

achieve a high degree of confidence in the evaluated upper limits, we used for the computation of A the net number of counts (that is, target minus background) recorded in $AB\bar{H}\bar{M}\bar{L}$, plus *three times* the standard error in this net number.

Following a suggestion by C. Werntz,¹⁰ we have calculated a lower limit of the half-life of H⁴, assuming a modest production cross section $\sigma_p=0.1 \mu\text{b}$. Our result for this lower limit is 2 years.

It may be noticed here that our setup, especially counter B , is also sensitive to gamma rays—but with a smaller efficiency. For instance, $\eta>4\%$ for 2½-MeV gamma's in counter B .

¹⁰ C. Werntz (private communication).

IV. CONCLUSION

The upper limits of the production cross section of H⁴ from lithium are of the order of $2\times 10^{-4} \mu\text{b}$, many orders of magnitude smaller than the cross sections of similar process in other elements, as shown in Table II. We therefore conclude that it is very unlikely that H⁴ is a β emitter with a half-life ranging from 1 min to 2 years. It is also unlikely that H⁴ should have a half-life longer than 2 years because that would give a $\log ft\geq 14$ for its decay. It is clear that new decay schemes of a long-lived H⁴ not discussed here (for instance, one that involves a hitherto undiscovered level in He⁴) are also unlikely when we consider that no delayed gamma rays were observed.

Alpha-Particle Resonance*

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A phase-shift analysis of the elastic p - t cross section in the energy range 0.1 to 0.76 MeV has been made. It is shown that the low peak observed at 0.3 MeV is consistent with a 0^+ resonance at 0.5 ± 0.1 MeV. The shape of the observed cusp in the p - t elastic cross section at the threshold energy of the n -He³ channel is used to demonstrate that the energy behavior of the singlet and triplet s -wave phase obtained must be qualitatively unique. A direct comparison is made of the Breit-Wigner single-level approximation and the alternative two-channel scattering length description of the state.

I. INTRODUCTION

A PEAK has been observed in the energy spectrum of breakup neutrons from the reaction $t(d,np)t$ in two separate high-resolution experiments.^{1,2} The peak in the neutron distribution corresponds to an energy of 0.5 in the center of mass of the t - p system. The peak is most pronounced in the forward direction, disappearing entirely at about 60° in the laboratory. Such a distribution is typical of a stripping process in which the nucleon which interacts most strongly with the target nucleus interacts principally in an S state. The shape of the neutron peak can be fit fairly well³ by assuming an S -wave resonance in the t - p system at an energy of about 0.5 MeV. The excitation energy of this state is 20.4 MeV with respect to the He⁴ ground state.

However, as Watson has shown,⁴ in a three-body breakup one can expect peaks in the spectrum of one of the fragments even when the important phase shift of the remaining two-body system does not have a resonance

behavior. The only requirement is that this phase shift be a rapidly varying function of energy. Near a threshold this rapid variation can be due to a large scattering length. For example, a distinct peak is observed in the neutron spectrum from $d(p,pp)n$ due to the strong singlet S -wave interaction of the two protons. In order to determine whether one of the S -wave phase shifts actually passes through 90° , we have undertaken a phase-shift analysis of the differential cross section for elastic t - p scattering which has been recently measured by Jarmie *et al.*⁵ in the energy region 0.16 to 0.52 MeV.

The cross section was measured at a single angle of 120° in the center of mass. A low peak appears at about 0.3 MeV, which corresponds to the peak observed in the $t(d,np)t$ reaction. In the elastic scattering it is shifted to slightly lower energy because of the different energy dependence of the kinematic factors in the two-body elastic scattering as compared to the three-body final state. The presence of a large Coulomb amplitude in the elastic scattering also has the effect of making the peak less prominent. In the sections which follow the attempt to obtain the 1S_0 and 3S_1 phase shifts is discussed. For both S -wave phase shifts the effect of the closed n -He³

* Work partially supported by the U. S. Air Force Office of Scientific Research.

¹ H. W. Lefevre, R. R. Borchers, and C. H. Poppe, Phys. Rev. **128**, 1328 (1962).

