actual magnitude is not markedly affected by the form of the dispersion relation and is roughly that of the observed anisotropy.

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## Relativistic and Screening Effects in Radiative Electron Capture

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HE continuous gamma-ray spectrum (inner bremsstrahlung) accompanying orbital electron capture was recently investigated theoretically.<sup>1</sup> This theory takes the  $p$ -electron capture as well as the s-electron capture and the Coulomb effects into cons-electron capture and the Coulomb elects into con-<br>sideration and gives a better agreement with experi-<br>ments in the low-energy region than earlier theories.<sup>2,3</sup> ments in the low-energy region than earlier theories.<sup>2,3</sup> A check of the theory was subsequently made' by investigating the inner bremsstrahlung from  $A^{37}$  by the method of scintillation spectroscopy with particular emphasis on the low-energy region.

A general formulation of the problem of radiative capture from the various electronic states has been made.<sup>5</sup> According to this theory, the general expression for the radiative events  $\omega_k$  per 1S-electron capture  $(\omega_c)_{1S}$  can be written, in the absence of relativistic and screening effects, as

$$
\frac{\omega_k dk}{(\omega_c)_{1S}} = \frac{\alpha}{\pi} \sum_{l} \left(\frac{Z^2 \alpha^2}{2}\right)^2 \left[1 - \frac{x - (E_l - E_{1S})}{x_{\text{max}}}\right]^2 I_l(x) dx, \quad (1)
$$

where x is the photon energy given in units of  $Z^2$  ry  $=Z^2\times 13.5$  ev;  $x_{\text{max}}$  is the upper limit of the photon energy;  $E_l$  is the ionization potential for the *l*-electron, and  $I_i(x)$  is a tabulated function. The summation has been carried out for  $l=1S$ , 2S, 2P, and 3P. In Fig. 8 of reference 4 is shown the application of this theory to the inner bremsstrahlung from  $A^{37}$ . The agreement down to 100 kev is excellent. As predicted by the theory, the experimental distribution does show a sudden increase at around 30 kev. However, the experimental points below 100 kev lie below the theoretical curve. This discrepancy was found also for the inner bremsstrahlung from  $Fe<sup>55</sup>$  by Madansky and Rasetti (Fig. 9, reference 4).

In order to explain these discrepancies, the calculations have recently been performed<sup> $5$ </sup> taking account of the relativistic effects for the S-state spectrum, and including correction factors for screening. Both the



FIG. 1. Inner bremsstrahlung from  $A^{37}$ .

relativistic and screening corrections are energy- and charge-dependent, but the variation of the latter with energy is very small. The general expression (1) can therefore be written

$$
\frac{\omega_k dk}{(\omega_c)_{1S}} = \frac{\alpha}{\pi} \sum_{l} \frac{S_l(Z)}{S_{1S}(Z)} R_l(x,Z) \left(\frac{Z^2 \alpha^2}{2}\right)^2 \times \left[1 - \frac{x - (E_l - E_{1S})}{x_{\text{max}}}\right]^2 I_l(x) dx, \quad (2)
$$

where  $S_l(Z)$  is the screening correction factor for the *l*th electron and  $R_l(x,Z)$  is the relativistic correction factor for the energy  $x$  and charge  $Z$ . The numerical values for these correction factors were determined.

The experimental data<sup>4</sup> on  $A^{37}$  have been used in a comparison with the theory given by formula (2). The treatment of the data is exactly the same as before,<sup>4</sup> i.e., the experimental points are corrected only for background and the theoretical curve is corrected for the various effects in the NaI scintillation counter. Figure 1 shows the result. The agreement is now excellent over the whole energy region.

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## Decay of  $Co<sup>61</sup>$  and  $Cu<sup>61</sup>$

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HE decay of  $1.66$ -hr Co<sup>61</sup> and 3.33-hr Cu<sup>61</sup> was investigated in this institute with  $\beta$ - and  $\gamma$ -scintillation spectrometers in various coincidence setups, with