

Symmetries of the Strong Interactions

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An attempt is made to study the symmetry properties of the strong baryon-meson couplings without using arguments concerning the origin of the baryon mass differences. It is shown that too high a symmetry is incompatible with associated production experiments. The argument is independent of perturbation theory. It is assumed that the Σ and Λ have the same spin, that the (Σ, Λ) parity is even, and that the usual isotopic spin assignments are correct. The general conclusions may have to be revised if it would turn out that the commonly assumed baryon spectrum is incomplete.

I. INTRODUCTION

SEVERAL theoretical approaches have been made recently to a somewhat more detailed dynamics of the strong interaction of baryons with π and K mesons. The common idea is to make assumptions stronger than charge independence: one postulates¹⁻³ coupling constant equalities which are more restrictive than charge independence implies.

In these attempts a certain emphasis is laid on the notion that in the absence of some of the strong couplings⁴ there exist what may be called supermultiplets. For example, one assumes^{2,3} that in the absence of all strong K couplings the baryons are completely mass degenerate and then arrives at inequalities between the K -coupling constants to account for the large mass splits. Such arguments are perhaps plausible but not entirely convincing, as a satisfactory interpretation of mass differences is beyond the techniques of present field theories and, at least to some extent, it may be beyond its scope. It is the purpose of this paper to show that similar conclusions can be arrived at by arguments which are not in themselves tied to the interpretation of mass differences.

We shall begin by assuming that there exists an equality between the $[\Lambda, \Sigma, \pi]$ and the $[\Sigma, \Sigma, \pi]$ coupling constants. This is a weaker assumption on π interactions than the one made in the mentioned papers.^{2,3} We shall furthermore assume that the $[\Lambda, N, K]$ and $[\Sigma, N, K]$ have equal coupling strengths and likewise for $[\Sigma, \Lambda, K]$ and $[\Sigma, \Sigma, K]$. The relative magnitude of the π versus the K couplings is immaterial to the argument. Then the following result will be proved, independent of perturbation theory:

To the extent that one may neglect the (Σ, Λ) mass difference in dynamical calculations (not in the kinematics), the above assumptions are incompatible with the present experimental information on associated production in π -nucleon collisions. It should be emphasized that the neglect of $m_\Sigma - m_\Lambda$ means the following: relations will be derived between the transition prob-

abilities of certain processes. These relations are valid up to terms of relative order δ , where

$$\delta = (m_\Sigma - m_\Lambda) / m_\Lambda \sim 0.067,$$

and in some instances they are valid up to order $\delta^2 \sim 0.005$.

In this way one is led to recognize that within the realm of the strong interactions there occur "breaks in symmetry" irrespective of arguments concerning the hyperon mass spectrum. Of course, one cannot say so far whether they occur in the π or in the K couplings. It should be noted at once, however, that it is essential to the present reasoning that one may consider the commonly assumed baryon spectrum to be complete. In particular the above conclusion might have to be revised if it would turn out that there exist "excited Λ^0 states," i.e., hyperon states with $I=0, S=-1$ but with higher mass than the Λ^0 (see Sec. III). If this were the case, a high symmetry is not necessarily ruled out.

The method described in the next section is based on the recognition that the mentioned relations between coupling constants make it possible to define auxiliary quantum numbers by means of which one quickly arrives at the stated result. In Sec. III further comments are made. Section IV deals with some applications of the present method to specific cases of lower symmetry.

II. METHOD

We ask if the following set (I)-(IV) of assumptions are compatible with experiment (the discussion of a fifth assumption is deferred till Sec. III):

(I) The Σ and Λ spin are equal. Indications are that both spins are $\frac{1}{2}$. For convenience all baryon spins are taken to be $\frac{1}{2}$ in what follows and the K spin is assumed to be zero, as it probably is. However, it will become evident later that the value of the cascade and of the K spin are immaterial to the argument.

