

FIG. 1. γ spectrum of the yield from the 222-keV resonance and decay scheme for the 2.50-MeV level.

a ThC'' (2.62 Mev) source were used to calibrate the spectrometer.

PREVIOUS INVESTIGATIONS

The elastic scattering of protons from Mg^{24} in the range from 0.4 to 3.95 Mev has been thoroughly investigated by Mooring *et al.*⁶ The resonance at 418 keV was not observed. Koester⁷ interprets their data, and assigns the spin and parity $\frac{3}{2}^-$ to the level giving rise to a resonance at 825 keV.

Goldberg⁸ measured the energy and angular distribution of the neutrons in the reaction $\text{Mg}^{24}(d,n)\text{Al}^{25}$, and found groups corresponding to the levels of Al^{25} given in Table I. Two other levels of energies 1.94 and 2.92 Mev were also reported, but owing to the low statistical accuracy of their measurement, these levels were marked with a question in Goldberg's report. His spin assignments are also given in Table I.

The γ rays following the 222-keV resonance have been measured.⁹ Craig *et al.*¹⁰ report a γ ray of energy 2.03 ± 0.03 Mev with an isotropic distribution to the incident beam, and a γ ray of energy 0.47 ± 0.02 Mev.

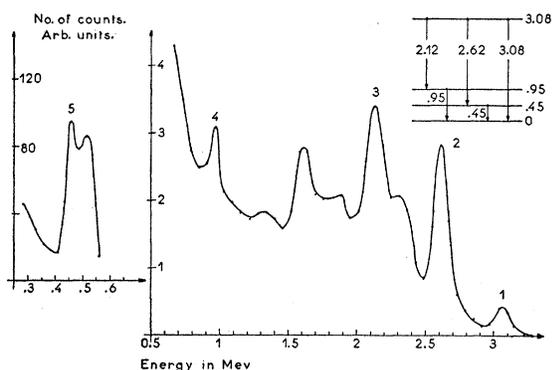


FIG. 2. γ spectrum of the yield from the 825-keV resonance and decay scheme for the 3.08-MeV level.

⁶ Mooring, Koester, Goldberg, Saxon, and Kaufmann, *Phys. Rev.* **84**, 703 (1951).

⁷ L. J. Koester, *Phys. Rev.* **85**, 643 (1952).

⁸ E. Goldberg, *Phys. Rev.* **89**, 760 (1953).

⁹ H. Casson, *Phys. Rev.* **89**, 809 (1953).

¹⁰ Craig, Cross, and Jarvis, *Phys. Rev.* **96**, 825(A) (1954).

The isotropic distribution is reported consistent with the following spins for the resonant level: $\frac{1}{2}^{\pm}, \frac{3}{2}^+$.

The Al^{25} ground-state spin of $5/2^+$ seems well established.^{8,11}

SPECTRA

Intensities

When a decay scheme consistent with our observed spectrum had been established, the areas under the photopeaks associated with the different γ rays were estimated. These areas were corrected in the following manner:

(1) First, correction was made for the absorption mechanism in the NaI crystal by the help of the experimental peak-to-total curve given by Bell.¹² This curve was roughly extrapolated to higher energies with the help of a measurement on the spectrum of the 2.76-MeV γ ray from a Na^{24} source. Our curve is given in Fig. 5. We believe that the discontinuity of Bell's curve near 0.5 Mev is due to the use of a positron emitter to

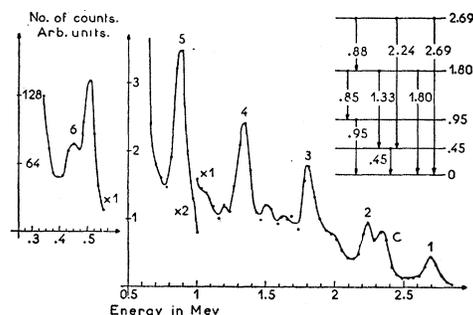


FIG. 3. γ spectrum of the yield from the 418-keV resonance and decay scheme of the 2.69-MeV level.

establish the point at 0.51 Mev. It might be difficult to find the exact peak-to-total ratio from the complex spectrum of positron annihilation radiation.¹³

(2) Secondly, the areas were corrected for the variation of counter efficiency with energy. The values given by Bell¹⁴ could be used for our crystal in the energy region under consideration when increased by 8%. This was found by independent calculations for our counter at a few energies. Bell's data had to be multiplied by the finite solid angle of the counter as seen from the target.