² C. H. Poppe, C. H. Holbrow, and R. R. Borchers, Phys. Rev. **129**, 733 (1963).

³ Carl Werntz, Phys. Rev. **128**, 1336 (1962).

⁴ K. M. Watson, Phys. Rev. **88**, 1163 (1952).

⁵ Nelson Jarmie, M. G. Silbert, D. B. Smith, and J. S. Loos, Phys. Rev. **130**, 1987 (1963).

channel and the coupling of the open p - l channel to it have been taken into account by using a 2×2 transition matrix for each spin and parity partial wave. Satisfactory fits to the differential cross section as well as to the $\text{He}^3(n,n)\text{He}^3$ and $\text{He}^3(n,p)t$ cross sections for thermal neutrons are obtained by assuming a broad 1S_0 resonance below the n - He^3 threshold.

II. PHASE-SHIFT PARAMETRIZATION

We are interested in center-of-mass energies in the range 0.1 to 0.76 MeV. At such low energies the singlet and triplet S -wave phase shifts should be the most important. For the sake of completeness we write down the S -wave contribution to the differential cross section in terms of the phase shifts.⁶

$$\frac{d\sigma^S}{d\Omega}(\theta, E_p) = \frac{1}{4k_p^2} \{ [\sin^2\delta_1 + 3\sin^2\delta_3] - \eta \csc^2\frac{1}{2}\theta [\sin\delta_1 \cos(\delta_1 + 2\eta \ln \sin\frac{1}{2}\theta) + 3\sin\delta_3 \cos(\delta_3 + 2\eta \ln \sin\frac{1}{2}\theta)] + \eta^2 \csc^4\frac{1}{2}\theta \}. \quad (1a)$$

The singlet phase shift is represented by δ_1 and the triplet by δ_3 . The proton wave number k_p is defined by $k_p = [3mE_p/2\hbar^2]^{1/2}$ and the Coulomb parameter η is related to k_p by the equation $\eta = me^2/\hbar k_p$. Since use will be made of the n - He^3 total cross sections for thermal neutrons we also write down the elastic and inelastic cross sections in terms of the appropriate T -matrix elements.

$$\sigma_{nn} = \frac{\pi}{k_n^2} [|T_{nn^1}|^2 + 3|T_{nn^3}|^2], \quad (1b)$$

$$\sigma_{np} = \frac{\pi}{k_n^2} [|T_{np^1}|^2 + 3|T_{np^3}|^2]. \quad (1c)$$

The neutron wave number is defined by

$$k_n = [3m(E_p - E_t)/2\hbar^2]^{1/2}.$$

The singlet and triplet phase shifts are related to the diagonal T -matrix elements T_{pp^1} and T_{pp^3} through the equations

$$e^{i\delta_1} \sin\delta_1 = T_{pp^1}, \quad e^{i\delta_3} \sin\delta_3 = T_{pp^3}. \quad (2)$$

The height of the peak definitely rules out a resonance in the 3S_1 partial wave. We thus assume that the resonance occurs in the singlet state. Upon making this assumption one is forced to take δ_3 to be small and negative in order to fit the curve at very low energies where the interference between the Coulomb and nuclear amplitudes is large. This is in agreement with the single-channel phase-shift analysis of Frank and Gammel⁷ in which the triplet S -wave phase shift was found to be small and negative and the singlet

large and positive in the energy region above the n - He^3 threshold.

1S_0 Phase Shift

The energy dependence of the phase shift δ_1 is taken to be given by a Breit-Wigner single-level approximation

$$\delta_1 = \alpha + \xi, \quad \alpha = \tan^{-1} \frac{-F_0(k_p a)}{G_0(k_p a)}, \quad (3)$$

$$\xi = \tan^{-1} \frac{\Gamma_p}{E_0 + \Delta_n + \Delta_p - E_p}, \quad \Gamma_p = P_p^+(E_p) \gamma_p^2,$$

$$\Delta_n = \gamma_n^2 [B_n - S_n^-(E_n)], \quad \Delta_p = \gamma_p^2 [B_p - S_p^+(E_p)].$$

