuovo Cimento

34, 274 (1964). <sup>16</sup> J. P. Lagnaux, J. Lemonne, J. Sacton, E. R. Fletcher, D. O'Sullivan, T. P. Shah, A. Thompson, P. Allen, Sr., M. Heeran, A. Montwill, J. E. Allen, D. H. Davis, D. A. Garbutt, V. A. Bull, P. V. March, M. Yaseen, T. Pniewski, and J. Zakrzewski, Nucl. Phys. 60, 97 (1964).

<sup>16</sup> M. J. Beniston, R. Levi Setti, W. Püschel, and M. Raymund, Phys. Rev. **134**, B641 (1964).

D. J. Prowse and Alice Lou, Bull. Am. Phys. Soc. 10, 114 (1965).

<sup>(1)</sup> J. Lemonne, C. Mayeur, J. Sacton, P. Vilain, G. Wilquet, D. Stanley, P. Allen, D. H. Davis, E. R. Fletcher, D. A. Garbutt, M. A. Shaukat, J. E. Allen, V. A. Bull, A. P. Conway, and P. V. March, Phys. Letters 18, 354 (1965).

and also to obtain a greater spatial resolution between double-centered stars.

Area scanning for obtaining the HF-like stars was performed in the usual manner.<sup>1,4</sup> A total of 31 223 interactions caused by beam particles was observed of which 1656 were classified as due to the production and subsequent decay of HF's. 93 hyperfragments were found to decay  $\pi^-$ -mesonically, of which 16 had ranges  $\leq 10 \mu$ . Although some contamination, due to the background phenomena of (1) scattering or interaction in flight of a low-energy stable particle and (2) slow  $\pi^-$ ,  $K^-$ , or  $\Sigma^-$  captures, is expected in the total sample of HF's, the sample of mesonic decays is expected to be free from any such contamination. This is because the only source of contamination among the mesonic HF's would be due to the re-emergent  $K^-$  mesons having ranges  $< 20 \,\mu$  (whence the discrimination between a HF and a  $K^{-}$  track becomes poor) and which produce stars with a  $\pi^-$  meson having kinetic energy  $(T_{\pi^-})$  in the interval 0-60 MeV (chosen on the basis of the observed  $T_{\pi}$ - distribution of the classified HF's; see, for example, Fig. 1). This contamination can be found as follows. In our total sample of primary interactions, we observed only 2 possible re-emitted  $K^-$  mesons having ranges in the interval 20-100  $\mu$ . It might therefore be reasonable to assume that in the range interval  $0-20 \mu$  not more than 2 re-emergent  $K^-$  mesons were produced. It is known, further, that only  $\sim 8\%$  of the K<sup>-</sup> captures give rise to a  $\pi^-$  meson of energy 0-60 MeV.<sup>19</sup> Thus in our sample the expected number of re-emitted  $K^-$  mesons in the range interval 0-20  $\mu$ which could simulate mesonic HF's would be  $2 \times 0.08$  $\sim 0.16$ . It is, therefore, evident that the sample of mesonic HF's is free from any contamination, and we have applied no correction to this effect.



FIG. 1. Distribu-tions of the total visible energy release  $(E_{vis})$  in the decays of mesonic hyperfragments having (a)  $R_{\rm HF} > 10 \,\mu$ , (b)  $R_{\rm HF} \leq 10 \,\mu$  and parent stars with  $\sum Z_i \leq 6$ , and (c)  $R_{\rm HF} \leqslant 10 \,\mu$ and parent with  $\Sigma Z_i > 6$ . stars