(II) The (Σ, Λ) parity is even. Possible means to determine this parity experimentally have been discussed recently.⁵ The argument will be independent of

¹ J. Schwinger, Phys. Rev. **104**, 1164 (1956).

² M. Gell-Mann, Phys. Rev. **106**, 1296 (1957).

³ J. Schwinger, Ann. Phys. **2**, 407 (1957).

⁴ Of course, the effects of electromagnetic and weak couplings are ignored as well in making such arguments.

⁵ See A. Pais and S. B. Treiman, Phys. Rev. **109**, 1759 (1958). More precisely, (II) should read: the Σ and Λ couplings have the same space-time structure.

the parity of the K relative to (nucleon, Λ^0) and of the (Ξ , nucleon) parity.

If Σ and Λ would have either different spin or odd relative parity, the subsequent argument in which further assumptions are put to a test would be irrelevant.

(III) All strong couplings are charge independent. In this framework we may consider the following well-known set of strong π -baryon interactions⁶:

$$[N_1, N_1, \pi] = iG_1 \bar{N}_1 \boldsymbol{\tau} \gamma_5 N_1 \boldsymbol{\pi}, \quad (1)$$

$$[\Sigma, \Lambda, \pi] = iG_2 (\bar{\Sigma}^+ \gamma_5 \Lambda^0 \pi^+ + \bar{\Sigma}^0 \gamma_5 \Lambda^0 \pi^0 + \bar{\Sigma}^- \gamma_5 \Lambda^0 \pi^-) + \text{h.c.}, \quad (2)$$

$$[\Sigma, \Sigma, \pi] = iG_3 \{ (\bar{\Sigma}^0 \gamma_5 \Sigma^- - \bar{\Sigma}^+ \gamma_5 \Sigma^0) \pi^+ + (\bar{\Sigma}^+ \gamma_5 \Sigma^+ - \bar{\Sigma}^- \gamma_5 \Sigma^-) \pi^0 + (\bar{\Sigma}^- \gamma_5 \Sigma^0 - \bar{\Sigma}^0 \gamma_5 \Sigma^+) \pi^- \}, \quad (3)$$

$$[N_4, N_4, \pi] = iG_4 \bar{N}_4 \boldsymbol{\tau} \gamma_5 N_4 \boldsymbol{\pi}. \quad (4)$$

Here N_1 and N_4 are two-component fields:

$$N_1 = \begin{pmatrix} \hat{p} \\ n \end{pmatrix}, \quad N_4 = \begin{pmatrix} \Xi_0 \\ \Xi^- \end{pmatrix}; \quad (5)$$

the upper (lower) component corresponds to $\tau_3 = +1$ (-1). The K couplings are

$$[\Lambda, N_1, K] = F_1 \bar{N}_1 \cdot \Lambda^0 K + \text{h.c.}, \quad (6)$$

$$[\Sigma, N_1, K] = F_2 \bar{N}_1 \cdot \boldsymbol{\tau} \Sigma K + \text{h.c.}, \quad (7)$$

$$[N_4, \Lambda, K] = F_3 \bar{N}_4 \cdot \Lambda^0 K_c + \text{h.c.}, \quad (8)$$

$$[N_4, \Sigma, K] = F_4 \bar{N}_4 \cdot \boldsymbol{\tau} \Sigma K_c + \text{h.c.} \quad (9)$$

The notations are as follows: the dot to the right⁷ of \bar{N} stands for the choice between 1 and $i\gamma_5$ depending on whether the (N_1, Λ, K) parity is even (odd). As the (Σ, Λ) parity is assumed to be even, one has to make the same choice in Eqs. (6) and (7), and likewise in (8) and (9). As the Ξ parity is irrelevant for what follows, the choice for Eqs. (6) and (7) is so far independent from that for Eqs. (8) and (9). K is a two-component field, K_c its charge conjugate:

$$K = \begin{pmatrix} K^+ \\ K^0 \end{pmatrix}, \quad K_c = \begin{pmatrix} -\bar{K}^0 \\ \bar{K}^+ \end{pmatrix}. \quad (10)$$