These equations are valid only for negative values of the neutron energy, E_n . In terms of the threshold energy for $t(p,n)\text{He}^3$, E_t , $E_n = E_p - E_t$. The parameters describing the resonance are the resonant energy E_0 , the reduced neutron and proton widths γ_n^2 and γ_p^2 , and the channel radius a . The energy-dependent functions $P_p^+(E_p)$, $S_p^+(E_p)$, and $S_n^-(E_n)$ are listed in Ref. 6. The constants B_n and B_p are the logarithmic derivatives of the channel wave functions on the nuclear surface evaluated for $E_p = E_0$. We choose them such that $\delta_1(E_0) = 90^\circ$;

$$B_p = k_p a \left. \frac{G_0'(k_p a)}{G_0(k_p a)} \right|_{E_0}, \quad B_n = -K_n a |_{E_0}, \quad (4)$$

$$K_n = [3m(E_t - E_p)/2\hbar^2]^{1/2}.$$

3S_1 Phase Shift

A two-channel scattering-length approximation is used for the triplet shift. Ross and Shaw⁸ show that the energy dependence of the multichannel scattering matrix T can be expressed most conveniently through the introduction of an M matrix defined by the relation (for S waves, all channels unchanged)

$$T = k^{\frac{1}{2}} (M - ik)^{-1} k^{1/2}. \quad (5)$$

The M matrix has an effective-range-type expansion

$$M(E) = M(E_1) + \frac{1}{2} R [k^2 - k^2(E_1)]. \quad (6)$$

In the above equations all quantities are square matrices with the order of the matrix equal to the number of channels being considered. The elements $k_i^{\frac{1}{2}}$ of the diagonal matrix $k^{\frac{1}{2}}$ are the square roots of the wave numbers in the various open channels. $M(E_1)$ and R are constant matrices, the latter being approximately diagonal, $R_{ij} \cong 0$, $i \neq j$. For a charged channel one can show that Eqs. (5) and (6) are valid if one makes the replacement⁹

$$k_c \rightarrow C_0^2 k_c, \quad M(E_1) \rightarrow M(E_1) - g(\eta_c)/D, \quad (7)$$

$$C_0^2 = 2\pi\eta_c / (e^{2\pi\eta_c} - 1).$$

⁶ A. M. Lane and R. G. Thomas, Rev. Mod. Phys. **30**, 257 (1958).

⁷ R. M. Frank and J. L. Gammel, Phys. Rev. **99**, 1405 (1955).

⁸ Marc Ross and Gordon Shaw, Ann. Phys. (N. Y.) **13**, 147 (1961).

⁹ R. G. Sachs, Nuclear Theory (Addison-Wesley Publishing Company, Inc., Reading, Massachusetts, 1953), p. 126.

TABLE I. Sets of values of the parameters which yield satisfactory fits to the experimental p - t cross section.

a (10^{-13} cm)	E_0 (MeV)	γ_n^2 (MeV)	γ_p^2 (MeV)	α (10^{12} cm $^{-1}$)	β^2 (10^{24} cm $^{-2}$)	γ (10^{12} cm $^{-1}$)	$\frac{d\sigma^P}{d\Omega}(120^\circ, E_t)$ (mb/sr)
3.0	0.4	1.50	4.18	-3.06	+4.59	+0.94	91
3.0	0.5	0.50	4.44	-2.08	+3.52	+0.90	80
3.0	0.6	0.50	4.77	-1.57	+2.31	+1.14	57
3.6	0.4	3.00	3.02	-3.97	+3.39	+2.04	90
3.6	0.5	3.00	3.84	-2.66	+2.91	+1.69	76
3.6	0.6	2.00	3.52	-1.82	+2.23	+1.94	53
4.2	0.4	2.09	2.09	-2.87	+5.21	+1.08	94
4.2	0.5	1.70	2.40	-2.60	+3.24	+1.49	76
4.2	0.6	1.57	2.60	-1.90	+1.81	+1.77	53

