

is high and the deuteron energy rather low. We might therefore expect to find spin-flip stripping showing up most strongly for the lower lying states in reactions of large  $Q$  value.

#### ACKNOWLEDGMENTS

I am grateful to Professor W. C. Parkinson for reviving my interest in the first excited state of B<sup>11</sup> and for pointing out the interesting implications for strip-

ping theory. I should also like to thank Mr. A. G. Rubin for his help in taking the measurements.

*Note added in proof.*—Professor Parkinson has kindly informed me that the idea of spin flip by the departing nucleus in a stripping reaction is due not to him but to Professor A. P. French of the Cavendish Laboratory, Cambridge, and now of the University of South Carolina who conceived of it in about 1952 in terms of an exchange process of intrinsic spins. Professor Parkinson also informs me that the possibility of spin flip in the particular case of interest here is discussed by Dr. N. T. S. Evans in his Ph.D. thesis (1956) at the Cavendish Laboratory.

### Quadrupole Moments of Os<sup>189</sup>, Ta<sup>181</sup>, Lu<sup>175</sup>, and La<sup>139</sup>

KIYOSHI MURAKAWA AND TOHRU KAMEI\*

*Institute of Science and Technology, Komaba-machi, Meguro-ku, Tokyo, Japan*

(Received October 5, 1956)

The quadrupole moment of Os<sup>189</sup> was determined from the hyperfine structure of the level  $5d^66s^2\ ^5D_4$  of Os I and was found to be  $Q(\text{Os}^{189}) = (+0.8 \pm 0.2) \times 10^{-24}$  cm<sup>2</sup> without shielding correction. The quadrupole moments (without shielding correction) of Ta<sup>181</sup>, Lu<sup>175</sup>, and La<sup>139</sup> that were determined previously from the configurations  $5d^36s^2$ ,  $5d6s^2$ , and  $5d^26s$  respectively are, in units of  $10^{-24}$  cm<sup>2</sup>,  $+3.9 \pm 0.4$ ,  $+5.1 \pm 0.3$ , and  $+0.5 \pm 0.2$  respectively. If one assumes a shielding correction of  $-0.3$  for the  $5d$  electron, these values become  $Q(\text{Os}^{189}) = +0.6 \pm 0.14$ ,  $Q(\text{Ta}^{181}) = +2.7 \pm 0.3$ ,  $Q(\text{Lu}^{175}) = +3.6 \pm 0.2$ , and  $Q(\text{La}^{139}) = +0.3 \pm 0.1$  in units of  $10^{-24}$  cm<sup>2</sup>, where the probable error does not include the uncertainty of the shielding correction.

#### I. INTRODUCTION

ACCORDING to the calculations of Sternheimer,<sup>1</sup> the atomic core shields or antishields the nuclear quadrupole coupling, so that the quadrupole moment ( $Q$ ) deduced from the hyperfine structure (hfs) of atomic spectra must be multiplied by the factor  $1 + \Delta$ , in order to get the true quadrupole moment.  $\Delta$  is the shielding correction, which we called the "polarization correction" in previous work. Sternheimer has recently published a more accurate calculation concerning the shielding correction.<sup>2</sup>

In our previous work<sup>3,4</sup> on  $Q(\text{La}^{139})$ ,  $Q(\text{Lu}^{175})$ , and  $Q(\text{Ta}^{181})$ , the values of  $\Delta$  for the  $5d$  electron were taken from the tabulation in reference 1. The more accurate calculation<sup>2</sup> shows that these values must be revised. Sternheimer<sup>2</sup> calculated the values of  $\Delta$  for the configurations Cu I  $3d^94s^2$  and W I  $5d^4$ ; the other values are concerned with  $p$  electrons only. According to Sternheimer,<sup>5</sup> concerning the shielding correction for

the states Ta I  $5d^36s^2$  and Os I  $5d^6s^2$ , it is likely from his calculations for W I  $5d^4$  that for these states the anti-shielding will predominate, leading to  $\Delta < 0$ ; however, such a conclusion cannot be drawn with certainty, but could be verified only by specific calculations for these elements with the appropriate wave functions. In the present work, therefore, we shall leave the accurate calculation of the shielding correction of the  $5d$  electron of La, Os, Lu, and Ta for future work and tentatively assume that it is the same as in the case of W I  $5d^4$ , namely  $\Delta = -0.3$ , and examine whether it leads to reasonable values of  $Q$ .