(3) We next corrected for the variation with γ -ray energy of the absorption in the target backing and holder.

¹¹ M. G. Mayer, *Phys. Rev.* **78**, 16 (1950).

¹² P. R. Bell in K. Siegbahn, *Beta- and Gamma-ray Spectroscopy* (North-Holland Publishing Company, Amsterdam, 1955), Chap. V, Fig. 6.

¹³ Gerhart, Carlson, and Sherr, *Phys. Rev.* **94**, 917 (1954).

¹⁴ P. R. Bell, in *Beta- and Gamma-ray Spectroscopy*, edited by K. Siegbahn (North-Holland Publishing Company, Amsterdam, 1955), p. 154.

Angular variation of the γ-ray intensities was not considered.

As in the extrapolated yield method,⁹ the areas of the photopeaks in most cases still have to be estimated by extrapolation. Consequently, some arbitrariness seems unavoidable with a single-crystal arrangement.

The results of the intensity estimates are given in Table II together with the measured energies of the identified γ rays. The intensities are measured in relation to a pronounced γ ray in each spectrum. The energies are given from an estimate of the peak location. The higher possible error in the low-energy part of the spectra stems from the existence of the positron peak and a lower peak-to-background ratio.

Sources of Error

Decay of the Al²⁵ Ground State

This decay by positron emission might lead to excited states of Mg²⁵.¹⁵ γ rays from these levels might

TABLE I. Energies and spins of excited levels in Al²⁵ found by investigating the γ rays from the Mg²⁴(p,γ)Al²⁵ reaction at resonant energies 222, 418, and 825 keV. For comparison the results of Goldberg⁸ are given.

This work Mg ²⁴ (p,γ)Al ²⁵		Goldberg Mg ²⁴ (d,n)Al ²⁵	
Mev level energy	Spin	Mev level energy	Spin
3.08±0.03	(3/2-) ^a	3.09±0.06	
2.69±0.02	3/2+	2.70±0.05	
2.50±0.06	1/2+, 1/2-	2.51±0.05	
1.80±0.02	3/2-	1.81±0.04	
0.95±0.08	3/2+	0.95±0.03	3/2+, 5/2+
0.45±0.06		0.45±0.03	1/2+
		0	5/2+

^a Our spectrum agrees with this assignment by Koester.⁷

give errors in the spectra attributed to the decay of excited levels in Al²⁵. A spectrum of the γ rays from the positron emission is given in Fig. 6. A background was measured to include radiation from possible activities with longer half-lives. The activities built up in the two runs are not directly comparable, but a background of sufficient accuracy for the present purpose is obtained.

A high-energy tail follows the 0.51-Mev peak. The peak arises from the annihilation of positrons at rest, and the tail is well accounted for by the annihilation of positrons in flight and by bremsstrahlung. This was shown by a calculation following Bethe¹⁶ and Gerhart *et al.*¹³

Any possible radiation from the lowest excited level of Mg²⁵, with an energy of 0.58 Mev,¹⁷ is difficult to find, owing to the small distance in energy from the annihilation peak at 0.51 Mev. But an amount of more than 1% of the 0.51-Mev peak would have shown up

¹⁵ Hunt, Jones, and Churchill, Proc. Phys. Soc. (London) **67A**, 479 (1954).

¹⁶ H. A. Bethe, Proc. Roy. Soc. (London) **150**, 129 (1935).

¹⁷ P. M. Endt and J. C. Kluyver, Revs. Modern Phys. **26**, 95 (1954).