The length $D=1/\eta_c k_c$ and the functional form of $g(\eta_c)$ is given in Ref. 9. The function $-g(\eta)$ is a decreasing function of energy whereas, for positive effective range, $R_{ii}[k^2-k^2(E_t)]$ is an increasing function of energy. We have estimated that the changes in these two functions are of the same order in the energy range 0.1 to 0.76 MeV. Therefore, we take the scattering-length approximation to be that of choosing the M matrix to be a constant matrix;

$$M = \begin{pmatrix} \alpha & \beta \\ \beta & \gamma \end{pmatrix}. \quad (8)$$

In terms of the matrix elements α , β , and γ the three triplet T -matrix elements are

$$\begin{aligned} T_{pp}^3 &= C_0^2 k_p (\gamma - i k_n) d^{-1}, \\ T_{np}^3 &= T_{pn}^3 = C_0 k_p^{1/2} k_n^{1/2} \beta d^{-1}, \\ T_{nn}^3 &= k_n (\alpha - i C_0^2 k_p) d^{-1}, \\ d &= \|M - i k\|. \end{aligned} \quad (9)$$

One sees from Eqs. (1b) and (1c) that $|T_{nn}^3|^2$ and $|T_{np}^3|^2$ are defined only for $E_n \geq 0$. However, the representation given above for T_{pp}^3 can be analytically continued below E_t by making the replacement $k_n \rightarrow i K_n$. The expansion of δ_3 in terms of α , β , and γ can be obtained from Eq. (9). It is

$$C_0^2 k_p \cot \delta_3 = \alpha - \beta^2 / (\gamma + K_n). \quad (10)$$

p -Wave Phase Shifts

If no spin-orbit splitting occurs, only two p -wave phase shifts, the singlet and triplet, are required. If δ_1 is fixed at $E_p = E_t$ both p -wave phase shifts as well as δ_3 can be obtained from the angular dependence¹⁰ of $d\sigma/d\Omega(\theta, E_t)$. The contributions of these three phase shifts for $E_p < E_t$ can be estimated from a scattering length approximation. This calculation was actually carried out for a number of choices of the resonance parameters and in every case the calculated cross section was always much too high at $E_p = E_0$. The reason seems

to be that in assuming no spin-orbit splitting the entire isotropic contribution must come from $\sin^2 \delta_1 + 3 \sin^2 \delta_3$. This makes δ_3 come out to be equal to, roughly, -25° at E_t . Upon extrapolating down to E_0 the contribution of δ_3 to the cross section is too large. If the p waves contribute to the isotropic term, their contribution falls off much more rapidly with energy. The phase shift δ_3 can then be chosen to be smaller at E_t and the experimental cross section can be fit at E_0 since the p waves contribute very little at this lower energy. Since one must determine five p -wave T -matrix elements in the presence of spin-orbit splitting instead of two a unique determination of these elements is out of the question. Therefore, the drastic assumption was made that the contributions of the p waves to $d\sigma/d\Omega(120^\circ, E_p)$ for $E_p < E_t$ is proportional to E_p^2 . Including this approximation, the complete expression which was used for the differential cross section becomes

$$\frac{d\sigma}{d\Omega}(120^\circ, E_p) = \frac{d\sigma^S}{d\Omega}(120^\circ, E_p) + \frac{E_p^2}{E_t^2} \frac{d\sigma^P}{d\Omega}(120^\circ, E_t). \quad (11)$$

III. NUMERICAL FIT

Altogether 8 parameters are at our disposal to obtain a good fit. These are E_0 , γ_p^2 , γ_n^2 , a , α , β , γ , and $d\sigma^P/d\Omega(120^\circ, E_t)$. It turns out that if only five experimental quantities are matched one obtains a good fit at all energies. These quantities are:

$$\frac{d\sigma}{d\Omega}(120^\circ, 0.2 \text{ MeV}) = 210 \text{ mb/sr},$$

$$\frac{d\sigma}{d\Omega}(120^\circ, E_t) = 192 \text{ mb/sr},$$

and

$$\frac{d\sigma}{d\Omega}(120^\circ, E_0) \quad \text{which depends on } E_0; \quad (12)$$

also¹¹

$$\sigma_{nn} = 1.8 \text{ b},$$

$$\sigma_{np} = 5280 \text{ b}.$$

¹⁰ M. E. Ennis and A. Hemmendinger, Phys. Rev. **95**, 772 (1954).

