groups identified as arising from sodium were also in excellent agreement, and in no case did the difference between the results of the present investigation and those from the previous work differ by more than 6 kev . It is interesting to note that, although this previous study was carried out using an incident deuteron energy of 2 Mev , the present work, using much higher deuteron energies, did not disclose any additional excited states in $\mathrm{Na}^{24}$ between its ground state and $4.5-\mathrm{Mev}$ excitation energy. In the present investigation, levels in $\mathrm{Na}^{24}$ up to an excitation energy of approximately 5 Mev might have been detected. No evidence was found for states in this region above 4.5 Mev , although it is quite possible that low-intensity groups associated with sodium might have been obscured by the high density of intense groups from phosphorus.
The $Q$ value measured for the $\mathrm{P}^{31}(d, p) \mathrm{P}^{32}$ reaction was $5.709 \pm 0.010 \mathrm{Mev}$. This is in good agreement with the value of $5.704 \pm 0.008 \mathrm{Mev}$ reported previously. ${ }^{4}$ As in the previous work, the $B \rho$ value for the polonium alpha particles used for calibration purposes was assumed to be 331.59 kilogauss-centimeters. The energies of the excited states in $\mathrm{P}^{32}$ as determined in the present investigation are listed in Table I where they are compared with our earlier results and those of Dalton et al. ${ }^{1}$ The level tentatively measured at 3.141

Mev in the other work is confirmed, and several new levels have been found in the region of excitation which was previously obscured by contaminant groups. It appears that several of the proton groups whose angular distributions were measured by previous investigators probably consisted of several unresolved components. The results of the present study are summarized in Fig. 4 which shows an energy-level diagram for $\mathrm{P}^{32}$.
It is probable that the first excited state and the ground state of $\mathrm{P}^{32}$ have spins of 2 and 1 , respectively. The relative intensities of these related states, as excited in this reaction, would then be expected to be in the ratio of $2 J+1$, or 1.67 . The experimentally determined ratios were found to be 1.61 at 30 degrees; 1.52 at 50 degrees; 1.44 at 70 degrees; and 1.41 at 90 degrees. In the previous work, carried out at 90 degrees, the ratios were 1.7 and 1.2 for deuteron bombarding energies of 1.8 and 2.0 Mev , respectively.

## ACKNOWLEDGMENTS

We are indebted to our colleagues at the High Voltage Laboratory for much assistance during the course of this investigation and to our plate-reading group for their careful scanning of the photographic emulsions.

# Results of Stripping Analysis of the $\mathbf{C o}^{59}(d, p) \mathbf{C o}^{60}$ Reaction* $\dagger$ 

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(Received February 29, 1960)


#### Abstract

The MIT-ONR electrostatic generator and broad-range magnetic spectrograph have been used to investigate proton groups produced by bombarding thin cobalt targets with $6.0-\mathrm{Mev}$ deuterons. The angular distributions of the twenty-eight most intense proton groups corresponding to as many levels in $\mathrm{Co}^{60}$ were analyzed in terms of stripping theory to determine the orbital angular momentum of the captured neutron. The $Q$ values of the ( $d, p$ ) reaction were measured for sixty levels of $\mathrm{Co}^{60}$. The ground-state $Q$ value was found to be $5.262 \pm 0.011 \mathrm{Mev}$.


## I. INTRODUCTION

CHARGED-PARTICLE studies of $\mathrm{Co}^{59}$ by proton bombardment ${ }^{1}$ and of $\mathrm{Co}^{60}$ through the $\mathrm{Co}^{59}(d, p) \mathrm{Co}^{60}$ reaction ${ }^{2}$ have been done earlier at this

[^0]Laboratory. The objectives of the present work have been to try to resolve an uncertainty in the ground-state $Q$ value for the $\mathrm{Co}^{59}(d, p) \mathrm{Co}^{60}$ reaction, to determine more fully the excited levels of $\mathrm{Co}^{60}$, and to furnish information on the angular momentum and parity of these levels through stripping analysis.