Finally we consider the following assumption:

(IV) There exist these relations between the coupling constants

$$G_2 = G_3 = G; \quad F_1 = F_2 = F_I; \quad F_3 = F_4 = F_{II}. \quad (11)$$

⁶ As usual, a particle symbol denotes the corresponding annihilation operator. The γ_5 symbolizes the pseudoscalar nature of the π meson. From the point of view of the present argument the space-time structure of the coupling need not be specified in further detail. h.c. means hermitian conjugate.

⁷ This dot is dropped in the following.

TABLE I. Auxiliary quantum numbers S_1 and S_2 for the baryons and mesons.

	S_1	S_2
$\pi; N_1$ (nucleon)	0	0
K^\pm	± 1	0
$K^0 (\bar{K}^0)$	0	1(-1)
$N_2 (\Sigma^+, Y^0)$	0	-1
$N_3 (Z^0, \Sigma^-)$	-1	0
N_4 (cascade)	-1	-1

We now introduce the one dynamical approximation to be made (in the sense explained in Sec. I) which is the neglect of the Σ , Λ mass difference,⁸ the smallest such difference in the baryon system. It will never be necessary in what follows to ignore any other isotopic multiplet splitting. Then all π interactions can be collected as

$$[\pi] = i[G_1 \bar{N}_1 \boldsymbol{\tau} \gamma_5 N_1 + G(\bar{N}_2 \boldsymbol{\tau} \gamma_5 N_2 + \bar{N}_3 \boldsymbol{\tau} \gamma_5 N_3) + G_4 \bar{N}_4 \boldsymbol{\tau} \gamma_5 N_4] \boldsymbol{\pi}, \quad (12)$$

and the K interactions can be written as

$$[K] = F_I \sqrt{2} [(\bar{N}_1 N_2) K^0 + (\bar{N}_1 N_3) K^+] + F_{II} \sqrt{2} [(\bar{N}_4 N_2) \bar{K}^+ + (\bar{N}_4 N_3) \bar{K}^0] + \text{h.c.}, \quad (13)$$

where

$$N_2 = \begin{pmatrix} \Sigma^+ \\ Y^0 \end{pmatrix}, \quad N_3 = \begin{pmatrix} Z^0 \\ \Sigma^- \end{pmatrix}. \quad (14)$$

Here the following convenient quantities² have been introduced:

$$Z^0 = 2^{-1/2} (\Lambda^0 + \Sigma^0), \quad Y^0 = 2^{-1/2} (\Lambda^0 - \Sigma^0). \quad (15)$$

From Eqs. (12) and (13), it is at once evident that the possibility exists of invariantly gauging N_2 and K^0 oppositely. Likewise and independently one may proceed for N_3 and K^+ . The gauge of N_4 is then uniquely determined. Correspondingly one may assign two quantum numbers S_1, S_2 to each baryon and meson. An appropriate set of values of S_1, S_2 is given in Table I. We have

$$S = S_1 + S_2, \quad (16)$$

where S is the usual strangeness. S conservation is, of course, guaranteed to begin with by Eqs. (1-4) and (6-9). In the present situation, however, we have a stronger set of rules:

(A) The separate conservation of S_1, S_2 . (Observe that we may accordingly assign $I = \frac{1}{2}$ to all baryons, $I = 0(1)$ to $K(\pi)$ mesons. Then the charge operator is

$$Q = I_3 + S_1 + N/2.$$

(B) The invariance for the following combined interchanges:

$$N_2 \rightarrow N_3, \quad K^+ \rightarrow K^0, \quad -\bar{K}^0 \rightarrow \bar{K}^+.$$

⁸ The mass differences within an isotopic multiplet are neglected as usual.