¹¹ J. D. Seagrave, L. Cranberg, and J. E. Simmons, Phys. Rev. **119**, 1981 (1960).

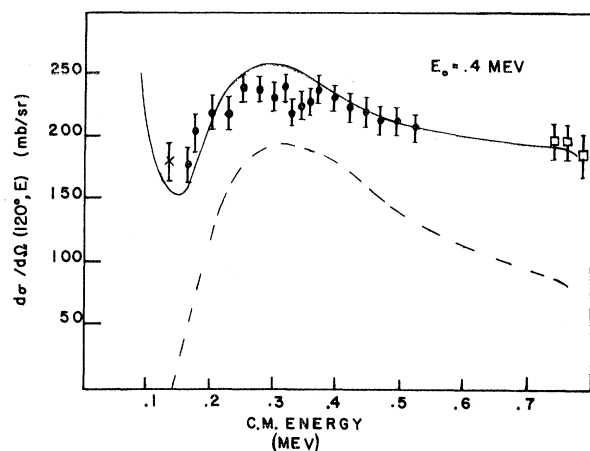


FIG. 1. p - t differential cross section at 120° calculated from the parameters of Table I listed for channel radius $a=4.2$ F and resonance energy $E_0=0.4$ MeV. The dashed curve shows the contribution of the singlet s -wave amplitude to the cross section. The data points have been reproduced from Ref. 5.

In our numerical fitting E_0 , a , and γ_n^2 were treated as independent parameters and the other five parameters determined for each set of values of the independent ones. Poppe² *et al.* found that $E_0 \cong 0.5$ MeV. In making our fits we selected three different values for E_0 so as to bracket this value. They are 0.4, 0.5, and 0.6 MeV. (For E_0 much lower than 0.4 MeV the contribution of the resonance to the cross section is higher than the observed value.) Three different values of the channel radius, a , were also employed, $a=3.0$, 3.6, and 4.2 F. The range of values possible for γ_n^2 was limited by two considerations. Firstly, the sum of the two reduced widths must be less than the Wigner limit, $\gamma_n^2 + \gamma_p^2 < 3\hbar^2/2ma^2$. Secondly, since the resonant state should be one of definite isobaric spin $\gamma_n^2 \cong \gamma_p^2$. Both of these conditions could be best satisfied for $a=4.2$ F. For this reason it is

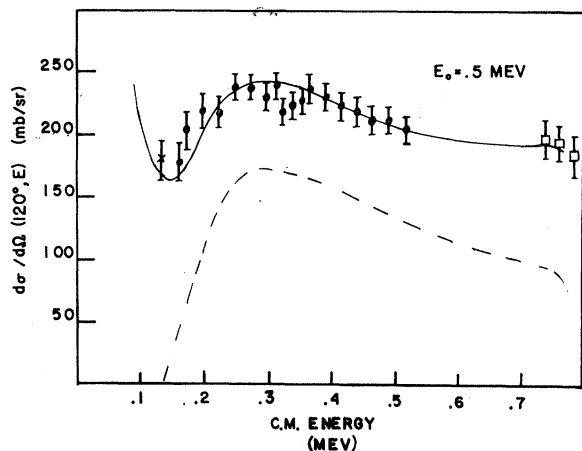


FIG. 2. p - t differential cross section at 120° calculated from the parameters of Table I listed for channel radius $a=4.2$ F and for resonance energy $E_0=0.5$ MeV. The dashed curve shows the contribution of the singlet s -wave amplitude to the cross section.

believed that the parameters obtained with this radius are the most reliable.

Table I contains sets of values of the eight parameters which give satisfactory fits. In most cases γ_n^2 was selected so that the ratio γ_n^2/γ_p^2 is as near to one as is possible under the constraint that the sum of the widths be less than the Wigner limit. The three curves obtained for $a=4.2$ F are displayed in Figs. 1-3. The curves for the two smaller values of the channel radius are virtually indistinguishable from the curves shown.