A $Q$ value for the ground-state transition of 5.260 $\pm 0.007 \mathrm{Mev}$ can be determined by subtracting the binding energy of the deuteron from the highest energy gamma ray observed by Bartholomew and Kinsey in the $\mathrm{Co}^{59}(n, \gamma) \mathrm{Co}^{60}$ reaction. ${ }^{3}$ The $\mathrm{Co}^{59}(d, p) \mathrm{Co}^{60}$ work of Foglesong and Foxwell ${ }^{2}$ gave a $Q$ value of $5.283 \pm 0.008$

[^1]

Fig. 1. Spectrum of protons emitted from a cobalt-on-Formvar target bombarded with $6.18-\mathrm{Mev}$ deuterons. Observation angle $\theta_{\text {lab }}=30^{\circ}$.

Mev, differing by 23 kev from the value determined by the $(n, \gamma)$ measurements. The present work attempts to resolve this discrepancy.

On the basis of the shell model, ${ }_{27} \mathrm{Co}^{59}$ is assumed to have a single hole in the proton $1 f_{7 / 2}$ shell, but the positions of the four neutrons above the $1 f_{7 / 2}$ shell are somewhat in doubt. The states $2 p_{3 / 2}$ and $1 f_{5 / 2}$ lie very close together. ${ }^{4}$ The experimental magnetic moments ${ }^{5-7}$ of $\mathrm{Co}^{58}$ and $\mathrm{Co}^{60}$, compared with the calculated magnetic moments, ${ }^{4}$ seem to indicate assignments of the thirty-first neutron in the $\mathrm{Co}^{58}$ ground state to the $f_{5 / 2}$ level and the thirty-third neutron in the $\mathrm{Co}^{60}$ ground state to the $p_{3 / 2}$ level.

The spin of the $\mathrm{Co}^{60}$ ground state has been determined by Dobrowolski et al. ${ }^{6}$ as $I=5$ by paramagnetic resonance hfs measurements. Beta decay and gammaray data ${ }^{8-10}$ establish the spins and parity of the ground state and first excited state (metastable state at 59 kev ) as $I=5^{+}$and $2^{+}$, respectively.

## II. EQUIPMENT AND PROCEDURE

The experimental arrangements at the MIT-ONR electrostatic generator have been described by Buechner et al. ${ }^{11}$ The broad-range spectrograph has been described by Browne and Buechner. ${ }^{12}$ Certain details of the techniques adopted when these facilities are being used for an angular-distribution measurement have been discussed in a paper by Bockelman et al. ${ }^{13}$ Briefly, protons emerging from the deuteron bombarded target

[^2]were deflected in the magnetic field of the spectrograph and focused on Eastman Kodak NTA 25-micron nuclear-track plates. The positions of the proton tracks on the plates determined the radii of curvature of the particle orbits in the magnetic field. ${ }^{12}$ The proton momentum spectrum was determined by counting the number of tracks within each half-millimeter strip across the plate. To facilitate plate reading, the emulsions were covered with aluminum foil during exposure to prevent charged particles heavier than protons from reaching the plates.
Deuterons with energies of 6.01 Mev were employed. By mistake the exposures at some angles were made with $6.18-\mathrm{Mev}$ deuterons. It is assumed that this change in input energy has a negligible effect on the angular distributions. The targets used were prepared by vacuum evaporation onto a thin Formvar film of naturally monoisotopic $\mathrm{Co}^{59}$ in the form of cobalt sponge obtained from Johnson, Matthey and Company, London. A mass analysis obtained by observation in the spectrograph of protons elastically scattered from a target indicated the presence of large amounts of tungsten from the evaporator crucible and carbon and oxygen from the Formvar backing. Small amounts of sodium and chlorine were also present, but no proton groups could be found that could be ascribed to these latter elements in the ( $d, p$ ) spectra. Since the targets were quite fragile, a total of five targets from two different evaporations were used during the total of 90 hours' exposure time.

## III. RESULTS

Data were taken at 5 -degree intervals for reaction angles between 10 and 60 degrees and at 10-degree intervals between 70 and 110 degrees. Most exposures were 500 microcoulombs in duration, but because of low yield, some were made longer. All results were normalized to 500 microcoulombs and the same target thickness. The result of a typical exposure is shown in Fig. 1. Because of the presence of the intense proton peaks from ( $d, p$ ) reactions on carbon and oxygen in the target, some levels in $\mathrm{Co}^{60}$ could not be observed at all angles. For instance, levels (34) and (35) of $\mathrm{Co}^{60}$ are
obscured in Fig. 1. However, because of the difference in mass, the contaminant peaks cover at other angles different parts of the spectrum, and the shift is sufficiently large so that no cobalt level was obscured at more than two angles.