The two rules (A) and (B) make it a trivial matter to prove the statement made in Sec. I. Let us first consider

$$\pi^- + p \rightarrow \Lambda^0 + K^0, \quad (17)$$

$$\pi^- + p \rightarrow \Sigma^0 + K^0. \quad (18)$$

According to rule (A) a π -nucleon state can combine with a $Y^0 K^0$, but not with a $Z^0 K^0$ state:

$$\langle Y^0 K^0 | \pi^- p \rangle \neq 0; \quad \langle Z^0 K^0 | \pi^- p \rangle = 0. \quad (19)$$

From Eqs. (15) and (19) we have therefore

$$\langle \Lambda^0 K^0 | \pi^- p \rangle = -\langle \Sigma^0 K^0 | \pi^- p \rangle, \quad (20)$$

or

$$d\sigma(\Lambda^0 K^0) \approx d\sigma(\Sigma^0 K^0). \quad (21)$$

The near-equality sign serves to remind one of the kinematical phase space differences. This relation is not unreasonable. Experiment indicates⁹ that the total cross sections for Λ^0 and Σ^0 production are not very different, while both reactions are characterized by a similar-looking backward peaking of the distribution in angle between the incoming π^- and the emerging hyperon (in the center-of-mass system). Considerable uncertainty seems to attach to the information regarding the Σ^0 reaction, however.

More precisely, Eq. (21) means that the transition probabilities for $\Lambda^0 K^0$ and $\Sigma^0 K^0$ production are equal up to terms of order δ . (An inspection of the problem in perturbation theory indicates that this estimate may be too cautious.)

Next consider the reactions

$$\pi^- + p \rightarrow \Sigma^- + K^+, \quad (22)$$

$$\pi^+ + p \rightarrow \Sigma^+ + K^+. \quad (23)$$

We note first that the rule (B) implies in particular the interchange $Y^0 \leftrightarrow \Sigma^-$, $K^+ \leftrightarrow K^0$. Hence it follows from Eqs. (15) and (20) that

$$\langle \Sigma^- K^+ | \pi^- p \rangle = -\sqrt{2} \langle \Sigma^0 K^0 | \pi^- p \rangle, \quad (24)$$

or

$$d\sigma(\Sigma^- K^+) = 2d\sigma(\Sigma^0 K^0). \quad (25)$$

Experimentally⁸ the Σ^- -production reaction has a cross section which seems to be somewhat smaller than that for the Λ^0 case. The factor two in Eq. (25) is at any rate inadmissible. Even more striking is the discrepancy in angular distribution: the Σ^- is peaked forward, the Σ^0 backward.

Furthermore it follows from Eqs. (13) and (14) that

$$\langle \Sigma^+ K^+ | \pi^+ p \rangle = 0, \quad (26)$$

so that the Σ^+ reaction would be forbidden which it

certainly is not.¹⁰ More precisely, Eq. (26) means that the cross section for $\Sigma^+ K^+$ production is zero to order δ^2 . This statement in itself has little meaning as presumably many large coupling constants are involved. It seems reasonable to say, however, that the present assumptions would indicate a ratio of order δ^2 between $\Sigma^- K^+$ and $\Sigma^+ K^+$ production which is an experimentally inadmissible result.

Thus we come to the conclusion stated in Sec. I that the assumptions (III) and (IV) are incompatible with experiment to the extent that one may rely on a theoretical argument in which δ is neglected. It is easy to find further paradoxes. For example, the reaction

$$K^0 + p \rightarrow K^+ + n \quad (27)$$

is forbidden, as was noted by Barshay¹¹ in a related context. Again the forbiddenness means a ratio $\sim \delta^2$ as compared to nonexchange scattering. Furthermore $K^- + p \rightarrow \Sigma^+ + \pi^-$ is forbidden, etc.