#### II. QUADRUPOLE MOMENT OF Os<sup>189</sup>

In previous work,<sup>3,6</sup> the hfs of Os I  $\lambda 4260(5d^66s^2\ ^5D_4 - 5d^66s6p\ ^7D_5)$ <sup>7</sup> was studied,<sup>4</sup> but the splitting of the final level for the isotope Os<sup>189</sup> ( $I = \frac{3}{2}$ ) could not be deduced from the observed hfs by a purely empirical method, and this introduced uncertainty in deducing the value of  $Q(\text{Os}^{189})$  (footnote 22 of reference 3). In the present work the hfs of Os I  $\lambda 4420(5d^66s^2\ ^5D_4 - 5d^66s6p\ ^7D_4)$  was studied, and the result of the measurement is shown schematically in Fig. 1. From Fig. 1 of the present work and Fig. 3 of reference 3, we get the interval factor  $A = 0.008$  cm<sup>-1</sup>, and the quadrupole coupling constant  $B = 0.104 \times 10^{-3}$  cm<sup>-1</sup> for the common final level  $5d^66s^2\ ^5D_4$  for the isotope Os<sup>189</sup>.

\* Present address: Institute of Nuclear Study, University of Tokyo, Tanashi, Tokyo, Japan.

<sup>1</sup> R. M. Sternheimer, Phys. Rev. **80**, 102 (1950); **84**, 244 (1951); **86**, 316 (1952).

<sup>2</sup> R. M. Sternheimer, Phys. Rev. **95**, 736 (1954). Sternheimer's  $1/(1-R)$  is our  $1+\Delta$ .

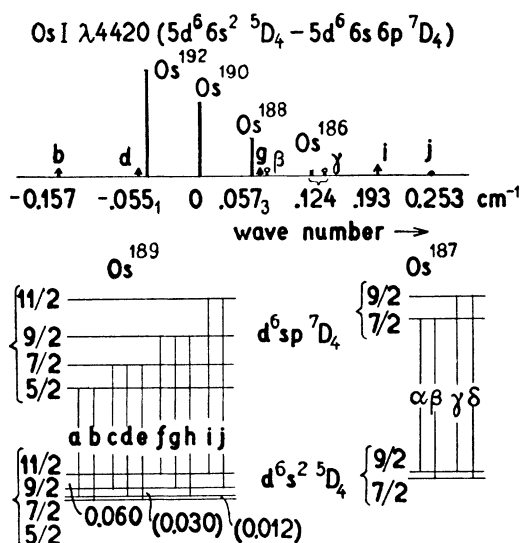
<sup>3</sup> K. Murakawa, Phys. Rev. **98**, 1285 (1955). Erratum: Eq. (5) should read  $(d^4s\ ^6D_3\ \frac{1}{2} | \omega | d^4s\ ^6D_1\ \frac{1}{2}) = -(2/4375)(584R_2' - 91R_2'' + 132S_2)$ .

<sup>4</sup> T. Kamei, Phys. Rev. **99**, 789 (1955).

<sup>5</sup> R. M. Sternheimer (private communication). We thank Professor Sternheimer for these suggestions and for communicating to us the result of his improved calculations prior to publication.

<sup>6</sup> K. Murakawa and S. Suwa, Phys. Rev. **87**, 1048 (1952).

<sup>7</sup> The classification and the term notation of the Os I spectrum are taken from W. Albertson, Phys. Rev. **45**, 304 (1934).

FIG. 1. hfs of Os I  $\lambda 4420$ .

Using the formula given in reference 3, we get  $Q(\text{Os}^{189}) = (+0.8 \pm 0.2) \times 10^{-24} \text{ cm}^2$  without shielding correction. If we assume a shielding correction  $\Delta = -0.3$ , this becomes  $Q(\text{Os}^{189}) = (+0.6 \pm 0.14) \times 10^{-24} \text{ cm}^2$ .

### III. QUADRUPOLE MOMENT OF Ta<sup>181</sup>

Analysis<sup>4</sup> of the hfs of Ta I  $5d^3 6s^2$  yielded the result that  $Q(\text{Ta}^{181}) = (+4.3 \pm 0.4) \times 10^{-24} \text{ cm}^2$ , if we assume that  $\Delta = 0.103$ ; this shows that  $Q(\text{Ta}^{181}) = (+3.9 \pm 0.4) \times 10^{-24} \text{ cm}^2$  without shielding correction. If we assume  $\Delta = -0.3$ , this becomes  $Q(\text{Ta}^{181}) = (+2.7 \pm 0.3) \times 10^{-24} \text{ cm}^2$ . If we assume a strong coupling between the unbalanced nucleon and the nuclear surface, our spectroscopic quadrupole moment yields (according to the formula given by Bohr<sup>8</sup>) the intrinsic quadrupole moment  $Q_0(\text{Ta}^{181}) = 6 \times 10^{-24} \text{ cm}^2$ . On the other hand, the Coulomb excitation experiment of Huus *et al.*<sup>9</sup> yielded the result that  $Q_0(\text{Ta}^{181}) = 7 \times 10^{-24} \text{ cm}^2$ , and Goodman's investigation<sup>10</sup> gave  $Q_0(\text{Ta}^{181}) = 6.7 \times 10^{-24}$

<sup>8</sup> A. Bohr, Phys. Rev. **81**, 134 (1951); A. Bohr and B. R. Mottelson, Kgl. Danske Videnskab. Selskab, Mat.-fys. Medd. **27**, No. 16 (1953).