The $Q$ values were computed from four exposures at different angles. This insured at least three separate $Q$ value determinations for each level, with but one exception, level (54). The average $Q$ value and excitation energy for the ground level and fifty-nine excited levels are given in Table I. A separate series of computations for the ground level at twelve different angles gave as an average the result shown in the table with a standard random deviation of less than 2 kev . A total standard uncertainty of 11 kev is assigned to all $Q$ values. This error figure is due largely to various systematic uncertainties in the proton and deuteron energies. The uncertainty in the employed $B \rho$ value ( 331.59 kilogausscm ) for polonium alpha particles has been discussed in an earlier paper. ${ }^{14}$
When plotted to a larger scale, several peaks in Fig. 1 have half-widths greater than normal, or they display structure. When this is seen at all angles of observation, contaminant elements may be ruled out as the cause, and it is possible that the peaks represent closely spaced doublets. The $Q$ values given apply then to the member of the doublet with the highest proton energy (lowest excitation energy) with errors possibly slightly higher than 9 kev . The following peak numbers represent suspected doublets: (2), (10), (19), and (25), with (19) being the largest and having the most consistent structure.
The agreement of the $Q$ value for the ground-state level, 5.262 Mev , with that which is obtained from the work of Bartholomew and Kinsey, 5.260 Mev , is excellent. The $Q$ value reported by Foglesong and Foxwell is about 20 kev higher. This difference may have been caused by an effect noted by Strait et al., ${ }^{15}$ who observed that, at high field strengths, the iron of the 180-degree annular magnet then used showed saturation effects and caused errors in the energy measurements. In the work of Foglesong and Foxwell, this error would indeed be about 20 kev (high) according to our estimate for the ground-state level.
A comparison with previous work for the various excited levels is also shown in Table I. Except for level numbers less than nine and level (48), the $Q$ values given by Foglesong and Foxwell are in excellent agreement with the present work. No level was found that corresponded to a level with $Q$ value 2.659 Mev reported by Foglesong and Foxwell. The gamma-ray energies quoted from the work of Groshev et al. ${ }^{16}$ in Table I are

[^3]TABLE I. $\mathrm{Co}^{59}(d, p) \mathrm{Co}^{60} Q$ values and excitation energies.