III. COMMENTS

(1) In the language of field theory, the neglect of the (Σ, Λ) mass difference is made only with respect to the virtual appearance of these particles (internal lines). To correct for this in a given order of approximation is simple but perhaps not too meaningful. One would expect such qualitative statements as Eq. (25) to be true within a 10% margin.

(2) It is readily verified that the present results also hold true if one replaces Eq. (11) by

$$G_1 = -G_2, \quad F_1 = -F_2, \quad F_3 = -F_4. \quad (28)$$

(3) It has been suggested by Gell-Mann² and by Schwinger³ that the following G symmetry be imposed:

$$G_1 = G_2 = G_3 = G_4. \quad (29)$$

If this is true, at least one of the F symmetries of Eq. (12) is broken. These authors come, of course, to the same conclusion by considering the baryon mass splitting. Evidently neither the latter nor the present arguments are sufficient to decide which of the two (or both): G or F symmetry, is broken.

(4) A break in either F or G symmetry (or in both) destroys the validity of the rules (A) and (B) of Sec. II simultaneously. It is interesting to note that the retention of rule (A) combined with a violation of rule (B) would mean: first that the relation (21) between the Λ^0 - and Σ^0 -production cross sections is maintained, second that the unwanted relation (25) is no longer valid. Theoretically a situation of this kind corresponds to a violation of the assignments $I=1$ for Σ and $I=0$

⁹ D. Glaser, *Proceedings of the Seventh Annual Rochester Conference on High-Energy Nuclear Physics, 1957* (Interscience Publishers, New York, 1957), Sec. V; Brown, Glaser, and Perl, *Phys. Rev.* **108**, 1036 (1957); see also Graves and Glaser (to be published); L. B. Leipuner and R. K. Adair, *Phys. Rev.* **109**, 1347 (1958); Planos, Samios, Schwartz, Steinberger, and Eisler, Nevis Report R173 (unpublished).

¹⁰ See, for example, Vandervelde, Cronin, and Glaser (to be published). Note that the relations (25) and (26) are equivalent to the statement that the reactions in question go only via the $I=\frac{1}{2}$ channel.

¹¹ S. Barshay, *Phys. Rev.* **109**, 2160 (1958). This author also considers a coupling of the type $\bar{K}K\pi^2$. This interaction can likewise be dealt with by the present method.

for Λ^0 . It would not affect in any way the meaning and the range of validity of the charge independence concept as applied to π -nucleon phenomena.

The reason for making this remark is that some doubt has been expressed recently^{9,10} about the validity of charge independence. There is some indication, although the evidence is not very firm, for a violation of one of the so-called triangle inequalities which relate the cross section for the reactions (18), (22), (23). This inequality follows from charge independence together with the notion that the Σ states form an $I=1$ triplet. If further experiments would confirm the violation in question, one might consider a description of the (Σ, Λ) system as a (triplet, singlet) with some admixture¹² of (doublet, doublet). Consequences of this would be the existence of a contribution to the $\Sigma^+ - \Sigma^-$ and to the $K^+ - K^0$ mass difference without the intermediary of the electromagnetic field. The experimental magnitude of these differences¹³ suggests perhaps that such admixtures should be small. At any rate, rule (A) must of necessity be broken to avoid the null result of Eq. (26).

(5) There is another way, however, in which apparent violations of charge independence could come about: Let us assume for the moment that there exists a particle $\Lambda^{0'}$ which, like the Λ^0 , has $I=0, S=-1$. As long as $m(\Lambda^{0'}) - m(\Sigma^0) < m(\pi^0)$, $\Lambda^{0'}$ would be stable against π emission into either Σ or Λ^0 ; the latter transition would be forbidden as an isotopic $0 \rightarrow 0$ reaction. On the other hand, the reactions $\Lambda^{0'} \rightarrow \Lambda^0 + \gamma$ [and $\Lambda^{0'} \rightarrow \Sigma^0 + \gamma$ if $m(\Lambda^{0'}) > m(\Sigma^0)$] would be allowed and would generally be of comparable speed to $\Sigma^0 \rightarrow \Lambda^0 + \gamma$. Thus a hypothetical $\Lambda^{0'}$ would introduce an "anomalous Σ^0 effect" which would necessitate a reinterpretation of the experimental information that bears on the triangle inequalities.