<sup>9</sup> Huus, Bjerregaard, and Elbek, Kgl. Danske Videnskab. Selskab, Mat.-fys. Medd. **30**, No. 17 (1956).

<sup>10</sup> C. Goodman, quoted by C. H. Townes, Symposium on Quadrupole Moment held at the University of Kyoto (Japan) in June, 1956 (unpublished).

$\text{cm}^2$ . The spectroscopic value of  $Q_0$  is now in good agreement with these values, and this shows that the above-mentioned value of  $\Delta$  is correct at least qualitatively.

### IV. QUADRUPOLE MOMENT OF Lu<sup>175</sup>

Using the data published by Gollnow,<sup>11</sup> Kamei<sup>4</sup> got  $Q(\text{Lu}^{175}) = +5.7 \times 10^{-24} \text{ cm}^2$  from the hfs of the level Lu I  $5d6s^2 \ ^2D_{3/2}$  assuming that  $\Delta = 0.107$ . This shows that  $Q(\text{Lu}^{175}) = +5.5 \times 10^{-24} \text{ cm}^2$  without shielding correction. If we assume  $\Delta = -0.3$ , this becomes  $Q(\text{Lu}^{175}) = +3.9 \times 10^{-24} \text{ cm}^2$ ;  $Q_0(\text{Lu}^{175}) = 8 \times 10^{-24} \text{ cm}^2$ . On the other hand, Huus *et al.*<sup>9</sup> gave  $Q_0(\text{Lu}^{175}) = 9 \times 10^{-24} \text{ cm}^2$ , and Goodman<sup>10</sup> obtained  $Q_0(\text{Lu}^{175}) = 7.8 \times 10^{-24} \text{ cm}^2$ . The spectroscopic  $Q_0$  is again in good agreement with  $Q_0$  obtained from the Coulomb excitation experiment.

### V. QUADRUPOLE MOMENT OF La<sup>139</sup>

Under the assumption  $\Delta_d = 0.164$ , it was concluded<sup>3</sup> that  $Q(\text{La}^{139}) = (0.6 \pm 0.2) \times 10^{-24} \text{ cm}^2$  from the hfs of the level  $5d^2 6s \ ^4F_{3/2}$ . This means that  $Q(\text{La}^{139}) = (+0.5 \pm 0.2) \times 10^{-24} \text{ cm}^2$  without shielding correction. If we assume that  $\Delta_d = -0.3$ , we get  $Q(\text{La}^{139}) = (+0.35 \pm 0.1) \times 10^{-24} \text{ cm}^2$ . On the other hand,<sup>12</sup> the value  $+0.3 \times 10^{-24} \text{ cm}^2$  without shielding correction was obtained from the hfs of the level  $5d6s \ ^3D_1$  of La II. This small discrepancy can apparently be understood by assuming that the shielding correction for the configuration  $5d^2 6s$  of La I is somewhat larger than that for  $5d6s$  of La II in absolute magnitude.<sup>13</sup>

In summary, we may conclude that the data shown in Secs. III and IV indicate the validity of Sternheimer's idea of shielding or antishielding of the nuclear quadrupole coupling by the atomic core. However, owing to the rather small accuracy of the calculations, only one-digit discussions seem to be possible at the present time.

<sup>11</sup> H. Gollnow, Z. Physik **103**, 443 (1936).

<sup>12</sup> Full details of the deduction of  $Q(\text{La}^{139})$  were published by K. Murakawa, J. Phys. Soc. (Japan) **10**, 927 (1955).

<sup>13</sup> In a recent work G. Lührs [Z. Physik **141**, 486 (1955)] has come to the conclusion that the level  $5d^2 6s \ ^4F_{3/2}$  of La I is appreciably perturbed by the level  $5d6s^2 \ ^2D_{3/2}$ , and therefore he proposes to abandon the value of  $Q$  deduced from the level  $5d^2 6s \ ^4F_{3/2}$ . This conclusion is not in agreement with that of M. F. Crawford [Phys. Rev. **47**, 768 (1935)], who showed that the perturbation is negligibly small. Lührs' conclusion is also in conflict with the theory of G. Racah [Phys. Rev. **63**, 367 (1943), Table II and Eq. (81)], and is therefore extremely difficult to accept.