| Peak number | Present work |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $Q$ value | $E_{x}$ | $Q$ value ${ }^{\text {a }}$ | $E_{x}$ |  |  |
|  | (Mev) | (Mev) | (Mev) | (Mev) ${ }^{\text {a }}$ | $E_{x}$ | $E_{x}$ |
|  | $\pm 0.011$ | $\pm 0.006$ | $\pm 0.012$ | $\pm 0.009$ | $(\mathrm{Mev})^{\text {b }}$ | (Mev) ${ }^{\text {c }}$ |
| Ground | 5.262 | 0 | 5.283 | 0 |  |  |
| (1) | 5.204 | 0.058 | 5.223 | 0.060 |  |  |
| (2) | 4.980 | 0.282 | 4.997 | 0.285 | 0.290 | 0.285 |
| (3) | 4.830 | 0.432 | 4.838 | 0.445 |  | 0.445 |
| (4) | 4.761 | 0.501 | 4.770 | 0.513 | 0.511 | 0.512 |
| (5) | 4.721 | 0.541 | 4.726 | 0.557 |  |  |
| (6) | 4.650 | 0.612 | 4.661 | 0.622 | 0.562 | 0.619 |
| (7) | 4.524 | 0.738 |  |  | 0.735 |  |
| (8) | 4.479 | 0.783 | 4.491 | 0.792 | 0.80 | 0.796 |
| (9) | 4.256 | 1.006 | 4.271 | 1.012 |  | 1.012 |
| (10) | 4.055 | 1.207 | 4.046 | 1.237 | 1.25 | 1.236 |
| (11) | 3.925 | 1.337 |  |  |  |  |
| (12) | 3.885 | 1.377 | 3.889 | 1.394 |  | 1.376 |
| (13) | 3.815 | 1.447 |  |  |  |  |
| (14) | 3.750 | 1.512 | 3.750 | 1.533 | 1.520 | 1.520 |
| (15) | 3.624 | 1.638 | 3.620 | 1.663 | (1.60) |  |
| (16) | 3.578 | 1.684 |  |  | 1.69 |  |
| (17) | 3.555 | 1.707 |  |  |  |  |
| (18) | 3.514 | 1.748 |  |  |  | 1.760 |
| (19) | 3.463 | 1.799 | 3.458 | 1.825 | 1.78 |  |
| (20) | 3.433 | 1.829 |  |  | 1.84 | 1.840 |
| (21) | 3.412 | 1.850 |  |  |  |  |
| (22) | 3.375 | 1.887 |  |  |  |  |
| (23) | 3.339 | 1.923 |  |  |  | . |
| (24) | 3.283 | 1.979 | 3.278 | 2.005 |  |  |
| (25) | 3.231 | 2.031 | 3.218 | 2.065 | 2.03 |  |
| (26) | 3.131 | 2.131 | 3.129 | 2.154 |  | 2.135 |
| (27) | 3.112 | 2.150 |  |  |  |  |
| (28) | 3.045 | 2.217 |  |  | 2.20 |  |
| (29) | 2.988 | 2.274 | 2.988 | 2.295 |  |  |
| (30) | 2.952 | 2.310 |  |  | 2.30 | 2.307 |
| (31) | 2.914 | 2.348 | 2.913 | 2.370 |  |  |
| (32) | 2.835 | 2.427 |  |  |  |  |
| (33) | 2.671 | 2.591 | 2.673 | 2.610 | 2.59 | 2.583 |
|  |  |  | 2.659 | 2.624 |  |  |
| (34) | 2.528 | 2.734 |  |  |  |  |
| (35) | 2.500 | 2.762 | 2.497 | 2.786 |  |  |
| (36) | 2.417 | 2.845 | 2.413 | 2.870 |  |  |
| (37) | 2.378 | 2.884 |  |  | 2.88 |  |
| (38) | 2.363 | 2.899 | 2.359 | 2.924 |  | 2.90 |
| (39) | 2.320 | 2.942 |  |  |  |  |
| (40) | 2.295 | 2.967 |  |  |  |  |
| (41) | 2.252 | 3.010 | 2.245 | 3.038 |  |  |
| (42) | 2.214 | 3.048 |  |  |  |  |
| (43) | 2.197 | 3.065 |  |  |  |  |
| (44) | 2.176 | 3.086 | 2.163 | 3.120 |  |  |
| (45) | 2.147 | 3.115 | 2.145 | 3.138 |  | 3.12 |
| (46) | 2.077 | 3.185 | 2.075 | 3.208 |  |  |
| (47) | 2.047 | 3.215 |  |  | 3.21 |  |
| (48) | 2.024 | 3.238 | 1.995 | 3.288 |  |  |
| (49) | 1.978 | 3.284 | 1.979 | 3.304 |  |  |
| (50) | 1.948 | 3.314 |  |  |  | 3.30 |
| (51) | 1.923 | 3.339 |  |  | 3.35 |  |
| (52) | 1.895 | 3.367 |  |  |  | 3.36 |
| (53) | 1.843 | 3.419 |  |  |  |  |
|  | (1.798) | (3.464) |  | . |  | 3.46 |
| (56) | 1.764 | 3.498 |  |  |  |  |
|  | 1.698 | 3.564 |  |  |  |  |
| (57) | 1.671 | 3.591 |  |  | 3.60 |  |
| (58) | 1.609 | 3.653 |  |  |  |  |
| (59) | 1.580 | 3.682 |  |  |  | 3.69 |

${ }^{\mathrm{a}}$ See reference 2.
Atomnaya Energ, 3 A. M. Dromidov, V. N. Lutsenko, and V. I. Pelekhov, Atomnaya Energ. 3, 187 (1957).
assumed to represent transitions directly to the ground level. Two low-energy gamma rays at 0.454 and 0.562 Mev are not included in the table. Possibly they
represent transitions from levels (4) and (6) to level (1). Two gamma rays at 3.36 and 3.69 Mev , observed by Bartholomew and Kinsey, ${ }^{3}$ possibly also arise from transitions from excited states to the ground state. The other excitation energies quoted in the last column are


Fig. 2. Examples of experimental angular distributions of protons with the $l_{n}$ value of the captured neutrons as indicated on each individual graph. The curves are smooth experimental curves, not theoretical ones.
computed on the assumption that the gamma rays observed represent transitions directly from the capture state to the excited state in question.