IV. DISCUSSION

It is clear that we have obtained a reasonable fit to $d\sigma/d\Omega(120^\circ, E_p)$ as well as reproducing the values of σ_{nn} and σ_{np} by assuming that a 0^+ resonance of the α particle occurs in the energy region between the t - p and n - He^3 thresholds. Because of the crude approximation made

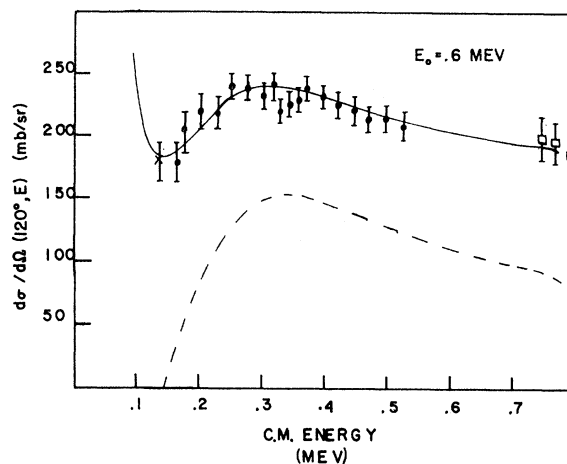


FIG. 3. p - t differential cross section at 120° calculated from the parameters of Table I listed for channel radius $a=4.2$ F and for resonance energy $E_0=0.6$ MeV. The dashed curve shows the contribution of the singlet s -wave amplitude to the cross section.

for the p waves the reduced widths and the resonant energy itself are only approximately determined. A more accurate phase-shift fit, one which is independent of assumptions regarding the energy behavior of the phase shifts, can be made only if the low-energy differential cross section is measured at other angles. A very accurate analysis at such low energy would be possible because of the large interference between the s -wave phase shifts and the Coulomb amplitude. The question naturally arises of whether our fit is qualitatively unique, that is, must one necessarily assume that the singlet phase shift passes through 90° at some energy below the n - He^3 threshold. We think that the observed cusp¹² in the t - p elastic cross section in the vicinity of the n - He^3 threshold does force one to this assumption.

If there were a single s -wave phase shift in the t - p

¹² Nelson Jarmie and Robert L. Allen, Phys. Rev. 114, 176 (1959).

system there would be a particularly simple relationship¹³ between the phase shift and the ratio of the energy derivatives of the differential cross section above and below E_t . This relationship is

$$\lim_{\Delta E \rightarrow 0} \frac{d}{dE_p} \frac{d\sigma}{d\Omega}(\theta, E_t + \Delta E) / \frac{d}{dE_p} \frac{d\sigma}{d\Omega}(\theta, E_t - \Delta E) = -\tan\delta. \quad (13)$$

Since the experimental resolution attained in Ref. 12

was of the order of 10 keV one can only estimate the required derivatives for $\Delta E > 10$ keV. From the curve for $\theta_{o.m.} = 59^\circ$ and for $\Delta E = 20$ keV we can obtain the estimate of $\sim +3$ for the required ratio. This corresponds to a value for δ of $+108^\circ$. Equation (13) can be generalized to the actual case where there are two s -wave phase shifts as well as a large Coulomb amplitude which interferes with both s waves. The result, which is obtained straightforwardly from the representation of the requisite T -matrix elements given in Eq. (9) is

$$\begin{aligned} \lim_{\Delta E \rightarrow 0} \frac{\frac{d}{dE_p} \frac{d\sigma}{d\Omega}(\theta, E_t + \Delta E)}{\frac{d}{dE_p} \frac{d\sigma}{d\Omega}(\theta, E_t - \Delta E)} = & - \left\{ |T_{np^1}|^2 \left[\sin^2 \delta_1 - \frac{\eta}{2} \operatorname{csc}^2 \frac{\theta}{2} \sin \left(2\delta_1 + 2\eta \ln \sin \frac{\theta}{2} \right) \right] \right. \\ & \left. + 3 |T_{np^3}|^2 \left[\sin^2 \delta_3 - \frac{\eta}{2} \operatorname{csc}^2 \frac{\theta}{2} \sin \left(2\delta_3 + 2\eta \ln \sin \frac{\theta}{2} \right) \right] \right\} \\ & \times \left\{ |T_{np^1}|^2 \left[\sin \delta_1 \cos \delta_1 - \frac{\eta}{2} \operatorname{csc} \frac{\theta}{2} \cos \left(2\delta_1 + 2\eta \ln \sin \frac{\theta}{2} \right) \right] \right. \\ & \left. + 3 |T_{np^3}|^2 \left[\sin \delta_3 \cos \delta_3 - \frac{\eta}{2} \operatorname{csc} \frac{\theta}{2} \cos \left(2\delta_3 + 2\eta \ln \sin \frac{\theta}{2} \right) \right] \right\}^{-1}. \quad (14) \end{aligned}$$