ABLE I. Analysis of the five short-ra	nge $(R_{\rm HF} \leq 10 \mu)$ mesor	ic hyperfragments (HF's)	) having parent stars with $\sum Z_i \leq 6.$ <sup>a</sup>
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	Decay products									
Event No.	$N_h$	$\Sigma Z_i$	R <sub>нғ</sub> (µ)	Identity	Range (µ)	Azimuth (deg)	Dip (deg)	energy (MeV)	Probable HF—identity and decay mode	$B_{\Lambda}$ (MeV)
(1)	4	$4+\pi^{\pm}$	9.7	$\begin{cases} \pi^- \\ p \\ p \\ (n) \end{cases}$	15 982 110 2.1	0 179.1 193.7	$^{+1.8}_{+51.1}_{-32.1}$	30.54 3.89 0.23	$\Delta \mathrm{H}^{3} \rightarrow \pi^{-} + p + p + n$	-0.59
(2)	2	$4+\pi^{\pm}$	8.8	$\begin{cases} \pi^- \\ p \\ \mathrm{He}^{3,4} \end{cases}$	14 750 254 blob	0 161.2	-35.1 +32.6	29.16 6.23 0.30,0.23		1.91 1.98
(3)	3	$4+2\pi^{\pm}$	8.4	$\begin{cases} \pi^- \\ p \\ \mathrm{He^4} \end{cases}$	7988 462 22	0 49.1 218.7	+70.6 +41.7 -53.3	20.33 8.90 5.17	$_{\rm A}{ m He^5} \rightarrow \pi^- + p + { m He^4}$	3.20
(4)	3	3	6.4	$\begin{cases} \pi^- \\ Be^7 \\ (n) \end{cases}$	14 849 1.4	0 180	-50.0 + 54.0	29.25 0.80	$_{\Delta}\mathrm{Li}^{8} \rightarrow \pi^{-} + \mathrm{Be}^{7} + n$	5.82
(5)	3	3	4.8	$\begin{cases} \pi^- \\ d \\ \mathrm{Li}^6 \end{cases}$	10 720 5.7 ~1.0	0 147.1 267	+36.7 -22.7 -17.3	24.14 0.62 0.24	$_{\Lambda} \mathrm{Li}^{8} \rightarrow \pi^{-} + d + \mathrm{Li}^{6}$	7.57

\* Explanation of symbols:  $R_{HF}$  = range of the HF:  $N_h$  = number of stable particles emitted at the HF-production star;  $\Sigma Z_i$  = total charge of emitted particles (other than HF) from the production star.

#### **B.** Standards Adopted

The kinetic energies of singly charged particles were calculated using the range-energy relations of Barkas.<sup>20</sup> The masses of nuclides were taken from the table of Everling et al.<sup>21</sup> The  $Q_0$  value in  $\Lambda \rightarrow p + \pi^-$  decay was taken as  $(37.60 \pm 0.12)$  MeV.<sup>22</sup>

### **III. ANALYSIS OF MESONIC DECAYS OF** SHORT-RANGE HF's

#### A. Selection of Heavy Spallation HF's

Some arguments<sup>14,16</sup> have recently been put forward which tend to indicate that the short-range HF's, generally assumed as spallation products, may contain an appreciable proportion of light HF's. We therefore proceed to select a sample of heavy spallation HF's, as "pure" as possible, in the following manner: We divide our sample of 16 HF's into two groups, Tables I and II, such that the total charge  $\sum Z_i$  of the emitted particles (other than the HF) at the production star is  $\leq 6$  or >6, respectively. Attributing at least one charge to the HF, it is seen that the events recorded in Table II belong exclusively to Ag and Br interactions, whereas those in Table I could be from either C, N, O or Ag, Br interactions. The 5 events in the latter group, on kinematical analysis, are found to be consistent with the interpretations AH3, AHe4.5, AHe5, ALi8, and ALi8 (see Table I). The remaining 11 events of Table II are now examined as follows.

In Fig. 1 we display the distributions of the visible energy release  $(E_{vis})$  in the decay of three groups of HF's: (a) long-range  $(>10 \mu)$  HF's (these are expected to belong exclusively to the light HF category), shortrange HF's originating from parent stars having (b)  $\sum Z_i \leq 6$  (Table I), and (c)  $\sum Z_i > 6$  (Table II). It is evident from the figure that the distributions (a) and (b), each belonging to light HF's, are similar; however, the distribution (c) is distinctly different from both and shows relatively small values of  $E_{vis}$ . The events in distribution (c) are, therefore, likely to belong to the heavy-HF category.

A close scrutiny of the production stars of these 11 HF's, however, reveals that two events (Nos. 15 and 16) are of ambiguous nature. Event No. 15 displays at its production star a recoil of range  $\sim 2 \mu$  and also three short tracks of ranges  $9 \mu$ ,  $14 \mu$ , and  $18 \mu$ ; this observation therefore suggests that the struck nucleus might have undergone fragmentation and the observed shortrange HF may belong to the light-HF category. In another event, No. 16, a recoil of range  $\sim 2 \mu$  (partly obscured by the neighboring tracks) is observed at its production star which again indicates that this event may also belong to the light-HF category. There is also an indication of a recoil of range  $\leq 0.5 \mu$  at the decay star of this event which for the observed  $\pi^-$  momentum, 88 MeV/c, can arise only for A < 20. It may be further noted from Fig. 1 that this even, having  $E_{vis} = 25$  MeV, falls in the border-line region of these distributions. From the above considerations we therefore discard these two events (Nos. 15 and 16) from the category of heavy spallation HF's. The remaining 9 events appear "clean" from all considerations but for the possibility that a short recoil at the production star may escape detection, either because it is too short to be visible or

<sup>&</sup>lt;sup>20</sup> W. H. Barkas, Nuovo Cimento 8, 201 (1958).