Figure 2 shows some examples of the experimental angular distributions. The cross section in microbarns per steradian was obtained by using a conversion factor equal to $1.31 \mu \mathrm{~b} /$ steradian per proton track. This is based on the known solid angle used for the spectrograph, $3.55 \times 10^{-4}$ steradian, and a target thickness of approximately $7.9 \times 10^{17}$ cobalt atom $/ \mathrm{cm}^{2}$, determined by an alpha-particle thickness gauge ${ }^{17}$ and by Rutherford scattering at 3 Mev .

The angular-distribution curves have been compared with theoretical stripping curves calculated with the aid of the tables prepared by Enge and Graue, ${ }^{18}$ based on the stripping theory as presented by Friedman and Tobocman. ${ }^{19}$ Peaks in the angular distribution centered around $0,23,35$, and 45 degrees have been recognized as arising from $l_{n}=0,1,2$, and 3 stripping, respectively. Level (26) in Fig. 2 has a maximum cross section at 60 degrees, suggesting $l_{n}=4$ stripping. A compromise value for the nuclear radius $R=6 \times 10^{-13} \mathrm{~cm}$ produces maxima in the theoretical distribution approximately at said angles. The stripping analysis further yields a value of $(2 J+1) \gamma$ where $J$ is the spin of the produced nuclear level and $\gamma$ is its reduced width. The value for $\gamma$ hereby obtained actually only resembles the reduced width for single-particle levels, and it is well known that for these levels the values obtained from stripping analyses are too small. The peak cross section, the cross section at $100-110$ degrees (back angle), the $l_{n}$ value, and the value of $(2 J+1) \gamma$ are presented in Table II. Many of the levels that have not been assigned an $l_{n}$ value appear to have forward peaking, indicating a stripping process. However, the experimental uncertainties are too large to determine the true positions of the maxima in these cases, partly because of low yield and partly because of interference by more intense $\mathrm{Co}^{60}$ or contaminant peaks in the spectrum.
The secondary maxima in the experimental angular distributions are much larger than in the theoretical distributions. At first it was thought that these secondary maxima indicated admixtures of higher $l_{n}$ value stripping. In most cases this is probably not so. For instance, the secondary maximum in the angular distribution for the $l_{n}=1$ ground state (Fig. 2) is not in the same position as the $l_{n}=3$ peak [level (3)]. Another argument is that recent work in this Laboratory shows that also in cases where higher $l_{n}$ value mixing is forbidden, the secondary maxima are large. A third argument is that the ratio of amplitudes of the two maxima stays reasonably constant for the majority of

[^4]Table II. Excitation energies, maximum and back-angle cross sections, $l_{n}$ and $\gamma$ values for the states of $\mathrm{Co}^{60}$ formed through the $\mathrm{Co}^{59}(d, p) \mathrm{Co}^{60}$ reaction.