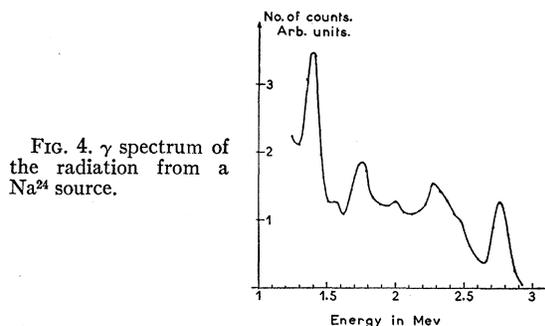


FIG. 4. γ spectrum of the radiation from a Na²⁴ source.

as a bulge on the side of this peak. Contributions from high-energy γ rays must be even smaller. We therefore conclude that the only error introduced in the Al²⁵ spectra from this source is due to the annihilation radiation.

Cascades

Two γ rays with energies E₁ and E₂ following each other in cascade faster than the resolution time of the counting equipment, will give rise to real coincidences in the counting crystal. If the intensity of the cascade is high, a measurable coincidence peak of energy E₁+E₂ will appear in the spectrum. The number N_c of counts in this peak can be found in relation to the number of counts N_{ph} in the photopeak of one of the γ rays in the cascade.

If there is only one route by which the lowest excited level can decay, then N_c=Ng₁k₂g₂k₂. N is the total number of photons in one of the two γ rays leaving the target, g is an energy dependent factor correcting for counter efficiency, solid angle and absorption, k is the peak-to-total ratio as given by Fig. 5 and gk gives the absolute probability of finding a γ ray counted in the appropriate photopeak. That is, N_{ph}=Ngk and N_c/N_{ph1}=g₂k₂; g and k are found as mentioned before.

Thus the coincidence peak to be expected from a cascade can be found. Incidentally, an absolute peak-to-total calibration can also be found using cascades. This ratio is given by gk, and consequently can be meas-

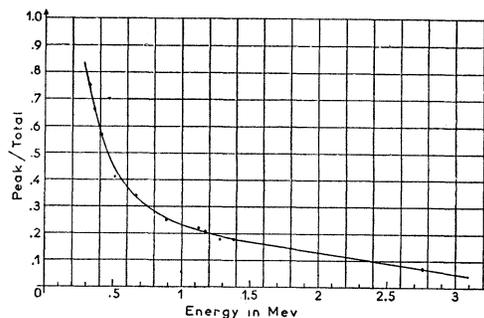


FIG. 5. Experimental peak to total ratio for a 1½-inch crystal of NaI(Tl). The data for the region up to 1.4 Mev are taken from Bell.¹²

TABLE II. γ rays from resonance reactions in $Mg^{24}(p,\gamma)Al^{25}$. Intensities given for each spectrum relative to a pronounced γ ray. All energies in Mev.

Resonance	0.222 (2.50 max energy)			0.418 (2.69 max energy)			0.825 (3.08 max energy)		
	Peak No.	E_γ	Intensity	Peak No.	E_γ	Intensity	Peak No.	E_γ	Intensity
	1	2.04 ± 0.03	1.0	1	2.69 ± 0.02	1.0	1	3.08 ± 0.03	0.4
	2	1.54 ± 0.05	0.1	2	2.24 ± 0.02	1.1	2	2.62 ± 0.02	1.0
	3	0.95 ± 0.07		3	1.80 ± 0.02	0.5	3	2.12 ± 0.03	<0.2
	4	0.46 ± 0.05		4	1.33 ± 0.03	0.8	4	0.95 ± 0.03	>0.06
							5	0.45 ± 0.04	
				5	0.88 ± 0.03				
					0.95	3.3			
					0.85				
				6	0.45 ± 0.05				

ured if radioactive sources of suitable properties can be found.

γ Radiation from Resonances in Carbon

The peak C in the spectrum from the 418-kev (Fig. 3) resonance can be attributed to the 456-kev resonance in C^{12} . The excitation energy of the corresponding level in N^{13} is 2.37 Mev.¹⁸ With a soot target a yield from this resonance was observed at a bombarding energy corresponding to the 418-kev resonance in Mg^{24} . In the γ spectrum of this yield a pronounced peak at 2.34 Mev was observed. The peak moved to 2.37 Mev when the energy of the bombarding protons was raised to above 450 kev. The movement was slight, but quite evident.