 <sup>&</sup>lt;sup>20</sup> W. H. Barkas, Nuovo Cimento 8, 201 (1990).
 <sup>21</sup> F. Everling, L. A. König, J. H. Mattauch, and A. H. Wapstra, Nucl. Phys. 18, 529 (1960).
 <sup>22</sup> B. Bhowmik and D. P. Goyal, Nuovo Cimento 28, 1494 (1992).

<sup>(1963).</sup> 

				Mass nu	umbers <sup>b</sup>	HF d	ecay prod	ucts Kinetic	Recoil	Assumed	Upper limit
Event No.	$R_{\mathbf{HF},\mathbf{s}} \over (\mu)$	$N_h$	$\Sigma Z_i$	$K^-$ in Ag	nt. in Br	Identity	Range (µ)	energy (MeV)	tum (MeV/c)	decay mode	of $B_{\Lambda}^{e}$ (MeV)
(6)	4.6	15	20	61±5	36±5	$\begin{cases} \pi^- \\ (p)^d \end{cases}$	3376 88	12.4 3.3	138	$\pi - p - r$	21.9
(7)	2.4	11	13	$74\pm5$	$49\pm5$	$\begin{cases} \pi^{-} \\ (p) \end{cases}$	2879 85	11.3 3.3	114	$\pi - p - r$	23.0
(8)	2.6	9	$12 + \pi^{\pm}$	$76\pm5$	$51\pm4$	$\begin{cases} \pi^{-} \\ (\eta) \end{cases}$	2332 79	10.0 3.1	105	$\pi - p - r$	24.5
(9)	2.1	11	$13 + \pi^{\pm}$	$76\pm5$	$49\pm5$	$\begin{cases} \langle P \rangle \\ \pi^{-} \\ \langle D \rangle \end{cases}$	373 183	3.5 5.1	105	$\pi - p - r$	29.0
(10)	4.4	7	$7+2\pi^{\pm e}$	$88 \pm 5$	63±4	$\begin{cases} \pi^{-} \\ \pi^{-} \\ (p) \end{cases}$	10 357	0.4 7.6	113	$\pi - p - r$	29.6
(11)	4.0	14	${\sim}27^{ m f}$	$\sim 45$	$\sim 20$	$\begin{cases} T \\ \pi^{-} \\ (p) \end{cases}$	1894 122	8.9 4.0	97	$\pi - p - r$	24.7
(12)	4.1	11	11	$80\pm5$	$55\pm5$	$\pi^{-}$	7069	18.9	75	$\pi - r$	26.7
(13)	1.2	7	$8 + \pi^+$	$86\pm4$	$60\pm4$	$\pi^{-}$	6649	18.3	74	$\pi - r$	27.3
(14)	3.2	8	9	$83\pm5$	$58 \pm 4$	$\pi^{-}$	1785	8.6	50	$\pi - r$	37.0
(15)	6.1	12 + r	>25 <sup>g</sup>	ambi	guous	π	7500	19.6	76	$\pi - r$	26.0
(16)	3.0	11 + r	$> 13 + \pi^{-} + \pi^{\pm f}$	ambi	guous	$\begin{cases} \pi^{-} \\ r \end{cases}$	$^{11,893}_{\sim 0.5}$	25.6 ?	88	$\pi - r$	20.0

TABLE II. Analysis of 11 short-range  $(R_{\rm HF} \leq 10 \,\mu)$  mesonic hyperfragments (HF's) having parent stars with  $\Sigma Z_i > 6.8$ 