| Peak number | $E_{x}(\mathrm{Mev})$ | Max cross section $\mu \mathrm{b} / \mathrm{sr}$ (lab) | Back-angle cross section $\mu \mathrm{b} / \mathrm{sr}$ (lab) | $\theta_{\text {opt }}$ degrees (lab) | $l_{n}$ | $\begin{gathered} 2(J+1) \gamma \\ (\mathrm{kev}) \mathrm{for} \\ R=6 \times 10^{13} \mathrm{~cm} \end{gathered}$ | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ground | 0 | 1200 | 177 | 23 | 1 | 55 |  |
| (1) | 0.058 | 720 | 94 | 23 | 1 | 33 |  |
| (2) | 0.282 | 477 | 87 | 23 | 1, (3) | 21 | (Double) |
| (3) | 0.432 | 108 | 50 | 46 | 3 | 27 | ( $I=1^{+}$) |
| (4) | 0.501 | 375 | 57 | 23 | 1 | 17 |  |
| (5) | 0.541 | 107 | 39 | 45 | 3 | 32 | $\left(I=2^{+}\right)$ |
| (6) | 0.612 | 710 | 114 | 24 | 1 | 31 |  |
| (7) | 0.738 | 35 | 21 |  |  |  | Poor statistics |
| (8) | 0.738 | 525 | 84 | 23 | ${ }_{1}^{1}$ | 22 |  |
| (10) | 1.207 | 136 | 55 |  | $(1,3)$ | 6 | Poor statistics (double) |
| (11) | 1.337 | 40 | 11 |  |  |  | Poor statistics |
| (12) | 1.377 | 235 | 108 | 29 | $(1,3)$ | 9 |  |
| $(13)$ $(14)$ | 1.447 | 54 145 | 11 26 | 25 | 1 | 6 | Poor statistics |
| (15) | 1.638 | 100 | 26 |  |  |  |  |
| (16) | 1.684 | 13 |  |  |  |  | Very weak |
| (17) | 1.707 | 13 |  |  |  |  | Very weak |
| (18) | 1.748 | 20 |  |  |  |  | Weak |
| (19) | 1.799 1.829 | 460 88 | 196 | 46 | 3 | 125 | Double |
| (21) | 1.850 | 156 | 26 | 27 | 1 | 5 |  |
| (22) | 1.887 | 91 |  | (25) | (1) |  |  |
| (23) | 1.923 | 52 |  |  |  |  |  |
| (24) | 1.979 | 220 | 71 | 45 | 3 | 57 |  |
| $(25)$ | ${ }_{2}^{2.131}$ | 90 160 | 26 110 | 25 58 | (4) | 3 | Double |
| (27) | 2.150 | 13 |  |  |  |  | Very weak |
| (28) | 2.217 | 19 |  |  |  |  |  |
| $(29)$ $(30)$ | 2.274 2.310 | 203 57 | 32 | 26 | 1 (3) | 7 |  |
| (31) | 2.348 | 188 | 50 | 45 | 3 | 49 |  |
| (32) | 2.427 | 15 |  |  |  |  | Very weak |
| (33) <br> $(34)$ | 2.591 | 150 87 | 50 |  |  | ] |  |
| (35) | 2.762 | 214 | 30 | 27 | 1 | 6 |  |
| (36) | 2.854 | 663 | 73 | $0^{+}$ | 0 | 7 | Interference from $C^{13}$ |
| (37) | 2.884 2.899 | 109 85 |  |  |  |  | ground state |
| (39) | 2.942 | 24 |  |  |  |  |  |
| (40) | 2.967 | 24 |  |  |  | ) |  |
| (41) | 3.010 | 281 | 54 | $0^{+}$ | 0 | 3 |  |
| (43) | 3.065 | 48 |  |  |  |  | Not well resolved. |
| (44) | 3.086 | 83 |  |  |  |  | Possibly more levels |
| $(45)$ $(46)$ | 3.115 3.185 | 60 885 | 118 | $0^{+}$ | 0 | 9 |  |
| (47) | 3.215 | 130 |  |  |  |  | Poor statistics |
| (48) | 3.238 | 206 | 47 | $0^{+}$ | 0 | 2 |  |
| (49) | 3.284 3.314 | 410 53 | 88 | $0^{+}$ | $(0,2)$ | 4 | Poor statistics |
| (51) | 3.339 | 253 | 58 | $0^{+}$ | $(0,2)$ | 3 |  |
| (52) | 3.367 3.419 | 53 23 |  |  |  | 7 |  |
| (54) | 3.464 | 47 |  |  |  |  |  |
| (55) | 3.498 | 82 |  |  |  |  | Interference from $\mathrm{O}^{17}$ |
| (56) | 3.564 | 212 | 40 | ${ }^{35}{ }^{+}$ | ${ }_{0}^{2}$ | 203 | ground state |
| (58) | 3.653 | 171 | 46 |  |  |  |  |
| (59) | 3.682 | 80 | 23 |  |  | J |  |

the levels. Only in cases where the relative secondary maximum in an $l_{n}=1$ curve is higher than usual and also displaced 'so as to line up better with the pure $l_{n}=3$ peak, is an $l_{n}=3$ contribution assumed (Table II). In this connection, it should be noted that the maximum cross section for one and the same value of
$\gamma$ drops off very rapidly with increasing $l_{n}$ value. The ratio between the calculated $l_{n}=1$ and $l_{n}=3$ cross sections in the present work is about 7. For an $l_{n}=3$ contribution to be detectable under the present circumstances, the final state would have to be at least a one-to-one mixture of $f$ state into the $p$ state,