Upon inserting the values of the phase shifts and the inelastic T -matrix elements obtained with $a = 4.2$ F into the right side of Eq. (14), the values of the ratio are obtained which are listed in Table II. The qualitative agreement is evident.

The main point of this analysis is that δ_1 must be slightly larger than 90° at E_t . If one assumes that it starts from 0° and increases, it clearly must pass through 90° ; a behavior similar to the singlet n - p phase shift is ruled out. The other possibility is that it starts from 180° and decreases rapidly to a value slightly greater than 90° at E_t . Such a behavior could only occur if there were a bound 0^+ state slightly below the t - p threshold. Since no such state was observed in the $t(d, np)t$ experiments, we must conclude that δ_1 does pass through 90° .

Next, we would like to examine a method of description of the resonance which is an alternative to the Breit-

Wigner formula. Dalitz and Tuan¹⁴ have also developed an effective-range-type expansion for analyzing multi-channel scattering. They have pointed out that a resonance of the type with which we are dealing in this paper—a resonance which is between the thresholds for two different channels—can be described by a scattering length or a “zero-range” approximation to the K matrix (the inverse of the M matrix). Reference to Eq. (10) of this paper makes it clear that if α , β , and γ are such that

$$\alpha - \frac{\beta^2}{\gamma + K_n} \begin{cases} < 0 & E_p > E_p' \\ > 0 & E_p < E_p' \end{cases}, \quad (15)$$

for some E_p' between the two thresholds δ_1 passes rapidly through 90° .

We have compared the behavior of δ_1 when computed from a Breit-Wigner resonance formula [Eq. (3)] to its behavior when computed from a constant M matrix [Eq. (8)]. In each case there are three constants to be determined. We have chosen the set of resonance parameters $E_0 = 0.5$ MeV, $\gamma_n^2 = 1.7$ MeV, and $\gamma_p^2 = 2.4$ MeV as the basis for the comparison. Then the constants α , β , and γ are chosen so that $\delta_1 = 90^\circ$ at $E_p = 0.5$ MeV and so that the two quantities $|T_{np^1}|^2/k_n^2$ and $|T_{np^3}|^2/k_n^2$ are the same in each case for $E_n = E_t$. The values of the phase shifts obtained by each method over the range of interest of the energy are listed in Table III.

TABLE II. The limit, as $E_p \rightarrow E_t^\pm$, of the ratio of the energy derivative of the p - t differential cross section above the n -He³ threshold to the energy derivative of the cross section below threshold. The ratio has been calculated for $\theta = 60^\circ$ using the three sets of parameters in Table I listed under $a = 4.2$ F. The “observed” value estimated from Fig. 1 of Ref. 12 is $+3$. E_0 is given in MeV.

$E_0 =$	0.4	0.5	0.6
$a/b =$	+2.31	+4.45	+6.48

¹³ R. G. Newton, Ann. Phys. (N. Y.) 4, 29 (1958).

¹⁴ R. H. Dalitz and S. F. Tuan, Ann. Phys. (Paris) 3, 307 (1960).

TABLE III. A comparison of the 1S_0 phase shift calculated from a Breit-Wigner single level formula to that calculated from a two-channel scattering length approximation.

C.m. energy MeV	δ_1 (B.W.) degrees	δ_1 (S.L.) degrees
0.20	47	55
0.50	90	90
0.76	105	109

There is a significant difference at the lowest energy. However, since the actual value of the phase shift is not known at each energy one can not choose one three-parameter fit over the other. Poorer agreement resulted from including the function $g(\eta)$ in the M matrix.