• Explanation of symbols:  $R_{\rm HF}$  =range of the HF;  $N_h$  =number of stable particles emitted at the HF-production star;  $\Sigma Z_i$  =total charge of emitted particles (other than HF) from the production star. • The two mass values shown should normally differ by 28 mass units ( $Ag^{108} - Br^{80}$ ). However, the actual masses differ by a smaller amount, because of the fact that the estimated number of neutrons emitted from Ag interaction is larger than that from Br interaction. • The error in  $B_A$  due to measurement and straggling is typically ~0.2 MeV. • See Ref. 27. • The charge of the HF, on decay kinematics alone, is necessarily  $\geq 2$ ; therefore, even if both the  $\pi$  mesons are negative, the total charge ( $\Sigma Z_i$  +HF-charge) emitted at the production star would be  $\geq 7$ . • The production star of this event has three program with ranges 17.6  $\mu$ , 30  $\mu$ , and 34  $\mu$  which on track-width measurements gave  $Z \sim 4$ , Z = 2, and  $Z \sim 5$ , respectively. The value of  $\Sigma Z_i$  is therefore an order-of-magnitude estimate. • The recoil track (r) in the production star is too short to permit charge measurements. The quoted  $\Sigma Z_i$  is therefore a lower limit.

because of obscuration by the neighboring tracks. Within this limitation, the 9 events, Nos. 6 to 14, can be classified as belonging to the residual spallation products of silver and bromine nuclei.23

#### B. Mass Determination of Spallation HF's

On the basis of the "spallation model"<sup>1</sup> one can assign, for each hyperfragment, two possible mass numbers as  $(108-\Delta A)$  or  $(80-\Delta A)$ ,<sup>24</sup> where  $\Delta A$  represents the total nucleonic mass carried away by the charged nuclides and neutrons emitted from the production star. We determined  $\Delta A$  in an individual event as follows. All the grey prongs were followed to rest or till they escaped the stack. Protons having energy  $\geq 35$  MeV were assumed to be emitted during the "cascade" stage<sup>25</sup> and for these an equal number of neutrons were assumed to be emitted. The remaining nuclides were then assumed to be emitted during the evaporation stage. The charges of these nuclides were determined from track-width measurements,26 or constant sagitta scattering method, or blob density versus range technique, depending on the available track length of the particle. Each charged nuclide was then assigned a mass number corresponding to the most abundant isotope (e.g., p, He<sup>4</sup>, Li<sup>7</sup>, etc.). Necessary corrections to take into account the emission of d, t, and He<sup>3</sup> were made on the basis of the calculations of Dostrovsky et al.25 on nuclear evaporation. For each event the number of neutrons emitted during the evaporation stage was also estimated on the basis of these calculations. The masses of all the charged particles and neutrons estimated as above were summed up to yield the value of  $\Delta A$ . The statistical uncertainty in  $\Delta A$  of an individual event was estimated as  $1 + (n_{ev} + n_{cas} + n_{dtHe^3})^{1/2}$ , where  $n_{ev}$  and  $n_{cas}$  represent the number of evaporated and cascade neutrons, respectively, and  $n_{dtHe^2}$  is the estimated number of neutrons accounting for the presence of d, t, and He<sup>3</sup>. The first term arises because the target nuclei Ag and Br both have equally abundant isotopes with a mass difference of 12 units. In this way the error in  $\Delta A$ typically amounted to  $\sim \pm 5$  mass units. The resulting pair of mass estimates for each hyperfragment are displayed in the fifth column of Table II.

<sup>&</sup>lt;sup>23</sup> It may be observed that in none of these 9 events is a charged stable particle of range  $2-30 \mu$  (short prongs) emitted in the decay. On consideration of the Coulomb barrier in heavy nuclei, this observation is generally taken (Ref. 9) to support the classification of HF's in the heavy category. It should be remarked, however, that this criterion is not of a definite nature since even in the decay stars of light HF's, short prongs are seen only in  ${\sim}50\%$  of the events (see, e.g., Ref. 16). <sup>24</sup> The mass numbers 108 and 80 represent the mean values of

the most abundant isotopes of Ag and Br nuclei (Ag<sup>107,109</sup> and Br<sup>79,81</sup>).

<sup>&</sup>lt;sup>25</sup> I. Dostrovsky, P. Rabinowitz, and R. Bivins, Phys. Rev. 111, 1659 (1958). See, however, A. Fliedner, D. M. Harmsen, and L. Schink, Nuovo Cimento 36, 751 (1965). The experimental ratios, (d+i)/(p+d+i) and  $(\text{He}^3+\text{He}^4)/(p+d+i)$ , found by these authors for stars with  $N_{A} > 6$  are consistent with the calculations of Dostrovsky et al.

<sup>&</sup>lt;sup>26</sup> See for example, B. Bhowmik, T. Chand, D. V. Chopra, and D. P. Goyal, Phys. Rev. 139, B1062 (1965).