The target nucleus, $\mathrm{Co}^{59}$, has spin and parity $\frac{7-}{2}$. The spin assignments for the levels with $l_{n}=0,1,2,3$, and 4 stripping are therefore, respectively, $3^{-}$and $4^{-}$, $2^{+}$to $5^{+}, 1^{-}$to $6^{-}, 0^{+}$to $7^{+}$, and finally $0^{-}$to $8^{-}$for $l_{n}=4$. Not all of these spin values are equally probable. Especially are the "strong" $l_{n}=3$ levels not likely to have spin 0 or 7 , since this would involve capturing the neutron in the $f_{7 / 2}$ subshell. This is presumably already filled. Proton spin flip is not likely either for the levels with large stripping cross sections.

It is interesting to compare the results of this work with the results of the stripping analysis of the
$\mathrm{Ni}^{60}(d, p) \mathrm{Ni}^{61}$ reaction. ${ }^{20}$ The difference between the two residual nuclei is that in $\mathrm{Ni}^{61}$ the proton $f_{7 / 2}$ shell is filled; in $\mathrm{Co}^{59}$ one proton is removed from this shell. In $\mathrm{Ni}^{61}$ the ground state is formed by $l_{n}=1$ stripping. The state is presumably a $p_{3 / 2}$ state. There is also a strong $l_{n}=1$ state at 0.28 Mev and some weaker ones around 1 and 2 Mev . Corresponding to each of these $\mathrm{Ni}^{61}$ levels, one might hope to find multiplets in $\mathrm{Co}^{60}$, for example, four $\left(f_{7 / 2}\right)^{-1} p_{3 / 2}$ states with spin $2^{+}, 3^{+}$, $4^{+}$, and $5^{+}$. The two strong $p$ states in $\mathrm{Ni}^{61}$ should then appear in $\mathrm{Co}^{60}$ as two multiplets with a total of eight or six states, depending upon whether the $0.28-\mathrm{Mev}$ state also is $p_{3 / 2}$ (most likely) or $p_{1 / 2}$. There are seven $p$ states of comparable intensity listed in Table IJ. Of these states, level (2) is almost certainly a doublet, but one of the members is rather weak. It is fruitless to do any more speculation about the structure of these levels before exact spin assignments have been made. Because of the large number of states involved, the relativeintensity rule (factor $2 J+1$ ) used with some success earlier ${ }^{14}$ is not of much help in this case.

In $\mathrm{Ni}^{61}$ only one level (at 65 kev ) was found with strong $l_{n}=3$ stripping contribution. In $\mathrm{Co}^{60}$ one should hope to find six corresponding levels, that is, members of the $\left(f_{7 / 2}\right)^{-1}\left(f_{5 / 2}\right)$ multiplet. Table II shows that there are six levels [since No. (19) is a doublet] with pure or almost pure $l_{n}=3$ stripping. The excitation energies range from 0.43 to 2.35 Mev . If these levels are indeed the members of the $\left(f_{7 / 2}\right)^{-1}\left(f_{5 / 2}\right)$ multiplet, they should have spin values $J=1^{+}$to $6^{+}$, and the relative values of $(2 J+1) \gamma$ would be expected to be determined mostly by the factor ${ }^{21}(2 J+1)$. The level with the lowest intensity and, hence, presumably the lowest spin value is No. (3), the $l_{n}=3$ state with the lowest energy. This agrees with Nordheim's "strong rule" predicting the $f_{7 / 2}$ proton and the $f_{5 / 2}$ neutron to couple antiparallel in the lowest state.

## ACKNOWLEDGMENTS

The plate scanning was done by W. Tripp and Miss Estelle Freedman. We are indebted to all our colleagues at the High Voltage Laboratory for help and advice and to Professor W. W. Buechner and Professor A. K. Kerman for enlightening discussions.

[^5]
[^0]:    * This work has been supported in part through funds provided by the U. S. Atomic Energy Commission, by the Office of Naval Research, and by the Air Force Office of Scientific Research.
    $\dagger$ Part of this work is from a joint thesis submitted by two of the authors (DLJ and CCA) to the Massachusetts Institute of Technology in partial fulfillment of the requirements for the degree of Master of Science in Physics under the Naval Postgraduate Training Program.
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