Constant Background

Peaks were observed in the constant background corresponding to the 2.62-Mev radiation from ThC'' and the 1.46-Mev radiation from the decay of K^{40} .¹⁷ The radiation probably comes from the walls and floor of our generator hall. One inch of lead was sufficient to bring the background down to a moderate level.

Different Spectra

222-kev Resonance Spectrum (Fig. 1)

The level at 2.50 Mev is chiefly de-excited via the 0.45-Mev level, giving the strong γ rays of 2.04- and 0.46-Mev energy. The peak at 2.50 corresponds to the energy of a γ ray to the ground state. This peak can be accounted for by coincidences between the 2.04- and 0.46-Mev γ rays to within 1% of the peak at 2.04 Mev. The transition to the ground state must, if it exists, be weak.

The photopeak of the 2.04-Mev γ ray is followed in the usual manner by a "one-quantum annihilation" peak and a "pair" peak at energies near 1.53 and 1.02 Mev. The peculiar sharpness of the 1.54-Mev peak and the broadening of the 1.02-Mev peak down to 0.9 Mev can be explained by assuming a transition from the 2.50-Mev level to the level at 0.95 Mev. A very rough

¹⁸ F. Ajzenberg and T. Lauritsen, *Revs. Modern Phys.* **27**, 77 (1955).

estimate for the intensity of this transition is given in Table II.

825-kev Resonance Spectrum (Fig. 2)

The picture from the previous spectrum is repeated. The de-excitation of the 3.08-Mev level via the 0.45-Mev level is evident, giving γ rays of energies 2.62 and 0.45 Mev. The transition to the 0.95-Mev level also is pronounced, giving γ rays of energies 2.12 Mev (energy coincident with the "annihilation" peak of the 2.26-Mev ray) and 0.95 Mev. The main structural difference from the previous spectrum is the existence of a ground state transition, which gives the 3.08-Mev peak.

418-kev Resonance Spectrum (Fig. 3)

The decay scheme of the 2.69-Mev level obviously is more complicated than the previous two. It can only be explained by the appearance of transitions to the 1.80-Mev level previously reported by Goldberg.⁸ Four possible routes exist for the de-excitation of the 2.69-Mev level. A direct transition to the ground state, a 2.24- and a 0.45-Mev transition via the first excited level, a 0.89-Mev transition to the 1.80-Mev level, and a 1.74- and a 0.95-Mev transition via the second excited level are possible. The existence of γ rays corresponding to the three first of these routes is evident from the peaks in the spectrum. The probability for the last route must be very small, as there is no pronounced peak at 1.74 Mev.

For the de-excitation of the 1.80-Mev level the following routes are possible: A 1.80-Mev transition to the ground state, a 1.35- and a 0.45-Mev transition via the first excited level, and a 0.85- and a 0.95-Mev transition via the second excited level. γ rays corresponding to the two first of these routes give rise to pronounced peaks in the spectrum. The high intensity of the 0.88-Mev peak, in relation to the peaks at 1.80 and 1.33 Mev, suggests that the last route also is probable. Separate runs on the 0.88-Mev peak with high resolution show pronounced shoulders on both sides of the peak, which also indicates that γ rays of energies 0.85 and 0.95 Mev may be present.

DISCUSSION OF SPINS

2.50-Mev Level

A spin of more than $\frac{1}{2}$ for the 2.50-Mev level would give the energy-favored transition to the ground state (spin $5/2+$) a higher probability than the transition to the first excited state (spin $\frac{1}{2}+$). We adopt the spin of $\frac{1}{2}+$ or $\frac{1}{2}-$ for the 2.50-Mev level.