Conversely, if a $\Lambda^{0'}$ were to exist, it can readily be seen that all the arguments of Sec. II would need a thorough revision. The symmetry implied by Eq. (11) could then not be ruled out on such general grounds. For the present we shall merely state that the results of Sec. II can only be maintained if one moreover makes the following assumption:

(V) The commonly known baryon spectrum is complete.

(6) The indications of a possible hierarchy of symmetries within the strong interactions are reminiscent of the developments in attempts to view the isotopic spin and strangeness rules jointly within a four-dimensional isotopic framework. The initial attempt in this direction¹⁴ failed as the degree of symmetry invoked was too high (full four-dimensional invariance for all

¹² This can be achieved dynamically in many ways. For example, one could generalize Eq. (12) to $[\pi]_j' = i \sum_{j=1}^4 G_j' \bar{N}_j \pi \gamma_5 N_j \pi$ with G_2' slightly different from G_3' .

¹³ See L. Alvarez, *Proceedings of the Seventh Annual Rochester Conference on High-Energy Nuclear Physics, 1957* (Interscience Publishers, Inc., New York, 1957).

¹⁴ A. Pais, *Proc. Natl. Acad. Sci. U. S. A.* **40**, 484 (1954).

TABLE II. Auxiliary quantum numbers S_1' and S_2' for the baryons and mesons.

	S_1'	S_2'
\bar{N}_1, π^0	0	0
π^\pm	± 1	∓ 1
K^\pm	± 1	0
$K^0(\bar{K}^0)$	0	1(-1)
Σ^+, Σ^0	0	-1
Σ^0, Σ^-	-1	0
N_4	-1	-1

strong interaction phenomena). A lower symmetry in this four-space which was subsequently suggested¹⁵ is compatible (but not in a compelling way) with the presently known phenomena. It may be noted that the condition (29) of G symmetry is stronger than that of full four-dimensional invariance.

IV. LOWER SYMMETRIES

The simplest way of breaking rules (A) and (B) of Sec. II is to assume that equalities (11) are true only with respect to the absolute values of the constants in question. Indeed, certain combinations of sign changes [other than Eq. (28)] are sufficient to invalidate the symmetries.¹⁶ In such a situation, methods similar to the one of Sec. II are helpful to pinpoint the way in which the lack of full symmetry shows itself. We shall briefly state a few results.

$$(a) \quad G_2 = G_3; \quad F_1 = -F_2, \quad F_3 = -F_4.$$

Denote the totality of the eight interactions by H and put

$$H = H_0 + H_1, \quad (30)$$

$$H_1 = i[G_1 \bar{p} \gamma_5 n + G_4 \bar{\Xi}^0 \gamma_5 \Xi^-] \pi^+ + \text{h.c.} \quad (31)$$

With respect to H_0 only, one can again introduce a set of auxiliary quantum numbers S_1', S_2' , with $S = S_1' + S_2'$. These numbers are listed in Table II. It is then easy to see that, if H_0 only were operative, the following statements hold true: (a) The masses of Σ and Λ , if equal in the absence of H_0 remain equal in the presence of H_0 . (b) The relation (21) is valid. (c) The reactions (22) and (27) are not allowed by H_0 .