We now turn to the question of the assignment of isobaric spin to the resonance. A nucleon and an $A=3$ nucleus in a given spin and parity state can be coupled to a total isobaric spin of either 0 or 1. A mixture of the two is possible only if a $T=0$ and a $T=1$ state of the four nucleon system with similar boundary conditions lie very close together in energy. In view of the singular lack of profusion of α -particle states this is very unlikely. An assignment of $T=1$ to the state would force one to the conclusion¹⁵ that a very weakly bound H^4 with a 0^+ ground state exists. H^4 would decay via β^- emission to the ground state of He^4 with a long lifetime of the order of an hour. A number of experiments¹⁶⁻¹⁸ been carried out in the past in which an H^4 with a lifetime of the order of several minutes or less could have been detected if it existed. In all cases no activity attributable to H^4 was observed. Very recently, Spicer¹⁹ and Nefkens and Moscati²⁰ have exposed lithium targets to gamma rays for times as long as several hours in order to detect the presence of an H^4 with a lifetime appropriate to a 0^+ state. They give upper limits for the cross section for production of $0.6 \mu\text{b}$ and $2 \times 10^{-4} \mu\text{b}$, respectively. Since the latter figure is many orders of magnitude lower than what can be reasonably expected the experimental evidence strongly favors a choice of $T=0$.

¹⁵ C. Wernitz and J. G. Brennan, Phys. Letters **6**, 113 (1963).

¹⁶ L. Rosen and J. E. Brolley, Jr., Phys. Rev. **117**, 1307 (1960).

¹⁷ H. A. Grench, W. L. Imhof, and F. J. Vaughn, Bull. Am. Phys. Soc. **7**, 268 (1962); AFSWC-TDR-62-26, 1962, Air Force project No. 8802 (unpublished).

¹⁸ Kenneth G. McNeill and Waldo Rall, Phys. Rev. **83**, 1244 (1951).

¹⁹ B. M. Spicer, Phys. Letters **6**, 88 (1963).

²⁰ B. M. K. Nefkens and G. Moscati (to be published).

Such a choice is also consistent with the shell model. Elliot and Skyrme²¹ have shown that the first excited state with the spatial partition [4] must be a $2\hbar\omega$, even parity state. Exciting a single nucleon into the $1p$ shell while retaining a totally symmetric space state leaves the He^4 in its ground state and changes only the state of the spurious center-of-mass motion introduced by using shell-model wave functions. A $T=0$, $S=0$ state of the four nucleon system which has a big probability for breaking into either $t-p$ or He^3-n would be expected to have a spatial wave function that transforms like [4]. The only difficulty with this is that if one takes the observed rms radius of the alpha and computes the corresponding value of $\hbar\omega$ one finds²² that $2\hbar\omega$ is roughly 50 MeV. This is considerably larger than the 20.4-MeV splitting of the ground and first excited state that has been observed. We are currently calculating the positions of the 0^+ , $T=0$ and $T=1$ states starting with a reasonable two-nucleon potential.

In the preceding discussion it has been assumed that the resonance in question is a pure isobaric spin state. Baz²³ has pointed out that there are many instances in light nuclei of resonances occurring very near the threshold for a new channel. These "threshold resonances" are characterized by having reduced widths for breakup into the new channel which are large compared to the other channel widths. This implies, in some cases, that a significant mixing of isobaric spin states is occurring. This mixing apparently does not occur in the state in question since it lies equally close to the two important channels. In fact, one can always find an energy E_p' , $0 < E_p' < 0.76$ MeV, such that $B_n = B_p$ for any reasonable choice of the channel radii. This indicates that the wave functions are very similar in the two channels even in the asymptotic region.

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²¹ J. P. Elliot and T. H. R. Skyrme, Proc. Roy. Soc. (London) **A232**, 561 (1955).

²² Paul Goldhammer, Rev. Mod. Phys. **35**, 40 (1963).

²³ A. S. Baz', in *Advances in Physics*, edited by N. F. Mott (Taylor and Francis, Ltd., London, 1959), Vol. 8, p. 349.