The existence of an energy-unfavored transition to the 0.95-Mev level can be explained by choosing the spin $\frac{3}{2}+$ for this level from the two values given by Goldberg.⁸

In the further discussion we will justify the assignment of spin $\frac{3}{2}-$ to the level at 1.80 Mev. The apparent nonexistence of γ rays indicating a transition from the 2.50- to the 1.80-Mev level, might be used to give a parity assignment for the 2.50-Mev level. An existing radiation from this transition might on the other hand be too weak to be detected. Therefore an unambiguous parity assignment can not be given.

3.08-Mev Level

Koester's⁶ spin assignment for this level, $\frac{3}{2}-$, gives electric dipole radiation for the transitions to lower levels. The present measurements agree well with this assumption. There is a similarity between the spectrum from this level and the γ rays emitted by the 3.405-Mev level¹⁹ in Mg^{25} , a $\frac{3}{2}-$ level in the mirror nucleus of Al^{25} .

2.69- and 1.80-Mev Levels

An assignment of the spins $\frac{1}{2}+$ or $\frac{3}{2}\pm$ to the 1.80-Mev level is possible from the intensities of the observed γ rays from this level. A spin of $\frac{1}{2}-$ would give too low a probability for the transition to the ground state, and higher spins will suppress the relatively strong transition to the first excited level.

The validity of Weisskopf's estimates of transition probabilities, based on the single-particle model,²⁰ is thoroughly discussed by Kinsey and Bartholomew.¹⁹ Arguments based on these considerations and similar to those given above seem to justify a spin assignment of $\frac{3}{2}$ for the 2.69-Mev level. As the ratio of magnetic dipole to electric quadrupole emission is not too well established, spins of $\frac{1}{2}+$ and $5/2+$ might also be possible.

The transition from the 2.69 to the 1.80-Mev level

¹⁹ B. B. Kinsey and G. A. Bartholomew, Phys. Rev. **93**, 1260 (1954).

²⁰ J. M. Blatt and V. F. Weisskopf, *Theoretical Nuclear Physics* (John Wiley and Sons, Inc., New York, 1952).

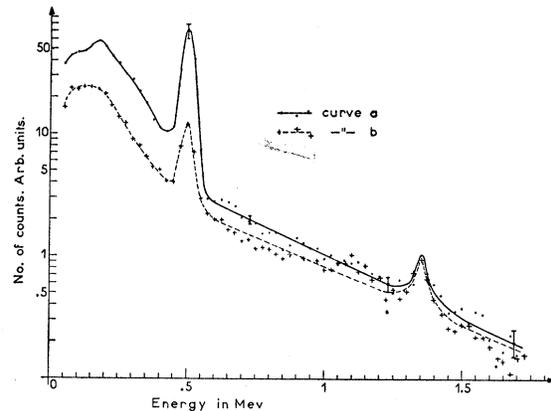


FIG. 6. (a) Radiation from annihilation of positrons in the decay of the Al^{25} ground state. The spectrum was obtained by 20-second bombardment of thin targets with protons of energy corresponding to the 825-kev resonance in Mg^{24} . The proton beam was then shut off and the γ rays counted in 10 sec. This run was repeated 100 times. (b) Background. 20 seconds of bombardment were followed by 10 sec of waiting and 25 sec of counting. 40 runs. The peak at 1.45 Mev is due to radiation from K^{40} in the constant background.

obviously is parity-favored, and the transitions to the lower levels are parity-unfavored. The only combination of spins mentioned leading to such transitions is a spin of $\frac{3}{2}-$ for the 1.80-Mev level and a spin of even parity for the 2.69-Mev level.

The assignment $\frac{3}{2}+$ is preferred for the 2.69-Mev level. The assignment is in agreement with earlier investigations⁸; it may especially be noted that the assumption of a D level at this energy can explain why a resonance at 418 kev was not found in the elastic scattering experiment of Mooring *et al.*⁶ The width of a D level may be too small at this energy to be resolved.

CONCLUSION

In conclusion, the levels and spins found in this investigation are compared with the results of Goldberg⁸ in Table I. We have found no evidence of the two dubious levels reported by Goldberg.

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