### C. $B_{\Lambda}$ Determination of Spallation HF's

The decay configuration of the 9 spallation HF's (Table II) display either a  $\pi^-$  meson associated with a black track,<sup>27</sup> or just a slow negative pion. The former is classified as  $\pi - p - r$  and the latter as  $\pi - r$  events, the recoil nucleus generally remaining undetected in both the cases. The upper limits of  $B_{\Lambda}$  displayed in the last column of Table II have been computed from the visible energies at the decay stars in the usual manner<sup>9</sup> assuming  $Q_0 = 37.6$  and 45.6 MeV for  $\pi - p - r$  and  $\pi - r$ decay modes, respectively. These values of  $B_{\Lambda}$  are treated as upper limits because of the possibilities of the decay recoil being left in an excited state and/or of neutron emission in HF decay.<sup>28</sup> It is, however, likely that some of the spallation residues in which the  $\Lambda$ remains trapped may not be on the stability line and therefore the  $B_{\Lambda}$ 's computed in  $\pi - r$  events, assuming a mean  $B_N = 8$  MeV, may be incorrect by a few ( $\sim \pm 2$ ) MeV, the actual value depending on the degree of neutron excess or deficiency as the case may be.

#### IV. DISCUSSION AND CONCLUSIONS

The upper limits of  $B_{\Lambda}$  obtained for the present events vary over a large range, from 21.9 to 37.0 MeV. As pointed out earlier, these events may involve excited recoils and/or the emission of neutrons in their decays. Assessment of the amount of excitation of the decay recoil seems difficult; however, the effect of the neutron emission can be ascertained. In the case of neutron emission the visible energy in the decay is underestimated by an amount equal to the sum of the separation and kinetic energies of the neutron. The average separation energy in the heavy-nuclei region is  $\sim 8$  MeV. This value can have an uncertainty of  $\sim \pm 2$  MeV if the spallation residues do not lie on the stability line (see IIIC). Thus, in the case of neutron emission, the  $B_{\Lambda}$  is overestimated by  $\gtrsim 6$  MeV. We now proceed to examine the possibility of neutron emission in the present events. In the light HF region  $(A \leq 20)$ , the  $B_{\Lambda}$ 's are approximately given by the relation<sup>29</sup>

### $B_{\Lambda} = (0.97A - 1.7)$ MeV.

Thus, the  $B_{\Lambda}$  for an HF of mass A = 20 should be ~18 MeV. The HF's presented in this paper have masses  $\gtrsim 35$ , their  $B_{\Lambda}$ 's should, therefore, be a good deal higher than 18 MeV. Now, if we postulate neutron emission in events 6 to 8, their  $B_{\Lambda}$ 's would become  $\leq 18$  MeV. We thus rule out the possibility of the emission of even slow neutrons in these events. Neutron emissions are possible in events 9, 10 and 12 to 14. In event No. 11,  $B_{\Lambda} = 24.7$  MeV and its mass is inaccurately known as  $\sim 45$  or  $\sim 20$ . Now, if the higher mass value is accepted, then the neutron emission seems to be unlikely, and in that case the HF belongs to the heavy HF category. In case of a neutron emission the  $B_{\rm A}$ would be reduced to  $\leq 18$  MeV, which is consistent with the lower mass value, i.e.,  $\sim 20$ . This event is, therefore, an ambiguous event. The last two events (Nos. 15 and 16) are probably light having  $A \leq 20$  for reasons mentioned earlier (Sec. IIIA), and their apparently large  $B_{\Lambda}$ 's can be easily explained by postulating neutron emissions in their decays.

On the basis of our data (considering the events Nos. 6, 7, and 8) we thus conclude that for the HF's having masses in the region  $A \simeq 35$  to 80, the upper limits of  $B_{\Lambda}$  could vary from 21.9 to 24.5 MeV. This is in good agreement with the previous estimates<sup>9,10,15,18</sup> of upper limits of  $B_{\Lambda} \simeq 23-25$  MeV found valid for heavy hyperfragments having  $40 \leq A \leq 100$ .

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<sup>&</sup>lt;sup>27</sup> In all cases, these black tracks were identified as having Z=1; the characteristic Coulomb scattering at their ends show that they are most probably due to protons.

<sup>&</sup>lt;sup>28</sup> Since the time for  $\gamma$  emission is much shorter than the HF life time, the decay of an HF from an excited state giving rise to an underestimate of  $B_{\rm A}$  is very unlikely (see, for example, Refs. 15 and 18).

<sup>&</sup>lt;sup>29</sup> W. G. G. James, Nuovo Cimento Suppl. 23, 285 (1962).