One shows next that the substitution

$$\Sigma^0 \rightarrow \Lambda^0, \quad \Sigma^\pm \rightarrow \mp \Sigma^\pm, \quad (32)$$

$$K \rightarrow K, \quad \pi \rightarrow \pi, \quad N_1 \rightarrow -\tau_3 N_1, \quad N_4 \rightarrow -\tau_3 N_4 \quad (33)$$

¹⁵ A. Pais, *Proceedings of the Fifth Annual Rochester Conference on High-Energy Physics, 1955* (Interscience Publishers, Inc., New York, 1955). In the work of A. Salam and J. C. Polkinghorne, *Nuovo cimento* **2**, 685 (1955), the π and K mesons are treated in the same way as in the foregoing two papers (apart from their comment on the τ meson which is no longer relevant). The difference between the two formulations lies in the description of the baryons: in the former case half-integral representations are used, in the latter integral ones. Whether either attempt is fruitful will presumably depend on further developments in particle dynamics.

¹⁶ Some of the cases listed below have been considered by Schwinger, reference 3. See also S. Barshay, *Phys. Rev.* **107**, 1454 (1957).

yields

$$H_0 \rightarrow H_0, \quad H_1 \rightarrow -H_1. \quad (34)$$

This means that with regard to H_1 we have something like a Furry theorem. For example, it follows immediately that

(a) To the extent that one neglects δ in dynamical calculations, a mass displacement between Λ and Σ comes about because of contributions odd in H_1 . It follows trivially that to the extent of validity of the Gell-Mann identity¹⁷ for the baryon masses, the Λ and Σ masses remain degenerate under the present conditions.

(b) The matrix elements for the reactions (22) and (27) are odd in H_1 (barring terms of relative order δ).

$$(\beta) \quad G_2 = -G_3, \quad F_1 = F_2, \quad F_3 = F_4.$$

The analysis and results are substantially the same as in the previous case.

$$(\gamma) \quad G_2 = G_3, \quad F_1 = F_2, \quad F_3 = -F_4.$$

Again the rules (A) and (B) are broken but now the dynamics looks entirely different. Here the lack of symmetry is one between the nucleon-doublet and the cascade-doublet. Put

$$H = H_0' + H_1', \quad (35)$$

$$H_1' = iF_3 [(\bar{\Sigma}^- \bar{K}^+ - \bar{\Sigma}^0 \bar{K}^0) \Lambda^0 + (\bar{\Sigma}^- \bar{K}^+ + \bar{\Sigma}^0 \bar{K}^0) \Sigma^0] + \text{h.c.} \quad (36)$$

¹⁷ See reference 2, footnote 13.

With respect to H_0' one can use the assignments of Table I and the conclusions of Sec. II. With respect to the substitution

$$N_1 \rightarrow N_1, \quad N_2 \rightarrow -N_2, \quad N_3 \rightarrow N_3, \quad N_4 \rightarrow N_4, \quad (37)$$

$$\pi \rightarrow \pi, \quad K \rightarrow \tau_3 K, \quad K_c \rightarrow \tau_3 K_c,$$

one has

$$H_0' \rightarrow H_0', \quad H_1' \rightarrow -H_1', \quad (38)$$

and thus one obtains a Furry theorem for H_1' with similar kinds of applications as were mentioned above. The remaining sign combinations for the constants form an analogous pattern.

Thus the separation of H into a 0 and a 1 part seems useful to get an over-all insight in this complicated dynamical situation. It is to be hoped that other arguments of a rather qualitative kind may yield further clues about the maze of baryon-meson interactions.

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Note added in proof.—In connection with symmetry considerations one sometimes finds in the recent literature the statement that baryon self-energies are even functions of the coupling constants.¹⁸ In general this is not the case, however. For any baryon the most general expression for the self-energy is

$$W = W^{(1)} + F_1 F_2 G_2 W^{(2)} + F_3 F_4 G_2 W^{(3)} + F_1 F_2 F_3 F_4 W^{(4)},$$

where the four functions $W^{(i)}$ are all even in F_i , $i = 1, \dots, 4$ and in G_2 .

¹⁸ See, e.g., J. C. Polkinghorne, *Nuovo cimento* **6**, 864 (1957).